World development indicators

Which country will develop more

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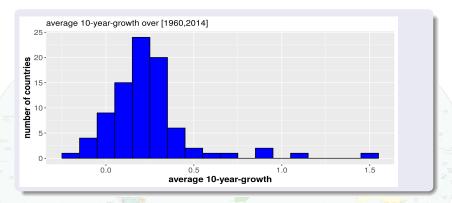
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10-year-Growth definition and average



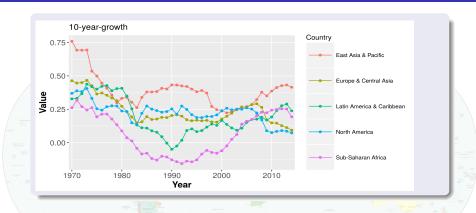
Definition

The 10-year-Growth is the 10-year percentage variation of the GDP per capita in local currency. More formally,

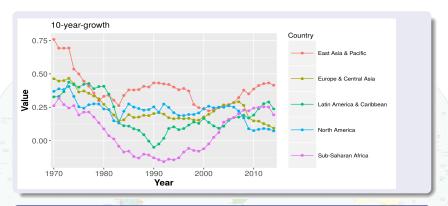
$$Growth_t := \frac{GDP_t - GDP_{t-10}}{GDP_{t-10}} \tag{1}$$

where GDP is the Gross Domestic Product per capita

10-year-growth by region



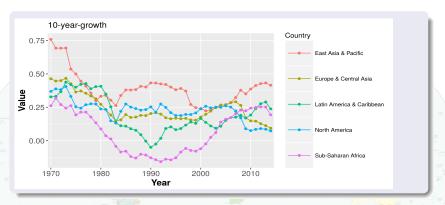
10-year-growth by region



Remark 1

significant differences between decades \implies dummy for decades

10-year-growth by region



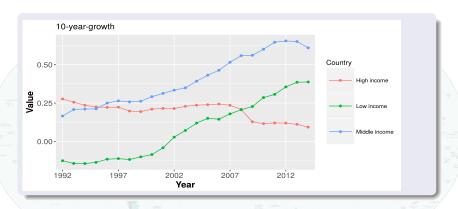
Remark 1

significant differences between decades \implies dummy for decades

Remark 2

different growth patterns for different regions \implies dummy for Asia and dummy for Africa

10-year-growth by Income group



Remark 3

different growth patterns for different Income groups \implies dummy for High Income and dummy for Low Income

The Regressors: State and Environmental variables

State variables

- Education := $\frac{\text{tot enrolment primary school}}{\text{population}}$ [%]
- Health := $\frac{1}{\text{life expectancy at birth}}$ [year]⁻¹
- Fertility := average number of births per woman

The Regressors: State and Environmental variables

State variables

- $\bullet \ \, \mathsf{Education} := \tfrac{\mathsf{tot} \ \mathsf{enrolment} \ \mathsf{primary} \ \mathsf{school}}{\mathsf{population}} \quad [\%]$
- Health := $\frac{1}{\text{life expectancy at birth}}$ [year]⁻¹
- Fertility := average number of births per woman

Envirnonmental variables

- Inflation [%]
- GDP := log(GDP)
- FDI := financial capital owned by foreign investors [% of GDP]
- Openess := $\frac{Inport + Export}{GDP}$
- Consumption := households consumption expenditure [% of GDP]
- Investment := government expenditures for goods and services [% of GDP]

The Dummies: decade, income and region

Let
$$X = [\underline{x}_1, \underline{x}_2, \dots, \underline{x}_{3n}]^T$$
 be the design matrix

Dummies for decades

$$D_{1} = \begin{cases} 1 & \text{if } \underline{x}_{i} \in [1983, 1993) \\ 0 & \text{otherwise} \end{cases} \qquad D_{2} = \begin{cases} 1 & \text{if } \underline{x}_{i} \in [1993, 2003) \\ 0 & \text{otherwise} \end{cases}$$
 (2)

