

KCOR: Depletion-Neutralized Cohort Comparison via Gamma-Frailty Normalization Under Selection-Induced Hazard Curvature

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Abstract

Retrospective cohort studies often estimate the mortality impact of medical interventions, but selection can create non-exchangeable cohorts that defeat standard comparisons. In particular, selective uptake can induce systematic differences in mortality curvature—differences in the time-evolution of cohort hazards driven by frailty heterogeneity and depletion of susceptibles—that violate the assumptions of standard epidemiologic tools such as Cox proportional hazards models, age-standardized mortality rates, and inverse-probability weighting. We introduce **KCOR (Kirsch Cumulative Outcomes Ratio)**, a method that neutralizes selection-induced curvature before cohort comparison by estimating and inverting a gamma-frailty mixture model in **cumulative-hazard space**. KCOR v6 fits cohort-specific selection parameters during epidemiologically quiet periods and transforms observed cumulative hazards to depletion-neutralized baseline cumulative hazards, which are then compared cumulatively via ratios. We describe the KCOR framework, its mathematical foundation, and its validation using prespecified negative and positive control tests designed to stress selection-induced curvature. KCOR requires only event timing—dates of intervention (enrollment) and dates of death (with birth date or year needed only for age stratification)—making it applicable to minimal record-level mortality datasets. Empirically, in illustrative applications, KCOR v6 frequently estimates negligible frailty variance for some cohorts while estimating substantial frailty-driven depletion for others, reflecting asymmetric selection at cohort entry. Importantly, these differences arise from observed hazard curvature rather than from any exposure-specific assumptions. After frailty neutralization, cumulative hazards are approximately linear, enabling direct cohort comparison free of selection-induced curvature. KCOR therefore enables interpretable cumulative cohort comparisons in settings where treated and untreated hazards are non-proportional because selection induces different depletion dynamics.

1. Introduction

1.1 Retrospective cohort comparisons under selection

Randomized controlled trials (RCTs) are the gold standard for causal inference, but are often infeasible, underpowered for rare outcomes, or unavailable for questions that arise after rollout. As a result, observational cohort comparisons are widely used to estimate intervention effects on outcomes such as all-cause mortality.

However, when intervention uptake is voluntary, prioritized, or otherwise selective, treated and untreated cohorts are frequently **non-exchangeable** at baseline and evolve differently over follow-up. This problem is not limited to any single intervention class; it arises whenever the same factors that influence treatment uptake also influence outcome risk.

1.2 Curvature (shape) is the hard part: non-proportional hazards from frailty depletion

Selection does not merely shift mortality **levels**; it can alter mortality **curvature**—the time-evolution of cohort hazards. Frailty heterogeneity and depletion of susceptibles naturally induce curvature even when individual-level hazards

are simple functions of time. When selection concentrates high-frailty individuals into one cohort (or preferentially removes them from another), the resulting cohort-level hazard trajectories can be strongly non-proportional.

One convenient way to formalize “curvature” is in cumulative-hazard space: if the cumulative hazard $H(t)$ were perfectly linear in time, then its second derivative would be zero, whereas selection-induced depletion generally produces negative concavity (downward curvature) in observed cumulative hazards during otherwise stable periods.

This violates core assumptions of many standard tools:

- **Cox PH**: assumes hazards differ by a time-invariant multiplicative factor (proportional hazards).
- **IPTW / matching**: can balance measured covariates yet fail to balance unmeasured frailty and the resulting depletion dynamics.
- **Age-standardization**: adjusts levels across age strata but does not remove cohort-specific time-evolving hazard shape.

KCOR is designed for this failure mode: **cohorts whose hazards are not proportional because selection induces different depletion dynamics (curvature)**. Approximate linearity of cumulative hazard after adjustment is therefore not assumed, but serves as an internal diagnostic indicating that selection-induced depletion has been successfully removed.

Although this manuscript is motivated in part by mortality analyses conducted during the COVID-19 vaccination period, the methodological problem addressed here is general. The COVID setting provides unusually clear examples of selection-induced non-proportional hazards—because uptake was voluntary, rapidly time-varying, and correlated with baseline health—making residual confounding easy to diagnose using control outcomes such as non-COVID mortality. However, KCOR is not specific to COVID, vaccination, or infectious disease. The estimator applies to any retrospective cohort comparison in which selection induces differential depletion dynamics that violate proportional hazards assumptions.

1.3 Evidence from the literature: residual confounding despite meticulous matching

Two large, rigorously designed observational analyses illustrate the core empirical motivation: even extremely careful matching and adjustment can leave large residual differences in non-COVID mortality, indicating confounding and selection that standard pipelines do not eliminate.

1.3.1 Denmark (negative controls highlight confounding)

Obel et al. used Danish registry data to build 1:1 matched cohorts and applied negative control outcomes to assess confounding. Their plain-language summary includes the following:

Meaning: The negative control methods indicate that observational studies of SARS-CoV-2 vaccine effectiveness may be prone to substantial confounding which may impact the observed associations. This bias may both lead to underestimation of vaccine effectiveness (increased risk of SARS-CoV2 infection among vaccinated individuals) and overestimation of the vaccine effectiveness (decreased risk of death after of SARS-CoV2 infection among vaccinated individuals). Our results highlight the need for randomized vaccine efficacy studies after the emergence of new SARS-CoV-2 variants and the rollout of multiple booster vaccines.¹

This is a direct statement that observational designs—even with careful matching and covariate adjustment—can remain substantially confounded when selection and health-seeking behavior differ between cohorts.

1.3.2 Qatar (time-varying HVE despite meticulous matching)

Chamaletty et al. analyzed matched national cohorts and explicitly measured the **time-varying healthy vaccinee effect (HVE)** using non-COVID mortality as a control outcome. They report a pronounced early-period reduction in non-COVID mortality among vaccinated individuals despite meticulous matching, followed by reversal later in follow-up, consistent with dynamic selection and depletion processes.²

Together, these studies motivate a methods gap: we need estimators that explicitly address **time-evolving selection-induced curvature**, not only baseline covariate imbalance.

Table 1: Summary of two large matched observational studies showing residual confounding / HVE despite meticulous matching.

Study	Design	Matching/adjustment	Key control finding	Implication for methods
Obel et al. (Denmark) ¹	Nationwide registry cohorts (60–90y)	1:1 match on age/sex + covariate adjustment; negative control outcomes	Vaccinated had higher rates of multiple negative control outcomes, but substantially lower mortality after unrelated diagnoses	Strong evidence of confounding in observational VE estimates; “negative control methods indicate... substantial confounding”
Chamaletty et al. (Qatar) ²	Matched national cohorts (primary series and booster)	Exact 1:1 matching on demographics + coexisting conditions + prior infection; Cox models	Strong early reduction in non-COVID mortality (HVE), with time-varying reversal later	Even meticulous matching leaves time-varying residual differences consistent with selection/frailty depletion

1.4 Contribution of this work

This paper introduces **KCOR**, a method that transforms observed cohort hazards to remove selection-induced depletion dynamics prior to comparison, enabling interpretable cumulative cohort comparisons under selection-induced non-proportional hazards.

This manuscript is **methods-only**:

- We present the estimator, model assumptions, and uncertainty quantification.
- We validate the method using prespecified negative and positive controls designed to stress selection-induced curvature.
- We defer any applied real-world intervention conclusions to a separate, dedicated applied paper.

KCOR is proposed as a diagnostic and normalization estimator for selection-induced hazard curvature; causal interpretation requires additional assumptions beyond the scope of this methods paper.

2. Methods

Table 2: Notation used throughout the Methods section. θ_d denotes the cohort-specific depletion (frailty variance) parameter governing curvature in the observed cumulative hazard.

