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In [1]: import pymongo
import pandas as pd
import numpy as np

from pymongo import MongoClient
from bson.objectid import ObjectId

import datetime

import matplotlib.pyplot as plt

from collections import defaultdict

%matplotlib inline
import json
plt.style.use('ggplot')

import seaborn as sns

from math import log10, floor

from time import time

from sklearn.feature_extraction.text import TfidfVectorizer, CountVectorizer

from sklearn.cluster import KMeans, MiniBatchKMeans
```

CU Woot Math Method 2 for unserved discovery of new behavior traits

1) Convert response field dictionary into a document

2) Develop word vector using term frequency - inverse document frequency

3) Use K-Means to cluster documents

4) Map traits to clusters to validate technique

In the first results presented to Woot Math a 100K sample of the entire data set was chosen. In this report, I'll start with the same type of analysis to develop the same heat map. In the meeting Sean and Brent suggested using just one of the qual_id and repeat the experiment and then look at the samples in clusters without traits. I'll do that in a subsequent analysis

Part 1. Heat map with 100 K sample of all qual_id's

```
In [2]: ## Connect to local DB  
  
client = MongoClient('localhost', 27017)  
print ("Setup db access")
```

Setup db access

```
In [3]: #  
# Get collections from mongodb  
#  
#db = client.my_test_db  
db = client.test
```

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In [4]: chunk = 100000  
start = 0  
end = start + chunk
```

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In [5]: #reponses = db.anon_student_task_responses.find({'correct':False})[start:end]  
reponses = db.anon_student_task_responses.find()[start:end]
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In [6]: df_responses = pd.DataFrame(list(reponses))
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In [7]: print (df_responses.shape)  
  
(100000, 27)
```

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In [8]: ## Make the documents to be analyzed
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In [9]: ## Functions for turning dictionary into document

def make_string_from_list(key, elem_list):
    # Append key to each item in list
    ans = ''
    for elem in elem_list:
        ans += key + '_' + elem

def make_string(elem, key=None, top=True):
    ans = ''
    if not elem:
        return ans
    if top:
        top = False
        top_keys = []
        for idx in range(len(elem.keys())):
            top_keys.append(True)

    for idx, key in enumerate(elem.keys()):
        if top_keys[idx]:
            top = True
            top_keys[idx] = False
            ans += ' '
        else:
            top = False
            #print ('ans = ', ans)
            #print (type(elem[key]))
            if type(elem[key]) is str or\
                type(elem[key]) is int:
                #print ('add value', elem[key])
                value = str(elem[key])
                #ans += key + '_' + value + ' ' + value + ' '
                ans += key + '_' + value + ' '
            elif type(elem[key]) is list:
                #print ('add list', elem[key])
                temp_elem = dict()
                for item in elem[key]:
                    temp_elem[key] = item
                    ans += make_string(temp_elem, top)
            elif type(elem[key]) is dict:
                #print ('add dict', elem[key])
                for item_key in elem[key].keys():
                    temp_elem = dict()
                    temp_elem[item_key] = elem[key][item_key]
                    ans += key + '_' + make_string(temp_elem, top)
            elif type(elem[key]) is float:
                #print ('add dict', elem[key])
                sig = 2
                value = elem[key]
                value = round(value, sig-int(
                    floor(log10(abs(value))))-1)
                value = str(value)

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        #ans += key + '_' + value + ' ' + value + ' '
        ans += key + '_' + value + ' '
    # ans += ' ' + key + ' '
    #print ('not handled', elem[key])

    return ans

```

```

In [10]: # Makes the cut & paste below easier
df3 = df_responses

```

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In [11]: df3['response_doc'] = df3['response'].map(make_string)

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In [12]: df3['response_doc'] = df3['response_doc'].map(lambda x: x + ' ')
df3['response_doc'] = df3['response_doc'].map(lambda x: x.replace('/', '_'))
df3['response_doc'] = df3['response_doc'] + ' ' + df3['txt']
df3['response_doc'] = df3['response_doc'].map(lambda x: x + ' ')
df3['response_doc'] = df3['response_doc'].map(lambda x: x.replace("\n", ""))
df3['response_doc'] = df3['response_doc'].map(lambda x: x.replace("?", " "))

```

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In [ ]:

```

Sample Documents

```
In [13]: for idx in range(20):
        print ("Sample number:", idx, "\n", df3.iloc[idx]['response_doc'])
```

Sample number: 0

fraction_cblock_chains_right_442 fraction_cblock_chains_sum_numerator_1 sum_denominator_2 sum__as3_type_Fraction fraction_cblock_chains_pieces_1_2 fraction_cblock_chains_left_97 fraction_cblock_chains_lcm_sum_numerator_1 lcm_sum_denominator_2 lcm_sum__as3_type_Fraction plain_image_groups_total_1 plain_image_groups_url_assets_cms_wootmath_fractions_number_line_markers_end_marker_noline.swf plain_image_groups_total_1 plain_image_groups_url_assets_cms_wootmath_fractions_number_line_markers_start_marker.swf plain_image_groups_total_1 plain_image_groups_url_assets_cms_wootmath_fractions_number_line_objects_dog.swf plain_image_groups_total_1 plain_image_groups_url_assets_cms_wootmath_fractions_number_line_objects_cat_dog_trail.swf den_2 fraction_input_value_1_2 num_1 fraction_cblock_total_count_1 fraction_cblock_counts_1_2_1 whole_1

Use the 1/2 pieces to figure out how far the dog traveled. Answer: 1/2

Sample number: 1

fraction_cblock_total_count_4 plain_image_groups_total_1 plain_image_groups_url_assets_cms_wootmath_fractions_number_line_objects_panda.swf plain_image_groups_total_1 plain_image_groups_url_assets_cms_wootmath_fractions_number_line_markers_start_marker.swf input_4 fraction_cblock_chains_right_856 fraction_cblock_chains_sum_numerator_1 sum_denominator_1 sum__as3_type_Fraction fraction_cblock_chains_pieces_1_4 pieces_1_4 pieces_1_4 fraction_cblock_chains_left_165 fraction_cblock_chains_lcm_sum_numerator_4 lcm_sum_denominator_4 lcm_sum__as3_type_Fraction numberline_associations_numberline_associations_position_720.0 numberline_associations_pos_value_1.0 numberline_associations_object_name fraction_cblock_counts_1_4_4 Drag the panda to 4/4 of a yard from the start. Answer: 4/4

Sample number: 2

fraction_cblock_chains_left_176 fraction_cblock_chains_lcm_sum_numerator_2 lcm_sum_denominator_8 lcm_sum__as3_type_Fraction fraction_cblock_chains_right_348 fraction_cblock_chains_pieces_1_8 pieces_1_8 fraction_cblock_chains_sum_numerator_1 sum_denominator_4 sum__as3_type_Fraction fraction_cblock_chains_left_590 fraction_cblock_chains_lcm_sum_numerator_1 lcm_sum_denominator_6 lcm_sum__as3_type_Fraction fraction_cblock_chains_right_705 fraction_cblock_chains_pieces_1_6 fraction_cblock_chains_sum_numerator_1 sum_denominator_6 sum__as3_type_Fraction fraction_cblock_chains_left_176 fraction_cblock_chains_lcm_sum_numerator_1 lcm_sum_denominator_4 lcm_sum__as3_type_Fraction fraction_cblock_chains_right_348 fraction_cblock_chains_pieces_1_4 fraction_cblock_chains_sum_numerator_1 sum_denominator_4 sum__as3_type_Fraction fraction_cblock_chains_left_176 fraction_cblock_chains_lcm_sum_numerator_1 lcm_sum_denominator_1 lcm_sum__as3_type_Fraction fraction_cblock_chains_right_866 fraction_cblock_chains_pieces_1 fraction_cblock_chains_sum_numerator_1 sum_denominator_1 sum__as3_type_Fraction fraction_cblock_total_count_5 fraction_cblock_counts_1_1 fraction_cblock_counts_1_8_2 fraction_cblock_counts_1_6_1 fraction_cblock_counts_1_4_1 fraction_cblock_containment_piece0 lcm_sum_numerator_2 lcm_sum_denominator_8 lcm_sum__as3_type_Fraction piece0 piece0 pieces_1_8 pieces_1_8 piece0_sum_numerator_1 sum_denominator_4 sum__as3_type_Fraction Model how many eighths are equal to one fourth. Answer: 2

Sample number: 3

fraction_cblock_chains_left_176 fraction_cblock_chains_lcm_sum_numerator_1 lcm_sum_denominator_2 lcm_sum__as3_type_Fraction fraction_cblock_chains_right_521 fraction_cblock_chains_pieces_1_2 fraction_cblock_chains_sum_numerator_1 sum_denominator_4 sum__as3_type_Fraction fraction_cblock_chains_left_590 fraction_cblock_chains_lcm_sum_numerator_1 lcm_sum_denominator_6 lcm_sum__as3_type_Fraction fraction_cblock_chains_right_705 fraction_cblock_chains_pieces_1_6 fraction_cblock_chains_sum_numerator_1 sum_denominator_6 sum__as3_type_Fraction fraction_cblock_chains_left_176 fraction_cblock_chains_lcm_sum_numerator_1 lcm_sum_denominator_4 lcm_sum__as3_type_Fraction fraction_cblock_chains_right_348 fraction_cblock_chains_pieces_1_4 fraction_cblock_chains_sum_numerator_1 sum_denominator_4 sum__as3_type_Fraction fraction_cblock_chains_left_176 fraction_cblock_chains_lcm_sum_numerator_1 lcm_sum_denominator_1 lcm_sum__as3_type_Fraction fraction_cblock_chains_right_866 fraction_cblock_chains_pieces_1 fraction_cblock_chains_sum_numerator_1 sum_denominator_1 sum__as3_type_Fraction fraction_cblock_total_count_5 fraction_cblock_counts_1_1 fraction_cblock_counts_1_8_2 fraction_cblock_counts_1_6_1 fraction_cblock_counts_1_4_1 fraction_cblock_containment_piece0 lcm_sum_numerator_2 lcm_sum_denominator_8 lcm_sum__as3_type_Fraction piece0 piece0 pieces_1_8 pieces_1_8 piece0_sum_numerator_1 sum_denominator_4 sum__as3_type_Fraction Model how many eighths are equal to one fourth. Answer: 2

```
chains_sum_numerator_1 sum_denominator_2 sum__as3_type_Fraction fraction_cblock_chains_left_176 fraction_cblock_chains_lcm_sum_numerator_4 lcm_sum_denominator_8 lcm_sum__as3_type_Fraction fraction_cblock_chains_right_521 fraction_cblock_chains_pieces_1_8 pieces_1_8 pieces_1_8 pieces_1_8 fraction_cblock_chains_sum_numerator_1 sum_denominator_2 sum__as3_type_Fraction fraction_cblock_chains_left_176 fraction_cblock_chains_lcm_sum_numerator_1 lcm_sum_denominator_1 lcm_sum__as3_type_Fraction fraction_cblock_chains_right_866 fraction_cblock_chains_pieces_1 fraction_cblock_chains_sum_numerator_1 sum_denominator_1 sum__as3_type_Fraction fraction_cblock_total_count_6 fraction_cblock_counts_1_1 fraction_cblock_counts_1_2_1 fraction_cblock_counts_1_8_4 fraction_cblock_containment_[Fraction] 1_2 lcm_sum_numerator_4 lcm_sum_denominator_8 lcm_sum__as3_type_Fraction [Fraction] 1_2 [Fraction] 1_2 pieces_1_8 pieces_1_8 pieces_1_8 pieces_1_8 [Fraction] 1_2 sum_numerator_1 sum_denominator_2 sum__as3_type_Fraction Model how many halves are equal to four eighths. Answer: 1
```

Sample number: 4

```
fraction_circle_containment_[Fraction] 1_2 lcm_sum_numerator_4 lcm_sum_denominator_8 lcm_sum__as3_type_Fraction [Fraction] 1_2 [Fraction] 1_2 pieces_1_8 pieces_1_8 pieces_1_8 pieces_1_8 [Fraction] 1_2 sum_numerator_1 sum_denominator_2 sum__as3_type_Fraction fraction_circle_total_count_6 fraction_circle_groups_x_512 fraction_circle_groups_y_300 fraction_circle_groups_scale_1.0 fraction_circle_groups_pieces_1_2 pieces_1_8 pieces_1_8 pieces_1_8 pieces_1_8 pieces_1 fraction_circle_groups_chains_right_180 chains_pieces_1_8 pieces_1_8 pieces_1_8 pieces_1_8 chains_left_0 fraction_circle_counts_1_1 fraction_circle_counts_1_2_1 fraction_circle_counts_1_8_4 Cameron ate 4/8 of a pizza. C over the pizza to model how many halves of a pizza he ate. Answer: 1
```