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Dummies for Income

$$I_1 = \begin{cases} 1 & \text{if } \underline{x}_i \in \mathsf{High\ Income} \\ 0 & \text{otherwise} \end{cases} \qquad I_2 = \begin{cases} 1 & \text{if } \underline{x}_i \in \mathsf{Low\ Income} \\ 0 & \text{otherwise} \end{cases} \tag{3}$$

The Dummies: decade, income and region

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Dummies for decades

$$D_{1} = \begin{cases} 1 & \text{if } \underline{x}_{i} \in [1983, 1993) \\ 0 & \text{otherwise} \end{cases} \qquad D_{2} = \begin{cases} 1 & \text{if } \underline{x}_{i} \in [1993, 2003) \\ 0 & \text{otherwise} \end{cases}$$
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Dummies for Income

$$I_1 = \begin{cases} 1 & \text{if } \underline{x}_i \in \mathsf{High\ Income} \\ 0 & \text{otherwise} \end{cases} \qquad I_2 = \begin{cases} 1 & \text{if } \underline{x}_i \in \mathsf{Low\ Income} \\ 0 & \text{otherwise} \end{cases} \tag{3}$$

Dummies for Region

$$R_1 = \begin{cases} 1 & \text{if } \underline{x}_i \in \mathsf{East Asia} \\ 0 & \text{otherwise} \end{cases} \qquad R_2 = \begin{cases} 1 & \text{if } \underline{x}_i \in \mathsf{Sub-Saharan Africa} \\ 0 & \text{otherwise} \end{cases} \tag{4}$$

Linear Model: complete model

Let
$$\epsilon \sim N(0, \sigma^2)$$

complete model

$$\begin{aligned} \textit{Growth} &= \beta_0 + \beta_1 \text{fertility} + \beta_2 \text{FDI} + \beta_3 \text{GDP} + \beta_4 \text{education} + \beta_5 \text{consumption} + \\ & \beta_6 \text{inflation} + \beta_7 \text{health} + \beta_8 \text{investment} + \beta_9 \text{openess} + \\ & \beta_{10} D_1 + \beta_{11} D_2 + \beta_{12} R_1 + \beta_{13} R_2 + \beta_{14} I_1 + \beta_{15} I_2 + \\ & D_1 (\beta_{16} \text{GDP} + \beta_{17} \text{fertility} + \beta_{18} \text{investment}) + \\ & D_2 (\beta_{19} \text{GDP} + \beta_{20} \text{fertility} + \beta_{21} \text{investment}) + \\ & I_1 (\beta_{22} \text{GDP} + \beta_{23} \text{fertility} + \beta_{24} \text{investment}) + \\ & I_2 (\beta_{25} \text{GDP} + \beta_{26} \text{fertility} + \beta_{27} \text{investment}) + \\ & R_1 (\beta_{28} \text{GDP} + \beta_{29} \text{fertility} + \beta_{30} \text{investment}) + \\ & R_2 (\beta_{31} \text{GDP} + \beta_{32} \text{fertility} + \beta_{33} \text{investment}) + \epsilon \end{aligned}$$

Let
$$\epsilon \sim N(0, \sigma^2)$$

reduced model

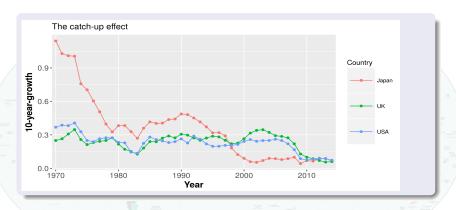
$$Growth = \beta_0 + \beta_1 \text{fertility} + \beta_2 \text{GDP} + \beta_3 \text{consumption} + \beta_4 \text{investment} + \beta_5 \text{education} + \beta_6 \text{FDI}$$

$$\beta_7 D_1 + \beta_8 D_2 + \beta_9 R_1 + \beta_{10} R_2 + \beta_{11} I_1 + \beta_{12} I_2 + D_1 (\beta_{13} \text{GDP} + \beta_{14} \text{investment}) + D_2 (\beta_{15} \text{GDP}) + I_1 (\beta_{16} \text{GDP} + \beta_{17} \text{fertility} + \beta_{18} \text{investment})$$

$$I_2 (\beta_{19} \text{investment}) + R_1 (\beta_{20} \text{GDP} + \beta_{21} \text{fertility}) + R_2 (\beta_{22} \text{fertility} + \beta_{23} \text{investment}) + \epsilon$$