Symbol	Meaning
d	cohort index (enrollment definition \times age group \times dose/exposure)
t	event time since enrollment (discrete bins, e.g., weeks)
$h_d^{\text{obs}}(t)$	observed cohort hazard at time t
$H_d^{\text{obs}}(t)$	observed cumulative hazard (after skip/stabilization)
$h_{0,d}(t)$	depletion-neutralized baseline hazard for cohort d
$H_{0,d}(t)$	depletion-neutralized baseline cumulative hazard
θ_d	frailty variance (selection strength) for cohort d

Symbol	Meaning
k_d	baseline hazard level for cohort d under default baseline shape

2.1 Conceptual framework: level vs curvature under selection

Differences in mortality between cohorts can arise from:

- **Level effects:** multiplicative shifts in hazard that are constant over time.
- **Curvature effects:** differences in the time-evolution of cohort hazards induced by heterogeneity and selective depletion.

Selection bias commonly produces curvature differences through frailty mixing and depletion. KCOR’s strategy is to **estimate and remove the selection-induced depletion component**, then compare cohorts on a cumulative scale.

2.2 Cohort construction and estimand

KCOR is defined for **fixed cohorts** at enrollment. Required inputs are minimal: for each individual, the intervention or enrollment date(s) and the date of death, with birth date or year included only if age stratification is performed.

- Cohorts are fixed at enrollment and defined by intervention status at the start of the enrollment week; doses administered during the enrollment week do not affect cohort assignment (i.e., dose status is determined by doses received **strictly before** the enrollment week start).
- No censoring or cohort switching is permitted in the primary estimand.
- Analysis proceeds in **event time t** (time since enrollment).

This fixed-cohort design corresponds to an intent-to-treat-like estimand under selection. It is chosen deliberately to avoid time-varying deferral bias, immortal time bias, and dynamic health-based sorting that arise when individuals change exposure status during follow-up. Dynamic “as-treated” formulations are treated as sensitivity analyses rather than primary estimands.

2.2.1 KCOR data representation and reproducibility

All analyses were performed using the KCOR (Kirsch Cumulative Outcomes Ratio) framework, which operates on fixed-cohort, time-indexed observational data under explicitly defined enrollment and outcome semantics.

To ensure reproducibility across jurisdictions with differing privacy and disclosure-control regimes, KCOR supports three formally defined data representations:

1. Record-level data
2. Aggregated outcome summary data
3. Hazard summary data

These formats differ only in disclosure surface; they are analytically equivalent under the KCOR methodology.

The precise definitions of enrollment, cohort freezing, time indexing, risk sets, outcomes, stratifiers, and disclosure-control constraints are specified in the **KCOR data format specification**, which is versioned and publicly available:

KCOR File Format Specification
[documentation/specs/KCOR_file_format.md](https://github.com/kirsch-corporation/KCOR/blob/main/documentation/specs/KCOR_file_format.md)

All KCOR results presented in this paper can be reproduced from any data representation that conforms to this specification.

2.3 Hazard estimation and cumulative hazards (discrete time)

Let t denote event time since enrollment (e.g., weeks), $D_d(t)$ deaths during interval t in cohort d , and $N_d(t)$ the number at risk at the start of interval t . In discrete time, hazards are treated as piecewise-constant and can be computed from interval risk as

$$h_d^{\text{obs}}(t) = -\ln \left(1 - \frac{D_d(t)}{N_d(t)} \right). \quad (1)$$

We work primarily in **cumulative-hazard space**, accumulating observed hazards after an optional stabilization skip (see §2.7):

$$H_d^{\text{obs}}(t) = \sum_{s \leq t} h_d^{\text{eff}}(s) \Delta t, \quad \Delta t = 1 \text{ (one time bin)}. \quad (2)$$

2.4 Selection model: gamma frailty and the cumulative-hazard identity

2.4.1 Individual hazards with multiplicative frailty

Model individual hazards in cohort d as multiplicative frailty on top of a baseline hazard:

$$h_{i,d}(t) = z_{i,d} h_{0,d}(t), \quad z_{i,d} \sim \text{Gamma}(\text{mean} = 1, \text{var} = \theta_d). \quad (3)$$

Gamma frailty is used not as a claim of biological truth, but as a mathematically minimal and widely used model for unobserved heterogeneity whose Laplace transform yields a closed-form relationship between observed and baseline cumulative hazards³. In KCOR, gamma frailty is therefore a **depletion-neutralizing approximation**: its adequacy is treated as empirically testable and is assessed using prespecified negative controls and sensitivity analyses rather than assumed dogmatically.

Frailty $z_{i,d}$ captures latent heterogeneity in baseline risk and drives selective depletion: higher-frailty individuals die earlier, changing the cohort composition over time and inducing curvature in $h_d^{\text{obs}}(t)$ even when $h_{0,d}(t)$ is simple.

2.4.2 Gamma-frailty identity (core mathematics)

Let the baseline cumulative hazard be

$$H_{0,d}(t) = \int_0^t h_{0,d}(s) ds. \quad (4)$$

Integrating over gamma frailty yields a closed-form relationship between the observed cohort cumulative hazard and the baseline cumulative hazard:

$$H_d^{\text{obs}}(t) = \frac{1}{\theta_d} \log(1 + \theta_d H_{0,d}(t)). \quad (5)$$

This identity can be inverted exactly:

$$H_{0,d}(t) = \frac{e^{\theta_d H_d^{\text{obs}}(t)} - 1}{\theta_d}. \quad (6)$$

This inversion is the **KCOR v6 normalization step**: it transforms the observed cumulative hazard into a depletion-neutralized baseline cumulative hazard for each cohort.

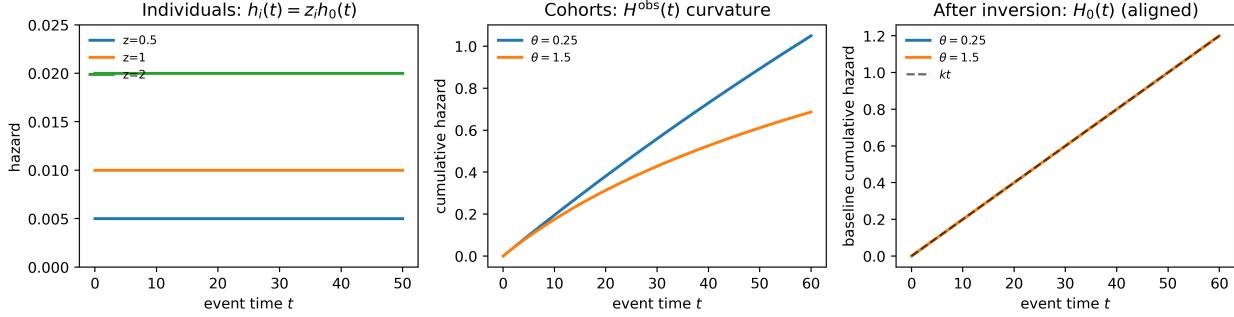


Figure 1: Three-panel schematic illustrating the KCOR v6 normalization logic. Left: individual hazards differ only by multiplicative frailty z , with no treatment effect. Middle: aggregation over heterogeneous frailty induces cohort-level curvature in observed cumulative hazards $H^{\text{obs}}(t)$ despite identical baseline hazards. Right: inversion of the gamma-frailty identity recovers aligned baseline cumulative hazards $H_0(t)$, demonstrating depletion-neutralization. This figure is schematic and intended for conceptual illustration; it does not represent empirical data.

2.4.3 Baseline shape for fitting (default)

To identify θ_d from data, KCOR fits the gamma-frailty model during epidemiologically quiet periods. In the reference specification, the baseline time-shape is taken to be constant over the fit window:

$$h_{0,d}(t) = k_d g(t), \quad g(t) = 1, \quad H_{0,d}(t) = k_d t. \quad (7)$$

This choice minimizes degrees of freedom and forces curvature during quiet periods to be explained by selection (frailty) rather than by an explicit time-varying baseline.

