Inference for imputed latent classes using multiple imputation

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Abstract. I introduce a command to multiply impute latent classes following gsem, lclass() latent class analysis. This allows properly propagating uncertainty in class membership to downstream analysis that may characterize the demographic composition of the classes, or use the class as a predictor variable in statistical models.

Keywords: st0001, postlca_class_predpute, latent class analysis, multiple imputation

1 Latent class analysis

Latent class analysis (LCA) is a commonly used statistical and quantitative social science technique of modeling counts in high dimensional contingency tables, or tables of associations of categorical variables Hagenaars and McCutcheon (2002); McCutcheon (1987). LCA is a form of loglinear modeling, so let us explain that first. If the researcher has several categorical variables X_1, X_2, \ldots, X_p with categories 1 through $m_j, j = 1, \ldots, p$, at their disposal, and can produce counts $n_{k_1 k_2 \ldots k_p}$ in a complete p-dimensional table, the first step could be modeling in main effects:

$$\mathbb{E}\log n_{k_1k_2...k_p} = \text{offset} + \sum_{j=1}^p \sum_{k=1}^{m_j} \beta_{jk_j}$$

$$\tag{1}$$

with applicable identification constraints (such as the sum of the coefficients of a single variable is zero, or the coefficient for the first category of a variable is zero). Parameter estimates can be obtained by maximum likelihood, as equation (1) is a Poisson regression model. This model can be denoted as $X_1 + X_2 + \ldots + X_p$ main effects model. The fit of the model is assessed by the Pearson χ^2 test comparing the expected vs. observed cell counts, or the likelihood ratio test against a saturated model where each cell has its own coefficient. If the model were to be found inadequate, the researcher can entertain adding interactions, e.g. the interaction of X_1 and X_2 would have $m_1 \times m_2$ terms for each pair of values of these variables, rather than $m_1 + m_2$ main effects:

$$\mathbb{E}\log n_{k_1k_2...k_p} = \text{offset} + \sum_{k_1=1}^{m_1} \sum_{k_2=1}^{m_2} \beta_{12,k_1k_2} + \sum_{j=3}^p \sum_{k=1}^{m_j} \beta_{jk_j}$$
 (2)

This model can be denoted as $X_1 \# X_2 + X_3 + \ldots + X_p$.

In the loglinear model notation, the latent class models are models of the form $C\#(X_1+X_2+\ldots+X_p)$. Categorical latent variable C is the latent class. The model is now a mixture of Poisson regressions, and maximum likelihood estimation additionally involves estimating the prevalence of each class of C.

Further extensions of latent class analysis may include:

- 1. Analysis with interactions of the observed variables;
- 2. Analysis with complex survey data (in which case estimation proceeds with svy prefix, and the counts are the weighted estimates of the population totals in cells);
- 3. Constrained analyses with structural zeroes or ones (e.g. that every member of class C = 1 must have the value $X_1 = 1$);
- 4. Constrained analyses where some variables have identical coefficients across classes.

1.1 Official Stata implementation

Official Stata gsem, lclass() implements the main effects LCA. The syntax is that of the SEM families, with the variables that the arrow points to interpreted as the outcome variables, and the latent class variable being the source of the arrow:

```
. webuse gsem_lca1
. gsem (accident play insurance stock <- ), logit lclass(C 2)</pre>
```

The goodness of fit test against the free tabulation counts is provided by estat gof (not available after the complex survey data analysis.)

As LCA is implemented through gsem, all the link functions and generalized linear model families are supported, extending the "mainstream" LCA.

1.2 Hopefully useful examples

LCA has found use in analyses of complicated economic concepts from (measured with error) survey data.

Kolenikov and Daley analyzed the latent classes of employees using the U.S. Department of Labor Worker Classification Survey. The observed variables were (composite) self-report of the employment status (are you an employee at your job; do you refer to your work as your business, your client, your job, etc.); tax status (the forms that the worker receives from their firm: W-2, 1099, K-1, etc.); behavioral control (functions the worker performs and the degree of control over these functions, such as direct reporting to somebody, schedule, permission to leave, etc.); and non-control composite (hired for fixed time or specific project). They found the best fitting model to contain three classes: employees-and-they-know-it (59%), nonemployees-and-they-know-it (24%), and

confused (17%) who classify themselves as employees but their tax documentation is unclear, and other variables tend to place them into non-employee status.

1.3 Scope for this package

Researchers are often interested in describing the latent classes or using these classes in analysis as predictors or as moderators. The official [SEM] **gsem postestimation** commands provide limited possibilities, namely reporting of the means of the dependent variables by class via **estat lcmean**. For nearly all meaningful applications of LCA, this is insufficient.

The program distributed with the current package, postlca_class_predpute, provides a pathway for the appropriate statistical inference that would account for uncertainty in class prediction. This is achieved through the mechanics of multiple imputation (van Buuren 2018). The name is supposed to convey that

- 1. it is supposed to be run after LCA as a post-estimation command;
- 2. it predicts / imputes the latent classes.

2 The new command

Imputation of latent classes, a gsem postestimation command:

```
\begin{stsyntax}
    postlca\_class\_predpute,
    lcimpute(\varname)
    addm(\num)
    \optional{ seed(\num) }
\end{stsyntax}
```

lcimpute(varname) specifies the name of the latent class variable to be imputed. This option is required.

addm(#) specifies the number of imputations to be created. This option is required. seed(#) specifies the random number seed.

3 Examples

3.1 Stata manual data set example

The LCA capabilities of Stata are exemplified in [SEM] Example 50g:

```
frame change defaultcap frame gsem_lca1: clearcap frame drop gsem_lca1frame create gsem_lca1
```

. frame change gsem_lca1

.

