1 Introduction

Consider the linear convection-diffusion equation

$$\frac{\partial T}{\partial t} + v \frac{\partial T}{\partial y} = \frac{1}{\text{Pr Re}} \frac{\partial^2 T}{\partial y^2} \,, \tag{1}$$

subject to the initial conditions

(a)
$$T(y, t = 0) = \cos(2\pi y)\sin(\pi y)$$

(b) $T(y, t = 0) = \cos(2\pi y)$, (2)

and parameters

Re = 1 (Reynolds number, molten glass)

Pr = 25 (Prandtl number, molten glass)

$$\Delta t = 0.001$$
 (Time step) (3)

 $L_y = 2$ (Domain y-length)

 $N = 2^n + 1$ (Number of y-points, where $n = 5, 6$).

1.1 PROBLEM 1

Use the Fourier pseudo-spectral method to numerically integrate (1) with the given parameters. Use the Euler explicit method for time advancement. Higher resolution with n = 6 will improve the accuracy of the method for the initial condition (a). Plot T as a function of time t at $t = \{0.2, 2, 5, 10\}$.

1.2 PROBLEM 2

Use the FTCS Euler explicit method with second-order finite differences for the same computation, and compare results to the Fourier pseudo-spectral method using the same mesh resolution.

- 2 METHODOLOGY
- 3 RESULTS
- 4 Discussion
- 5 REFERENCES

No external references were used other than the course notes for this assignment.

APPENDIX: MATLAB CODE

The following code listings generate all figures presented in this homework assignment.