2.5 Estimation during quiet periods (cumulative-hazard least squares)

KCOR estimates (k_d, θ_d) independently for each cohort d using only time bins that fall inside a prespecified **quiet window** in calendar time (ISO week space). The quiet window is prespecified and applied consistently across cohorts within an analysis; robustness to alternate quiet-window bounds is assessed in sensitivity analyses. Quiet periods are identified diagnostically via stability of observed cumulative hazards and absence of external shocks, rather than by a fixed universal numeric threshold. Let \mathcal{T}_d denote the set of event-time bins t whose corresponding calendar week lies in the quiet window, with t also satisfying $t \geq \text{SKIP_WEEKS}$.

Under the default baseline shape, the model-implied observed cumulative hazard is

$$H_d^{\text{model}}(t; k_d, \theta_d) = \frac{1}{\theta_d} \log(1 + \theta_d k_d t). \quad (8)$$

Identifiability of (k_d, θ_d) comes from curvature in cumulative-hazard space: the mapping $t \mapsto H_d^{\text{obs}}(t)$ is nonlinear when $\theta_d > 0$. When depletion is weak (or the quiet window is too short to show curvature), the model smoothly collapses to a linear cumulative hazard, since $H_d^{\text{model}}(t; k_d, \theta_d) \rightarrow k_d t$ as $\theta_d \rightarrow 0$. Operationally, near-linear $H_d^{\text{obs}}(t)$ naturally drives $\hat{\theta}_d \approx 0$; fit diagnostics such as n_{obs} and RMSE in H -space provide a practical check on whether the selection parameters are being identified from the quiet-window data. In practice, lack of identifiable curvature naturally manifests as $\hat{\theta} \rightarrow 0$, providing an internal diagnostic for non-identifiability over short or sparse follow-up.

In applied analyses, this behavior is most commonly observed in vaccinated cohorts, whose cumulative hazards during quiet periods are often close to linear. In such cases, the gamma-frailty fit collapses naturally to $\hat{\theta}_d \approx 0$, indicating minimal detectable depletion. This outcome is data-driven and reflects the absence of observable selection-induced curvature rather than a modeling assumption. When residual time-varying risk contaminates a nominally quiet window, $\hat{\theta}$ estimates naturally shrink toward zero, signaling limited identifiability rather than inducing spurious correction.

Parameters are estimated by constrained nonlinear least squares:

$$(\hat{k}_d, \hat{\theta}_d) = \arg \min_{k_d > 0, \theta_d \geq 0} \sum_{t \in \mathcal{T}_d} [H_d^{\text{obs}}(t) - H_d^{\text{model}}(t; k_d, \theta_d)]^2. \quad (9)$$

We fit in cumulative-hazard space rather than maximizing a likelihood because the primary inputs are discrete-time, cohort-aggregated hazards and the objective is stable estimation of selection-induced depletion curvature during quiet periods. Least squares on $H_d^{\text{obs}}(t)$ is numerically robust under sparse events, emphasizes shape agreement over the fit window, and yields diagnostics (e.g., RMSE in H -space) that directly reflect the quality of the depletion fit. Likelihood-based fitting can be treated as a sensitivity analysis, but is not required for the normalization identity itself.

Reference implementation defaults (this repo)

The manuscript describes KCOR generically; for reproducibility, this repository's KCOR v6 defaults are:

- **Quiet window:** ISO weeks 2022-24 through 2024-16 (inclusive).
- **Skip weeks:** a fixed prespecified skip, SKIP_WEEKS = DYNAMIC_HVE_SKIP_WEEKS (see code), applied by setting $h_d^{\text{eff}}(t) = 0$ for $t < \text{SKIP_WEEKS}$.
- **Observed hazard transform used to build H_d^{obs} from weekly mortality risk:** if $\text{MR}_{d,t} = D_{d,t}/Y_{d,t}$ is the weekly mortality input,

$$h_d^{\text{obs}}(t) = -\log\left(\frac{1 - 1.5 \text{MR}_{d,t}}{1 - 0.5 \text{MR}_{d,t}}\right). \quad (10)$$

This form provides a second-order accurate approximation to the continuous-time hazard while remaining numerically stable for small mortality-rate (MR) values.

- **Fit method:** nonlinear least squares in cumulative-hazard space (not MLE), with constraints $k_d > 0$ and $\theta_d \geq 0$.
- **Cohort indexing (implementation):** enrollment period (sheet) \times YearOfBirth group \times Dose, plus an all-ages cohort (YearOfBirth = -2).

2.6 Normalization (depletion-neutralized cumulative hazards)

After fitting, KCOR computes the depletion-neutralized baseline cumulative hazard for each cohort d by applying the inversion to the full post-enrollment trajectory:

$$\tilde{H}_{0,d}(t) = \frac{e^{\hat{\theta}_d H_d^{\text{obs}}(t)} - 1}{\hat{\theta}_d}. \quad (11)$$

This normalization maps each cohort into a depletion-neutralized baseline-hazard space in which the contribution of gamma frailty parameters (θ_d, k_d) to hazard curvature has been factored out. (*Conceptually, this places all cohorts into an equivalent θ -factored comparison space.*) In this space, cumulative hazards are directly comparable across cohorts, and remaining differences reflect real differences in baseline risk rather than selection-induced depletion.

When $\hat{\theta}_d \approx 0$, this mapping leaves the observed cumulative hazard essentially unchanged, whereas cohorts with substantial depletion undergo a pronounced upward correction.

An adjusted hazard may be recovered by differencing:

$$\tilde{h}_{0,d}(t) \approx \tilde{H}_{0,d}(t) - \tilde{H}_{0,d}(t-1). \quad (12)$$

The key object for KCOR is $\tilde{H}_{0,d}(t)$; differenced hazards are optional diagnostics.

2.7 Stabilization (early weeks)

In many applications, the first few post-enrollment intervals can be unstable due to immediate post-enrollment artifacts (e.g., rapid deferral, short-term sorting, administrative effects). KCOR supports a prespecified stabilization rule by excluding early weeks from accumulation and from quiet-window fitting. The skip-weeks parameter is prespecified and evaluated via sensitivity analysis to exclude early enrollment instability rather than to tune estimates.

In discrete time, define an effective hazard for accumulation:

$$h_d^{\text{eff}}(t) = \begin{cases} 0, & t < \text{SKIP_WEEKS} \\ h_d^{\text{obs}}(t), & t \geq \text{SKIP_WEEKS}. \end{cases} \quad (13)$$

Then compute $H_d^{\text{obs}}(t)$ from $h_d^{\text{eff}}(t)$ as in §2.3.

2.8 KCOR estimator (v6)

For cohorts A and B , KCOR compares depletion-neutralized cumulative hazards:

$$\text{KCOR}(t) = \frac{\tilde{H}_{0,A}(t)}{\tilde{H}_{0,B}(t)}. \quad (14)$$

This is a cumulative comparison in hazard space after removing cohort-specific selection-induced depletion dynamics estimated during quiet periods.

2.9 Uncertainty quantification

KCOR can be equipped with uncertainty intervals via:

- **Analytic variance propagation** for cumulative hazards combined with delta-method approximations for the ratio, and/or
- **Monte Carlo resampling** to capture uncertainty from event realization and from estimation of (k_d, θ_d) and the resulting normalization.

Uncertainty intervals reflect stochastic event realization and model-fit uncertainty in the selection-parameter estimation. They do not assume sampling from a superpopulation and may be interpreted as uncertainty conditional on the observed risk sets and modeling assumptions.

2.10 Algorithm summary and reproducibility checklist

Table 3: Step-by-step KCOR v6 algorithm (high-level), with recommended prespecification and diagnostics.