. webuse gsem_lca1.dta, clear
(Latent class analysis)

. describe

Contains data from https://www.stata-press.com/data/r18/gsem_lca1.dta
Observations: 216 Latent class analysis
Variables: 4 17 Jan 2023 12:52
(_dta has notes)

Variable name	Storage type	Display format	Value label	Variable label
accident	byte	%9.0g		Would testify against friend in accident case
play	byte	%9.0g		Would give negative review of friend's play
insurance	byte	%9.0g		Would disclose health concerns to friend's insurance company
stock	byte	%9.0g		Would keep company secret from friend

Sorted by: accident play insurance stock

. gsem (accident play insurance stock <-), logit lclass(C 2)
 (output omitted)</pre>

Generalized structural equation model

Number of obs = 216

Log likelihood = -504.46767

		Coefficient	Std. err.	z	P> z	[95% conf.	interval]
1.C		(base outcom	me)				
2.C	_cons	9482041	. 2886333	-3.29	0.001	-1.513915	3824933

Class: 1

Response: accident Family: Bernoulli Link: Logit Response: play Family: Bernoulli Link: Logit Response: insurance Family: Bernoulli Link: Logit Response: stock Family: Bernoulli Link: Logit

		Coefficient	Std. err.	z	P> z	[95% conf.	interval]
accide		0.400.740					
	_cons	.9128742	.1974695	4.62	0.000	.5258411	1.299907
play							
	_cons	7099072	.2249096	-3.16	0.002	-1.150722	2690926
insura	ınce						

	_cons	6014307	.2123096	-2.83	0.005	-1.01755	1853115
stock							
	_cons	-1.880142	.3337665	-5.63	0.000	-2.534312	-1.225972
Class: 2 (output omitted)							
		Coefficient	Std. err.	z	P> z	[95% conf.	interval]
accide	nt						
	_cons	4.983017	3.745987	1.33	0.183	-2.358982	12.32502
play							
	_cons	2.747366	1.165853	2.36	0.018	.4623372	5.032395
insura	nce						
	_cons	2.534582	.9644841	2.63	0.009	.6442279	4.424936
stock							
	_cons	1.203416	.5361735	2.24	0.025	.1525356	2.254297

One of the official post-estimation commands available after gsem, lclass() is the computation of the class-specific means of the outcome variables:

. set rmsg on

r; t=0.00 14:45:54

. estat lcprob

Latent class marginal probabilities

Number of obs = 216

		Delta-method std. err.	[95% conf.	interval]
C				
1	.7207539	.0580926	.5944743	.8196407
2	.2792461	.0580926	.1803593	.4055257

r; t=1.13 14:45:55

. estat lcmean

 $\\ \ \, \text{Latent class marginal means} \\$

Number of obs = 216

	1	Delta-method		
	Margin	std. err.	[95% conf.	interval]
1				
accident	.7135879	.0403588	.6285126	.7858194
play	.3296193	.0496984	.2403573	.4331299
insurance	.3540164	.0485528	.2655049	.4538042
stock	.1323726	.0383331	.0734875	.2268872
2				
accident	.9931933	.0253243	.0863544	.9999956
play	.9397644	.0659957	.6135685	.9935191
insurance	.9265309	.0656538	.6557086	.9881667
stock	.769132	.0952072	.5380601	.9050206

```
r; t=4.48 14:46:00
. set rmsg off
```

The mutiple imputation version of this estimation task could look as follows:

```
. set rmsg on
r; t=0.00 14:46:00
. postlca_class_predpute, lcimpute(lclass) addm(10) seed(12345)
(216 missing values generated)
(10 imputations added; M = 10)
r; t=0.05 14:46:00
. mi estimate : prop lclass
Multiple-imputation estimates
                                   Imputations
                                                              10
                                   Number of obs
                                                             216
Proportion estimation
                                   Average RVI
                                                          0.4594
                                   Largest FMI
                                                          0.3319
                                   Complete DF
                                                             215
DF adjustment:
                 Small sample
                                                           55.99
                                   DF:
                                           min
                                                           55.99
                                           avg
Within VCE type:
                      Analytic
                                                           55.99
                                           max
                                                   Normal
               Proportion
                             Std. err.
                                            [95% conf. interval]
      lclass
                  .7236111
                             .0367281
                                            .6500355
                                                         .7971867
          1
          2
                  .2763889
                             .0367281
                                            .2028133
                                                        .3499645
r; t=2.01 14:46:02
. mi estimate : mean accident, over(lclass)
Multiple-imputation estimates
                                   Imputations
                                                              10
                                                             216
Mean estimation
                                   Number of obs
                                   Average RVI
                                                          0.3882
                                   Largest FMI
                                                          0.4485
                                   Complete DF
                                                             215
DF adjustment:
                                                           35.59
                 Small sample
                                   DF:
                                           min
                                                          116.62
                                            avg
Within VCE type:
                      Analytic
                                                          197.64
                                           max
                           Mean
                                  Std. err.
                                                 [95% conf. interval]
c.accident@lclass
                       .7144964
                                  .0369935
                                                 .6415438
                                                              .7874491
                                                             1.021031
                       .9934973
                                  .0135709
                                                 .9659633
```

Note: Numbers of observations in e(_N) vary among imputations. r; t=2.40 14:46:04

. set ${\tt rmsg}$ off

The name of the latent class variable (here, lclass) and the number of imputations are required. The seed is optional, but of course is strongly recommended for reproducibility of the results, as the underlying data are randomly simulated. The multiple imputation version is notably faster.

As one of many diagnostic outputs of MI, the increase in variances / standard errors

due to imputations serves as an indication of how much of a problem would treating the singly imputed (e.g. modal probability) latent classes would have been. In the above output, the fraction of missing data (FMI) is 33% to 40%, and the relative variance increase (RVI) is the similar range from 39% to 45%. This means that the analysis with the deterministic (modal) imputation of the classes would have had standard errors that are about 20% too small.

```
. webuse gsem_lca1.dta, clear
(Latent class analysis)
. quietly gsem (accident play insurance stock <-), logit lclass(C 2)
. predict post_1, class(1) classposterior
. gen byte lclass_modal = 2 - (post_1 > 0.50)
. mean post_1 lclass_modal
Mean estimation
                                             Number of obs = 216
                                            [95% conf. interval]
                      Mean
                             Std. err.
      post 1
                  .7207539
                             .0257112
                                            .6700756
                                                         .7714321
lclass modal
                  1.328704
                             .0320361
                                            1.265559
                                                        1.391849
. mean accident, over(lclass_modal)
Mean estimation
                                                        Number of obs = 216
                                                        [95% conf. interval]
                                 Mean
                                         Std. err.
c.accident@lclass_modal
                              .6896552
                                         .0385529
                                                        .6136651
                                                                    .7656452
                      2
                                    1
                                                0
```

3.2 NHANES complex survey data example

In many important and realistic applications of LCA, including the case that necessitated the development of this package, the data come from complex survey designs that require setting the data up for the appropriate survey-design adjusted analyses. See [SVY] svyset, [MI] mi svyset, and Kolenikov and Pitblado (2014).

