

# Improving Boundary Condition Stability in PHASTA

## 1 INTRODUCTION

## 2 INITIAL OUTLINE OF PHASTA

PHASTA begins execution at `main`, located in `phSolver/[in]compressible`, depending on which branch is desired. This function initializes MPI, and then calls `phasta`, located in `/phSolver/common`. Here, inputs are read and computed in `input`, and then the solver is run by calling `proces`, a Fortran routine. Within `proces`, `gendat` generates geometry and BC data.

Routines followed by an asterisk (\*) are outlined in further detail separately.

**INCOMPRESSIBLE ONLY**, and we ignore cardiovascular impedance and RCR boundary stuff.

### ■ `main`

- initialize MPI
- `phasta`
  - initialize PETSc
  - `input_fform` — read ASCII data from `input.config` and `solver.inp`
  - `input*` — populate data structures with problem set-up and solver parameters
  - `proces*` — generate problem data and calls the solution driver
  - finalize PETSc
- finalize MPI

Inputs:

### ■ `input` — populate data structures with problem set-up and solver parameters

- `readnblk` — read and blocks data
  - read `numstart.dat` and finds appropriate `restart.dat` files
  - read geometry from Posix or SyncIO files using `phio_readheader`
  - calculate maximum number of boundary element nodes
  - initialize constants like `ndof`, `ndofBC`, `ndiBCB`, and `ndBCB`
  - `genblk` — read and block connectivity
  - read BC mapping array into `nBC`
  - read temporary boundary condition code into `iBCtmp`
  - read BC data into `BCinp`
  - read periodic BC data into `iperread`
  - `genbkb` — generate boundary element blocks and traces for gather/scatter operations
  - read restart data for solution `qold`, displacement `uold`, and accelerations `acold`
- assert valid input constants (e.g. `icoord`, `navier`, `iexec`) defined in `common.h`

- `genint` — generate integration information: number of quadrature points on the interior `nint` and boundary `nintb`, their weights `Qwt` and `Qwtb`, and locations `Qpt` and `Qptb`
- estimate number of global nonzeros `nnz` based on basis function order `ipord`
- compute fluid thermodynamic properties

Process:

■ `proces` — generate problem data and call the solution driver

- `gendat` — generate geometry and BC data
  - `genshp` — generate interior element shape functions and derivatives
    - loop through element topologies, getting their coordinate system and element type, and then generate the parent element shape functions and their derivatives by calling either `shpTet` (tets), `shphex` (hexes), `shp6w` (wedges), or `shppyr` (pyramids)
    - these are all C routines, and some are in `phasta/shapeFunction/`, whereas others are in `phasta/phSolver`
    - return `shp(a,i,j,p)` and `shgl(a,i,p)`, which are indexed by topology index `a`, spatial dimension(s) `i` and `j`, and the integration point index `p = 1,...,nint`
  - `geniBC` — generate boundary condition codes
    - set `iBC = iBCtmp` if this partition has boundary nodes; see code for `BCinp` description
  - `genBC` — generate the essential boundary conditions
    - set `BCtmp = BCinp` if this partition has boundary nodes; `BCtmp(nshg,6+5*I3nsd)` has a second index of  $\rho$ ,  $T$ ,  $p$ , velocities, scalars (?)
    - `genwnm` — calculate wall normals and modify `BCtmp` with the appropriate constraints
    - `genotwn` — determine first “off-the-wall-node” for each node, store result in `otwn(nshg)`
    - `genBC1` — account for arbitrarily-oriented velocity constraints  $u_r$ ,  $u_s$ , and  $u_t$ , finally storing the simplified boundary condition constraint result in `BC`; note that second index of `BC` holds  $\rho$ ,  $T$ ,  $p$ ,  $u_1$ ,  $u_2$ ,  $u_3$ , and scalars
  - `genshpb` — generate boundary element shape functions and derivatives (like `genshp`), storing results in `shpb` and `shglb`
  - LES: call `setfilt`, `filtprep`, and depending on `iLES`’ value, `setave` and `aveprep`
  - `genini` — generate initial values of solution variables
    - `restar` — sort initial values into `y` (called `q` inside `restar`) and `ac` from `qold` and `acold`, respectively, that were read in `readnblk`
    - `itrBC*` and `itrBCSclr*` — satisfy BCs
- `setper` and `perprep` — store inverse of sum of one and number of slaves in `rcount`
- LES: `keeplhsG` and `setrls`
- `initStats` — allocate arrays to store flow statistics
- RANS: `initTurb`
- `itrdrv*` — iterate the discrete solution using the predictor multi-corrector algorithm

Numerical solution of the time-integrated unsteady Navier-Stokes equations occurs within `itrdrv`. Working arrays are listed in Table 2.