Step	Operation	Output	Prespecify?	Diagnostics
1	Choose enrollment date and define fixed cohorts	Cohort labels	Yes	Verify cohort sizes/risk sets
2	Compute discrete-time hazards $h_d^{\text{obs}}(t)$	Hazard curves	Yes (binning/transform)	Check for zeros/sparsity
3	Apply stabilization skip and accumulate $H_d^{\text{obs}}(t)$	Observed cumulative hazards	Yes (skip rule)	Plot $H_d^{\text{obs}}(t)$

Step	Operation	Output	Prespecify?	Diagnostics
4	Select quiet-window bins in calendar ISO-week space	Fit points \mathcal{T}_d	Yes	Overlay quiet window on hazard plots
5	Fit (k_d, θ_d) via cumulative-hazard least squares	$\hat{k}_d, \hat{\theta}_d$	Yes	RMSE, residuals, fit stability
6	Normalize: invert gamma-frailty identity to $\tilde{H}_{0,d}(t)$	Depletion-neutralized cumulative hazards	Yes	Compare pre/post shapes; sanity checks
7	Cumulate and ratio: compute KCOR(t)	KCOR(t) curve	Yes (horizon)	Flat under negative controls
8	Uncertainty	CI / intervals	Yes	Coverage on positive controls

3. Validation and control tests

This section is the core validation claim of KCOR:

- **Negative controls (null under selection):** under a true null effect, KCOR remains approximately flat at 1 even when selection induces large curvature differences.
- **Positive controls (detect injected effects):** when known harm/benefit is injected into otherwise-null data, KCOR reliably detects it.

3.0 Frailty normalization behavior under empirical validation

Across examined age strata in the Czech Republic mortality dataset, fitted frailty parameters exhibit a pronounced asymmetry across cohorts. Some cohorts show negligible estimated frailty variance ($\hat{\theta} \approx 0$), while others exhibit substantial frailty-driven depletion. This pattern reflects differences in selection-induced hazard curvature at cohort entry rather than any prespecified cohort identity.

As a consequence, KCOR normalization leaves some cohorts' cumulative hazards nearly unchanged, while substantially increasing the depletion-neutralized cumulative hazard for others. This behavior is consistent with curvature-driven normalization rather than cohort identity. This pattern is visible directly in adjusted versus unadjusted cumulative hazard plots and is summarized quantitatively in the fitted-parameter logs (see `KCOR_summary.log`).

After frailty neutralization, the adjusted cumulative hazards $\tilde{H}_{0,d}(t)$ are approximately linear in event time. Residual deviations from linearity reflect real time-varying risk—such as seasonality or epidemic waves—rather than selection-induced depletion. This linearization serves as an internal diagnostic indicating that frailty-driven curvature has been effectively removed.

3.1 Negative controls: null under selection-induced curvature

3.1.1 Fully synthetic negative control (recommended)

Design a simulation where:

- Individual hazards follow a baseline hazard $h_0(t)$ multiplied by frailty z .
- Two cohorts have different frailty variance θ (or different selection rules), creating different cohort-level curvature in $h_d^{\text{obs}}(t)$.
- **No treatment effect is applied** (both cohorts share the same baseline hazard $h_0(t)$).

After estimating (k_d, θ_d) during quiet periods and applying gamma-frailty inversion, KCOR should remain approximately constant at 1 over follow-up.

In-model “gamma-frailty” stress test (highly convincing null)

One especially clear falsification test is an **in-model gamma-frailty null**: simulate data directly from the gamma-frailty model with the same $h_0(t)$ but different θ between cohorts. This induces strong, visibly different hazard curvature from depletion alone. Because the data-generating process matches the model, the fitted normalization is exact up to sampling noise, and KCOR should be flat at 1.

Suggested construction (example):

- Time unit: weeks.
- Baseline hazard shape: $g(t) = 1$ during quiet periods; choose a baseline level k in the chosen time units.
- Cohort A: $\theta_A > 0$ (stronger depletion).
- Cohort B: $\theta_B > 0$ (weaker depletion).

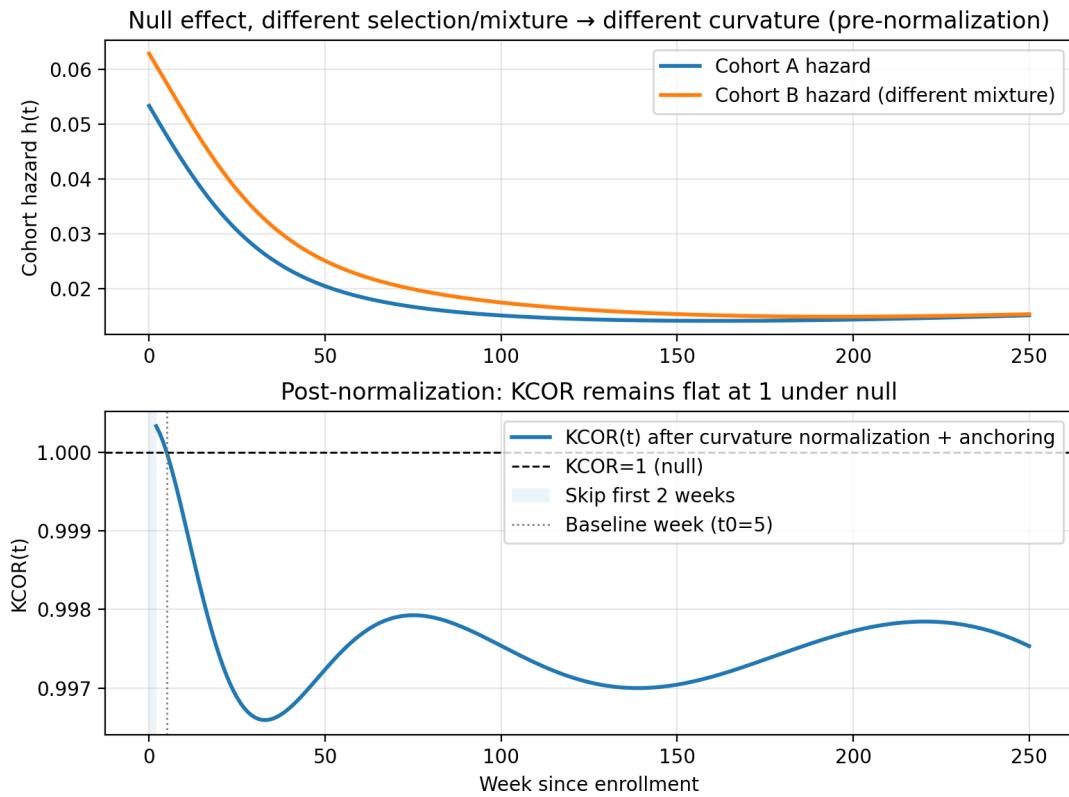


Figure 2: Synthetic negative control under strong selection (different curvature) but no effect: KCOR remains flat at 1. Top panel shows cohort hazards with different frailty-mixture weights inducing different curvature. Bottom panel shows KCOR(t) remaining near 1.0 after normalization, demonstrating successful depletion-neutralization under the null.

3.1.2 Empirical “within-category” negative control (already implemented in repo)

The repository includes a pragmatic negative control construction that repurposes a real dataset by comparing “like with like” while inducing large composition differences (e.g., age band shifts). In this construction, age strata are remapped into pseudo-doses so that comparisons are, by construction, within the same underlying category; the expected differential effect is near zero, but the baseline hazards differ strongly.

These age-shift negative controls deliberately induce extreme baseline mortality differences (10–20 year age gaps)

while preserving a true null effect by construction, since all vaccination states are compared symmetrically. The near-flat KCOR trajectories are consistent with the estimator neutralizing selection-induced depletion curvature without introducing spurious time trends or cumulative drift.

For the empirical age-shift negative control (Figures 3–4), we use aggregated weekly cohort summaries derived from the Czech Republic administrative mortality and vaccination dataset and exported in KCOR_CMR format.

Notably, KCOR estimates frailty parameters independently for each cohort without knowledge of exposure status; the observed asymmetry in depletion correction arises entirely from differences in hazard curvature rather than from any vaccination-specific assumptions.