The standard data set for the [SVY] commands is an extract from the National Health and Nutrition Examination Survey, Round Two (NHANES II) data. I will use a handful of binary health outcomes and one ordinal outcome to demonstrate LCA; the ordinal outcome is arguably an extension that is not quite well covered in the "classical" social science LCA.

```
. frame change default
. cap frame nhanes2: clear
. cap frame drop nhanes2
. frame create nhanes2
. frame change nhanes2
.
```

```
. webuse nhanes2.dta, clear
. svyset
Sampling weights: finalwgt
            VCE: linearized
    Single unit: missing
       Strata 1: strata
 Sampling unit 1: psu
          FPC 1: <zero>
. svy , subpop(if hlthstat<8) : ///</pre>
          gsem ///
                  (heartatk diabetes highbp <-, logit) ///
                  (hlthstat <-, ologit) ///
          , lclass(C 2) nolog startvalues(randomid, draws(5) seed(101))
(running gsem on estimation sample)
Survey: Generalized structural equation model
Number of strata = 31
                                                 Number of obs =
                                                                       10,351
                                                 Population size = 117,157,513
Number of PSUs = 62
                                                 Subpop. no. obs =
                                                                       10,335
                                                 Subpop. size = 116,997,257
                                                 Design df
                                                                            31
                           Linearized
               Coefficient std. err.
                                           t
                                               P>|t|
                                                          [95% conf. interval]
1.C
                (base outcome)
2.C
                 1.330043
                           .1259401
                                        10.56 0.000
                                                          1.073186
                                                                      1.586899
       _cons
Class:
Response: heartatk
                                                        Number of obs = 10,335
Family: Bernoulli
Link:
         Logit
Response: diabetes
                                                        Number of obs = 10,335
Family: Bernoulli
Link:
          Logit
Response: highbp
                                                        Number of obs = 10,335
Family:
         Bernoulli
Link:
          Logit
Response: hlthstat
                                                        Number of obs = 10,335
Family:
          Ordinal
Link:
         Logit
                           Linearized
               Coefficient std. err.
                                           t
                                               P>|t|
                                                          [95% conf. interval]
heartatk
                -1.874967
                            .1150791
                                       -16.29
                                                0.000
                                                         -2.109672
                                                                     -1.640261
diabetes
                -1.785271
                            .0805057
                                       -22.18
                                                0.000
                                                         -1.949463
                                                                     -1.621078
      _cons
highbp
                 .4244921
                             .076861
                                         5.52
                                               0.000
                                                          .2677332
                                                                      .5812511
       _cons
/hlthstat
```

cut1	-3.659014	.8903346			-5.474863	-1.843165
cut2	-2.272516	.4402984			-3.17051	-1.374521
cut3	2566588	.2032721			671235	. 1579173
cut4	1.229244	.1951641			.8312038	1.627283
Class: 2						
Response: hear Family: Berr Link: Logi	noulli				Number of ob	s = 10,335
Response: diak Family: Berr Link: Logi	noulli				Number of ob	s = 10,335
Response: high Family: Bern Link: Logi	noulli				Number of ob	s = 10,335
Response: hlth Family: Ordi Link: Logi	inal				Number of ob	s = 10,335
		Linearized				
	Coefficient	std. err.	t	P> t	[95% conf.	interval]
heartatk _cons	-6.081307	.6280801	-9.68	0.000	-7.362285	-4.800329
diabetes						
_cons	-5.223215	.6044468	-8.64	0.000	-6.455993	-3.990438
highbp						
_cons	8166105	.0750027	-10.89	0.000	9695795	6636415
/hlthstat						
cut1	657824	.0483113			7563555	5592926
cut2	.7123144	.0649814			.5797839	.8448448

. set rmsg on

r; t=0.00 14:46:16

cut3 cut4

. estat lcprob

Latent class marginal probabilities

2.647239

24.64389

2.403934

-4.199113

2.890544

53.48689

	Margin	Delta-method std. err.	[95% conf.	interval]
C				
1	.2091523	.0208315	.1698206	.2547976
2	.7908477	.0208315	.7452024	.8301794

.1192958

14.1421

r; t=10.03 14:46:26

. estat lcmean

 ${\tt Latent\ class\ marginal\ means}$

```
      Number of strata = 31
      Number of obs = 10,351

      Number of PSUs = 62
      Population size = 117,157,513

      Design df = 31
```

	1	Delta-method		
	Margin	std. err.	[95% conf.	interval]
1				
heartatk	.1329681	.0132672	.1081603	.1624295
diabetes	.1436535	.0099036	.1246119	.1650562
highbp	.6045577	.018375	.5665363	.6413552
hlthstat				
Excellent	.0251111	.0217959	.0041733	.1366775
Very good	.0683138	.021455	.0355579	.127263
Good	.3427603	.0254834	.2928195	.3964437
Fair	.3375009	.0210993	.2958981	.3817814
Poor	.2263139	.0341724	.1642029	.3033906
2				
heartatk	.00228	.0014287	.0006343	.0081599
diabetes	.0053611	.0032231	.0015686	.0181559
highbp	.3064836	.0159419	.2749643	.3399221
hlthstat				
Excellent	.3412286	.01086	.319438	.3637112
Very good	.3296838	.0082507	.3130796	.346724
Good	.2629283	.0094265	.2441597	.2826002
Fair	.0661594	.0073704	.052623	.0828732
Poor	1.98e-11	2.81e-10	5.68e-24	.9857545

r; t=80.58 14:47:47

This analysis approximates breaking down the population into "generally healthy" and "unhealthy" groups, as e.g. the gradient of *hlthstat* variable between the classes shows. The official gsem postestimation commands take approximately forever to run (there is underlying margins implementation with iterations over the numeric derivatives step size used to compute the stadnard errors). There is an interaction of svy and gsem in that svy forces its own starting values that happen to be infeasible for LCA, hence the need to specify the initial random search. The use of the postlca_class_predpute command makes it possible to run the analylsis much faster, and to conduct complementary analyses, e.g. analysis of the racial composition of the two classes.