■ `itrdrv`

- `initTimeSeries` — initialize time series collection to `varts.*.dat` files using `xyzts.dat` input

- initialize `istep` and `ifuncs(:)` to zero
- set `yold = y` and `acold = ac`, that is, populate  $\underline{Y}^n$  and  $\underline{Y}_{,t}^n$  with their converged solutions from the previous time step, which came from a restart file
- `initEQS` — create the `rowp` and `colm` maps to facilitate sparse storage of the tangent matrix
  - determine how many scalar equations need solution, `nsclrsol` (# scalars + 1 if temperature)
  - determine whether we are solving the flow
  - `genadj` — pre-process the adjacency list
    - `do iblk = 1, nelblk` — loop over blocks (groups of elements with the same topology)
      - ▶ `Asadj` — generate adjacency data structures `row_fill_list` and `adjcnt`
        - ▷ declare `row_fill_list` to have dimension `(nshg, 15*nnz)`, where `15*nnz` is a high estimate of the maximum number of adjacent nodes
        - ▷ `row_fill_list(A,:)` holds global nodes that share local support with global node `A`
        - ▷ `adjcnt(A)` holds the number of nodes adjacent to `A`, that is, how many entries `row_fill_list(A,:)` was populated with on purpose
        - ▷ *note*: some operations here are  $\mathcal{O}(n^2)$ , but  $n$  is relatively small on each processor, and this process only needs to be done once for a given mesh connectivity
      - build the `colm` array (which is trivial to do at this point)
      - sort `rowp`, because we binary search it when computing the sparse  $\underline{A} \underline{p}$ -product, and also compute the number of non-zero blocks `icnt` on this partition
    - set `nnz_tot = icnt`
    - depending on `nsolflow` and `nsclrsol` (whether this is a flow or scalar solve), initialize certain constants, such as `equType`, `nDofs`, `nPermDims`, `nTmpDims`, and allocate certain arrays, such as `apermS` and `atempS`
  - initialize `lstep0 = lstep + 1` to hold the first time step solved by the current run
  - `do itsq = 1, ntseq` — loop over time sequences; as far as I can tell `ntseq = 1` is the default in `input.config`, and time sequences are not often used
    - set `itseq = itsq`
    - set iteration-specific variables `nstp = nstep`, `nitr = niter`, `LCtime = loctim`, and `dtol(:) = delt看(:)`, where all of the longer-named variables are indexed by `itseq`
    - `itrSetup` — set up time integration parameters
      - calculate  $\alpha_m$ ,  $\alpha_f$ , and  $\gamma$  as functions of  $\rho_\infty$  (`almi`, `alfi`, and `gami` as functions of `rhoinf`)
      - set inverse of global time step `Dtgl` and CFL data `CFLfl`
    - calculate number of flow solves per time step, store in `nitr` (IC), `niter` (C)
    - initialize `istop = 0`; flag can be set to stop the solver based on statistics of the residual
    - `do istp = 1, nstp` — main loop over time steps
      - LES: `lesmodels`
      - `asbwmod` — set traction BCs if turbulence wall model is set (`itwmod`)
      - `itrPredict*` — predict primitive variables at time  $n + 1$
      - `itrBC*` — satisfy BCs on primitive variables; return a modified `y`
      - `itrBCSclr` — satisfy BCs on scalar `isclr`; return a modified `y`
      - `do istepc = 1, seqsize` — loop over individual solves of flow and scalar
        - ▶ `icode = stepseq(istepc)` — get sequence code
        - ▶ *if* this is a flow solve
          - ▷ `SolFlow*` — perform a flow solve

- ▶ `else if` this is a scalar solve
  - ▷ `SolSclr` — perform a scalar solve
- ▶ `else` this is an update
  - ▷ `itrCorrect*` and `itrBC*` — update flow if desired
  - ▷ `itrCorrectSclr` and `itrBCSclr` — update scalar if desired
- `stsGetStats` — obtain time averaged statistics
- find solution at end of time step and move it to old solution variables
- increment `istep` and `lstep`
- `Bflux` — compute the consistent boundary flux if desired
- deallocate variables and close files
- deallocate variables and close files

Iteration routines...