Two snapshots illustrate that KCOR is near-flat even under 10–20 year age differences:

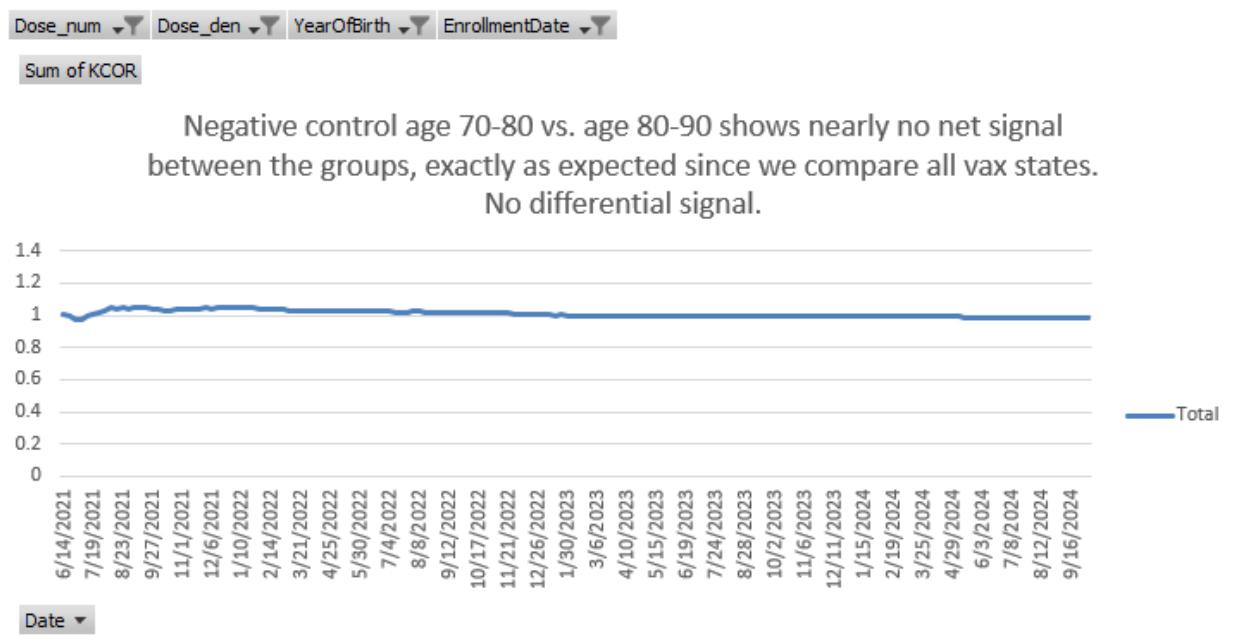


Figure 3: Empirical negative control with approximately 10-year age difference between cohorts. Despite large baseline mortality differences, KCOR remains near-flat at 1 over follow-up, consistent with a true null effect. Data source: Czech Republic mortality and vaccination dataset processed into KCOR_CMR aggregated format (negative-control construction; see Appendix B.2)⁴.

Table 4: Example end-of-window KCOR values from the empirical negative control (pooled/ASMR summaries), showing near-null behavior under large composition differences. (Source: `test/negative_control/out/KCOR_summary.log`)

Enrollment	Dose comparison	KCOR (pooled/ASMR)	95% CI
2021_24	1 vs 0	1.0097	[0.992, 1.027]
2021_24	2 vs 0	1.0213	[1.000, 1.043]
2021_24	2 vs 1	1.0115	[0.991, 1.033]
2022_06	1 vs 0	0.9858	[0.970, 1.002]
2022_06	2 vs 0	1.0756	[1.055, 1.097]
2022_06	2 vs 1	1.0911	[1.070, 1.112]

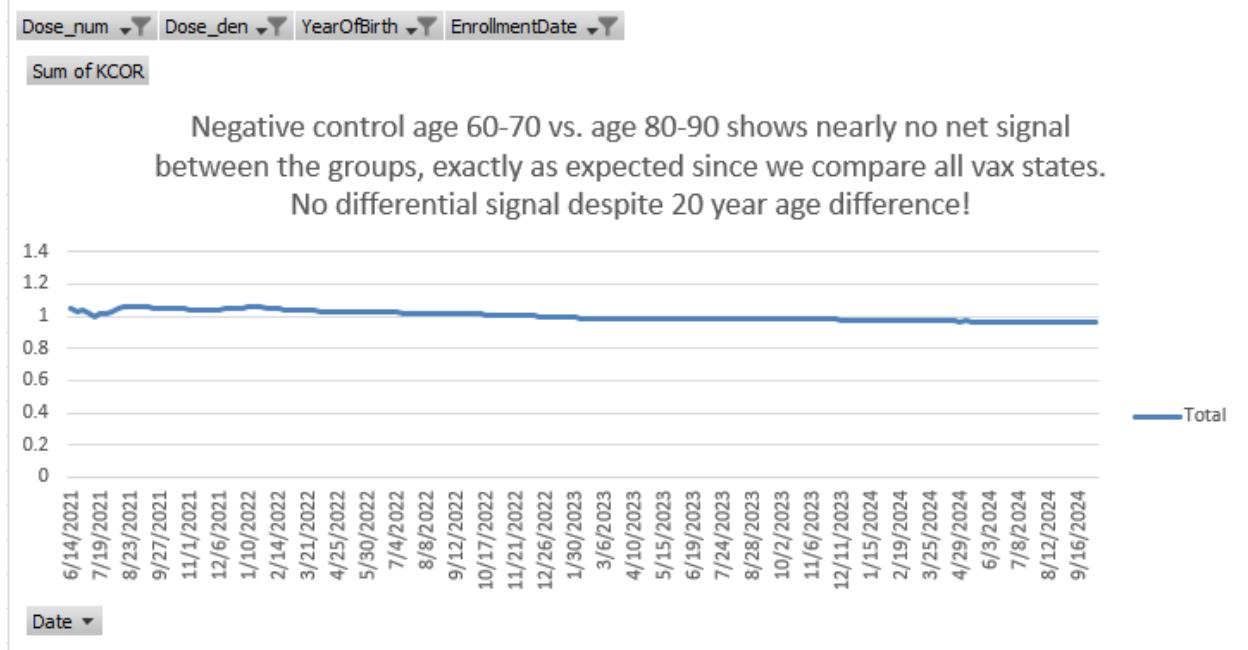


Figure 4: Empirical negative control with approximately 20-year age difference between cohorts. Even under extreme composition differences, KCOR exhibits no systematic drift, demonstrating robustness to selection-induced curvature. Data source: Czech Republic mortality and vaccination dataset processed into KCOR_CMR aggregated format (negative-control construction; see Appendix B.2).

3.2 Positive controls: detect injected harm/benefit

The effect window is a simulation construct used solely for positive-control validation and does not represent a real-world intervention period or biological effect window.

Positive controls are constructed by starting from a negative-control dataset and injecting a known effect into the data-generating process for one cohort, for example by multiplying the *baseline* hazard by a constant factor r over a prespecified interval:

$$h_{0,\text{treated}}(t) = r \cdot h_{0,\text{control}}(t) \quad \text{for } t \in [t_1, t_2], \quad (15)$$

with $r > 1$ for harm and $0 < r < 1$ for benefit.

After gamma-frailty normalization (inversion), KCOR should deviate from 1 in the correct direction and with magnitude consistent with the injected effect (up to discretization and sampling noise).

Table 5: Positive control results comparing injected hazard multipliers to detected KCOR deviations. Both scenarios show KCOR deviating from 1.0 in the expected direction, validating that the estimator can detect true effects.