[.] set rmsg off

Imputations

10

FPC 1: <zero>
r; t=0.22 14:47:47
. mi estimate : prop lclass
Multiple-imputation estimates

Number of obs 10,351 Proportion estimation Average RVI 0.5318 Largest FMI 0.3641 10350 Complete DF DF adjustment: Small sample DF: min 73.85 73.85 avg Within VCE type: Analytic 73.85

	Proportion	Std. err.	Norn [95% conf.	
lclass				
1	.2675394	.0053851	.256809	.2782698
2	.7324606	.0053851	.7217302	.743191

r; t=1.53 14:47:49

. mi estimate : prop hlthstat if hlthstat < 8, over(lclass)</pre>

 ${\tt Multiple-imputation\ estimates}$ Imputations 10 Proportion estimation Number of obs 10,335 Average RVI Largest FMI Complete DF 10334 36.31 DF adjustment: Small sample DF: min avg Within VCE type: Analytic max

	Proportion	Std. err.	Nor [95% conf.	
hlthstat@lclass				
Excellent 1	.0196036	.0034636	.0126501	.0265572
Excellent 2	.3104144	.0055292	.2995676	.3212613
Very good 1	.0550625	.0061217	.0426506	.0674743
Very good 2	.3217978	.0056545	.3106989	.3328966
Good 1	.2971359	.0106787	.2758813	.3183905
Good 2	.2795891	.0056354	.2685025	.2906756
Fair 1	.3635286	.0106978	.3423564	.3847008
Fair 2	.0881987	.003944	.0803607	.0960367
Poor 1	.2646694	.0089821	.2470257	.282313
Poor 2	0	(no observa	tions)	

Note: Numbers of observations in e(_N) vary among imputations. r; t=3.01 14:47:52

. mi estimate : prop race, over(lclass)

Multiple-imputation estimates Imputations 10 Proportion estimation Number of obs 10,351 0.4677 Average RVI Largest FMI 0.4671 Complete DF 10350 DF adjustment: Small sample 45.27 DF: \min avg 119.43 Within VCE type: 321.80 Analytic max

	Proportion	Std. err.	Normal [95% conf. interval]
race@lclass			
White 1	.839782	.0093485	.8209563 .8586078
White 2	.8889046	.0042799	.8804196 .8973897
Black 1	.1434614	.0085447	.1263568 .160566
Black 2	.0908358	.0038489	.0832192 .0984524
Other 1	.0167566	.0031195	.0105146 .0229986
Other 2	.0202596	.0017697	.0167778 .0237413

Note: Numbers of observations in e(_N) vary among imputations. r; t=2.98 14:47:55

3.3 Choosing the number of imputations

One "researcher's degrees of freedom" aspect of this analysis is the number of imputations M that need to be created. What this number affects the most is the stability of the standard errors obtained through the multiple imputation process. This stability is internally assessed with estimated degrees of freedom associated with the variance estimate (Barnard and Rubin 1999). With M=10 imputations, the smaller "poor health" class have about 50 degrees of freedom:

```
. mi estimate : prop race, over(lclass)
Multiple-imputation estimates
                                   Imputations
                                                              10
                                                          10,351
                                   Number of obs
Proportion estimation
                                   Average RVI
                                                          0.4677
                                   Largest FMI
                                                          0.4671
                                                           10350
                                   Complete DF
DF adjustment:
                 Small sample
                                   DF:
                                           min
                                                           45.27
                                                          119.43
                                           avg
Within VCE type:
                      Analytic
                                           max
                                                          321.80
```

Proportion	Std. err.	Normal [95% conf. interval]
.839782	.0093485	.8209563 .8586078
.8889046	.0042799	.8804196 .8973897
.1434614	.0085447	.1263568 .160566
.0908358	.0038489	.0832192 .0984524
.0167566	.0031195	.0105146 .0229986
.0202596	.0017697	.0167778 .0237413
	.839782 .8889046 .1434614 .0908358 .0167566	.839782 .0093485 .8889046 .0042799 .1434614 .0085447 .0908358 .0038489 .0167566 .0031195

Note: Numbers of observations in e(_N) vary among imputations.

. mr estimate, t	ii tabie			
Multiple-imputat	tion estimates	Imputations	=	10
Proportion estim	nation	Number of obs	=	10,351
		Average RVI	=	0.4677
		Largest FMI	=	0.4671
		Complete DF	=	10350
DF adjustment:	Small sample	DF: min	=	45.27
		avg	=	119.43

[.] set rmsg off

Within VCE ty	pe: Analy	tic	max =	321.80
	Proportion	Std. err.	df	Normal std. err.
race@lclass				
White 1	.839782	.0093485	45.3	34.13
White 2	.8889046	.0042799	106.2	18.59
Black 1	.1434614	.0085447	57.9	28.28
Black 2	.0908358	.0038489	126.3	16.62
Other 1	.0167566	.0031195	59.0	27.89
Other 2	.0202596	.0017697	321.8	9.38

Note: Numbers of observations in e(_N) vary among imputations.

The public use version of the NHANES II data uses the approximate design that has 62 PSU in 31 strata, resulting in 31 design degrees of freedom. The imputation degrees of freedom barely exceed that. Let us push the number of imputations up:

```
. webuse nhanes2.dta, clear
  qui svy , subpop(if hlthstat<8) : ///</pre>
          gsem ///
                   (heartatk diabetes highbp <-, logit) ///
                   (hlthstat <-, ologit) ///
          , lclass(C 2) nolog startvalues(randomid, draws(5) seed(101))
. postlca_class_predpute, lcimpute(lclass) addm(62) seed(9752)
(10,351 missing values generated)
(62 imputations added; M = 62)
Sampling weights: finalwgt
             VCE: linearized
     Single unit: missing
        Strata 1: strata
 Sampling unit 1: psu
           FPC 1: <zero>
. mi estimate : prop race, over(lclass)
Multiple-imputation estimates
                                    Imputations
                                                               62
                                    Number of obs
                                                           10,351
{\tt Proportion} \ {\tt estimation}
                                    Average RVI
                                                           0.2483
                                    Largest FMI
                                                           0.2893
                                    Complete DF
                                                           10350
DF adjustment:
                 Small sample
                                            min
                                                           671.70
                                                         1,786.62
                                            avg
Within VCE type:
                      Analytic
                                                        3,092.35
                                                   Normal
               Proportion
                             Std. err.
                                            [95% conf. interval]
 race@lclass
                                                         .8524827
                  .8369206
                              .0079313
                                            .8213584
    White 1
    White 2
                  .8900061
                              .0038498
                                            .8824571
                                                          .897555
    Black 1
                  .1455849
                              .007628
                                            .1306162
                                                         .1605536
    Black 2
                  .0900031
                              .0035541
                                            .0830334
                                                         .0969728
    Other 1
                  .0174946
                             .0029465
                                            .0117091
                                                           .02328
    Other 2
                  .0199908
                              .001709
                                              .01664
                                                         .0233417
```

