

### R Tutorial for Statistical Learning

#### Qidi Peng

#### 12: Subset selection methods

| Code   | Comments  | Results |
|--|---|---------|
| #Delete variables having missing data from a data set. |   |         |
| install.packages("ISLR");                              | The functions detecting and deleting missing data can   |         |
|  | be found in the package "ISLR".                         |         |
| library (ISLR);  | Load the package "ISLR".                                |         |
| fix(Hitters);  | Check the data frame "Hitters", which is baseball       |         |
|  | players' personal information. We observe that there    |         |
|  | are missing data in the variable "Salary".              |         |
| is.na(Hitters\$Salary);                                | To check which data is missing. True is existing; False | [1] 59  |
|  | means missing. R regards True as 1 and False as 0.      | [1] 263 |
| sum(is.na(Hitters\$Salary));                           | Number of existing data in "Salary".                    |         |
| sum(1-is.na(Hitters\$Salary));                         | Number of missing data in "Salary".                     | [1] 0   |
| Hitters =na.omit(Hitters);                             | Extract the players who have not any missing data.      |         |
| sum(is.na(Hitters ));                                  | Check the extracted data set. There is no longer        |         |
|  | missing data.   |         |
| #Best subset methods.                                  |   |         |
| install.packages("leaps");                             | The best subset methods function can be found in the    |         |
|  | package "leaps".  |         |
| library(leaps);  | Load the package.                                       |         |
| help(regsubsets.formula);                              | The function regsubsets.formula() performs best         |         |
|  | subset method.  |         |
| regfit.full=regsubsets(Salary~.,Hitters);              | Let Y=Salary, we perform subset selection among all     |         |
|  | other variables in the data set Hitters.                |         |
| summary(regfit.full);                                  | Print the results. String "*" means the corresponding   |         |
|  | variable is selected by the method. For instance, this  |         |
|  | output indicates that the best one-variable model       |         |
|  | contains only "CRBI" and the best two-variable model    |         |
|  | contains only "Hits" and "CRBI". In the output,         |         |
|  | Forced in means whether the variable is contained by    |         |
|  | all models; Forced out means whether the variable is    |         |
|  | excluded by all models.                                 |         |
|  |   |         |
|  | By default, regsubsets() only reports results up to the |         |

| regfit.full=regsubsets(Salary~.,data=Hitters,nvmax =19); | best eight-variable model. But the nymax option can        |        |
|--|--|--------|
|  | be used in order to return as many variables as are        |        |
|  | desired.   |        |
|  | Output the results for up to best 19-variable model.       |        |
| reg.summary=summary(regfit.full);                        | ·  |        |
| Reg.summary;   |  |        |
| 2  |  |        |
| #model selection.  |  |        |
|  | Show all the statistics (variables) contained in           |        |
| names(reg.summary);                                      | reg.summary.   |        |
|  | Show the Cp statistic for all 19 models, the one which     |        |
| reg.summary\$cp;   | minimizes the test MSE is the one containing 10            |        |
|  | variables.   |        |
|  | Show the BIC, the one containing 6 variables is the        |        |
| reg.summary\$bic;  | minimizer of BIC.  |        |
| -  | The R2 statistic is increasing. It is not surprising since |        |
| reg.summary\$rsq;  | R2 is a measure for fitting training data. More            |        |
|  | variables, more accurate.                                  |        |
|  | The adjusted R2 chooses the 11-variable model.             |        |
| reg.summary\$adjr2;                                      | Unlike R2, It does the job to measure the test error.      |        |
|  | Open 4 windows of size 2*2. We are going to illustrate     |        |
| par(mfrow = c(2,2));                                     | the 4 statistics of all the 19 models: RSS, adjusted R2,   |        |
|  | Cp and BIC.  |        |
|  | In Window (1,1), present the plot of RSS. Since RSS        |        |
| plot(reg.summary\$rss ,xlab=" Number of Variables        | is to measure training error, it is decreasing as number   |        |
| ",ylab=" RSS", type="l");                                | of variables increases.                                    |        |
|  | In Window (1,2), present the adjusted R2, it has a         |        |
| plot(reg.summary\$adjr2 ,xlab =" Number of Variables ",  | maximum.   |        |
| ylab=" Adjusted RSq",type="l");                          | Find the maximizer of the adjusted R2.                     |        |
| which.max(reg.summary\$adjr2);                           | Paint this maximum in red.                                 | [1] 11 |
| points (11, reg.summary\$adjr2[11], col ="red",cex =2,   |  |        |
| pch =20);  | In Window (2,1), present Cp. The best model                |        |
| plot(reg.summary\$cp ,xlab =" Number of Variables        | minimizes Cp.  |        |
| ",ylab="Cp", type="l");                                  | Find the minimizer of Cp.                                  |        |
| which.min(reg.summary\$cp);                              | Paint the minimum value point of Cp in red.                | [1] 10 |
| points (10, reg.summary\$cp [10], col ="red",cex =2, pch |  |        |
| =20);  | In Window (2,2), plot BIC VS number of variables.          |        |
| plot(reg.summary\$bic ,xlab=" Number of Variables        |  |        |
| ",ylab=" BIC", type="l");                                | Find the minimizer of BIC.                                 |        |
| which.min(reg.summary\$bic);                             | Add this minimum point in red.                             | [1] 6  |
| points(6, reg.summary\$bic[6], col ="red",cex=2,pch      | We see that all these statistics propose different         |        |
| =20);  | models. It is reasonable because each statistic has a      |        |
|  | different statistical point of view.                       |        |
|  | Coefficient estimates of the best 6-variable model.        |        |