Scenario	Effect window	Hazard multiplier r	Expected direction	Observed KCOR at week 80
Benefit	week 20–80	0.8	< 1	0.825
Harm	week 20–80	1.2	> 1	1.107

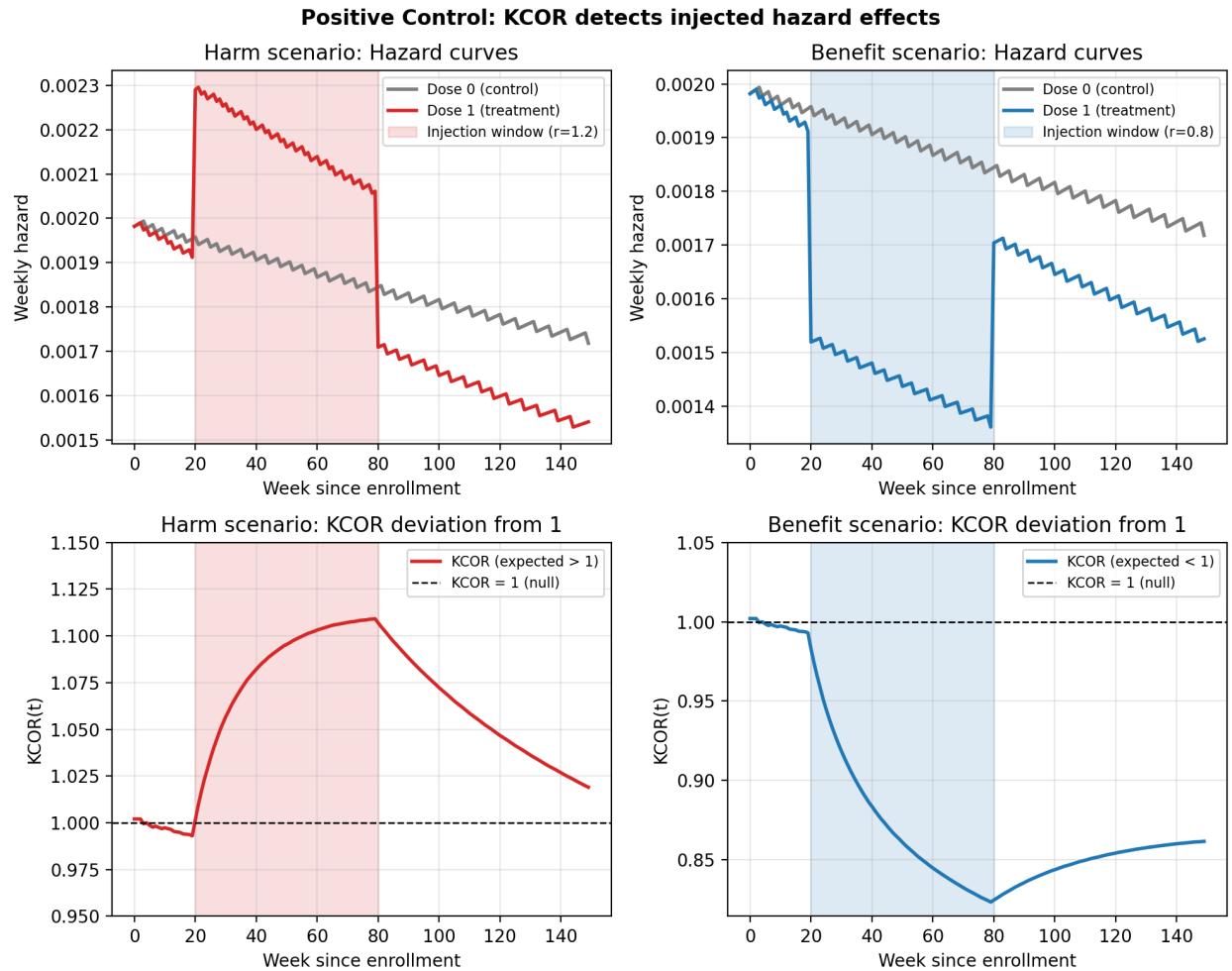


Figure 5: Positive control validation: KCOR correctly detects injected effects. Left panels show harm scenario ($r=1.2$), right panels show benefit scenario ($r=0.8$). Top row displays cohort hazard curves with effect window shaded. Bottom row shows $KCOR(t)$ deviating from 1.0 in the expected direction during the effect window.

3.3 Sensitivity analyses (robustness checks)

The primary analysis uses a prespecified quiet window applied uniformly across cohorts; sensitivity analyses explicitly vary quiet-window bounds and related prespecified choices to assess robustness.

KCOR results should be robust (up to numerical tolerance) to reasonable variations in:

- Quiet-window selection (calendar ISO-week bounds)
- Stabilization skip (early-bin handling)
- Time-binning resolution
- Age stratification and/or stratified analyses where appropriate
- Baseline shape choice $g(t)$ (default $g(t) = 1$; alternatives can be assessed as sensitivity)

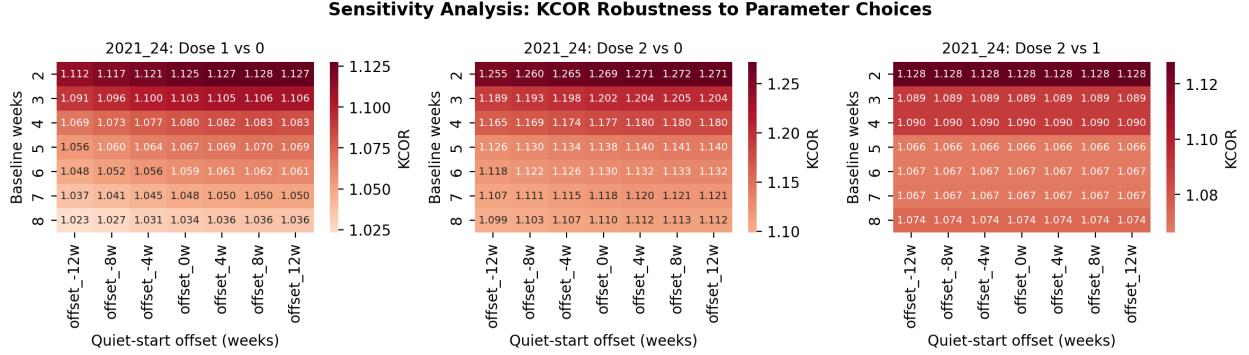


Figure 6: Sensitivity analysis summary showing KCOR values across parameter grid. Heatmaps display KCOR estimates for different combinations of baseline weeks (rows) and quiet-window start offsets (columns). Color scale centered at 1.0 shows stability of estimates across parameter choices, with values remaining close to 1.0 across the grid.

Across all tested parameter ranges, KCOR values remained within approximately $\pm 5\%$ of unity, indicating stability under reasonable variations in fitting choices.

4. Discussion

4.1 What KCOR estimates

KCOR is a **cumulative** comparison of depletion-neutralized cumulative hazards. It is designed for settings where selection induces non-proportional hazards such that conventional proportional-hazards estimators can be difficult to interpret.

Under the working assumptions that:

1. selection-induced depletion dynamics can be estimated during quiet periods using a gamma-frailty mixture model, and
2. the fitted selection parameters can be used to invert observed cumulative hazards into depletion-neutralized baseline cumulative hazards,

then the remaining differences between cohorts are interpretable, **conditional on the stated selection model and quiet-window validity**, as differences in baseline hazard level (on a cumulative scale), summarized by $\text{KCOR}(t)$.

The observation that frailty correction is negligible for vaccinated cohorts but substantial for the unvaccinated cohort is not incidental. It reflects the asymmetric action of healthy-vaccinee selection, which concentrates lower-frailty individuals into vaccinated cohorts at enrollment while leaving the unvaccinated cohort heterogeneous. KCOR explicitly detects and removes this asymmetry by mapping cohorts into a frailty-factored comparison space rather than assuming proportional hazards.

4.2 Relationship to negative control methods

Negative control outcomes/tests are widely used to *detect* confounding. KCOR’s objective is different: it is an estimator intended to *neutralize a specific confounding structure*—selection-induced depletion dynamics—prior to comparison. Negative and positive controls are nevertheless central to validating the estimator’s behavior.

This asymmetry helps explain why standard observational analyses often report large apparent mortality benefits during periods lacking a plausible causal mechanism: vaccinated cohorts are already selection-filtered, while unvaccinated hazards are suppressed by ongoing frailty depletion. Unadjusted comparisons therefore systematically understate unvaccinated baseline risk and exaggerate apparent benefit.