Note: Numbers of observations in e(_N) vary among imputations.

```
. mi estimate, dftable
Multiple-imputation estimates
                                   Imputations
                                                             62
                                                         10,351
Proportion estimation
                                   Number of obs
                                   Average RVI
                                                         0.2483
                                  Largest FMI
                                                         0.2893
                                                          10350
                                   Complete DF
DF adjustment:
                                                         671.70
                 Small sample
                                          min
                                                       1,786.62
                                           avg
Within VCE type:
                     Analytic
                                                       3,092.35
                                           max
```

	Proportion	Std. err.	df	Normal std. err.
race@lclass				
White 1	.8369206	.0079313	1100.3	13.14
White 2	.8900061	.0038498	2639.5	7.08
Black 1	.1455849	.007628	1004.8	13.98
Black 2	.0900031	.0035541	2211.1	8.08
Other 1	.0174946	.0029465	671.7	18.45
Other 2	.0199908	.001709	3092.4	6.26

Note: Numbers of observations in e(_N) vary among imputations.

The MI degrees of freedom are now comfortably above 600. In many i.i.d. data situations, increasing the number of imputations to several dozens can often send the MI degrees of freedom to approximate infinity (the reported numbers are in hundreds of thousands). With complex survey designs that have limited degrees of freedom within each implicate, this may not materialize. Researchers are encouraged to adopt the workflow where, in parallel, they

- 1. start with a small number of imputations, like addm(10) in the example above, and develop the analysis code for all the substantive analyses, and
- 2. working with the key outcomes or analyses, experiment with several values of *M* to find a reasonable trade-off when degrees of freedom exceed the sample size for i.i.d. data, and/or exceed the design degrees of freedom for complex survey data by a factor of 3–5.

Then a chosen value of M can be used for all analyses in the paper.

Even a large number of replications may not protect the researcher from classes that may have structural zeroes. These produce zero standard errors and missing degrees of freedom and variance increase statistics:

```
. mi estimate , dftable : prop hlthstat if hlthstat < 8, over(lclass)
Multiple-imputation estimates
                                  Imputations
Proportion estimation
                                  Number of obs
                                                        10,335
                                  Average RVI
                                 Largest FMI
                                                        10334
                                 Complete DF
DF adjustment:
               Small sample
                                 DF:
                                         min
                                                 =
                                                        234.37
                                         avg
```

Within VCE type:	Analytic		max	=	•
	Proportion	Std. err.		df	Normal std. err.
hlthstat@lclass					
Excellent 1	.0183993	.0033919		309.7	32.68
Excellent 2	.3111818	.0054853		6242.4	3.09
Very good 1	.0573944	.0062471		234.4	41.21
Very good 2	.3212476	.0056361		4001.1	5.03
Good 1	.2947403	.0104573		575.3	20.57
Good 2	.2804536	.0055871		2155.5	8.23
Fair 1	.3656239	.010418		1033.8	13.71
Fair 2	.087117	.00393		549.1	21.27
Poor 1	.2638421	.0087535		4603.6	4.40
Poor 2	0	(no observa	ations)	

Note: Numbers of observations in e(_N) vary among imputations.

.

4 User's guide to sj.sty

The Stata Journal is produced using statapress.cls and sj.sty, a IATEX 2ε document class and package, respectively, each developed and maintained at StataCorp by the Stata Press staff. These files manage the look and feel of each article in the Stata Journal.

4.1 The title page

Each insert must begin with title-generating commands. For example,

```
\inserttype[st0001]{article}
\author{short author list}{%
  First author\\First affiliation\\City, State/Country\\Email address
  \and
  Second author\\Second affiliation\\City, State/Country\\Email address
}
\title[short toc title]{Long title for first page of journal insert}
\sjSetDOI{!!}
\maketitle
```

Here \inserttype identifies the tag (for example, st0001) associated with the journal insert and the insert type (for example, article). The default \inserttype is "notag", possibly with a number appended. \author identifies the short and long versions of the list of authors (that is, J. M. Doe for the short title and John Michael Doe for the long). The short author list is only the author initial(s) and last name, and the long author list is the author initial(s) and last name, author affiliation(s), and city and state or country (spelled out with accents applied as necessary). An email address should be included for, at least, the corresponding author. \title identifies the short (optional) and long (required) versions of the title of the journal insert. The optional argument to \title is not given, the long title is used. The required argument to \title is placed in the table of contents with the short author list. Titles should not have any font changes or TeX macros in them. \sjSetDOI{!!} is filled in by Stata Press with a DOI. \maketitle must be the last command of this sequence; it uses the information given in the previous commands to generate the title for a new journal insert.

4.2 The abstract

The abstract is generated using the abstract environment. The abstract states the purpose of the article and area of research. Abstracts must be able to stand alone from the full-text article. For this reason, fully cite references rather than merely supplying the author and date. Also, avoid introduction of acronyms in the abstract. The \keywords are also appended to the abstract. Here is an example abstract with keywords:

```
\begin{abstract}
This is an example article. You should change the \input{} line in
\texttt{main.tex} to point to your file. If this is your first submission to
the {\sl Stata Journal}, please read the following 'getting started''
```

```
information.
```

```
\keywords{\inserttag, command name(s), keyword(s)}
\end{abstract}
```

\inserttag will be replaced automatically with the tag given in \inserttype (here st0001). The first keyword will be the article tag (assigned by Stata Press); other keywords for indexing purposes should be added by the author(s). Community-contributed command names should be listed after the article tag. Plural terms and multiple concepts should be avoided.

4.3 Sectioning

All sections are generated using the standard LATEX sectioning commands: \section, \subsection,

Sections in articles are numbered. If the optional short section title is given, it will be put into bookmarks for the electronic version of the journal; otherwise, the long section title is used. Like article titles, section titles should not have any font changes or TeX macros in them.