■ `itrPredict` — predict solution variables at time  $n + 1$

- `if (ipred .eq. 1)` — we are using same-velocity prediction, as discussed in class
  - set  $\underline{Y}^{n+1}(i) = \underline{Y}^n$  with `y = yold`
  - set  $\underline{Y}_{,t}^{n+1}(i) = (1 - 1/\gamma)\underline{Y}_{,t}^n$  with `ac = acold * (gami-one)/gami`
- other prediction methods (zero-acceleration, same-acceleration, and same-delta) are also supported with different values of `ipred`

Boundary conditions are set with the `iBC` and `BC` arrays. The bits of `iBC`, in increasing order, indicate whether the following BCs are set:  $\rho$ ,  $T$ ,  $p$ ,  $u_1$ ,  $u_2$ ,  $u_3$ , scalars 1–4, periodicity, scaled plane extraction (SPEBC), axisymmetry, and deformable wall (for cardiovascular cases). This means for each global node, `iBC` has at least 14 bits. Note that `ibits(i,a,l)` extracts bits `a+1` through `a+l` of the integer `i`, and returns the base-10 integer. This routine is used to help identify and process boundary condition flags held in `iBC`. For example, if `ibits(iBC,3,3).eq. 1` then  $u_1$  is the only velocity component specified essential BC.

■ `itrBC` — satisfy BCs on the primitive variables

- impose limits on flow variables in `y`, using the `ylimit` data structure of dimension `(3, nflow)`, whose first index contains the limit flag, lower limit, and upper limit for each flow variable
- velocity
- pressure
- local periodic
- global periodic

Once boundary conditions have been satisfied, `SolFlow` is called to perform a flow solve:

■ `SolFlow` — perform a flow solve; output `res` preconditioned residual,

- `itrYAlpha` — compute  $\underline{Y}^{n+\alpha_f}(i)$  and  $\underline{Y}_{,t}^{n+\alpha_m(i)}$ , store respectively in `yAlpha` and `acAlpha`
- `ElmGMR` — compute tangent matrix, residual vector, and preconditioning matrix for GMRES

Going through lectures 26 and 27.

First in the compressible code. Data structures are used in `solgmr -> elmgmr` (sparse). Section on diffusive flux reconstruction, set up some arrays for interior elements. call `asigmr`, took care of volume

integrals. now come to boundary elements, which is where integral over gamma takes place. block boundary elements as a separate list of elements with separate connectivity. as `asbmfg` is called, `mienb` holds boundary elements. computing normal gradients requires nodes off of the boundary. solution goes into `asbmfg` (no time derivatives are input, unlike `asigmr`), out comes a modified solution. in `asibmfg`: working with a block of elements; solution and coordinates are localized, local residual is zeroed, call `e3b`, assemble local residual. in `e3b`: loop over quadrature points (`ngaussb`), `getshpb` to get boundary shape functions, `e3bvar` called with surface normals, need `Fv{2,3,4}` to evaluate the floating flux, let `e3bvar` compute `Fv` values and fluxes, then test if we should use computed value or value from prescribed boundary condition. in `e3bvar`: interpolate nodal values to quadrature points, call `getthm` to compute thermodynamic state, compute element metrics for mapping physical space to get `wdetj`, compute `rou,p` and `tau*n,heat` (normal flux, pressure, traction vector, heat flux) that is, `rou` takes  $h^m(\xi_l)$ , `p` takes  $h^p(\xi_l)$ , `tau*n` takes  $h_*^v(\xi_l)$ , etc. what's passed out is these things and the raw variables, their gradients, and the derived thermodynamic state. Back to `e3b`, do convective pressure, n-s, heat terms. after return from `e3bvar`, if no natural bc flag is set, we overwrite `rou,p` with floating values. compute euler stuff; then compute viscous stuff. get floating flux `tau*n`, overwrite where bits are not set. be careful what's passed out and in. also compute aerodynamic forces and heat flux in `e3b`, since we're doing surface integrals anyway.

incompressible is different, slightly. don't interpolate temperature at the outset; compute normal via cross-product; compute deformation gradient, local and global variable gradients; `unm` has the floating value of  $\underline{u} \cdot \underline{n}$ . eventually compute `tau*n`, which has the total stress floating value. skip over a bunch of deforming-wall stuff. iBCB did not come in to `e3bvar`; only floating flux stuff is computed in `e3bvar` for incompressible. all nodal interpolation is now done in `e3b`:

for Dirichlet bcs, `iBC` was a bitmap to boundary conditions `BC`

for natural bcs, `ibcb(1:nelin block (npro),...)` is a bitmap to boundary conditions `BCB(:,...)`, where ... takes normal flux, pressure, traction vector, and heat flux take values 1–4.

going through more code... (2016-03-30)

this stuff is used in `irdrv` when it calls `solgmrs`, calls `elmgmrs` to populate `lshk` with current iteration's tangent values (same for `res`). allows us to start `gmres`; factorize matrix; precondition rhs with `i3lu`; `spsi3pre` sparse matrix preconditioning of `lshk`; copy preconditioned residual into `uBrg`, which is a collection of Krylov vectors; calculate it's norm, make orthonormal; outer `gmres` loop `do 2000` can be skipped, which is the `gmres` restart; actual start of GMRES discussed in class is `uBrg` statement just before `do 1000`; `sumgat` does off-processor (communication).