4.3 Practical guidance for use

Recommended reporting includes:

- Enrollment definition and justification
 - Risk set definitions and event-time binning
 - Quiet-window definition and justification
 - Baseline-shape choice $g(t)$ and fit diagnostics
 - Skip/stabilization rule and robustness to nearby values
 - Predefined negative/positive controls used for validation
 - Sensitivity analysis plan and results
-

5. Limitations

- **Model dependence:** Normalization relies on the adequacy of the gamma-frailty model and the baseline-shape assumption during the quiet window.
- **θ estimation is data-driven:** KCOR does not impose $\theta = 0$ for any cohort. The frequent observation that $\hat{\theta} \approx 0$ for vaccinated cohorts is a data-driven result of the frailty fit and should not be interpreted as an assumption of homogeneity.
- **Sparse events:** When event counts are small, hazard estimation and parameter fitting can be unstable.
- **Contamination of quiet periods:** External shocks (e.g., epidemic waves) overlapping the quiet window can bias selection-parameter estimation.
- **Causal interpretation:** KCOR supports interpretable cohort comparison under stated assumptions, but it is not a substitute for randomization; causal claims require explicit causal assumptions and careful validation.
- **Non-gamma frailty:** The KCOR framework assumes that selection acts approximately multiplicatively through a time-invariant frailty distribution, for which the gamma family provides a convenient and empirically testable approximation. In settings where depletion dynamics are driven by more complex mechanisms—such as time-varying frailty variance, interacting risk factors, or shared frailty correlations within subgroups—the curvature structure exploited by KCOR may be misspecified. In such cases, KCOR diagnostics (e.g., poor curvature fit or unstable θ estimates) serve as indicators of model inadequacy rather than targets for parameter tuning. Extending the framework to accommodate dynamic or correlated frailty structures would require explicit model generalization rather than modification of KCOR normalization steps and is left to future work. Empirically, KCOR’s validity depends on curvature removal rather than the specific parametric form; alternative frailty distributions that generate similar depletion geometry would yield equivalent normalization.

5.1 Failure modes and diagnostics (recommended)

KCOR is designed to neutralize selection-induced depletion curvature under its stated model and windowing assumptions. Reviewers and readers should expect the method to degrade when those assumptions are violated. Common failure modes include:

- **Mis-specified quiet window:** If the quiet window overlaps major external shocks (epidemic waves, policy changes, reporting artifacts), the fitted $(\hat{k}_d, \hat{\theta}_d)$ may absorb non-selection dynamics, biasing normalization.

- **External time-varying hazards masquerading as frailty depletion:** Strong secular trends, seasonality, or outcome-definition changes can introduce curvature that is not well captured by gamma-frailty depletion alone. For example, COVID-19 waves disproportionately increase mortality among frail individuals; if one cohort has higher baseline frailty, such a wave can preferentially deplete that cohort, producing the appearance of a benefit in the lower-frailty cohort that is actually due to differential frailty-specific mortality from the external hazard rather than from the intervention under study.
- **Extremely sparse cohorts:** When events are rare, $H_d^{\text{obs}}(t)$ becomes noisy and (k_d, θ_d) can be weakly identified, often manifesting as unstable \hat{k}_d or wide uncertainty.
- **Non-frailty-driven curvature:** Administrative censoring, cohort-definition drift, changes in risk-set construction, or differential loss can induce curvature unrelated to latent frailty.

Practical diagnostics to increase trustworthiness include:

- **Quiet-window overlays** on hazard/cumulative-hazard plots to confirm the fit window is epidemiologically stable.
- **Fit residuals in H -space** (RMSE, residual plots) and stability of $(\hat{k}_d, \hat{\theta}_d)$ under small perturbations of the quiet-window bounds.
- **Sensitivity analyses** over plausible quiet windows and skip-weeks values.
- **Prespecified negative controls:** KCOR curves should remain near-flat at 1 under control constructions designed to induce composition differences without true effects.

In practice, prespecified negative controls—such as the age-shift controls presented in §3.1.2—provide a direct empirical check that KCOR does not generate artifactual cumulative effects under strong selection-induced curvature.

5.2 Conservativeness and edge-case detection limits

Because KCOR compares fixed enrollment cohorts, subsequent uptake of the intervention among initially unexposed individuals (or additional dosing among exposed cohorts) introduces treatment crossover over time. Such crossover attenuates between-cohort contrasts and biases KCOR(t) toward unity, making the estimator conservative with respect to detecting sustained net benefit or harm. Analyses should therefore restrict follow-up to periods before substantial crossover or stratify by dosing state when the data permit.

KCOR analyses commonly exclude an initial post-enrollment window to avoid dynamic Healthy Vaccinee Effect artifacts. If an intervention induces an acute mortality effect concentrated entirely within this skipped window, that transient signal will not be captured by the primary analysis. This limitation is addressed by reporting sensitivity analyses with reduced or zero skip-weeks and/or by separately evaluating a prespecified acute-risk window.

In degenerate scenarios where an intervention induces a purely proportional level-shift in hazard that remains constant over time and does not alter depletion-driven curvature, KCOR’s curvature-based contrast may have limited ability to distinguish such effects from residual baseline level differences under minimal-data constraints. Such cases are pathological in the sense that they produce no detectable depletion signature; in practice, KCOR diagnostics and control tests help identify when curvature-based inference is not informative.

6. Conclusion

KCOR provides a principled approach to retrospective cohort comparison under selection-induced hazard curvature by estimating and inverting a gamma-frailty mixture model to remove cohort-specific depletion dynamics prior to comparison. Validation via negative and positive controls supports that KCOR remains near-null under selection without effect and detects injected effects when present. Applied analyses on specific datasets are best reported separately from this methods manuscript.

Declarations (journal requirements)

Ethics approval and consent to participate

Not applicable. This is a methods-only manuscript. The primary validation results use synthetic data. Empirical negative-control figures (Figures 3–4) use aggregated cohort summaries derived from Czech Republic administrative data; no record-level data are shared in this manuscript.⁴

Consent for publication

Not applicable.

Data availability

- Synthetic validation data (negative and positive control datasets) and generation scripts are available in the project repository under `test/negative_control/` and `test/positive_control/`.
- Sensitivity analysis outputs are available under `test/sensitivity/out/`.
- The reference implementation includes example datasets in KCOR_CMR format for reproducibility.
- A formal specification of the KCOR data formats is provided in `documentation/specs/KCOR_file_format.md`, including schema definitions and disclosure-control semantics.

Code availability

- The KCOR v6 reference implementation and complete validation suite are available in the project repository.
- Repository URL: <https://github.com/skirsch/KCOR>
- Zenodo DOI: 10.5281/zenodo.18050329

Competing interests

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Authors' contributions

Steven T. Kirsch conceived the method, wrote the code, performed the analysis, and wrote the manuscript.

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[TODO]

Supplementary material

Supplementary appendices provide mathematical derivations and full control-test specifications.

Appendix A. Mathematical derivations

A.1 Frailty mixing induces hazard curvature

Consider a cohort where individual i has hazard $h_i(t) = z_i \cdot h_0(t)$, with frailty z_i drawn from a distribution with mean 1 and variance $\theta > 0$. Let $S_i(t) = \exp(-z_i H_0(t))$ be the individual survival function, where $H_0(t) = \int_0^t h_0(s) ds$.

The cohort survival function is the expectation over frailty:

$$S^{\text{cohort}}(t) = E_z[S_i(t)] = E_z[\exp(-zH_0(t))] = \mathcal{L}_z(H_0(t)),$$

where $\mathcal{L}_z(\cdot)$ is the Laplace transform of the frailty distribution. The cohort hazard is then:

$$h^{\text{cohort}}(t) = -\frac{d}{dt} \log S^{\text{cohort}}(t).$$

Even when $h_0(t) = k$ is constant (so $H_0(t) = kt$), the cohort hazard $h^{\text{cohort}}(t)$ is generally time-varying because high-frailty individuals die earlier, shifting the surviving population toward lower frailty over time. This is the mechanism by which frailty heterogeneity induces **curvature** in cohort-level hazards.