4.4 The bib option

BIBTEX is a program that formats citations and references according to a bibliographic style. The following two commands load the bibliographic style file for the *Stata Journal* (sj.bst) and open the database of bibliographic entries (sj.bib):

```
\bibliographystyle{sj}
\bibliography{sj}
```

Here are some example citations: Akaike (1973), Ben-Akiva and Lerman (1985), Dyke and Patterson (1952), Greene (2003), Kendall and Stuart (1979), Hilbe (1993a), Hilbe (1994), Hilbe (1993b), Maddala (1983), and Goossens, Mittelbach, and Samarin (1994). They are generated by using the \citet and \citet* commands from the natbib package. Here we test \citeb and \citebetal: Akaike [1973], Ben-Akiva and Lerman [1985], Dyke and Patterson [1952], Greene [2003], Kendall and Stuart [1979], Hilbe [1993a], Hilbe [1994], Hilbe [1993b], Maddala [1983], and Goossens, Mittelbach, and Samarin [1994]. Sometimes using the \cite macros will result in an overfull line as shown above. The solution is to list the author names and the citation year separately, for example, Ben-Akiva and Lerman [\citeyear{benAkivaLerman}].

The bib option of statapress.sty indicates that citations and references will be formatted using BIBTEX and the natbib package. This option is the default (meaning that it need not be supplied), but there is no harm in supplying it to the statapress document class in the main LATEX driver file (for example, main.tex).

```
\documentclass[bib]{sj}
```

If you choose not to use BiBTFX, you can use the nobib option of statapress.sty.

\documentclass[nobib]{statapress}

BIBTEX and bibliographic styles are described in Goossens, Mittelbach, and Samarin (1994).

4.5 Author information

The About the authors section is generated by using the aboutauthors environment. There is also an aboutauthor environment for journal inserts by one author. For example,

\begin{aboutauthor}
Text giving background about the author goes in here.
\end{aboutauthor}

5 User's guide to stata.sty

stata.sty is a LATEX package containing macros and environments to help authors produce documents containing Stata output and syntax diagrams.

5.1 Citing the Stata manuals

The macros for generating references to the Stata manuals are given in table 1.

Table 1: Stata manual references

Example	Result
\bayesref{bayes}	[BAYES] bayes
\cmref{cmchoiceset}	[CM] cmchoiceset
\dref{Data types}	D Data types
\dsgeref{dsge}	$[ext{DSGE}]$ \mathbf{dsge}
\ermref{eregress}	[ERM] eregress
\fnref{Statistical functions}	[FN] Statistical functions
\fmmref{fmm:~betareg}	[FMM] fmm: betareg
\grefa{Graph Editor}	[G-1] Graph Editor
\grefb{graph}	[G-2] graph
\grefci{line_options}	[G-3] $line_options$
\grefdi{connectstyle}	[G-4] connectstyle
\gsref{6~Using the Data Editor}	[GS] 6 Using the Data Editor
\irtref{irt}	[IRT] irt
\lassoref{Lasso intro}	[LASSO] Lasso intro
\metaref{meta}	[META] meta
\meref{me}	[ME] me
\mreff{Intro}	[M-0] Intro
\mrefa{Ado}	[M-1] Ado
\mrefb{Declarations}	M-2 Declarations
\mrefc{mata clear}	M-3 mata clear
\mrefd{Matrix}	M-4 Matrix
\mrefe{st_view(\$\$)}	$[M-5]$ st_view()
\mrefg{Glossary}	[M-6] Glossary
\miref{mi impute}	[MI] mi impute
\mvref{cluster}	[MV] cluster
\pref{syntax}	[P] syntax
\pssrefa{Intro}	[PSS-1] Intro
\pssrefb{power}	[PSS-2] power
\pssrefc{ciwidth}	[PSS-3] ciwidth
\pssrefd{Unbalanced designs}	[PSS-4] Unbalanced designs
\pssrefe{Glossary}	[PSS-5] Glossary
\pssref{Subject and author index}	[PSS] Subject and author index
\rptref{Dynamic documents intro}	[RPT] Dynamic documents intr
\rref{regress}	[R] regress
\spref{Intro}	[SP] Intro
\stref{streg}	[ST] streg
\svyref{svy:~tabulate oneway}	[SVY] svy: tabulate oneway
\tsref{arima}	[TS] arima
\uref{1~Read thisit will help}	[U] 1 Read this—it will help
\xtref{xtreg}	[XT] xtreg

5.2 Stata syntax

Here is an example syntax display:

This syntax is generated by

```
\begin{stsyntax}
\dunderbar{reg}ress
    \optindepvars\
    \optif\
    \optin\
    \optweight\
    \optional{,
    \underbar{nocons}tant
    \underbar{h}ascons
    tsscons
    vce({\it vcetype\/})
    \underbar{1}evel(\num)
    \underbar{b}eta
    \underbar{ef}orm(\ststring)
    \dunderbar{dep}name(\varname)
    {\it display\_options}
    \underbar{nohe}ader
    \underbar{notab}le
   plus
    \underbar{ms}e1
    \underbar{coefl}egend}
\end{stsyntax}
```

Each command should be formatted using a separate stsyntax environment. Table 2 contains an example of each syntax macro provided in stata.sty.

Table 2: Stata syntax elements

Macro	Result	Macro	Result
\LB	[\ifexp	if
\RB]	\optif	$\left[\ if \ ight]$
\varname	varname	\inrange	in
\optvarname	$[\ varname\]$	\optin	$[\ in\]$
\varlist	varlist	\eqexp	=exp
\optvarlist	$[\ varlist\]$	\opteqexp	[=exp]
\newvarname	newvar	\byvarlist	by $varlist$:
\optnewvarname	$[\ newvar\]$	\optby	$\left[ext{ by } varlist: ight]$
\newvarlist	new var list	\optional{text}	$[{ t text}]$
\optnewvarlist	$\left[\ newvarlist \ \right]$	\optweight	$\big[\ weight\ \big]$
\depvar	depvar	\num	#
\optindepvars	$[\ indepvars\]$	\ststring	string
\opttype	$[\ type\]$		

 $\verb|\underbar| is a standard macro that generates underlines. The \verb|\dunderbar| macro from stata.sty generates the underlines for words with descenders. For example,$

- {\tt \underbar{reg}ress} generates regress
- {\tt \dunderbar{reg}ress} generates regress

The plain TeX macros \it, \sl, and \tt are also available. \it should be used to denote "replaceable" words, such as *varname*. \sl can be used for emphasis but should not be overused. \tt should be used to denote words that are to be typed, such as command names.