| coef(regfit.full,6);                                       |   |
|--|---|
| #Forward and backward stepwise selection methods.          |   |
| regfit.fwd=regsubsets (Salary~.,data=Hitters,nvmax         | In regsubsets(), the argument "method="forward""        |
| =19,method="forward");                                     | can perform forward stepwise selection.                 |
| summary(regfit.fwd);                                       | Output the results.                                     |
| regfit.bwd=regsubsets (Salary~.,data=Hitters,nvmax         | The argument "method="backward"" can perform            |
| =19,method="backward");                                    | backward stepwise selection                             |
| summary(regfit.bwd);                                       | Output the results                                      |
| coef(regfit.full,7);                                       | We compare the best subsets, forward and backward       |
| coef(regfit.fwd ,7);                                       | stepwise methods. We observe that they provide the      |
| coef(regfit.bwd,7);  | same one to six-variables models, but the               |
| coefficient.bwd,/),  | seven-variable models are different. This shows the 3   |
|  | methods are quite accurate when dealing with small      |
|  | number of predictors.                                   |
|  | number of predictors.                                   |
|  |   |
| # Cross validation.  |   |
| fix(predict.regsubsets);                                   | There is no predict() function for the subsets methods, |
| #In the separate pad write:                                | we create one here.                                     |
| function(object,newdata,id){                               |   |
| form=as.formula(object\$call[[2]]);                        |   |
| mat=model.matrix (form,newdata);                           |   |
| coefi=coef(object,id=id);                                  |   |
| xvars=names(coefi);  |   |
| mat[,xvars]%*%coefi}                                       |   |
| k=10;  | 10-fold cross validation.                               |
| set.seed (1);  |   |
| folds=sample (1:k,nrow(Hitters),replace =TRUE);            |   |
| cv.errors =matrix (NA ,k,19, dimnames =list(NULL ,         |   |
| paste (1:19) ));   |   |
| · · · · · · · · · · · · · · · · · · ·                      |   |
| for(j in 1:k){best.fit=regsubsets                          | Compute the test errors for each subset, using best     |
| (Salary~.,data=Hitters[folds !=j,],                        | subsets method.   |
| nvmax =19);for(i in  |   |
| 1:19){pred=predict.regsubsets(best.fit,Hitters[folds==j,], |   |
| id≕i);   |   |
| cv.errors [j,i]=mean((Hitters\$Salary[folds                |   |
| ==j]-pred)^2)}};   | We use the apply() function to average over the         |
|  | columns of this matrix in order to obtain a vector for  |
| mean.cv.errors =apply(cv.errors ,2, mean);                 | which the jth element is the cross validation error for |
| mean.cv.errors;  | the j-variable model.                                   |

| which.min(mean.ev.errors); | This function tells you which model does the cross-validation selects. Attention, the result is random. |  |
|----------------------------|---|--|
|                            |   |  |
|                            |   |  |