Sample number: 5

```
image_object_groups_total_6 image_object_groups_on_3 image_object_groups_url_assets_objects_singles_watch.swf image_object_groups_off_3 S hade 1/2 of the 6 watches. Answer: 1/2
```

Sample number: 6

```
Shade 1/4 of the circle.answer={:n=>3, :d=>12}
```

Sample number: 7

```
Shade 1/3 of the rectangle.answer={:n=>2, :d=>6}
```

Sample number: 8

```
fraction_circle_groups_x_512 fraction_circle_groups_scale_1 fraction_circle_groups_chains_pieces_1_8 pieces_1_8 pieces_1_8 pieces_1_8 chains_left_0 chains_right_180 fraction_circle_groups_pieces_1_8 pieces_1_8 pieces_1_8 pieces_1_8 pieces_1_2 pieces_1 fraction_circle_groups_y_300 fraction_circle_containment_piece_0 sum_denominator_2 sum_numerator_1 sum__as3_type_Fraction piece_0 piece_0 pieces_1_8 pieces_1_8 pieces_1_8 pieces_1_8 piece_0 lcm_sum_denominator_8 lcm_sum_numerator_4 lcm_sum__as3_type_Fraction fraction_circle_counts_1_1 fraction_circle_counts_1_2_1 fraction_circle_counts_1_8_4 fraction_circle_total_count_6 Drag one eighth pieces to cover all of the 1/2 piece. Answer: 4
```

Sample number: 9

```
fraction_circle_groups_x_512 fraction_circle_groups_scale_1.0 fraction_circle_groups_chains_pieces_1_8 pieces_1_8 pieces_1_8 pieces_1_8 chains_left_0 chains_right_180 fraction_circle_groups_pieces_1_2 pieces_1_8 pieces_1_8 pieces_1_8 pieces_1_8 pieces_1 fraction_circle_groups_y_300 fraction_circle_containment_[Fraction] 1_2 sum_denominator_2 sum_numerator_1 sum__as3_type_Fraction [Fraction] 1_2 [Fraction] 1_2 pieces_1_8 pieces_1_8 pieces_1_8 pieces_1_8 [Fraction] 1_2 lcm_sum_denominator_8 lcm_sum_numerator_4 lcm_sum__as3_type_Fraction fra
```

fraction_circle_counts_1_1 fraction_circle_counts_1_2_1 fraction_circle_counts_1_8_4 fraction_circle_total_count_6 Drag one half pieces to cover all of the $\frac{4}{8}$ shown. Answer: 1

Sample number: 10

fraction_circle_groups_x_512 fraction_circle_groups_scale_1.0 fraction_circle_groups_chains_pieces_1_4 pieces_1_4 chains_left_0 chains_right_180 fraction_circle_groups_pieces_1_2 pieces_1_4 pieces_1_4 pieces_1 fraction_circle_groups_y_300 fraction_circle_containment_[Fraction] 1_2_sum_denominator_2 sum_numerator_1 sum___as3_type_Fraction [Fraction] 1_2_[Fraction] 1_2_pieces_1_4 pieces_1_4 [Fraction] 1_2_lcm_sum_denominator_4 lcm_sum_numerator_2 lcm_sum___as3_type_Fraction fraction_circle_counts_1_1 fraction_circle_counts_1_2_1 fraction_circle_counts_1_4_2 fraction_circle_total_count_4 Drag one half pieces to cover all of the $\frac{2}{4}$ shown. Answer: 1

Sample number: 11

radio_choice_C radio_group_problem_choice_C radio_group_problem_text_3_6 radio_text_3_6 What fraction has 6 as the denominator $() \frac{6}{7} () \frac{4}{5} () \frac{3}{6}$ Answer: $\frac{3}{6}$

Sample number: 12

fraction_cblock_chains_sum_denominator_10 sum_numerator_1 sum___as3_type_Fraction fraction_cblock_chains_lcm_sum_denominator_10 lcm_sum_numerator_1 lcm_sum___as3_type_Fraction fraction_cblock_chains_pieces_1_10 fraction_cblock_chains_left_1024 fraction_cblock_chains_right_1458 fraction_cblock_chains_sum_denominator_5 sum_numerator_1 sum___as3_type_Fraction fraction_cblock_chains_lcm_sum_denominator_10 lcm_sum_numerator_2 lcm_sum___as3_type_Fraction fraction_cblock_chains_pieces_1_10 pieces_1_10 fraction_cblock_chains_left_1024 fraction_cblock_chains_right_1297 fraction_cblock_chains_sum_denominator_10 sum_numerator_1 sum___as3_type_Fraction fraction_cblock_chains_lcm_sum_denominator_10 lcm_sum_numerator_1 lcm_sum___as3_type_Fraction fraction_cblock_chains_pieces_1_10 fraction_cblock_chains_left_1024 fraction_cblock_chains_right_1531 fraction_cblock_chains_sum_denominator_10 sum_numerator_1 sum___as3_type_Fraction fraction_cblock_chains_lcm_sum_denominator_10 lcm_sum_numerator_1 lcm_sum___as3_type_Fraction fraction_cblock_chains_pieces_1_10 fraction_cblock_chains_left_1024 fraction_cblock_chains_right_1214 fraction_cblock_chains_sum_denominator_10 sum_numerator_1 sum___as3_type_Fraction fraction_cblock_chains_lcm_sum_denominator_10 lcm_sum_numerator_1 lcm_sum___as3_type_Fraction fraction_cblock_chains_pieces_1_10 fraction_cblock_chains_left_1024 fraction_cblock_chains_right_1424 fraction_cblock_chains_sum_denominator_5 sum_numerator_2 sum___as3_type_Fraction fraction_cblock_chains_lcm_sum_denominator_10 lcm_sum_numerator_4 lcm_sum___as3_type_Fraction fraction_cblock_chains_pieces_1_10 pieces_1_10 pieces_1_10 pieces_1_10 fraction_cblock_chains_left_544 fraction_cblock_chains_right_820 fraction_cblock_chains_sum_denominator_84 sum_numerator_73 sum___as3_type_Fraction fraction_cblock_chains_lcm_sum_denominator_84 lcm_sum_numerator_73 lcm_sum___as3_type_Fraction fraction_cblock_chains_pieces_1_7 pieces_1_7 pieces_1_6 pieces_1_6 pieces_1_4 fraction_cblock_chains_left_1001 fraction_cblock_chains_right_1272 fraction_cblock_chains_sum_denominator_35 sum_numerator_17 sum___as3_type_Fraction fraction_cblock_chains_lcm_sum_denominator_35 lcm_sum_numerator_17 lcm_sum___as3_type_Fraction fraction_cblock_chains_pieces_1_7 pieces_1_7 pieces_1_5 fraction_cblock_chains_left_981 fraction_cblock_chains_right_1316 fraction_cblock_chains_sum_denominator_28 sum_numerator_11 sum___as3_type_Fraction fraction_cblock_chains_lcm_sum_denominator_28 lcm_sum_numerator_11 lcm_sum___as3_type_Fraction fraction_cblock_chains_pieces_1_7 pieces_1_4 fraction_cblock_chains_left_1001 fraction_cblock_chains_right_1272 fraction_cblock_chai