When describing the options of a new command, the \hangpara and \morehang commands provide a means to reproduce a paragraph style similar to that of the Stata reference manuals. For example,

level(#) specifies the confidence level, as a percentage, for confidence intervals. The
 default is level(95) or as set by set level; see [U] 20.8 Specifying the width
 of confidence intervals.

was generated by

```
\hangpara {\tt level(\num)} specifies the confidence level, as a percentage, for confidence intervals. The default is {\tt level(95)} or as set by {\tt set level}; see \uref{20.8~Specifying the width of confidence intervals}.
```

5.3 Stata output

sysuse auto

When submitting Stata Journal articles that contain Stata output, also submit a do-file and all relevant datasets that reproduce the output (do not forget to set the random-number seed when doing simulations). Results should be reproducible. Begin examples by loading the data. Code should be written to respect a linesize of 80 characters. The following is an example of the stlog environment containing output from simple linear regression analysis on two variables in auto.dta:

```
(1978 Automobile Data)
. regress mpg weight
     Source
                     SS
                                        MS
                                                        Number of obs =
                                                        F( 1,
                                                                  72) =
                                                                         134.62
                                                        Prob > F
       Model
                 1591.9902
                               1
                                   1591.9902
                                                                         0.0000
   Residual
                851.469256
                              72
                                  11.8259619
                                                        R-squared
                                                                          0.6515
                                                        Adj R-squared = 0.6467
      Total
                2443.45946
                              73 33.4720474
                                                        Root MSE
                                                                       = 3.4389
         mpg
                    Coef.
                            Std. Err.
                                                 P>|t|
                                                            [95% Conf. Interval]
     weight
                -.0060087
                             .0005179
                                        -11.60
                                                 0.000
                                                           -.0070411
                                                                       -.0049763
       _cons
                 39.44028
                            1.614003
                                         24.44
                                                 0.000
                                                           36.22283
                                                                        42.65774
```

The above listing was included using

```
\begin{stlog}
\input{output1.log.tex}\nullskip
\end{stlog}
```

where output1.log.tex is a Stata log file converted to include TEX macros by using the sjlog command (more on sjlog shortly). \nullskip adjusts the spacing around the log file.

On occasion, it is convenient (maybe even necessary) to be able to omit some of the output or let it spill onto the next page. Here is a listing containing the details of the following discussion:

```
\begin{stlog}
. sysuse auto
(1978 Automobile Data)
{\smallskip}
. regress mpg weight
{\smallskip}
\oom
{\smallskip}
\clearpage
\end{stlog}
```

The \oom macro creates a short message indicating omitted output in the following example, and the \clearpage macro inserts a page break.

```
. sysuse auto
(1978 Automobile Data)
. regress mpg weight
(output omitted)
```

The output in output1.log.tex was generated from the following output.do:

```
* output.do
set more off
capture log close
sjlog using output1, replace
sysuse auto
regress mpg weight
sjlog close, replace
sort weight
predict yhat
set scheme sj
scatter mpg yhat weight, c(. 1) s(x i)
graph export output1.eps, replace
```

output.do generates a .smcl file, .log file, and .log.tex file using sjlog. The actual file used in the above listing was generated by

```
. sjlog type output.do
```

sjlog.ado is provided in the Stata package for sjlatex. sjlog is a Stata command that helps generate log output to be included in LATEX documents using the stlog environment. If you have installed the sjlatex package, see the help file for sjlog for more details. The lines that make up the table output from regress are generated from line-drawing macros defined in stata.sty; these were macros written using some font metrics defined in Knuth (1986).

By default, stlog sets an 8-point font for the log. Use the auto option to turn this behavior off, allowing you to use the current font size, or change it by using \fontsize{#}{#}\selectfont. The call to stlog with the auto option looks like \begin[auto]{stlog}.

Here is an example where we are using a 12-point font.

. sjlog type output.do

5.4 About tables

Tables should be created using the standard IATEX methods. See Lamport (1994) for a discussion and examples. Tables should be included in the main text rather than at the end of the document. Tables should be called out in the text prior to appearance.

There are many user-written commands that produce LATEX output, including tables. Christopher F. Baum has written outtable, a Stata command for creating LATEX tables from Stata matrices. Ben Jann's well-known estout command can also produce LATEX output. To find other user-written commands that produce LATEX output, try

. net search latex

Tables with notes

Table 3 shows the order and format to use for notes to tables.

Table 3: Industrial clusters

China		United States	
Core of cluster	Size (in #	Core of cluster	Size (in #
	of units)		of units)
Construction	28 ^a	Public administration and	30 ^b
		defense; compulsory social	
		security	
Food, beverages, and to-	3	Food, beverages, and to-	2
bacco		bacco	
Textiles and textile prod-	2	Chemicals and chemical	1
ucts		products	
Chemicals and chemical	1	Basic metals and fabri-	1
products		cated metal	
Transport equipment	1	Transport equipment	1
$L_a = 0.602***$		$L_a = 0.567$	
$L_w = 0.828**$		$L_w = 0.837$	
$L_m = 0.335^*$		$L_m = 0.287$	
$K^* = 5$		$K^* = 5$	
K = 35		K = 35	

SOURCE: Pew Research Center.

NOTE: U.S. industrial clusters based on U.S. input—output flows of goods expressed in millions of dollars between 35 ISIC industries from the WIOD data. The minimum number of clusters $\mathbf{k}()$ was set equal to five. The algorithm returns L_a , L_w , and L_m , which refer to the average of the internal relative flows, the population-weighted average of the internal relative flows, and the minimum of the internal relative flows, respectively. K^* and K refer to the number of defined regional clusters and the number of distinct starting units, respectively.

Order of notes should be

- 1. source notes
- 2. notes applying to the whole table
- 3. notes applying to specific parts of the table

^a This note pertains only to row 1 column 2.

^b This note pertains only to row 1 column 4.