## 13: Ridge regression and the lasso

| Codes  | Comments   | Results      |
|--|--|--------------|
| # Ridge regression. We perform a regression y~x.     |  |              |
| x=model.matrix (Salary~.,Hitters )[,-1];             | Define predictor set (including all predictors, the salaries of players are declined and the qualitative |              |
| y=Hitters\$Salary;                                   | variables are converted to dummy variables).  Define the response y.                                     |              |
| install.packages("glmnet");                          | Ridge and the lasso are contained in the package   |              |
| library (glmnet);                                    | "glmnet". We install it.   |              |
| grid =10^ seq (10,-2, length =100);                  | We choose a grid for the tuning parameter lambda,  |              |
|  | from 10^10 to 10^-2. The mesh is not equal size.   |              |
| ridge.mod =glmnet(x,y,alpha =0,lambda=grid);         | Perform a ridge regression for y~x. When the   |              |
|  | argument alpha=0, we fit ridge regression; when  |              |
|  | alpha=1, we fit the lasso regression; when 0 <alpha<1,< td=""><td></td></alpha<1,<>                      |              |
|  | we fit a ridge-the lasso mixture model.  |              |
| help(glmnet);  | To check more information on glmnet().   |              |
| coef(ridge.mod)[,50];                                | The estimates of the coefficients of the 50th lambda   |              |
|  | value (lambda=11498 in this case.)   | [1] 11497.57 |
| ridge.mod\$lambda [50];                              | The corresponding lambda.  |              |
| predict(ridge.mod,s=50,type ="coefficients")[1:20,]; | Predict the first 20 estimates of the coefficients for   |              |
|  | lambda=50.   |              |
| #subset validation.                                  |  |              |
|  |  |              |

| not good (1).   | Sat a good for subset validation                        |   |
|---|---|---|
| set.seed (1);   | Set a seed for subset validation.                       |   |
| train=sample (1: $nrow(x)$ , $nrow(x)/2$ );                               | Select a training data set index.                       |   |
| test=(- train );  | Define test data set index.                             |   |
| y.test=y[test];   | Define test data set.                                   |   |
|   |   |   |
| ridge.mod =glmnet (x[train ,],y[train],alpha =0, lambda =grid , thresh    | Perform ridge regression using training data set.       |   |
| =1e-12);  |   |   |
| ridge.pred=predict (ridge.mod ,s=4, newx=x[test,]);                       | Predict the regression, using lambda=4 (must be the     |   |
|   | same length as the test set).                           | [1] 101036.8                            |
| mean(( ridge.pred -y.test)^2);  | Calculate the test MSE. The result is random.           |   |
|   |   |   |
|   |   |   |
|   |   |   |
|   |   |   |
| # The lasso.  |   |   |
| $lasso.mod = glmnet \ (x[train \ ,],y[train],alpha = 1,\ lambda = grid);$ | Perform the lasso on the training data (take alpha=1).  |   |
| plot(lasso.mod);  |   |   |
|   | Illustrate the results. We see most of the coefficients |   |
| coef(lasso.mod)[,50];   | are around 0.   |   |
|   | Check the coefficients for lambda=11498. Most are       |   |
| #Cross validation for choosing lambda; subset validation for              | zero.   |   |
| #calculating the test MSE.  |   |   |
| set.seed (1);   |   |   |
| help(cv.glmnet);  |   |   |
| <pre>cv.out =cv.glmnet (x[train ,],y[train],alpha =1);</pre>              | Check the cross validation function for glmnet.         |   |
|   | Run a 10-fold (by default) cross validation for the     |   |
|   | lasso regression on the training data set, in order to  |   |
| plot(cv.out);   | choose lambda.  |   |
|   | Illustrate the results. We see how the test MSE         |   |
| bestlam =cv.out\$lambda.min;  | behaves as log(lambda) increases.                       |   |
| bestlam;  | Return the best lambda among the grid.                  |   |
| lasso.pred=predict (lasso.mod ,s=bestlam ,newx=x[test ,]);                |   | [1] 32.18284                            |
| mean(( lasso.pred -y.test)^2);  | Make the lasso prediction using the best lambda.        | ,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,, |
| X   | Calculate the test MSE by using subset validation.      | [1] 101918.2                            |
|   | The result is random.                                   | [1] 101710.2                            |
|   | The result is failuoili.                                | I                                       |