A.2 Gamma-frailty identity derivation

For gamma-distributed frailty $z \sim \text{Gamma}(\alpha = 1/\theta, \beta = 1/\theta)$ with mean 1 and variance θ , the Laplace transform is:

$$\mathcal{L}_z(s) = (1 + \theta s)^{-1/\theta}.$$

The cohort survival function becomes:

$$S^{\text{cohort}}(t) = (1 + \theta H_0(t))^{-1/\theta}.$$

The observed cumulative hazard is $H^{\text{obs}}(t) = -\log S^{\text{cohort}}(t)$, giving:

$$H^{\text{obs}}(t) = \frac{1}{\theta} \log(1 + \theta H_0(t)).$$

This is the gamma-frailty identity (Equation {#eq:gamma-frailty-identity} in the main text).

A.3 Inversion formula

Solving for $H_0(t)$ from the gamma-frailty identity:

$$\theta H^{\text{obs}}(t) = \log(1 + \theta H_0(t))$$

$$e^{\theta H^{\text{obs}}(t)} = 1 + \theta H_0(t)$$

$$H_0(t) = \frac{e^{\theta H^{\text{obs}}(t)} - 1}{\theta}.$$

This inversion recovers the baseline cumulative hazard from the observed cumulative hazard, conditional on the frailty variance θ .

A.4 Variance propagation (sketch)

For uncertainty quantification, variance in $\text{KCOR}(t) = \tilde{H}_{0,A}(t)/\tilde{H}_{0,B}(t)$ can be approximated via the delta method. If $\text{Var}(\tilde{H}_{0,d})$ is available (e.g., from bootstrap or analytic propagation through the inversion), then:

$$\text{Var}(\text{KCOR}) \approx \text{KCOR}^2 \left[\frac{\text{Var}(\tilde{H}_{0,A})}{\tilde{H}_{0,A}^2} + \frac{\text{Var}(\tilde{H}_{0,B})}{\tilde{H}_{0,B}^2} - 2 \frac{\text{Cov}(\tilde{H}_{0,A}, \tilde{H}_{0,B})}{\tilde{H}_{0,A}\tilde{H}_{0,B}} \right].$$

In practice, Monte Carlo resampling provides a more robust approach that captures uncertainty from both event realization and parameter estimation.

Appendix B. Control-test specifications

B.1 Negative control: synthetic gamma-frailty null

The synthetic negative control (Figure fig. 2) is generated using:

- **Data source:** example/Frail_cohort_mix.xlsx (pathological frailty mixture)
- **Generation script:** code/generate_pathological_neg_control_figs.py
- **Cohort A weights:** Equal weights across 5 frailty groups (0.2 each)
- **Cohort B weights:** Shifted weights [0.30, 0.20, 0.20, 0.20, 0.10]
- **Frailty values:** [1, 2, 4, 6, 10] (relative frailty multipliers)
- **Base weekly probability:** 0.01
- **Weekly log-slope:** 0.0 (constant baseline during quiet periods)
- **Skip weeks:** 2
- **Normalization weeks:** 4
- **Time horizon:** 250 weeks

Both cohorts share identical per-frailty-group death probabilities; only the mixture weights differ. This induces different cohort-level curvature under the null.

B.2 Negative control: empirical age-shift construction

The empirical negative control (Figures fig. 3 and fig. 4) is generated using:

- **Data source:** Czech Republic administrative mortality and vaccination data, aggregated into KCOR_CMR format
- **Generation script:** test/negative_control/code/generate_negative_control.py
- **Construction:** Age strata remapped to pseudo-doses within same vaccination category
- **Age mapping:**
 - Dose 0 → YoB {1930, 1935}
 - Dose 1 → YoB {1940, 1945}
 - Dose 2 → YoB {1950, 1955}
- **Output YoB:** Fixed at 1950 (unvax cohort) or 1940 (vax cohort)
- **Sheets processed:** 2021_24, 2022_06

This construction ensures that dose comparisons are within the same underlying vaccination category, preserving a true null while inducing 10–20 year age differences.

B.3 Positive control: injected effect

The positive control (Figure fig. 5 and Table tbl. 5) is generated using:

- **Generation script:** test/positive_control/code/generate_positive_control.py
- **Initial cohort size:** 100,000 per cohort
- **Baseline hazard:** 0.002 per week
- **Frailty variance:** $\theta_0 = 0.5$ (control), $\theta_1 = 1.0$ (treatment)
- **Effect window:** weeks 20–80
- **Hazard multipliers:**
 - Harm scenario: $r = 1.2$
 - Benefit scenario: $r = 0.8$
- **Random seed:** 42
- **Enrollment date:** 2021-06-14 (ISO week 2021_24)

The injection multiplies the treatment cohort's baseline hazard by factor r during the effect window, while leaving the control cohort unchanged.

B.4 Sensitivity analysis parameters

The sensitivity analysis (Figure fig. 6) varies:

- **Baseline weeks:** [2, 3, 4, 5, 6, 7, 8]
- **Quiet-start offsets:** [-12, -8, -4, 0, +4, +8, +12] weeks from 2022-24
- **Quiet-window end:** Fixed at 2024-16
- **Dose pairs:** 1 vs 0, 2 vs 0, 2 vs 1
- **Cohorts:** 2021_24

Output grids show KCOR values for each parameter combination.

Appendix C. Additional figures and diagnostics

C.1 Fit diagnostics

For each cohort d , the gamma-frailty fit produces diagnostic outputs including:

- **RMSE in H -space:** Root mean squared error between observed and model-predicted cumulative hazards over the quiet window. Values < 0.01 indicate excellent fit; values > 0.05 may warrant investigation.
- **Fitted parameters:** \hat{k}_d (baseline hazard level) and $\hat{\theta}_d$ (frailty variance). Very small $\hat{\theta}_d$ (< 0.01) indicates minimal detected depletion; very large values (> 5) may indicate model stress.
- **Number of fit points:** n_{obs} observations in quiet window. Larger n_{obs} provides more stable estimates.

Example diagnostic output from the reference implementation:

```
KCOR6_FIT, EnrollmentDate=2021_24, YoB=1950, Dose=0,
k_hat=4.29e-03, theta_hat=8.02e-01,
RMSE_Hobs=3.37e-03, n_obs=97, success=1
```

C.2 Residual analysis

Fit residuals $r_t = H_d^{\text{obs}}(t) - H_d^{\text{model}}(t; \hat{k}_d, \hat{\theta}_d)$ should be examined for:

- **Systematic patterns:** Residuals should be approximately random around zero. Systematic curvature in residuals suggests model inadequacy.
- **Outliers:** Individual weeks with large residuals may indicate data quality issues or external shocks.
- **Autocorrelation:** Strong autocorrelation in residuals suggests the model is missing time-varying structure.

C.3 Parameter stability checks

Robustness of $(\hat{k}_d, \hat{\theta}_d)$ should be assessed by:

- **Quiet-window perturbation:** Shift the quiet-window start/end by ± 4 weeks and re-fit. Stable parameters should vary by $< 10\%$.
- **Skip-weeks sensitivity:** Vary SKIP_WEEKS from 0 to 8 and verify KCOR trajectories remain qualitatively similar.
- **Baseline-shape alternatives:** Compare default $g(t) = 1$ to mild linear trends and verify normalization is not sensitive to this choice.

The sensitivity analysis (§3.3 and Figure fig. 6) provides a systematic assessment of parameter stability.

C.4 Quiet-window overlay plots

Recommended diagnostic: overlay the prespecified quiet window on hazard and cumulative-hazard time series plots. The fit window should:

- Avoid major epidemic waves or external mortality shocks
- Contain sufficient event counts for stable estimation
- Span a time range where baseline mortality is approximately stationary

Visual inspection of quiet-window placement relative to mortality dynamics is an essential diagnostic step.

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