Symbol	Dimension	Description
<code>nshg</code>		# global shape functions ( <code>nshg = nnp</code> if piecewise linear)
<code>nnp</code>		# global nodal points
<code>npro</code>		# elements in a block of same-topology elements, indexed by $e$
<code>nshl</code>		# nodes per element, indexed by $a$
<code>ndof</code>		# degrees of freedom, including scalars for turbulence models
<code>nflow</code>		# flow variables (4 incompressible, 5 compressible)
<code>ntseq</code>		# time sequences, which seems seldom used and defaults to 1
<code>nstep</code>		# time steps requested per sequence
<code>nelblk</code>		# blocks
<code>ipord</code>		order of basis functions
<code>lstep</code>		current time step
<code>lstep0</code>		first time step solved by current run, initialized to <code>lstep+1</code>
<code>istep</code>		step number relative to start of run
<code>iter</code>		iteration number
<code>niter</code>	(MAXTS)	# multi-corrector iterations per time step
<code>loctim</code>	(MAXTS)	local time stepping flag (?)
<code>deltol</code>	(MAXTS, 2)	velocity and pressure delta ratios
<code>impl</code>	(MAXTS)	heat, flow, and scalar solver flags (1's, 10's and 100's places)
<code>iturb</code>		indicates which turbulence model to use
<code>ifunc</code>		function evaluation counter, <code>niter*(lstep-lstep0)+iter</code>
<code>ifuncs</code>	(6)	function evaluation counter (?)
<code>y</code>	( <code>nshg</code> , <code>ndof</code> )	$\underline{Y}_A^{n+\alpha_f(i)}$ (meaning changes throughout)
<code>ac</code>	( <code>nshg</code> , <code>ndof</code> )	$\underline{Y}_{A,t}^{n+\alpha_m(i)}$ (meaning changes throughout)
<code>yold</code>	( <code>nshg</code> , <code>ndof</code> )	$\underline{Y}_A^{(i)}$ (meaning changes throughout)
<code>acold</code>	( <code>nshg</code> , <code>ndof</code> )	$\underline{Y}_{A,t}^{(i)}$ (meaning changes throughout)
<code>x</code>	( <code>nshg</code> , <code>nsd</code> )	node coordinates
<code>iBC</code>	( <code>nshg</code> )	BC codes
<code>BC</code>	( <code>nshg</code> , <code>ndofBC</code> )	BC constraint parameters
<code>iper</code>	( <code>nshg</code> )	periodicity table
<code>mien</code>	( <code>nelblk</code> )	pointer to IEN array (interior): has dimension ( <code>nshg</code> , <code>15*nnz</code> )
<code>mienb</code>	( <code>nelblk</code> )	pointer to IEN array (boundary): has dimension ( <code>nshg</code> , <code>15*nnz</code> )
<code>shp</code>	( <code>nshape</code> , <code>ngauss</code> )	element shape functions at Gauss points (interior)
<code>shb</code>	( <code>nshapeb</code> , <code>ngaussb</code> )	element shape functions at Gauss points (boundary)
<code>shgl</code>	( <code>nsd</code> , <code>nshape</code> , <code>ngauss</code> )	local shape function gradients at Gauss points (interior)
<code>shglb</code>	( <code>nsd</code> , <code>nshapeb</code> , <code>ngaussb</code> )	local shape function gradients at Gauss points (boundary)

### 3 GENERAL NOTES

- In PHASTA, a block contains elements of the same topology.

### 4 LIFE'S PERSISTENT PHASTA QUESTIONS

- Is `gold`, allocated in `readnblk.f` ever deallocated? Can't find it.
- Why do most of the time step parameters have dimension `MAXTS`?
  - It also seems that some parameters are indexed by `itseq`, but don't change from step to step.
- When is it the case that `ndof`  $\neq$  `nflow`? For example during its limit-imposing stage, `itrbc` loops over `nflow` when indexing `y`'s dimension of size `ndof`.
- Often the value of `datmat(1,2,1)` is assigned to a variable like `rmu`; where is it calculated? Kinematic viscosity? See `getdiff`.
- In `genBC1`, `BC(:,1)` gets assigned both density and pressure, so what goes in `BC(:,6)???`