# 14: Principal component regression (PCR)

| Codes                            | Comments                                     | Results |
|----------------------------------|--|---------|
| #Principal component regression. |  |         |
| install.packages("pls");         | Install the package which contains principal |         |
| library(pls);                    | component regression function pcr().         |         |

| pcr.fit=pcr(Salary~.,                            | One directly performs the PCR.                     |              |
|--|--|--------------|
| data=Hitters ,scale=TRUE ,validation="CV");      |  |              |
| validationplot(pcr.fit ,val.type="MSEP");        | Plot the cross validation MSE VS number of         |              |
|  | components (predictors). Attention, this cross     |              |
|  | validation method is used to select the principal  |              |
|  | components.  |              |
| summary(pcr.fit);                                | Output the results. From the summary we see that   |              |
|  | the best model contains 7 predictors.              |              |
|  |  |              |
| #Calculate the test MSE using subset validation. |  |              |
| pcr.pred=predict (pcr.fit ,x[test ,], ncomp =7); | Use the 7 principle components, we make prediction |              |
|  | using the training data set.                       |              |
| mean((pcr.pred -y.test)^2);                      | Calculate the test MSE.                            | [1] 85199.48 |
|  |  |              |
| pcr.fit=pcr(y~x,scale =TRUE ,ncomp =7);          | Perform the PCR only with 7 components.            |              |
| summary(pcr.fit);                                | Print the results.                                 |              |
|  |  |              |

### 15: Tree-Based Methods

| Codes   | Comments   | Results |
|---|--|---------|
| #Classification tree                          |  |         |
| install.packages("tree");                     | Install the package which contains tree-based        |         |
|   | functions for classification and regression.         |         |
| library(tree);                                |  |         |
| library(ISLR);                                |  |         |
| attach(Carseats);                             | Consider dataset" Carseat"s for classification.      |         |
| High=ifelse(Carseats\$Sales <=8,"No","Yes "); | ifelse() function is used to create a variable,      |         |
|   | which takes on a value of Yes if the Sales           |         |
|   | variable exceeds 8, and takes on a value of No       |         |
|   | otherwise. Here we artificially create response      |         |
|   | labels (2~classes), called High, for each            |         |
|   | predictor.   |         |
| Carseats =data.frame(Carseats ,High);         | Create a data matrix of (X,Y), predictors and        |         |
|   | responses.   |         |
| set.seed(2);                                  |  |         |
| train=sample (1:nrow(Carseats), 200);         | Select 200 training data.                            |         |
| Carseats .test=Carseats[-train ,];            | The rest data are for testing. It is validation set. |         |
| High.test=High[-train];                       | Run classification tree.                             |         |
| tree.carseats                                 | Output the results.                                  |         |
| =tree(High~Sales ,Carseats ,subset=train);    | Plot the results.                                    |         |
| summary(tree.carseats);                       | Predict the rest data.                               |         |
| plot(tree.carseats);                          | Test the prediction by using validation set. Display |         |

| tree.pred=predict(tree.carseats ,Carseats .test ,type="cla        | the results by confusion matrix.                | High.test tree.pred |
|---|---|---------------------|
| ss"); table(tree.pred ,High.test)                                 |   | No Yes              |
|   |   | No 86 27            |
|   |   | Yes 30 57           |
| #Regression tree  |   |                     |
| library(MASS);  | Use data "Boston".                              |                     |
| set.seed(1);  |   |                     |
| train = sample (1:nrow(Boston), nrow(Boston)/2);                  | Use half data for fitting, half for validation. |                     |
| tree.boston=tree(medv~.,Boston , subset=train) ;                  | Fit regression tree.                            |                     |
| summary(tree.boston);   | Output the results.                             |                     |
| plot(tree.boston);  | Plot the results.                               |                     |
| <pre>yhat=predict (tree.boston ,newdata=Boston[-train ,]) ;</pre> | Perform subset validation.                      |                     |
| boston.test=Boston[-train ,"medv"];                               |   |                     |
| plot(yhat ,boston.test);  | Use plot to compare true values and predicted   |                     |
| abline (0,1);   | values.   |                     |
| mean((yhat -boston.test)^2)                                       | Calculate the test MSE.                         | [1] 25.05           |
|   |   |                     |
|   |   |                     |
|   |   |                     |