^{***} denotes p < 0.01; ** denotes p < 0.05; * denotes p < 0.1.

4. notes on significance levels

Special notes:

- Use \centering because the center environment adds unnecessary vertical spacing.
- Place the \begin{threeparttable} line above the caption.

Tables should be included in the main text rather than at the end of the document. Tables should be called out in the text prior to appearance.

5.5 Encapsulated PostScript (EPS)

You can include figures by using either \includegraphics or \epsfig.

```
\begin{figure} [h!]
\begin{center}
\includegraphics{eps/output1.eps}
\end{center}
\caption{Scatterplot with simple linear regression line}
\label{fig}
\end{figure}
\begin{figure} [h!]
\begin{center}
\epsfig{file=output1}
\end{center}
\caption{Scatterplot with simple linear regression line}
\label{fig}
\end{figure}
\label{fig}
\end{figure}
\label{fig}
\end{figure}
\end{figure}
```

Figure 1 is included using \epsfig from the epsfig package.

The graph was generated by running output.do, the do-file given in section 5.3. The epsfig package is described in Goossens, Mittelbach, and Samarin (1994).

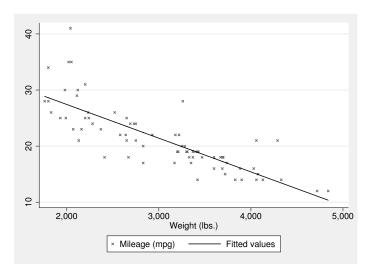


Figure 1: Scatterplot with simple linear regression line

EPS is the preferred format for graphs and line art. Figures should be included in the main text rather than at the end of the document and should be called out in the text prior to appearance. If your article is written in Word, you should submit your figures as separate EPS files. Rasterized-based files of at least 300 dpi (dots per inch) are acceptable. Avoid using bitmaps for figures and graphs, because even if images are outputted at 300 dpi, bitmaps can increase the size of the resulting file for printing. (However, bitmaps will be allowed for photographs, which are used in, for example, the Stata Journal Editors' prize announcement.) Images should be submitted in black and white (grayscale). We recommend that graphs created in Stata use the sj scheme.

5.6 Stored results

The stresults environment provides a table to describe the stored results of a Stata command. It consists of four columns: the first and third column are for Stata result identifiers (for example, r(N), e(cmd)), and the second and fourth columns are for a brief description of the respective identifier. Each group of results is generated using the \stresultsgroup macro. The following is an example containing a brief description of the results that regress stored to e():

Scal	lars			
	e(N)	number of observations	e(F)	F statistic
	e(mss)	model sum of squares	e(rmse)	root mean squared error
	e(df_m)	model degrees of freedom	$e(ll_r)$	log likelihood
	e(rss)	residual sum of squares	e(ll_r0)	log likelihood, constant-only
	e(df_r)	residual degrees of freedom		model
	e(r2)	R-squared	$e(N_clust)$	number of clusters
Mac	cros			
	e(cmd)	regress	e(wexp)	weight expression
	e(depvar)	name of dependent variable	e(clustvar)	name of cluster variable
	e(model)	ols or iv	e(vcetype)	title used to label Std. Err.
	e(wtype)	weight type	e(predict)	program used to implement
				predict
Mat	rices			
	e(b)	coefficient vector	e(V)	variance-covariance matrix of
				the estimators
Fun	ctions			
	e(sample)	marks estimation sample		

Alternatively, you can use the stresults2 environment to create a two column table. This format works better if your descriptions are long.

5.7 Examples and notes

The following are environments for examples and notes similar to those given in the Stata reference manuals. They are generated using the stexample and sttech environments, respectively.

Example

This is the default alignment for a Stata example.

4

Example

For this example, \stexamplehskip was set to 0.0pt before beginning. This sentence is supposed to spill over to the next line, thus revealing that the first sentence was indented.

This sentence is supposed to show that new paragraphs are automatically indented (provided that \parindent is nonzero).

4

□ Technical note

For this note, \sttechhskip was set to -13.90755pt (the default) before beginning. This sentence is supposed to spill over to the next line, thus revealing that the first sentence was indented.

This sentence is supposed to show that new paragraphs are automatically indented (provided that \parindent is nonzero).

5.8 Special characters

Table 4 contains macros that generate some useful characters in the typewriter (fixed width) font. The exceptions are \stcaret and \sttilde, which use the currently specified font; the strictly fixed-width versions are \caret and \tytilde, respectively.

Table 4: Special characters

Macro	Result	Macro	Result
\stbackslash	\	\sttilde	~
\stforslash	/	\tytilde	~
\stcaret	^	\lbr	{
\caret	^	\rbr	}

5.9 Equations and formulas

In (3), \overline{x} was generated using \star Here \star equivalent to the TeX macro \star

$$E(\overline{x}) = \mu \tag{3}$$

In (4), $\widehat{\beta}$ was generated using \sthat{\beta}. Here \sthat is equivalent to the TeX macro \widehat.

$$V(\widehat{\beta}) = V\{(X'X)^{-1}X'y\} = (X'X)^{-1}X'V(y)X(X'X)^{-1} \tag{4}$$

Formulas should be defined and follow a concise style. Different disciplines adhere to different notation styles; however, if the notation cannot be clearly interpreted, you may be asked to make changes. The bolding and font selection guidelines are the following:

- Matrices are capitalized and bolded; for instance, $\Pi + \Theta + \Phi B$.
- Vectors are lowercased and bolded; for instance, $\pi + \theta + \phi \mathbf{b}$.
- Scalars are lowercased and nonbolded; for instance, $r_2 + c_1 c_2$.

Sentence punctuation should not be used in formulas set off from the text.

Formulas in line with the text should use the solidus (/) instead of a horizontal line for fractional terms.

Nesting of grouping is square brackets, curly braces, and then parentheses, or $[\{()\}]$.

Only those equations explicitly referred to in the text should be assigned an equation number.

6 References

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About the authors

Stas Kolenikov is Principal Statistician at NORC who has been using Stata and writing Stata programs for about 25 years. He had worked on economic welfare and inequality, spatiotemporal environmental statistics, mixture models, missing data, multiple imputation, structural equations with latent variables, resampling methods, complex sampling designs, survey weights, Bayesian mixed models, combining probability and non-probability samples, latent class analysis, and likely some other stuff, too.