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ns_sum_denominator_7 sum_numerator_1 sum__as3_type_Fraction fraction
_cblock_chains_lcm_sum_denominator_7 lcm_sum_numerator_1 lcm_sum__as
3_type_Fraction fraction_cblock_chains_pieces_1_7 fraction_cblock_chain
s_left_1024 fraction_cblock_chains_right_1300 fraction_cblock_chains_
sum_denominator_7 sum_numerator_1 sum__as3_type_Fraction fraction_cbl
ock_chains_lcm_sum_denominator_7 lcm_sum_numerator_1 lcm_sum__as3_ty
pe_Fraction fraction_cblock_chains_pieces_1_7 fraction_cblock_chains_1
eft_1024 fraction_cblock_chains_right_1248 fraction_cblock_chains_sum_
denominator_6 sum_numerator_1 sum__as3_type_Fraction fraction_cblock_c
hains_lcm_sum_denominator_6 lcm_sum_numerator_1 lcm_sum__as3_type_Fr
action fraction_cblock_chains_pieces_1_6 fraction_cblock_chains_left_1
024 fraction_cblock_chains_right_1316 fraction_cblock_chains_sum_deno
minator_6 sum_numerator_1 sum__as3_type_Fraction fraction_cblock_chain
s_lcm_sum_denominator_6 lcm_sum_numerator_1 lcm_sum__as3_type_Fracti
on fraction_cblock_chains_pieces_1_6 fraction_cblock_chains_left_1024
fraction_cblock_chains_right_1387 fraction_cblock_chains_sum_denomina
tor_6 sum_numerator_1 sum__as3_type_Fraction fraction_cblock_chains_l
cm_sum_denominator_6 lcm_sum_numerator_1 lcm_sum__as3_type_Fraction f
raction_cblock_chains_pieces_1_6 fraction_cblock_chains_left_1024 frac
tion_cblock_chains_right_1220 fraction_cblock_chains_sum_denominator_
6 sum_numerator_1 sum__as3_type_Fraction fraction_cblock_chains_lcm_s
um_denominator_6 lcm_sum_numerator_1 lcm_sum__as3_type_Fraction fract
ion_cblock_chains_pieces_1_6 fraction_cblock_chains_left_1024 fraction
_cblock_chains_right_1387 fraction_cblock_chains_sum_denominator_5 su
m_numerator_1 sum__as3_type_Fraction fraction_cblock_chains_lcm_sum_
denominator_5 lcm_sum_numerator_1 lcm_sum__as3_type_Fraction fraction_
cblock_chains_pieces_1_5 fraction_cblock_chains_left_1024 fraction_cbl
ock_chains_right_1358 fraction_cblock_chains_sum_denominator_5 sum_n
umerator_3 sum__as3_type_Fraction fraction_cblock_chains_lcm_sum_deno
minator_5 lcm_sum_numerator_3 lcm_sum__as3_type_Fraction fraction_cblo
ck_chains_pieces_1_5 pieces_1_5 pieces_1_5 fraction_cblock_chains_le
ft_1024 fraction_cblock_chains_right_1337 fraction_cblock_chains_sum_
denominator_2 sum_numerator_1 sum__as3_type_Fraction fraction_cblock_c
hains_lcm_sum_denominator_4 lcm_sum_numerator_2 lcm_sum__as3_type_Fr
action fraction_cblock_chains_pieces_1_4 pieces_1_4 fraction_cblock_ch
ains_left_1024 fraction_cblock_chains_right_1523 fraction_cblock_chain
s_sum_denominator_4 sum_numerator_1 sum__as3_type_Fraction fraction_
cblock_chains_lcm_sum_denominator_4 lcm_sum_numerator_1 lcm_sum__as3
_type_Fraction fraction_cblock_chains_pieces_1_4 fraction_cblock_chains
_left_1024 fraction_cblock_chains_right_1272 fraction_cblock_chains_s
um_denominator_4 sum_numerator_1 sum__as3_type_Fraction fraction_cblo
ck_chains_lcm_sum_denominator_4 lcm_sum_numerator_1 lcm_sum__as3_typ
e_Fraction fraction_cblock_chains_pieces_1_4 fraction_cblock_chains_le
ft_1024 fraction_cblock_chains_right_1358 fraction_cblock_chains_sum_
denominator_2 sum_numerator_1 sum__as3_type_Fraction fraction_cblock_c
hains_lcm_sum_denominator_2 lcm_sum_numerator_1 lcm_sum__as3_type_Fr
action fraction_cblock_chains_pieces_1_2 fraction_cblock_chains_left_1
024 fraction_cblock_chains_right_1531 fraction_cblock_chains_sum_deno
minator_2 sum_numerator_1 sum__as3_type_Fraction fraction_cblock_chain
s_lcm_sum_denominator_4 lcm_sum_numerator_2 lcm_sum__as3_type_Fracti
on fraction_cblock_chains_pieces_1_4 pieces_1_4 fraction_cblock_chains
_left_1024 fraction_cblock_chains_right_1389 fraction_cblock_chains_s
um_denominator_4 sum_numerator_1 sum__as3_type_Fraction fraction_cblo
ck_chains_lcm_sum_denominator_4 lcm_sum_numerator_1 lcm_sum__as3_typ
e_Fraction fraction_cblock_chains_pieces_1_4 fraction_cblock_chains_le
ft_1024 fraction_cblock_chains_right_1216 fraction_cblock_chains_sum_
denominator_4 sum_numerator_1 sum__as3_type_Fraction fraction_cblock_c

```


hains_lcm_sum_denominator_4 lcm_sum_numerator_1 lcm_sum__as3_type_Fraction fraction_cblock_chains_pieces_1_4 fraction_cblock_chains_left_1024 fraction_cblock_chains_right_1351 fraction_cblock_chains_sum_denominator_1 sum_numerator_1 sum__as3_type_Fraction fraction_cblock_chains_lcm_sum_denominator_1 lcm_sum_numerator_1 lcm_sum__as3_type_Fraction fraction_cblock_chains_pieces_1 fraction_cblock_chains_left_1024 fraction_cblock_chains_right_2045 fraction_cblock_chains_sum_denominator_1 sum_numerator_1 sum__as3_type_Fraction fraction_cblock_chains_lcm_sum_denominator_1 lcm_sum_numerator_1 lcm_sum__as3_type_Fraction fraction_cblock_chains_pieces_1 fraction_cblock_chains_left_130 fraction_cblock_chains_right_820 fraction_cblock_containment_bar1_sum_denominator_5 sum_numerator_2 sum__as3_type_Fraction bar1_bar1_pieces_1_10 pieces_1_10 pieces_1_10 pieces_1_10 bar1_lcm_sum_denominator_10 lcm_sum_numerator_4 lcm_sum__as3_type_Fraction fraction_cblock_containment_[Fraction] 1_4_sum_denominator_5 sum_numerator_1 sum__as3_type_Fraction [Fraction] 1_4_[Fraction] 1_4_pieces_1_5 [Fraction] 1_4_lcm_sum_denominator_5 lcm_sum_numerator_1 lcm_sum__as3_type_Fraction fraction_cblock_containment_[Fraction] 1_sum_denominator_10 sum_numerator_1 sum__as3_type_Fraction [Fraction] 1_[Fraction] 1_pieces_1_10 [Fraction] 1_lcm_sum_denominator_10 lcm_sum_numerator_1 lcm_sum__as3_type_Fraction fraction_cblock_total_count_41 fraction_cblock_counts_1_2 fraction_cblock_counts_1_7_7 fraction_cblock_counts_1_4_10 fraction_cblock_counts_1_6_6 fraction_cblock_counts_1_5_5 fraction_cblock_counts_1_2_1 fraction_cblock_counts_1_10_10 Model 4/10 on the black bar using the fraction pieces below. Answer: [object Object]

Sample number: 13

whole_fraction_input_value_4_6 fraction_cblock_chains_sum_denominator_3 sum_numerator_2 sum__as3_type_Fraction fraction_cblock_chains_lcm_sum_denominator_6 lcm_sum_numerator_4 lcm_sum__as3_type_Fraction fraction_cblock_chains_pieces_1_6 pieces_1_6 pieces_1_6 pieces_1_6 fraction_cblock_chains_left_96 fraction_cblock_chains_right_522 num_4 plain_image_groups_total_1 plain_image_groups_url_assets_cms_wootmath_fractions_number_line_markers_end_marker.swf plain_image_groups_total_1 plain_image_groups_url_assets_cms_wootmath_fractions_number_line_markers_start_marker.swf plain_image_groups_total_1 plain_image_groups_url_assets_cms_wootmath_fractions_number_line_objects_beetle.swf plain_image_groups_total_1 plain_image_groups_url_assets_cms_wootmath_fractions_number_line_objects_beetle_trail.swf den_6 fraction_cblock_total_count_4 fraction_cblock_counts_1_6_4 Use the 1/6 pieces to figure out how far the beetle traveled. Answer: 4/6

Sample number: 14

plain_image_groups_total_1 plain_image_groups_url_assets_cms_wootmath_fractions_number_line_objects_panda.swf plain_image_groups_total_1 plain_image_groups_url_assets_cms_wootmath_fractions_number_line_markers_start_marker.swf input_8 numberline_associations_position_634 numberline_associations_pos_value_0.88 numberline_associations_obj_name_object numberline_associations_fraction_cblock_chains_sum_denominator_8 sum_numerator_7 sum__as3_type_Fraction fraction_cblock_chains_lcm_sum_denominator_8 lcm_sum_numerator_7 lcm_sum__as3_type_Fraction fraction_cblock_chains_pieces_1_8 pieces_1_8 pieces_1_8 pieces_1_8 pieces_1_8 pieces_1_8 pieces_1_8 fraction_cblock_chains_left_165 fraction_cblock_chains_right_769 fraction_cblock_total_count_7 fraction_cblock_counts_1_8_7 Drag the panda to 7/8 of a yard from the start. Answer: 7/8

Sample number: 15

input_8 One yard on the number line is divided into Answer: sixths

Sample number: 16

numberline_associations_position_580.0 numberline_associations_pos_

value_1.0 numberline_associations_ obj_name_answer_text numberline_associations_ obj_value_3_3 input_ Drag the fraction to its correct location on the number line. Answer: $3/3$

Sample number: 17

plain_image_groups_ total_1 plain_image_groups_ url_assets_cms_wootmath_fractions_number_line_objects_shark.swf plain_image_groups_ total_1 plain_image_groups_ url_assets_cms_wootmath_fractions_number_line_markers_start_marker.swf input_6 numberline_associations_ position_722 numberline_associations_ pos_value_1.0 numberline_associations_ obj_name_object numberline_associations_ fraction_cblock_chains_ sum_ denominator_1 sum_ numerator_1 sum_ __as3_type_Fraction fraction_cblock_chains_ lcm_sum_ denominator_6 lcm_sum_ numerator_6 lcm_sum_ __as3_type_Fraction fraction_cblock_chains_ pieces_1_6 pieces_1_6 pieces_1_6 pieces_1_6 pieces_1_6 pieces_1_6 fraction_cblock_chains_ left_165 fraction_cblock_chains_ right_856 fraction_cblock_total_count_6 fraction_cblock_counts_ 1_6_6 Drag the shark to $1/6$ of a yard from the start. Answer: $1/6$

Sample number: 18

whole_ fraction_input_value_1_3 fraction_cblock_chains_ sum_ denominator_1 sum_ numerator_1 sum_ __as3_type_Fraction fraction_cblock_chains_ lcm_sum_ denominator_3 lcm_sum_ numerator_3 lcm_sum_ __as3_type_Fraction fraction_cblock_chains_ pieces_1_3 pieces_1_3 pieces_1_3 fraction_cblock_chains_ left_96 fraction_cblock_chains_ right_657 num_1 plain_image_groups_ total_1 plain_image_groups_ url_assets_cms_wootmath_fractions_number_line_markers_end_marker.swf plain_image_groups_ total_1 plain_image_groups_ url_assets_cms_wootmath_fractions_number_line_markers_start_marker.swf plain_image_groups_ total_1 plain_image_groups_ url_assets_cms_wootmath_fractions_number_line_objects_snail.swf plain_image_groups_ total_1 plain_image_groups_ url_assets_cms_wootmath_fractions_number_line_objects_snail_trail.swf den_3 fraction_cblock_total_count_3 fraction_cblock_counts_ 1_3_3 Use the $1/3$ pieces to figure out how far the snail traveled. Answer: $3/3$

Sample number: 19

whole_ fraction_input_value_3_4 fraction_cblock_chains_ sum_ denominator_4 sum_ numerator_3 sum_ __as3_type_Fraction fraction_cblock_chains_ lcm_sum_ denominator_4 lcm_sum_ numerator_3 lcm_sum_ __as3_type_Fraction fraction_cblock_chains_ pieces_1_4 pieces_1_4 pieces_1_4 fraction_cblock_chains_ left_96 fraction_cblock_chains_ right_545 num_3 plain_image_groups_ total_1 plain_image_groups_ url_assets_cms_wootmath_fractions_number_line_markers_end_marker_noline.swf plain_image_groups_ total_1 plain_image_groups_ url_assets_cms_wootmath_fractions_number_line_markers_start_marker.swf plain_image_groups_ total_1 plain_image_groups_ url_assets_cms_wootmath_fractions_number_line_objects_dog.swf plain_image_groups_ total_1 plain_image_groups_ url_assets_cms_wootmath_fractions_number_line_objects_cat_dog_trail.swf den_4 fraction_cblock_total_count_3 fraction_cblock_counts_ 1_4_3 Use the $1/4$ pieces to figure out how far the dog traveled. Answer: $3/4$

```
In [14]: data_samples = df3['response_doc']
```

```
In [15]: n_features = 1000
n_samples = len(data_samples)
n_topics = 50
n_top_words = 20
```

```
In [16]: print("Extracting tf-idf features ...")
tfidf_vectorizer = TfidfVectorizer(max_df=0.95, min_df=2,
                                   max_features=n_features,
                                   stop_words='english')

t0 = time()
tfidf = tfidf_vectorizer.fit_transform(data_samples)
print("done in %0.3fs." % (time() - t0))
```

Extracting tf-idf features ...
done in 7.887s.

```
In [17]: # Number of clusters
true_k = 100

km = MiniBatchKMeans(n_clusters=true_k, init='k-means++', n_init=1,
                    init_size=1000, batch_size=1000, random_state=42)
```

```
In [18]: print("Clustering with %s" % km)
t0 = time()
km.fit(tfidf)
print("done in %0.3fs" % (time() - t0))
print()
```

Clustering with MiniBatchKMeans(batch_size=1000, compute_labels=True, init='k-means++',
init_size=1000, max_iter=100, max_no_improvement=10,
n_clusters=100, n_init=1, random_state=42, reassignment_ratio=0.0
1,
tol=0.0, verbose=0)
done in 2.938s

```
In [19]: print("Top terms per cluster:")

order_centroids = km.cluster_centers_.argsort()[:, :-1]
terms = tfidf_vectorizer.get_feature_names()
for i in range(true_k):
    print("Cluster %d:\n" % i, end='')
    for ind in order_centroids[i, :30]:
        print(' --- %s\n' % terms[ind], end='')
    print()
```

Top terms per cluster:

Cluster 0:

```
--- write
--- used
--- divideboth
--- denominator
--- numerator
--- form
--- simplest
--- number
--- enter
--- divide
--- answer
--- 12
--- 15
--- 10
--- den_8
--- far
--- line
--- fraction_input_value_3_8
--- whole_
--- num_3
--- fraction
--- fraction_input_value_2_8
--- fraction_input_value_1_8
--- num_2
--- num_1
--- fraction_input_value_2_4
--- fraction_circle_containment_
--- fraction_circle_total_count_13
--- fraction_input_value_3
--- fraction_circle_total_count_12
```

Cluster 1:

```
--- fraction_cblock_chains_
--- pieces_1_8
--- lcm_sum_
--- sum_
--- __as3_type_fraction
--- denominator_8
--- numerator_1
--- denominator_1
--- bar1_
--- fraction_cblock_counts_
--- fraction
--- fraction_cblock_containment_
```

```
--- numerator_8
--- left_130
--- denominator_4
--- pieces_1
--- numerator_5
--- denominator_2
--- numerator_3
--- right_820
--- left_176
--- numerator_7
--- left_100
--- 1_4_
--- 1_8_8
--- bar2_
--- gray
--- pieces_1_4
--- bar
--- 1_1
```

Cluster 2:

```
--- pieces_1_12
--- fraction_circle_groups_
--- chains_
--- sum_
--- lcm_sum_
--- denominator_12
--- __as3_type_fraction
--- circle1_
--- fraction_circle_counts_
--- unit_
--- 12
--- unit1_
--- unit2_
--- fraction_circle_containment_
--- numerator_11
--- scale_0
--- fraction_cblock_chains_
--- object
--- pieces_1
--- numerator_12
--- y_350
--- scale_1
--- unit0_
--- 1_1
--- circle
--- 55
--- numerator_1
--- fraction
--- answer
--- twelfth
```

Cluster 3:

```
--- plain_image_groups_
--- pieces_1_9
--- fraction_cblock_chains_
--- total_1
--- swf
```

```
--- denominator_9
--- lcm_sum_
--- sum_
--- _as3_type_fraction
--- url_assets_cms_wootmath_fractions_number_line_markers_start_marker
--- left_96
--- bitmap_text_interp_
--- bitmap_text_inputs_
--- denominator_3
--- url_assets_cms_wootmath_fractions_number_line_markers_end_marker
--- 1_9_3
--- travel
--- 1_3_
--- fraction_cblock_counts_
--- did
--- input_a_3
--- numerator_2
--- yard
--- figure
--- fraction_cblock_total_count_3
--- use
--- far
--- 1_9_6
--- traveled
--- numerator_3
```

Cluster 4:

```
--- match
--- shade
--- fraction_input_value_
--- fraction
--- input_a_
--- choose
--- comparison
--- bar
--- correct
--- 1_3
--- 3_4
--- 1_4
--- 2_5
--- 1_6
--- 2_3
--- 6_8
--- 2_4
--- 3_5
--- 4_8
--- 3_6
--- equivalent
--- 1_8
--- 2_8
--- shaded
--- bitmap_text_inputs_
--- bitmap_text_interp_
--- enter
--- 4_6
--- answer
--- 3_8
```

Cluster 5:

```
--- fraction_circle_groups_  
--- circle1_1_  
--- circle1_2_  
--- lcm_sum_  
--- sum_  
--- fraction_circle_counts_  
--- y_350  
--- scale_1  
--- __as3_type_fraction  
--- numerator_1  
--- pieces_1_12  
--- object  
--- fraction_circle_containment_  
--- x_750  
--- chains_  
--- say  
--- x_250  
--- pieces_1_6  
--- pieces_1_4  
--- cover  
--- pieces_1_15  
--- pieces_1_8  
--- piece  
--- dark  
--- pieces_1_10  
--- blue  
--- denominator_12  
--- denominator_6  
--- left_270  
--- pieces_1_9
```

Cluster 6:

```
--- numberline_associations_  
--- line  
--- number  
--- location  
--- pos_value_0  
--- drag  
--- correct  
--- obj_value_a  
--- mile  
--- label  
--- pos_value_1  
--- biked  
--- divide  
--- ran  
--- obj_name_answer_text  
--- input_8  
--- lengths  
--- answer  
--- pos_value_2  
--- obj_name_answer_text1  
--- input_12  
--- obj_name_answer_text2  
--- labels
```

```
--- obj_name_a_text
--- total
--- stopped
--- distance
--- input_9
--- equal
--- 25
```

Cluster 7:

```
--- arrange
--- greatest
--- order
--- boxes
--- fractions
--- drag
--- fraction
--- 10
--- 81
--- 43
--- 42
--- 63
--- 51
--- 123
--- 52
--- 83
--- 54
--- 32
--- 31
--- answer
--- 44
--- 12
--- 41
--- decimals
--- 15
--- 73
--- 14
--- 16
--- 18
--- 20
```

Cluster 8:

```
--- plain_image_groups_
--- total_1
--- swf
--- choose
--- comparison
--- correct
--- url_assets_cms_wootmath_fractions_number_line_mug_mug_half_01
--- input_
--- input_a_
--- url_assets_cms_wootmath_fractions_number_line_juice_oj_tupperware_fo
urths_02
--- answer
--- fraction_cblock_total_count_7
--- fraction_cblock_total_count_8
--- fraction_circle_total_count_4
--- fraction_circle_total_count_3
```



```
--- fraction_circle_total_count_2
--- fraction_circle_total_count_16
--- fraction_circle_total_count_15
--- fraction_circle_total_count_14
--- fraction_cblock_total_count_4
--- fraction_circle_total_count_13
--- fraction_cblock_total_count_17
--- fraction_cblock_total_count_5
--- fraction_circle_total_count_12
--- fraction_circle_total_count_11
--- fraction_cblock_total_count_18
--- fraction_cblock_total_count_2
--- fraction_cblock_total_count_6
--- fraction_circle_total_count_5
--- fraction_circle_total_count_10
```

Cluster 9:

```
--- object
--- tenths
--- grid
--- hundredths
--- model
--- answer
--- decimal
--- tenth
--- 10
--- 15
--- 13
--- 11
--- 14
--- 16
--- 80
--- 12
--- 17
--- 18
--- 22
--- 20
--- 60
--- 40
--- 19
--- input_a_8
--- input_8
--- fraction_circle_total_count_7
--- fraction_circle_total_count_6
--- fraction_circle_total_count_5
--- fraction_circle_total_count_4
--- fraction_circle_total_count_8
```

Cluster 10:

```
--- pieces_1_12
--- fraction_circle_groups_
--- chains_
--- 1_2_
--- lcm_sum_
--- sum_
--- 1_3_
--- fraction
```

```
--- fraction_circle_counts_  
--- denominator_12  
--- __as3_type_fraction  
--- scale_1  
--- reds  
--- fraction_circle_containment_  
--- unit_  
--- right_270  
--- y_300  
--- x_300  
--- numerator_1  
--- l_12_6  
--- l_12_4  
--- input_a_6  
--- yellow  
--- input_6  
--- left_30  
--- equals  
--- numerator_6  
--- brown  
--- pieces_1_3  
--- fraction_circle_total_count_7
```

Cluster 11:

```
--- image_object_groups_  
--- 14  
--- total_14  
--- shade  
--- swf  
--- 12  
--- 11  
--- off_2  
--- off_4  
--- 10  
--- 13  
--- answer  
--- off_3  
--- off_6  
--- url_assets_objects_singles_piranha  
--- off_1  
--- piranhas  
--- off_5  
--- light  
--- robots  
--- on_2  
--- url_assets_objects_singles_cat  
--- url_assets_objects_singles_octopus  
--- cats  
--- on_0  
--- on_4  
--- on_1  
--- on_3  
--- popcorn  
--- boxes
```

Cluster 12:

```
--- fraction_input_value_1_7
```

```
--- den_7
--- num_1
--- whole_
--- smallest
--- enter
--- fraction
--- answer
--- plain_image_groups_
--- shaded
--- smaller
--- parts
--- circle
--- total_1
--- greatest
--- swf
--- equal
--- object
--- flower
--- wearing
--- 10
--- cats
--- polygon
--- piranhas
--- radio_text_is
--- common
--- radio_choice_b
--- fractions
--- choose
--- comparison
```

Cluster 13:

```
--- pieces_1_8
--- fraction_circle_groups_
--- chains_
--- sum_
--- lcm_sum_
--- fraction_circle_counts_
--- denominator_8
--- __as3_type_fraction
--- fraction
--- 1_2_
--- fraction_circle_containment_
--- pieces_1_4
--- piece_0_
--- scale_1
--- 1_4_
--- unit_
--- left_0
--- y_300
--- scale_0
--- unit1_
--- numerator_1
--- pieces_1
--- unit2_
--- x_512
--- denominator_4
--- circle1_
```

```
--- 1_8_4
--- 1_1
--- cover
--- numerator_2
```

Cluster 14:

```
--- pieces_1_10
--- fraction_cblock_chains_
--- sum_
--- lcm_sum_
--- __as3_type_fraction
--- denominator_10
--- numerator_1
--- denominator_1
--- fraction_cblock_counts_
--- bar1_
--- denominator_5
--- denominator_2
--- left_80
--- bar2_
--- unit1_
--- left_100
--- fraction_cblock_containment_
--- unit2_
--- pieces_1
--- numerator_5
--- numerator_3
--- 10
--- fraction
--- pieces_1_6
--- numerator_9
--- numerator_2
--- numerator_4
--- numerator_7
--- right_770
--- pieces_1_5
```

Cluster 15:

```
--- input_
--- input_a_
--- correct
--- enter
--- choose
--- comparison
--- 20
--- 100
--- 10
--- 50
--- 60
--- 30
--- 80
--- 40
--- answer
--- 12
--- 22
--- 11
--- 17
```

```
--- 16
--- 14
--- 24
--- 18
--- 52
--- 13
--- 32
--- 51
--- 42
--- 41
--- complete
```

Cluster 16:

```
--- radio_group_problem_
--- numerator
--- missing
--- object
--- enter
--- whole_
--- radio_choice_a
--- choice_a
--- denominator
--- radio_choice_b
--- choice_b
--- mult_n_1_
--- mult_d_1_
--- fraction
--- answer
--- den_6
--- num_1
--- den_10
--- den_8
--- num_4
--- den_15
--- fraction_input_value_1_6
--- estimate
--- den_12
--- num_7
--- den_4
--- num_2
--- fraction_input_value_1_10
--- num_3
--- greater
```

Cluster 17:

```
--- fraction_circle_groups_
--- y_350
--- scale_1
--- fraction_circle_counts_
--- say
--- object
--- cover
--- fraction_circle_total_count_2
--- x_750
--- piece
--- x_250
--- brown
```

```
--- orange
--- pink
--- dark
--- 1_3_1
--- blue
--- 1_5_1
--- pieces_1_3
--- reds
--- fraction_circle_total_count_1
--- red
--- pieces_1_5
--- yellow
--- 1_4_1
--- answer
--- 1_2_1
--- pieces_1_2
--- pieces_1_4
--- pinks
```

Cluster 18:

```
--- fraction_cblock_chains_
--- lcm_sum_
--- sum_
--- __as3_type_fraction
--- numerator_1
--- denominator_1
--- left_175
--- fraction_cblock_counts_
--- denominator_12
--- denominator_4
--- denominator_3
--- unit2_
--- right_865
--- pieces_1_6
--- denominator_8
--- pieces_1_12
--- pieces_1
--- unit1_
--- denominator_2
--- unit3_
--- pieces_1_3
--- pieces_1_4
--- denominator_6
--- fraction
--- left_90
--- denominator_9
--- fraction_cblock_containment_
--- 1_
--- numerator_2
--- pieces_1_8
```

Cluster 19:

```
--- 1_2_
--- fraction_circle_groups_
--- pieces_1_2
--- fraction
--- chains_
```

```
--- sum_  
--- lcm_sum_  
--- pieces_1_4  
--- denominator_2  
--- fraction_circle_counts_  
--- __as3_type_fraction  
--- 1_  
--- fraction_circle_containment_  
--- numerator_1  
--- scale_1  
--- numerator_2  
--- y_300  
--- fraction_circle_total_count_3  
--- 1_2_2  
--- input_2  
--- pieces_1  
--- yellows  
--- 1_1  
--- left_0  
--- input_a_2  
--- x_512  
--- circle  
--- 1_4_2  
--- x_300  
--- half
```

Cluster 20:

```
--- pieces_1_7  
--- fraction_cblock_chains_  
--- denominator_7  
--- lcm_sum_  
--- sum_  
--- __as3_type_fraction  
--- bar1_  
--- numerator_1  
--- left_130  
--- denominator_1  
--- bar  
--- fraction_cblock_counts_  
--- black  
--- object  
--- seventh  
--- right_820  
--- dragging  
--- fraction_cblock_containment_  
--- numerator_3  
--- 1_1  
--- numerator_5  
--- pieces_1  
--- numerator_4  
--- numerator_2  
--- numerator_6  
--- model  
--- pieces  
--- right_228  
--- light  
--- answer
```

Cluster 21:

```
--- pieces_1_15
--- fraction_cblock_chains_
--- lcm_sum_
--- sum_
--- denominator_15
--- __as3_type_fraction
--- numerator_1
--- fraction_cblock_counts_
--- denominator_1
--- left_90
--- denominator_3
--- numerator_2
--- 15
--- fraction
--- denominator_5
--- pieces_1_3
--- unit1_
--- bar1_
--- 1_3_
--- right_780
--- fraction_cblock_containment_
--- plain_image_groups_
--- pieces_1_5
--- pieces_1
--- pieces_1_12
--- unit_
--- numerator_5
--- unit2_
--- numerator_7
--- left_130
```

Cluster 22:

```
--- equivalent
--- box
--- drag
--- fraction
--- answer
--- 12
--- 10
--- youranswer
--- fraction_circle_total_count_16
--- fraction_circle_total_count_13
--- fraction_circle_total_count_14
--- fraction_circle_total_count_15
--- fraction_circle_total_count_4
--- fraction_circle_total_count_2
--- fraction_circle_total_count_3
--- fraction_circle_total_count_11
--- fraction_circle_total_count_5
--- fraction_circle_total_count_6
--- fraction_circle_total_count_12
--- fraction_circle_total_count_1
--- fraction_circle_total_count_10
--- fraction_circle_total_count_8
--- fraction_circle_groups_
```



```
--- fraction_circle_counts_  
--- fraction_circle_containment_  
--- fraction_cblock_total_count_9  
--- fraction_cblock_total_count_8  
--- fraction_cblock_total_count_7  
--- fraction_cblock_total_count_6  
--- fraction_cblock_total_count_5
```

Cluster 23:

```
--- area_target_contents_  
--- plain_image_groups_  
--- image_object_groups_  
--- x_468  
--- swf  
--- total_1  
--- y_118  
--- drag  
--- night  
--- piranhas  
--- answer  
--- chocolate  
--- pizza  
--- off_5  
--- fish  
--- tenths  
--- on_0  
--- on_3  
--- box  
--- 10  
--- number  
--- total_12  
--- correct  
--- off_6  
--- off_3  
--- total_9  
--- on_2  
--- off_2  
--- total_6  
--- on_4
```

Cluster 24:

```
--- yards  
--- fraction_input_value_  
--- long  
--- bar  
--- length  
--- whole_  
--- divide  
--- yard  
--- lengths  
--- fraction  
--- line  
--- number  
--- num_1  
--- equal  
--- enter  
--- den_8
```

```
--- den_6
--- den_input_8
--- num_2
--- den_input_6
--- den_2
--- den_4
--- parts
--- num_3
--- den_3
--- answer
--- den_input_4
--- den_input_3
--- den_1
--- num_4
```

Cluster 25:

```
--- shaded
--- whole_
--- parts
--- den_6
--- num_5
--- fraction
--- den_8
--- equal
--- fraction_input_value_5_6
--- answer
--- rectangle
--- num_4
--- fraction_input_value_2_6
--- polygon
--- fraction_input_value_5_8
--- star
--- num_2
--- flower
--- num_3
--- den_7
--- num_1
--- wearing
--- num_7
--- fraction_input_value_3_6
--- fraction_input_value_4_6
--- greatest
--- enter
--- fraction_input_value_4_8
--- fraction_input_value_1_6
--- fraction_input_value_1_8
```

Cluster 26:

```
--- pieces_1_5
--- fraction_circle_groups_
--- chains_
--- denominator_5
--- lcm_sum_
--- sum_
--- circle1_
--- fraction_circle_counts_
--- 1_
```

```
--- __as3_type_fraction
--- scale_0
--- fraction_circle_containment_
--- fraction
--- unit1_
--- scale_1
--- pieces_1
--- circle
--- unit2_
--- unit_
--- object
--- oranges
--- black
--- 1_5_5
--- x_300
--- numerator_3
--- 1_1
--- numerator_5
--- numerator_4
--- fifth
--- input_a_5
```

Cluster 27:

```
--- make
--- true
--- boxes
--- fractions
--- comparison
--- drag
--- answer
--- decimal
--- use
--- pieces
--- 12
--- tenths
--- numbers
--- statement
--- enter
--- 41
--- 54
--- 63
--- input_
--- 55
--- 42
--- 10
--- input_a_4
--- input_4
--- 58
--- input_a_6
--- input_6
--- 43
--- 73
--- input_1
```

Cluster 28:

```
--- pizza
--- ate
```

```
--- fraction_circle_groups_  
--- eat  
--- x_475  
--- friend  
--- did  
--- y_384  
--- fraction_circle_total_count_1  
--- scale_1  
--- l_1  
--- fraction_circle_counts_  
--- greater  
--- 10  
--- pieces_1  
--- half  
--- 12  
--- answer  
--- came  
--- cut  
--- way  
--- express  
--- radio_group_problem_  
--- simplest  
--- den_6  
--- cover  
--- fraction_input_value_1  
--- whole_1  
--- num_4  
--- model
```

Cluster 29:

```
--- complete  
--- sentence  
--- addition  
--- bitmap_text_inputs_  
--- bitmap_text_interp_  
--- problem_text_2  
--- problem_text_1_2  
--- input_b_2  
--- problem_text_3  
--- input_a_2  
--- problem_text_0  
--- answer  
--- input_a_3  
--- problem_text_1  
--- 2_8  
--- input_a_5  
--- input_a_4  
--- input_b_3  
--- 3_6  
--- multiplication  
--- input_5  
--- input_2  
--- input_a_1  
--- input_b_4  
--- 10  
--- 2_6  
--- input_3
```

```
--- input_4
--- 4_6
--- 6_8
```

Cluster 30:

```
--- pieces_1_6
--- fraction_circle_groups_
--- chains_
--- sum_
--- lcm_sum_
--- fraction_circle_counts_
--- __as3_type_fraction
--- denominator_6
--- fraction_circle_containment_
--- fraction
--- unit1_
--- piece_0_
--- 1_3_
--- scale_1
--- unit2_
--- scale_0
--- y_300
--- circle1_
--- unit_
--- pieces_1_3
--- numerator_1
--- 1_2_
--- pieces_1
--- piece_1_
--- left_0
--- denominator_3
--- numerator_2
--- 1_
--- x_512
--- right_120
```

Cluster 31:

```
--- fraction_circle_groups_
--- scale_0
--- fraction_circle_counts_
--- piece
--- unit_
--- x_200
--- x_675
--- scale_1
--- x_811
--- box
--- pieces_1_10
--- pieces_1_6
--- unit
--- pieces_1_9
--- fraction_circle_total_count_4
--- pieces
--- x_550
--- y_415
--- y_450
--- chains_
```

```
--- 1_10_1
--- y_300
--- drag
--- answer
--- pieces_1_4
--- half
--- 1_6_1
--- pieces_1_5
--- lcm_sum_
--- sum_
```

Cluster 32:

```
--- represented
--- input0_0
--- grid
--- enter
--- answer
--- decimal
--- 55
--- pieces
--- drag
--- 54
--- fraction_circle_total_count_2
--- fraction_circle_total_count_3
--- fraction_circle_total_count_15
--- fraction_circle_total_count_4
--- fraction_circle_total_count_5
--- fraction_circle_total_count_14
--- fraction_circle_total_count_6
--- fraction_circle_total_count_13
--- fraction_circle_total_count_12
--- fraction_circle_total_count_16
--- youranswer
--- fraction_circle_total_count_8
--- fraction_circle_total_count_11
--- fraction_circle_total_count_10
--- fraction_circle_total_count_1
--- fraction_circle_groups_
--- fraction_circle_counts_
--- fraction_circle_containment_
--- fraction_cblock_total_count_9
--- fraction_cblock_total_count_8
```

Cluster 33:

```
--- plain_image_groups_
--- total_1
--- swf
--- png
--- answer
--- url_assets_cms_wootmath_fractions_number_line_markers_start_marker
--- total_2
--- enter
--- length
--- input_a_0
--- start
--- url_assets_cms_wootmath_fractions_ui_right_arrow
--- url_assets_cms_wootmath_fractions_ui_left_arrow
```

```
--- arrows
--- decimal
--- use
--- distance
--- traveled
--- locations
--- points
--- whole_
--- shape
--- drag
--- far
--- correct
--- url_assets_cms_wootmath_fractions_number_line_markers_end_marker
--- url_assets_cms_wootmath_fractions_number_line_objects_v2_bubble_trai
1
--- label
--- url_assets_cms_wootmath_fractions_number_line_objects_v2_bug_trail
--- swam
```

Cluster 34:

```
--- 12
--- arrange
--- greatest
--- boxes
--- fractions
--- drag
--- fraction
--- 11
--- answer
--- 10
--- grid
--- model
--- 100
--- fraction_cblock_chains_
--- middle
--- fraction_cblock_total_count_1
--- greater
--- lcm_sum_
--- sum_
--- decimal
--- numerator_1
--- __as3_type_fraction
--- bar
--- denominator_12
--- left_1024
--- fraction_cblock_counts_
--- denominator_6
--- 1_12_1
--- form
--- denominator_3
```

Cluster 35:

```
--- pieces_1_9
--- fraction_cblock_chains_
--- lcm_sum_
--- sum_
--- denominator_9
```

```
--- __as3_type_fraction
--- numerator_1
--- bar1_
--- denominator_1
--- fraction_cblock_counts_
--- left_130
--- denominator_3
--- den_9
--- numerator_2
--- fraction_cblock_containment_
--- white
--- numerator_9
--- fraction
--- numerator_7
--- pieces_1_3
--- right_820
--- right_819
--- 1_1
--- pieces_1
--- 1_9_9
--- bar
--- numerator_8
--- fraction_cblock_total_count_10
--- 1_3_
--- whole_
```

Cluster 36:

```
--- object
--- whole_1
--- fraction_input_value_1
--- form
--- mixed
--- simplest
--- enter
--- number
--- answer
--- num_1
--- long
--- den_3
--- num_2
--- den_4
--- mile
--- swam
--- num_3
--- difference
--- left
--- den_2
--- yards
--- homework
--- den_6
--- 2_3
--- biked
--- den_8
--- 1_4
--- pizzas
--- express
--- plain_image_groups_
```


Cluster 37:

```
--- numberline_associations_  
--- plain_image_groups_  
--- mile  
--- shark  
--- final  
--- total_1  
--- swf  
--- location  
--- pos_value_0  
--- walked  
--- flew  
--- url_assets_cms_wootmath_fractions_number_line_markers_start_marker  
--- tenths  
--- obj_name_obj  
--- thenswam  
--- input_11  
--- swam  
--- drag  
--- start  
--- obj_name_object  
--- 10  
--- input_6  
--- answer  
--- tenth  
--- input_8  
--- position_490  
--- position_550  
--- position_260  
--- input_4  
--- 75
```

Cluster 38:

```
--- decimal  
--- object  
--- input_0  
--- input_a_0  
--- enter  
--- answer  
--- model  
--- grid  
--- 14  
--- represented  
--- 15  
--- 13  
--- 16  
--- 17  
--- 11  
--- 19  
--- 18  
--- 22  
--- 50  
--- pieces  
--- 25  
--- drag  
--- 12
```

```
--- 33
--- 24
--- 34
--- 42
--- input_
--- input_a_
--- 31
```

Cluster 39:

```
--- number
--- did
--- shown
--- line
--- youranswer
--- form
--- simplest
--- miles
--- enter
--- mixed
--- bike
--- swim
--- far
--- whole_2
--- fraction_input_value_2
--- den_5
--- run
--- den_4
--- whole_
--- whole_1
--- fraction_input_value_1
--- num_1
--- den_6
--- fraction
--- improper
--- 1_4
--- num_9
--- num_2
--- answer
--- num_3
```

Cluster 40:

```
--- pieces_1_3
--- fraction_circle_groups_
--- chains_
--- 1_
--- sum_
--- lcm_sum_
--- fraction_circle_counts_
--- denominator_3
--- fraction
--- __as3_type_fraction
--- fraction_circle_containment_
--- 1_3_3
--- browns
--- circle1_
--- scale_1
--- circle
```

```
--- unit1_  
--- unit2_  
--- pieces_1  
--- scale_0  
--- input_3  
--- black  
--- x_300  
--- input_a_3  
--- numerator_3  
--- fraction_circle_total_count_4  
--- y_300  
--- numerator_1  
--- l_1  
--- numerator_2
```

Cluster 41:

```
--- radio_text_  
--- choose  
--- comparison  
--- input_  
--- correct  
--- answer  
--- fraction_circle_total_count_11  
--- fraction_circle_total_count_12  
--- fraction_circle_total_count_13  
--- fraction_circle_total_count_15  
--- fraction_circle_total_count_14  
--- fraction_circle_total_count_1  
--- fraction_circle_total_count_16  
--- fraction_circle_total_count_2  
--- fraction_circle_total_count_3  
--- fraction_circle_total_count_4  
--- fraction_circle_total_count_10  
--- youranswer  
--- fraction_circle_total_count_5  
--- fraction_circle_counts_  
--- fraction_circle_containment_  
--- fraction_cblock_total_count_9  
--- fraction_cblock_total_count_8  
--- fraction_cblock_total_count_7  
--- fraction_cblock_total_count_6  
--- fraction_cblock_total_count_5  
--- fraction_cblock_total_count_4  
--- fraction_cblock_total_count_3  
--- fraction_cblock_total_count_2  
--- fraction_cblock_total_count_18
```

Cluster 42:

```
--- pieces_1_7  
--- fraction_circle_groups_  
--- chains_  
--- denominator_7  
--- sum_  
--- lcm_sum_  
--- l_  
--- fraction_circle_counts_  
--- __as3_type_fraction
```

```
--- unit1_  
--- fraction  
--- fraction_circle_containment_  
--- circle1_  
--- scale_0  
--- unit2_  
--- scale_1  
--- pieces_1  
--- light  
--- 1_7_7  
--- circle  
--- input_a_7  
--- input_7  
--- x_300  
--- blues  
--- y_350  
--- fraction_circle_total_count_8  
--- black  
--- 1_7_  
--- 1_1  
--- numerator_7
```

Cluster 43:

```
--- fraction_cblock_chains_  
--- pieces_1_6  
--- lcm_sum_  
--- sum_  
--- __as3_type_fraction  
--- denominator_6  
--- numerator_1  
--- denominator_1  
--- bar1_  
--- fraction_cblock_counts_  
--- denominator_3  
--- left_130  
--- numerator_2  
--- numerator_5  
--- fraction_cblock_containment_  
--- fraction  
--- pieces_1  
--- left_90  
--- denominator_2  
--- unit1_  
--- unit2_  
--- bar  
--- right_820  
--- numerator_4  
--- left_176  
--- numerator_6  
--- pieces_1_3  
--- object  
--- 1_  
--- 1_1
```

Cluster 44:

```
--- tothe  
--- ans1
```

```
--- fractions
--- denominator
--- box
--- numerator
--- ans0
--- drag
--- answer
--- ans2
--- greater
--- input_a_3
--- input_a_2
--- input_a_4
--- input_a_5
--- input_a_6
--- input_a_7
--- input_a_1
--- input_a_8
--- input_a_0
--- input_a_
--- input_a_10
--- fraction_circle_total_count_12
--- fraction_circle_total_count_11
--- fraction_circle_groups_
--- fraction_circle_total_count_10
--- fraction_circle_total_count_13
--- fraction_cblock_total_count_4
--- fraction_circle_total_count_1
--- fraction_cblock_total_count_5
```

Cluster 45:

```
--- whole_
--- greatest
--- enter
--- fraction
--- num_2
--- den_7
--- den_5
--- fraction_input_value_2_3
--- num_4
--- fraction_input_value_4_5
--- den_3
--- answer
--- num_3
--- fraction_input_value_2_5
--- num_6
--- num_5
--- smallest
--- den_8
--- den_6
--- fraction_input_value_4_6
--- wearing
--- num_1
--- greater
--- num_7
--- form
--- simplest
--- fraction_input_value_1_4
```