	Model 1		2.00
(Intercept) fertility FDI GDP education consumption health	0.9531 (0.3791)* -0.0849 (0.0244)*** -0.0085 (0.0063) -0.0903 (0.0305)** -0.0025 (0.0010)* 0.0047 (0.0010)*** -21.0428 (11.8102)	investment:l2 GDP:R1 fertility:R1	0.0804 (0.0297)** -0.0354 (0.0073)*** 0.0327 (0.0088)*** -0.3070 (0.0348)*** -0.3880 (0.0362)*** -0.0527 (0.0274) -0.0425 (0.0073)***
R1 R2 I1 I2 investment	3.8459 (0.3718)*** 0.8626 (0.1585)*** 1.0546 (0.4503)* -0.4912 (0.1445)** 0.0407 (0.0063)***	R ² Adj. R ² Num. obs. RMSE	0.8705 0.8364 116 0.1134
D1 D2 GDP:D1 investment:D1 GDP:D2 GDP:l1	-0.3408 (0.1521)* -0.4913 (0.1369)*** 0.0841 (0.0182)*** -0.0189 (0.0048)*** 0.0640 (0.0163)*** -0.0783 (0.0474)	• D1 = [1903,1993)	

Results analysis: Conditional Convergence



Definition

the following principle is called **conditional convergence**: the lower the initial GDP the higher the growth over the next decade



Prediction model: no dummies for decades

Let $\epsilon \sim N(0, \sigma^2)$

prediction model

$$Growth = \beta_0 + \beta_1 \text{fertility} + \beta_2 \text{GDP} + \beta_3 \text{consumption} + \beta_4 \text{investment} + \beta_5 R_1 + \beta_6 R_2 + \beta_7 I_1 + \beta_8 I_2 + I_1 (\beta_9 \text{GDP} + \beta_{10} \text{fertility} + \beta_{11} \text{investment})$$

$$I_2(\beta_{12} \text{investment} + \beta_{13} \text{fertility}) + R_1 (\beta_{14} \text{GDP} + \beta_{15} \text{fertility}) + R_2 (\beta_{16} \text{fertility} + \beta_{17} \text{investment}) + \epsilon$$

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$$I_2(\beta_{12} \text{investment} + \beta_{13} \text{fertility}) + R_1 (\beta_{14} \text{GDP} + \beta_{15} \text{fertility}) + R_2 (\beta_{16} \text{fertility} + \beta_{17} \text{investment}) + \epsilon$$

Remark 4

The model has no time component: prediction based only on regressors value at prediction instant



predictor evaluation

 $fitting \ sample = [1983,2013] \qquad test \ sample = [2003,2013]$

Definition

- F_t = prediction for the growth in t with our model
- Y_t = realization of growth in t
- $e_t = prediction error$
- $ME = \sum_{t=0}^{n} \frac{1}{n} e_t = \text{mean error}$
- $MAD = \sum_{t=0}^{n} \frac{1}{n} ||e_t|| = \text{mean absolute deviation}$
- $RMSE = \sqrt{\sum_{t=0}^{n} \frac{1}{n}e_{t}^{2}} = root$ mean square error

predictor evaluation

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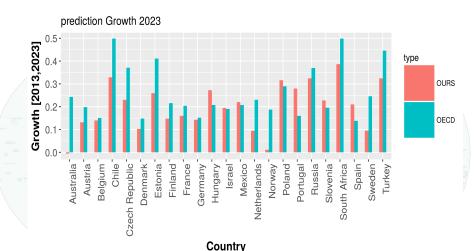
predictor performances

validation on n = 12 new countries

ME	MAD	RMSE
0.032	0.163	0.211

- slightly overestimating
- inaccurate out-of-sample

2023 growth prediction comparison



OECD = The Organisation for Economic Co-operation and Development is an intergovernmental economic organisation with 35 member countries, founded in 1960 to stimulate economic progress and world trade