```
--- fraction_input_value_3_8
--- num_
--- 10
```

Cluster 46:

```
--- mug
--- hot
--- chocolate
--- plain_image_groups_
--- total_1
--- swf
--- whole_
--- num_1
--- fraction
--- url_assets_cms_wootmath_fractions_number_line_mug_mug_half_01
--- fraction_input_value_1_2
--- den_4
--- den_3
--- den_2
--- fraction_input_value_1_3
--- answer
--- fraction_input_value_1_4
--- num_2
--- fraction_input_value_2_4
--- fraction_input_value_2_3
--- fraction_input_value_3_4
--- num_3
--- fraction_input_value_1_5
--- den_5
--- den_1
--- num_
--- den_
--- num_4
--- fraction_input_value_
--- fraction_input_value_1_6
```

Cluster 47:

```
--- pieces_1_10
--- fraction_circle_groups_
--- chains_
--- sum_
--- lcm_sum_
--- denominator_10
--- fraction_circle_counts_
--- fraction
--- __as3_type_fraction
--- 1_2_
--- unit_
--- scale_1
--- fraction_circle_containment_
--- circle1_
--- 10
--- 1_5_
--- purples
--- 1_
--- x_300
--- numerator_1
```

```
--- fraction_cblock_chains_  
--- scale_0  
--- y_300  
--- numerator_10  
--- pieces_1  
--- right_270  
--- denominator_5  
--- 1_1  
--- 1_10_5  
--- 1_10_
```

Cluster 48:

```
--- box  
--- drag  
--- answer  
--- shown  
--- homework  
--- person  
--- equivalent  
--- piece  
--- fraction  
--- shows  
--- far  
--- traveled  
--- 25  
--- 51  
--- yellow  
--- decimal  
--- bar  
--- pieces  
--- greater  
--- 24  
--- brown  
--- half  
--- 22  
--- unit  
--- input_  
--- 34  
--- frog  
--- 42  
--- circle  
--- fifth
```

Cluster 49:

```
--- numberline_associations_  
--- plain_image_groups_  
--- total_1  
--- swf  
--- start  
--- obj_name_object  
--- url_assets_cms_wootmath_fractions_number_line_markers_start_marker  
--- pos_value_0  
--- meter  
--- fraction_cblock_chains_  
--- input_12  
--- beetle  
--- drag
```

```
--- yard
--- 10
--- lcm_sum_
--- sum_
--- answer
--- pieces_1_8
--- __as3_type_fraction
--- pieces_1_6
--- left_165
--- tenths
--- pos_value_1
--- input_8
--- url_assets_cms_wootmath_fractions_number_line_objects_v2_snail
--- fraction_cblock_counts_
--- input_6
--- butterfly
--- snail
```

Cluster 50:

```
--- pitcher
--- juice
--- plain_image_groups_
--- orange
--- total_1
--- whole_
--- swf
--- fraction
--- num_1
--- answer
--- den_3
--- den_4
--- num_2
--- den_6
--- den_8
--- fraction_input_value_1_2
--- den_2
--- fraction_input_value_1_3
--- url_assets_cms_wootmath_fractions_number_line_juice_oj_tupperware_fo
urths_02
--- num_3
--- fraction_input_value_2_3
--- fraction_input_value_1_6
--- fraction_input_value_3_4
--- fraction_input_value_1_4
--- fraction_input_value_1_8
--- fraction_input_value_2_4
--- num_4
--- fraction_input_value_2_6
--- num_6
--- num_5
```

Cluster 51:

```
--- den_9
--- whole_
--- smallest
--- fraction
--- fraction_input_value_1_9
```



```
--- enter
--- answer
--- num_5
--- num_2
--- shaded
--- num_4
--- num_1
--- greater
--- wearing
--- num_8
--- num_6
--- num_7
--- num_3
--- piranhas
--- smaller
--- cats
--- greatest
--- 10
--- 15
--- fractions
--- ate
--- 12
--- different
--- num_9
--- divided
```

Cluster 52:

```
--- pieces_1_15
--- fraction_circle_groups_
--- chains_
--- 1_5_
--- 1_3_
--- denominator_15
--- fraction
--- sum_
--- lcm_sum_
--- fraction_circle_counts_
--- scale_1
--- __as3_type_fraction
--- greens
--- fraction_circle_containment_
--- x_300
--- right_270
--- orange
--- y_300
--- 1_15_5
--- pieces_1_5
--- left_342
--- 1_15_3
--- numerator_1
--- 1_5_1
--- pieces_1_3
--- left_30
--- circle1_
--- 1_15_
--- brown
--- input_a_5
```

Cluster 53:

```
--- 19
--- hundredths
--- 24
--- grid
--- model
--- object
--- answer
--- decimal
--- 12
--- half
--- input_0
--- input_a_0
--- 31
--- enter
--- bigger
--- fraction_circle_total_count_16
--- fraction_circle_total_count_6
--- fraction_circle_total_count_7
--- fraction_circle_total_count_2
--- fraction_circle_total_count_15
--- fraction_circle_total_count_4
--- fraction_circle_total_count_5
--- fraction_circle_total_count_3
--- fraction_circle_total_count_11
--- fraction_circle_total_count_14
--- fraction_circle_total_count_13
--- fraction_circle_total_count_12
--- fraction_circle_total_count_9
--- fraction_circle_total_count_10
--- fraction_circle_total_count_1
```

Cluster 54:

```
--- object
--- decimals
--- shown
--- input_
--- input_a_
--- choose
--- comparison
--- correct
--- model
--- answer
--- fraction_circle_total_count_2
--- fraction_circle_total_count_16
--- fraction_circle_total_count_12
--- fraction_circle_total_count_3
--- fraction_circle_total_count_4
--- fraction_circle_total_count_15
--- fraction_circle_total_count_14
--- fraction_circle_total_count_13
--- youranswer
--- fraction_circle_total_count_5
--- fraction_circle_total_count_10
--- fraction_circle_total_count_1
--- fraction_circle_groups_
```

```
--- fraction_circle_counts_  
--- fraction_circle_containment_  
--- fraction_cblock_total_count_9  
--- fraction_cblock_total_count_8  
--- fraction_cblock_total_count_7  
--- fraction_cblock_total_count_6  
--- fraction_cblock_total_count_5
```

Cluster 55:

```
--- half  
--- hundredths  
--- input_0  
--- input_a_0  
--- enter  
--- 09  
--- bigger  
--- 14  
--- 13  
--- radio_group_problem_  
--- answer  
--- 17  
--- 15  
--- 41  
--- 11  
--- 12  
--- 22  
--- 16  
--- 34  
--- 18  
--- 33  
--- fraction_circle_groups_  
--- estimate  
--- 40  
--- 20  
--- ate  
--- piece  
--- 24  
--- bar  
--- radio_text_one
```

Cluster 56:

```
--- plain_image_groups_  
--- fraction_cblock_chains_  
--- total_1  
--- swf  
--- lcm_sum_  
--- sum_  
--- __as3_type_fraction  
--- url_assets_cms_wootmath_fractions_number_line_markers_start_marker  
--- traveled  
--- url_assets_cms_wootmath_fractions_number_line_markers_end_marker  
--- fraction_cblock_counts_  
--- numerator_1  
--- far  
--- left_96  
--- figure  
--- use
```

```
--- pieces_1_8
--- pieces_1_6
--- pieces_1_10
--- denominator_3
--- pieces_1_4
--- pieces_1_3
--- denominator_4
--- denominator_2
--- answer
--- pieces
--- distance
--- fraction_cblock_total_count_1
--- shows
--- fraction_cblock_total_count_2
```

Cluster 57:

```
--- numberline_associations_
--- obj_value_1
--- obj_value_0
--- location
--- line
--- number
--- correct
--- pos_value_1
--- drag
--- pos_value_0
--- miles
--- input_9
--- pos_value_
--- obj_name_answer_text
--- input_5
--- labels
--- answer
--- object
--- label
--- input_8
--- input_7
--- input_
--- input_10
--- input_15
--- 1_3
--- 83
--- input_12
--- position_450
--- 55
--- 1_4
```

Cluster 58:

```
--- words
--- model_lbl_0
--- express
--- decimal
--- tenths
--- bitmap_text_interp_
--- bitmap_text_inputs_
--- model
--- answer
```

```
--- input_b_4
--- input_b_5
--- input_b_6
--- input_b_7
--- input_a_4
--- input_b_8
--- input_b_1
--- input_a_9
--- input_a_6
--- input_a_5
--- tenth
--- input_a_7
--- input_b_3
--- input_a_8
--- input_a_1
--- input_a_3
--- input_b_2
--- input_a_2
--- 10
--- input_a_
--- input_a_10
```

Cluster 59:

```
--- fraction_input_value_1_5
--- den_5
--- num_1
--- whole_
--- wearing
--- fraction
--- answer
--- num_3
--- shaded
--- robots
--- enter
--- plain_image_groups_
--- smallest
--- piranhas
--- smaller
--- circle
--- popcorn
--- total_1
--- rectangle
--- swf
--- greater
--- form
--- simplest
--- greatest
--- cats
--- boxes
--- object
--- 15
--- 10
--- fractions
```

Cluster 60:

```
--- image_object_groups_
--- shade
```

```
--- swf
--- off_2
--- total_8
--- on_0
--- 11
--- on_4
--- off_1
--- answer
--- on_2
--- on_3
--- off_3
--- off_4
--- 13
--- off_6
--- on_1
--- total_6
--- total_12
--- url_assets_objects_singles_cat
--- url_assets_objects_singles_octopus
--- cats
--- 12
--- 15
--- url_assets_objects_singles_piranha
--- total_3
--- total_9
--- 10
--- off_5
--- light
```

Cluster 61:

```
--- fraction_circle_groups_
--- unit_
--- lcm_sum_
--- sum_
--- unit1_
--- unit2_
--- fraction_circle_counts_
--- scale_0
--- __as3_type_fraction
--- numerator_1
--- fraction_circle_containment_
--- pieces_1_2
--- denominator_2
--- pieces_1
--- pieces_1_3
--- y_350
--- fraction_circle_total_count_2
--- denominator_3
--- y_300
--- x_512
--- x_700
--- 1_1
--- fraction_circle_total_count_4
--- bigger
--- pieces_1_4
--- 125
--- fraction
```

```
--- 1_2
--- answer
--- x_250
```

Cluster 62:

```
--- using
--- model
--- answer
--- equivalent
--- fraction
--- size
--- greater
--- pieces
--- thirds
--- browns
--- sixths
--- equal
--- fourths
--- cover
--- yellow
--- yellows
--- pinks
--- grays
--- piece
--- dark
--- blues
--- fifths
--- halves
--- oranges
--- smaller
--- cake
--- reds
--- pink
--- blue
--- fraction_circle_groups_
```

Cluster 63:

```
--- fraction_input_value_2_4
--- den_4
--- num_2
--- whole_
--- enter
--- fraction
--- answer
--- greatest
--- fractions
--- greater
--- different
--- smallest
--- equal
--- shaded
--- popcorn
--- plain_image_groups_
--- long
--- form
--- simplest
--- numerator
```

```
--- wearing
--- missing
--- parts
--- smaller
--- boxes
--- total_1
--- swf
--- flower
--- 12
--- rectangle
```

Cluster 64:

```
--- plain_image_groups_
--- url_assets_cms_wootmath_fractions_misc_objects_ant_alt
--- url_assets_cms_wootmath_fractions_misc_objects_ladybug_alt
--- bugs
--- ladybugs
--- swf
--- total_2
--- form
--- simplest
--- total_3
--- enter
--- whole_
--- total_4
--- num_1
--- fraction_input_value_1_2
--- den_2
--- fraction
--- answer
--- total_6
--- den_3
--- den_4
--- num_2
--- fraction_input_value_1_3
--- total_1
--- num_3
--- fraction_input_value_2_3
--- fraction_input_value_1_4
--- fraction_input_value_3_4
--- total_9
--- fraction_input_value_2_4
```

Cluster 65:

```
--- numberline_associations_
--- mile
--- plain_image_groups_
--- kangaroo
--- url_assets_cms_wootmath_fractions_number_line_objects_v2_kangaroo
--- obj_name_object
--- pos_value_0
--- total_1
--- swf
--- lengths
--- drag
--- divide
--- line
```



```
--- equal
--- bitmap_text_interp_
--- bitmap_text_inputs_
--- number
--- answer
--- den_input_6
--- den_input_3
--- den_input_8
--- input_5
--- den_input_4
--- 25
--- position_260
--- input_4
--- position_200
--- url_assets_cms_wootmath_fractions_number_line_objects_v2_giraffe
--- giraffe
--- panda
```

Cluster 66:

```
--- amounts
--- model
--- answer
--- tenths
--- box
--- drag
--- fraction_circle_total_count_4
--- fraction_circle_total_count_3
--- fraction_circle_total_count_2
--- fraction_circle_total_count_5
--- fraction_circle_total_count_6
--- fraction_circle_total_count_15
--- fraction_circle_total_count_14
--- fraction_circle_total_count_13
--- fraction_circle_total_count_12
--- fraction_circle_total_count_11
--- fraction_circle_total_count_16
--- youranswer
--- fraction_circle_total_count_1
--- fraction_circle_groups_
--- fraction_circle_counts_
--- fraction_circle_containment_
--- fraction_cblock_total_count_9
--- fraction_cblock_total_count_8
--- fraction_cblock_total_count_7
--- fraction_cblock_total_count_6
--- fraction_cblock_total_count_5
--- fraction_cblock_total_count_4
--- fraction_cblock_total_count_3
--- fraction_cblock_total_count_2
```

Cluster 67:

```
--- makes
--- statement
--- true
--- bitmap_text_interp_
--- bitmap_text_inputs_
--- number
```

```
--- enter
--- input_1
--- input_3
--- input_a_3
--- input_a_1
--- input_a_5
--- input_a_4
--- input_5
--- input_4
--- input_2
--- 10
--- input_a_2
--- input_a_6
--- input_6
--- 12
--- input_a_7
--- input_7
--- input_0
--- input_a_0
--- input_a_8
--- input_8
--- input_a_10
--- input_10
--- input_a_9
```

Cluster 68:

```
--- fraction_circle_groups_
--- fraction_circle_counts_
--- fraction_circle_total_count_1
--- scale_1
--- x_300
--- circle1_
--- circle
--- dark
--- yellow
--- say
--- cover
--- y_350
--- black
--- fraction_circle_total_count_2
--- blue
--- y_300
--- pieces_1
--- piece
--- answer
--- 1_1
--- pieces_1_2
--- sum_
--- lcm_sum_
--- grays
--- blues
--- equals
--- pieces_1_4
--- 1_2_1
--- equal
--- input_a_1
```

Cluster 69:

```
--- 15
--- den_15
--- whole_
--- smallest
--- enter
--- fraction
--- answer
--- 13
--- num_2
--- smaller
--- numerator
--- 11
--- num_11
--- num_1
--- denominator
--- greatest
--- greater
--- num_7
--- 12
--- num_4
--- grid
--- num_8
--- num_5
--- num_3
--- num_10
--- 14
--- num_9
--- model
--- 100
--- missing
```

Cluster 70:

```
--- fraction_cblock_chains_
--- sum_
--- lcm_sum_
--- bar1_
--- __as3_type_fraction
--- numerator_1
--- left_130
--- bar
--- denominator_1
--- fraction_cblock_counts_
--- black
--- object
--- right_820
--- dragging
--- fraction_cblock_total_count_2
--- denominator_3
--- denominator_2
--- 1_1
--- fraction_cblock_containment_
--- pieces_1_3
--- model
--- pieces_1
--- piece
--- pieces_1_2
```

```
--- numerator_2
--- denominator_6
--- denominator_5
--- denominator_12
--- denominator_9
--- fraction_cblock_total_count_3
```

Cluster 71:

```
--- comparison1
--- input_
--- input_a_
--- correct
--- enter
--- 100
--- 50
--- 22
--- 20
--- 24
--- 12
--- 40
--- 51
--- 11
--- 60
--- 30
--- 52
--- 10
--- 13
--- 19
--- 32
--- 25
--- 31
--- 14
--- 16
--- 80
--- 15
--- 18
--- fraction_circle_total_count_11
--- fraction_input_value_
```

Cluster 72:

```
--- numberline_associations_
--- obj_value_
--- label
--- yard
--- location
--- line
--- obj_name_eqn
--- number
--- pos_value_1
--- correct
--- drag
--- fraction_cblock_chains_
--- obj_name_answer_text
--- input_
--- pos_value_0
--- answer
--- lcm_sum_
```

```
--- sum_  
--- miles  
--- __as3_type_fraction  
--- input_8  
--- pieces_1_4  
--- input_6  
--- position_450  
--- pieces_1_3  
--- mile  
--- pos_value_  
--- fraction_cblock_counts_  
--- input_7  
--- numerator_1
```

Cluster 73:

```
--- plain_image_groups_  
--- radio_group_mc1_  
--- radio_group_mc2_  
--- text_yes  
--- choice_a  
--- total_1  
--- swf  
--- shapes  
--- object  
--- shaded  
--- text_no  
--- choice_b  
--- url_assets_cms_wootmath_fractions_equal_parts_fourths_fourth_03  
--- answer  
--- radio_group_problem_  
--- radio_choice_a  
--- denominator  
--- numerator  
--- fraction  
--- fraction_cblock_total_count_2  
--- fraction_cblock_total_count_3  
--- fraction_circle_total_count_13  
--- fraction_circle_total_count_12  
--- fraction_circle_total_count_11  
--- fraction_circle_total_count_10  
--- fraction_circle_total_count_1  
--- fraction_cblock_total_count_7  
--- fraction_circle_groups_  
--- fraction_circle_counts_  
--- fraction_cblock_total_count_4
```

Cluster 74:

```
--- grid  
--- model  
--- 10  
--- answer  
--- 100  
--- 11  
--- numbers  
--- 14  
--- 13  
--- boxes
```

```
--- drag
--- hundredths
--- decimal
--- 09
--- use
--- shown
--- covering
--- 18
--- pieces
--- 22
--- 17
--- 16
--- think
--- 20
--- 15
--- came
--- pizza
--- 1_10
--- cut
--- piece
```

Cluster 75:

```
--- bitmap_text_inputs_
--- bitmap_text_interp_
--- input_a_1
--- enter
--- missing
--- fraction_input_value_
--- form
--- simplest
--- numerator
--- input_a_2
--- answer
--- sum
--- fraction
--- numbers
--- 12
--- input_6
--- 10
--- input_a_6
--- 2_4
--- input_1
--- eqn_2
--- input_a_3
--- input_2
--- input_b_6
--- input_5
--- 15
--- 1_2
--- input_b_8
--- 2_3
--- input_a_5
```

Cluster 76:

```
--- problem_text_1
--- complete
--- addition
```

```
--- sentence
--- problem_text_1_2
--- bitmap_text_interp_
--- bitmap_text_inputs_
--- input_b_1
--- input_a_1
--- 1_8
--- 1_6
--- problem_text_0
--- input_1
--- 1_4
--- problem_text_2
--- answer
--- 1_10
--- input_a_2
--- 3_4
--- problem_text_3
--- 2_6
--- 4_6
--- 5_6
--- input_a_3
--- 6_8
--- input_b_2
--- 2_4
--- 2_8
--- input_a_0
--- 1_9
```

Cluster 77:

```
--- long
--- fraction_input_value_
--- bitmap_text_inputs_
--- bitmap_text_interp_
--- bar
--- fraction
--- answer
--- input_a_3
--- input_a_4
--- input_a_6
--- input_a_2
--- input_a_8
--- fourths
--- thirds
--- halves
--- sixths
--- input_a_1
--- 2_4
--- 2_3
--- eighths
--- 1_2
--- input_a_
--- 1_8
--- 3_4
--- input_a_5
--- fraction_circle_total_count_15
--- fraction_circle_total_count_14
--- fraction_circle_total_count_13
```

```
--- fraction_circle_total_count_16
--- fraction_cblock_total_count_9
```

Cluster 78:

```
--- fraction_input_value_1_2
--- den_2
--- num_1
--- whole_
--- 50
--- 100
--- enter
--- answer
--- form
--- simplest
--- fractions
--- greater
--- fraction
--- different
--- smallest
--- plain_image_groups_
--- express
--- 10
--- greatest
--- long
--- 12
--- total_1
--- swf
--- object
--- numerator
--- common
--- left
--- 30
--- multiplication
--- makes
```

Cluster 79:

```
--- fraction_cblock_chains_
--- lcm_sum_
--- sum_
--- pieces_1_4
--- __as3_type_fraction
--- denominator_4
--- numerator_1
--- bar1_
--- denominator_1
--- fraction_cblock_counts_
--- left_130
--- right_820
--- denominator_2
--- bar
--- numerator_3
--- fraction_cblock_containment_
--- pieces_1
--- numerator_2
--- 1_1
--- black
--- object
```



```
--- fourth
--- fraction
--- numerator_4
--- 1_4_4
--- dark
--- model
--- blue
--- 1_4_2
--- right_475
```

Cluster 80:

```
--- math
--- sentence
--- complete
--- tenths
--- correct
--- drag
--- answer
--- people
--- equally
--- amounts
--- undefined
--- express
--- object
--- cookies
--- bitmap_text_inputs_
--- bitmap_text_interp_
--- pizzas
--- 10
--- input_a_6
--- input_6
--- input_1
--- numbers
--- input_a_1
--- input_a_5
--- input_5
--- boxes
--- greater
--- input_a_2
--- input_2
--- 11
```

Cluster 81:

```
--- object
--- form
--- simplest
--- enter
--- answer
--- num_1
--- whole_3
--- fraction_input_value_3
--- mixed
--- fraction_input_value_2
--- whole_2
--- difference
--- number
--- sum
```

```
--- whole_  
--- num_3  
--- den_6  
--- den_3  
--- bar  
--- mult_d_1_  
--- mult_n_1_  
--- den_2  
--- den_4  
--- long  
--- black  
--- den_10  
--- model  
--- num_2  
--- den_5  
--- dragging
```

Cluster 82:

```
--- pieces_1_9  
--- fraction_circle_groups_  
--- chains_  
--- denominator_9  
--- sum_  
--- lcm_sum_  
--- fraction_circle_counts_  
--- 1_3_  
--- fraction  
--- __as3_type_fraction  
--- circle1_  
--- scale_1  
--- 1_  
--- fraction_circle_containment_  
--- whites  
--- x_300  
--- unit1_  
--- brown  
--- 1_9_3  
--- y_300  
--- unit2_  
--- pieces_1_3  
--- pieces_1  
--- numerator_1  
--- circle  
--- scale_0  
--- 1_3_1  
--- unit_  
--- 1_1  
--- 1_9_
```

Cluster 83:

```
--- mult_n_2_  
--- mult_d_2_  
--- mult_d_1_  
--- mult_n_1_  
--- enter  
--- bitmap_text_inputs_  
--- bitmap_text_interp_
```

```
--- form
--- simplest
--- answer
--- difference
--- missing
--- 10
--- numerator
--- 15
--- fraction_input_value_1
--- whole_1
--- whole_
--- den_12
--- 12
--- input_a_1
--- num_11
--- sum
--- den_15
--- 1_10
--- equation_2
--- equation_6
--- 1_5
--- 11
--- input_b_6
```

Cluster 84:

```
--- fraction_input_value_3_4
--- num_3
--- den_4
--- whole_
--- greatest
--- enter
--- fraction
--- answer
--- plain_image_groups_
--- long
--- shaded
--- total_1
--- swf
--- greater
--- piranhas
--- form
--- simplest
--- fractions
--- smallest
--- friends
--- 75
--- ate
--- pizza
--- eat
--- wearing
--- missing
--- did
--- numerator
--- object
--- difference
```

Cluster 85:

```
--- pieces_1_4
--- fraction_circle_groups_
--- chains_
--- sum_
--- lcm_sum_
--- fraction_circle_counts_
--- denominator_4
--- __as3_type_fraction
--- 1_
--- fraction_circle_containment_
--- unit_
--- scale_1
--- unit1_
--- fraction
--- piece_0_
--- circle1_
--- pieces_1
--- unit2_
--- scale_0
--- y_300
--- numerator_1
--- 1_4_4
--- 1_1
--- circle
--- fraction_circle_total_count_5
--- numerator_4
--- x_300
--- dark
--- black
--- right_180
```

Cluster 86:

```
--- den_12
--- smallest
--- 12
--- whole_
--- fraction_input_value_1_12
--- enter
--- fraction
--- smaller
--- answer
--- num_2
--- num_1
--- num_4
--- num_3
--- num_6
--- divided
--- num_5
--- num_7
--- greatest
--- num_9
--- 10
--- fraction_input_value_2_6
--- 15
--- den_6
--- greater
--- num_8
```

```
--- num_10
--- fractions
--- ate
--- complete
--- write
```

Cluster 87:

```
--- pieces_1_8
--- fraction_cblock_chains_
--- lcm_sum_
--- sum_
--- bar1_
--- __as3_type_fraction
--- denominator_8
--- left_130
--- numerator_1
--- bar
--- black
--- object
--- fraction_cblock_counts_
--- eighth
--- denominator_1
--- right_820
--- numerator_3
--- dragging
--- 1_1
--- denominator_4
--- pieces
--- fraction_cblock_containment_
--- numerator_5
--- model
--- pieces_1
--- numerator_7
--- numerator_6
--- numerator_4
--- numerator_2
--- right_302
```

Cluster 88:

```
--- numberline_associations_
--- plain_image_groups_
--- obj_name_object
--- mile
--- pos_value_0
--- total_1
--- swf
--- drag
--- input_5
--- url_assets_cms_wootmath_fractions_number_line_objects_v2_elephant
--- elephant
--- panda
--- url_assets_cms_wootmath_fractions_number_line_objects_v2_panda
--- hippo
--- rex
--- url_assets_cms_wootmath_fractions_number_line_objects_v2_trex
--- answer
--- url_assets_cms_wootmath_fractions_number_line_objects_v2_hippo
```

```
--- input_4
--- url_assets_cms_wootmath_fractions_number_line_objects_v2_giraffe
--- giraffe
--- input_7
--- input_3
--- 25
--- position_260
--- 17
--- pos_value_1
--- 75
--- input_9
--- position_200
```

Cluster 89:

```
--- pieces_1_12
--- fraction_circle_groups_
--- chains_
--- frac_piece_
--- fraction_circle_counts_
--- lcm_sum_
--- sum_
--- scale_1
--- denominator_12
--- __as3_type_fraction
--- 1_4_
--- fraction
--- fraction_circle_containment_
--- reds
--- numerator_1
--- 1_6_
--- piece1_
--- x_300
--- 1_12_3
--- piece
--- pieces_1_4
--- circle1_
--- cover
--- piece_0_
--- 1_12_2
--- left_270
--- y_350
--- y_300
--- 12
--- pieces_1_3
```

Cluster 90:

```
--- rectangle
--- fraction_input_value_
--- fraction
--- shade
--- shaded
--- 2_6
--- match
--- circle
--- 4_8
--- answer
--- object
```

```
--- input_a_3
--- 12
--- equivalent
--- input_a_2
--- 2_8
--- problem
--- input_a_6
--- 24
--- radio_choice_b
--- 13
--- 10
--- 16
--- 3_8
--- input_a_8
--- 15
--- input_a_4
--- 4_6
--- 1_4
--- input_12
```

Cluster 91:

```
--- whole_
--- 10
--- answer
--- den_10
--- fraction
--- enter
--- smallest
--- num_1
--- different
--- den_8
--- mile
--- greater
--- run
--- make
--- smaller
--- fraction_input_value_1_8
--- popcorn
--- bar
--- number
--- num_7
--- fraction_input_value_1_10
--- think
--- ran
--- 20
--- fractions
--- 24
--- ate
--- num_2
--- block
--- cake
```

Cluster 92:

```
--- den_12
--- whole_
--- num_10
--- 12
```

```
--- enter
--- greatest
--- fraction
--- answer
--- missing
--- 10
--- numerator
--- greater
--- ate
--- num_7
--- num_6
--- num_2
--- num_9
--- different
--- num_11
--- fractions
--- smaller
--- num_4
--- 11
--- num_5
--- num_3
--- equal
--- difference
--- shaded
--- numbers
--- write
```

Cluster 93:

```
--- fraction_cblock_chains_
--- pieces_1_5
--- lcm_sum_
--- sum_
--- denominator_5
--- __as3_type_fraction
--- numerator_1
--- bar1_
--- denominator_1
--- fraction_cblock_counts_
--- numerator_3
--- numerator_2
--- left_130
--- left_80
--- numerator_4
--- bar
--- fraction_cblock_containment_
--- unit2_
--- pieces_1
--- right_820
--- object
--- black
--- numerator_5
--- right_770
--- model
--- fraction
--- 1_5_5
--- fifth
--- left_90
```



```
--- unit1_  
  
Cluster 94:  
--- match  
--- fraction_input_value_  
--- shade  
--- fraction  
--- input_a_  
--- choose  
--- comparison  
--- correct  
--- circle  
--- flower  
--- polygon  
--- 1_3  
--- 2_3  
--- 4_8  
--- 3_8  
--- 3_6  
--- 1_6  
--- 2_4  
--- 1_4  
--- 4_6  
--- 2_8  
--- 3_5  
--- 2_5  
--- 2_6  
--- 5_6  
--- 6_8  
--- 1_8  
--- 12  
--- 1_9  
--- 10  
  
Cluster 95:  
--- pieces_1_12  
--- fraction_cblock_chains_  
--- sum_  
--- lcm_sum_  
--- __as3_type_fraction  
--- numerator_1  
--- denominator_12  
--- fraction_cblock_counts_  
--- left_100  
--- denominator_1  
--- denominator_2  
--- bar2_  
--- bar1_  
--- fraction_cblock_containment_  
--- fraction  
--- right_790  
--- denominator_3  
--- pieces_1  
--- right_445  
--- denominator_4  
--- 1_4_  
--- left_176
```

```
--- pieces_1_2
--- numerator_6
--- piece0_
--- 12
--- 1_3_
--- numerator_3
--- numerator_2
--- plain_image_groups_
```

Cluster 96:

```
--- fraction_cblock_chains_
--- lcm_sum_
--- sum_
--- __as3_type_fraction
--- numerator_1
--- bar2_
--- bar1_
--- left_100
--- denominator_1
--- denominator_2
--- fraction_cblock_counts_
--- right_790
--- fraction_cblock_containment_
--- pieces_1
--- denominator_3
--- pieces_1_2
--- denominator_4
--- bar0_
--- pieces_1_6
--- pieces_1_4
--- numerator_2
--- left_60
--- bar3_
--- left_200
--- denominator_6
--- right_445
--- pieces_1_8
--- pieces_1_3
--- 1_2
--- model
```

Cluster 97:

```
--- divided
--- fifths
--- yard
--- input_7
--- line
--- number
--- answer
--- sixths
--- input_a_2
--- input_8
--- input_a_4
--- input_a_3
--- input_a_6
--- input_a_1
--- input_a_5
```

```
--- input_a_8
--- num_1
--- whole_
--- object
--- fraction_input_value_1_6
--- mixed
--- fraction_input_value_1_8
--- fraction_input_value_1_4
--- den_6
--- enter
--- den_8
--- den_4
--- 18
--- input_a_9
--- rectangle
```

Cluster 98:

```
--- star
--- match
--- shade
--- fraction_input_value_
--- fraction
--- input_a_
--- choose
--- comparison
--- correct
--- 3_4
--- 1_4
--- 1_5
--- 1_8
--- 4_6
--- 2_5
--- 5_6
--- 2_8
--- 4_8
--- 6_8
--- 2_4
--- fraction_circle_total_count_6
--- fraction_circle_total_count_16
--- fraction_circle_total_count_5
--- fraction_circle_total_count_4
--- fraction_circle_total_count_3
--- fraction_circle_total_count_2
--- youranswer
--- fraction_circle_total_count_15
--- fraction_circle_total_count_14
--- fraction_circle_total_count_13
```

Cluster 99:

```
--- fraction_cblock_chains_
--- lcm_sum_
--- sum_
--- __as3_type_fraction
--- numerator_1
--- denominator_8
--- pieces_1_8
--- denominator_1
```

```

--- fraction_cblock_counts_
--- denominator_4
--- left_80
--- left_90
--- fraction
--- pieces_1
--- pieces_1_4
--- 1_
--- numerator_3
--- unit2_
--- fraction_cblock_containment_
--- left_176
--- denominator_2
--- right_780
--- right_770
--- numerator_2
--- left_150
--- right_262
--- 1_2
--- denominator_7
--- unit_
--- 1_8_

```

```
In [20]: df3['cluster_100'] = km.labels_
```

```
In [21]: df3['trait_1'] = df3['behavioral_traits'].apply(lambda x : x[0] if len(x) >
df3['trait_2'] = df3['behavioral_traits'].apply(lambda x : x[1] if len(x) >
```

```
In [22]: df_trait_1 = df3.groupby(['cluster_100', 'trait_1']).size().unstack(fill_val
df_trait_2 = df3.groupby(['cluster_100', 'trait_2']).size().unstack(fill_val
```

```
In [23]: df_cluster_100 = df3.groupby('cluster_100')
```

```
In [24]: df_trait_1.index.rename('cluster_100', inplace=True)
df_trait_2.index.rename('cluster_100', inplace=True)
df_traits = pd.concat([df_trait_1, df_trait_2], axis=1)
```

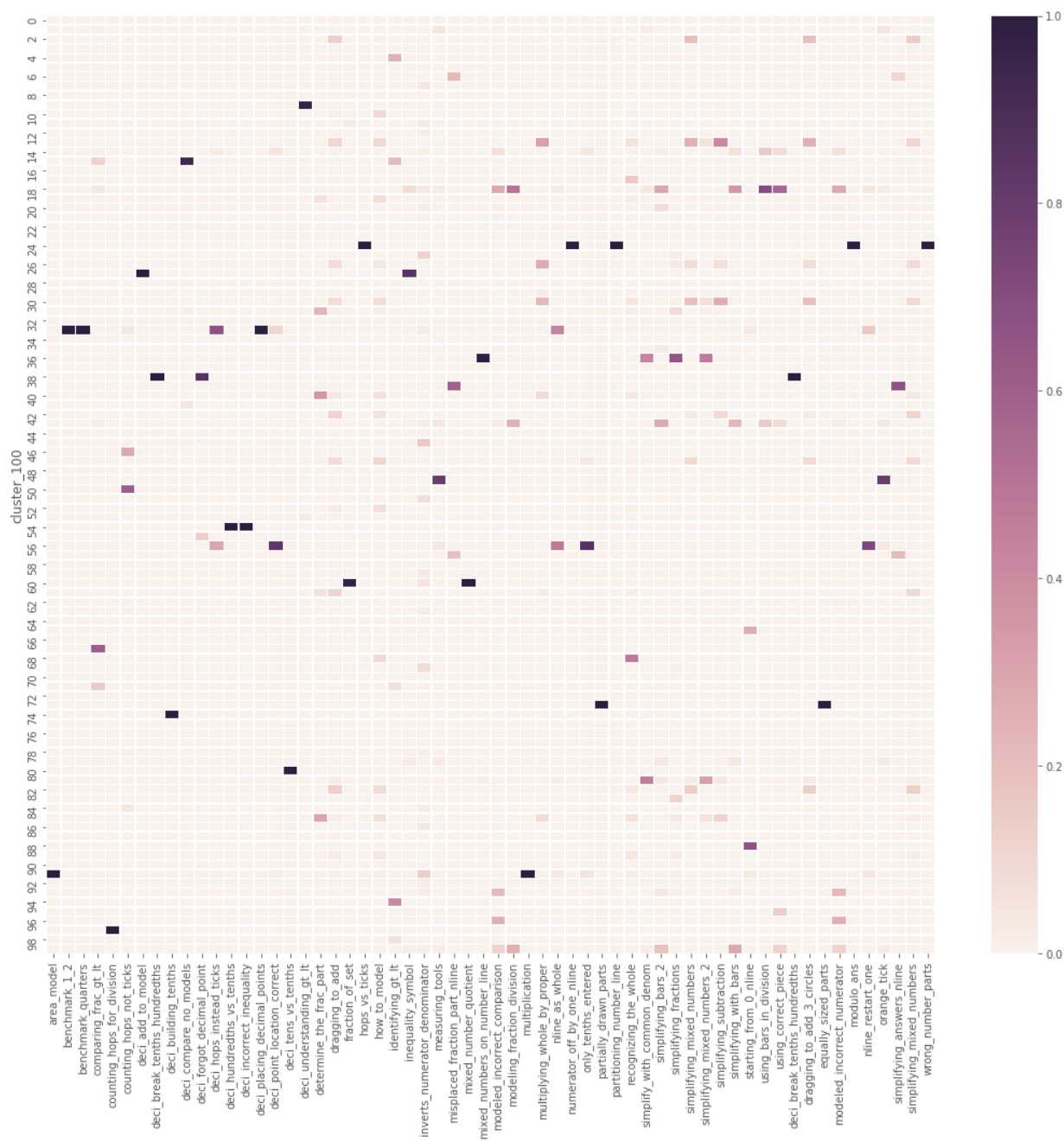
```
In [25]: df_traits = df_traits.drop('None', axis=1)
```

```
In [26]: #df_traits_norm = (df_traits - df_traits.mean()) / (df_traits.max() - df_traits.min())
df_traits_norm = (df_traits / (df_traits.sum())) )
```

```
In [27]: fig = plt.figure(figsize=(18.5, 16))
cmap = sns.cubehelix_palette(light=.95, as_cmap=True)
sns.heatmap(df_traits_norm, cmap=cmap, linewidths=.5)

#sns.heatmap(df_traits_norm, cmap="YlGnBu", linewidths=.5)
```

Out[27]: <matplotlib.axes._subplots.AxesSubplot at 0x11c6da7b8>



In []:

In []:

