Updates to the ipfraking ecosystem

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Abstract. Kolenikov (2014) introduced package **ipfraking** for weight calibration procedures known as iterative proportional fitting, or raking, of complex survey weights. This article briefly describes the original package, and adds updates to the core program, as well as a host of additional programs that are used to support the process of creating survey weights in the authors' production code.

Keywords: st0001, survey, calibration, weights, raking

1 Introduction and background

Large scale social, behavioral and health data are often collected via complex survey designs that may involve some or all of stratification, multiple stages of selection and unequal probabilities of selection (Korn and Graubard 1995, 1999). In an ideal setting, varying probabilities of selection are accounted for by using the Horvitz-Thompson estimator of the totals (Horvitz and Thompson 1952; Thompson 1997), and the remaining sampling fluctuations can be further ironed out by post-stratification (Holt and Smith 1979). However, on top of the planned differences in probabilities of obtaining a response from a sampled unit, non-response is a practical problem that has been growing more acute over the recent years (Groves et al. 2001; Pew Research Center 2012). The analysis weights that are provided along with the public use microdata by data collecting agencies are designed to account for unequal probabilities of selection, non-response, and other factors affecting imbalance between the population and the sample, thus making the analyses conducted on such microdata generalizable to the target population.

Earlier, I introduced (Kolenikov 2014) a Stata package called **ipfraking** that implements calibration of survey weights to known control totals to ensure that the resulting weighted data are representative of the population of interest. The process of calibration is aimed at aligning the sample totals of the key variables with those known for the population as a whole. The remainder of this section provides a condensed treatment of estimation with survey data using calibrated weights; full treatment was provided in the original paper.

For a given finite population \mathcal{U} of units indexed i = 1, ..., N, the interests of survey statisticians often lie in estimating the population total of a variable Y

$$T[Y] = \sum_{i \in \mathcal{U}} Y_i \tag{1}$$

A sample S of n units indexed by j = 1, ..., n is taken from U. If the probability to select the i-th unit is known to be π_i , then the probability weights, or design weights,

are given by the inverse probability of selection:

$$w_{1i} = \pi_i^{-1} \tag{2}$$

With these weights, an unbiased (design-based, non-parametric) estimator of the total (1) is (Horvitz and Thompson 1952)

$$t_1[y] = \sum_{j \in \mathcal{S}} \frac{y_j}{\pi_j} \equiv \sum_{j \in \mathcal{S}} w_{1j} y_j, \tag{3}$$

The subindex 1 indicates that the weights w_{1i} were used in obtaining this estimator. Probability weights protect the end user from potentially informative sampling designs, in which the probabilities of selection are correlated with outcomes, and the design-based methods generally ensure that inference can be generalized to the finite population even when the statistical models used by analysts and researchers are not specified correctly (Pfeffermann 1993; Binder and Roberts 2003).

Often, survey statisticians have auxiliary information on the units in the frame, and such information can be included it at the sampling stage to create more efficient designs. Unequal probabilities of selection are then controlled with probability weights, implemented as [pw=exp] in Stata (and can be permanently affixed to the data set with svyset command).

In many situations, however, usable information is not available beforehand, and may only appear in the collected data. The census totals of the age and gender distribution of the population may exist, but age and gender of the sampled units is unknown until the survey measurement is taken on them. It is still possible to capitalize on this additional data by adjusting the weights in such a way that the reweighted data conforms to these known figures. The procedures to perform these reweighting steps are generally known as weight calibration (Deville and Särndal 1992; Deville et al. 1993; Kott 2006, 2009; Särndal 2007).

Suppose there are several (categorical) variables, referred to as *control variables*, that are available for both the population and the sample (age groups, race, gender, educational attainment, etc.). Weight calibration aims at adjusting the margins, or low level interactions, via an iterative optimization aimed at satisfying the *control totals* for the control variables $\mathbf{x} = (x_1, \dots, x_p)$:

$$\sum_{j \in \mathcal{S}} w_{3j} \mathbf{x}_j = T[\mathbf{X}_j] \tag{4}$$

where the right hand side is assumed to be known from a census or a higher quality survey. Deville and Särndal (1992) framed the problem of finding a suitable set of weights as that of constrained optimization with the control equations (4) serving as constraints, and optimization targeted at making the discrepancy between the design weights w_{1j} and calibrated weights w_{3j} as close as possible, in a suitable sense.

In package ipfraking (Kolenikov 2014), I implemented a popular calibration algorithm, known as *iterated proportional fitting*, or as *raking*, which consists of iterative

updating (post-stratification) of each of the margins. (For an in-depth discussion of distinctions between raking and post-stratification, see Kolenikov (2016).) Since 2014, the continuing code development resulted in additional features that this update documents.

2 Updates to ipfraking program and package

Below, I provide full syntax, and list the new features in a dedicated section.

2.1 Syntax of ipfraking

```
ipfraking [if] [in] [weight], ctotal(matname [matname ...]) [
  generate(newvarname) replace double iterate(#) tolerance(#)
  ctrltolerance(#) trace nodivergence trimhiabs(#) trimhirel(#)
  trimloabs(#) trimlorel(#) trimfrequency(once|sometimes|often) double
  meta nograph ]
```

Note that the weight statement [pw=varname] is required, and must contain the initial weights.

Required options

<u>ctotal(matname [matname ...])</u> supplies the names of the matrices that contain the control totals, as well as meta-data about the variables to be used in calibration.

☐ Technical note

The row and column names of the control total matrices (see [P] **matrix rownames**) should be formatted as follows.

- rownames: the name of the control variable
- colnames: the values the control variables takes
- coleq: the name of the variable for which total is computed; typically it is identically equal to 1.

generate(newvarname) contains the name of the new variable to contain the raked weights.

replace indicates that the weight variable supplied in the [pw=varname] expression should be overwritten with the new weights.

One and only one of generate() or replace must be specified.

Linear calibration

linear requests linear calibration of weights.

Options to control convergence

- <u>tolerance(#)</u> defines convergence criteria (the change of weights from one iteration to next). The default is 10^{-6} .
- <u>iter</u>ate(#) specifies the maximum number of iterations. The default is 2000.
- <u>nodivergence</u> overrides the check that the change in weights is greater at the current iteration than in the previous one, i.e., ignores this termination condition. It is generally recommended, especially in calibration with simultaneous trimming.
- <u>ctrltolerance(#)</u> defines the criterion to assess the accuracy of the control totals. It does not impact iterations or convergence criteria, but rather only triggers alerts in the output. The default value is 10^{-6} .

trace requests a trace plot to be added.

Trimming options

- trimhiabs (#) specifies the upper bound U on the greatest value of the raked weights. The weights that exceed this value will be trimmed down, so that $w_{3j} \leq U$ for every $j \in \mathcal{S}$.
- trimhirel(#) specifies the upper bound u on the adjustment factor over the baseline weight. The weights that exceed the baseline times this value will be trimmed down, so that $w_{3j} \leq uw_{1j}$ for every $j \in \mathcal{S}$.
- trimloabs(#) specifies the lower bound L on the smallest value of the raked weights. The weights that are smaller than this value will be increased, so that $w_{3j} \geq L$ for every $j \in \mathcal{S}$.
- trimlorel(#) specifies the lower bound l on the adjustment factor over the baseline weight. The weights that are smaller than the baseline times this value will be increased, so that $w_{3j} \ge lw_{1j}$ for every $j \in \mathcal{S}$.
- trimfrequency (keyword) specifies when the trimming operations are to be performed. The following keywords are recognized:
 - often means that trimming will be performed after each marginal adjustment.
 - sometimes means that trimming will be performed after a full set of variables has been used for post-stratification. This is the default behavior if any of the numeric trimming options above are specified.
 - **once** means that trimming will be performed after the raking process is declared to have converged.

The numeric trimming options trimhiabs(#), trimhirel(#), trimloabs(#), trimlorel(#) can be specified in any combination, or entirely omitted to produce untrimmed weights. By default, there is no trimming.

Miscellaneous options

double specifies that the new variable named in generate() option should be generated as double type. See [D] data types.

meta puts information taken by ipfraking as inputs and produced throughout the process into characteristics stored with the variable specified in generate() option. See details in Section 2.2.

nograph omits the histogram of the calibrated weights, which can be used to speed up ipfraking (e.g., in replicate weight production).

2.2 New features of ipfraking

Since the first publication, the following features and options were added.

Reporting of results and errors by ipfraking was improved in several directions.

- 1. The discrepancy for the worst fitting category is now being reported.
- 2. The number of trimmed observations is reported.
- 3. If ipfraking determines that the categories do not match in the control totals received from ctotals() and those found in the data, a full listing of categories is provided, and the categories not found in one or the other are explicitly shown.

Linear calibration (Case 1 of Deville and Särndal (1992)) is provided with linear option. The weights are calculated analytically:

$$w_{j,\text{lin}} = w_{1j}(1 + \mathbf{x}_j'\lambda). \quad \lambda = \left(\sum_{j \in \mathcal{S}} w_{1j}\mathbf{x}_j\mathbf{x}_j'\right)^{-1} (T[\mathbf{X}_j] - t_1[y])$$
 (5)

This works very fast, but has an undesirable artefact of producing negative weights, as the range of weights is not controlled. (As raking works by multiplying the currents weights by positive factors, if the input weights are all positive, the output weights will be positive as well.) Negative weights are not allowed by the official svy commands or commands that work with [pweights]. In author's experience, running linear weights first, pulling up the negative and small positive weights (replace weight = 1 if weight <= 1) and re-raking using the "proper" iterative proportional fitting runs faster than raking from scratch. An example of linearly calibrated weights is given below in Section 5.

Option meta saves more information in characteristics of the calibrated weight variables. Using Example 3 from Kolenikov (2014) with trimming options, we have:

. capture drop rakedwgt3

rakedwgt3[note0]:

ipfraking [pw=finalwgt], gen(rakedwgt3) ///

trimhiabs(200000) trimloabs(2000) meta

Iteration 1, max rel difference of raked weights = 14.95826

ctotal(ACS2011_sex_age Census2011_region Census2011_race) ///

```
Iteration 2, max rel difference of raked weights = .21474256
 Iteration 3, max rel difference of raked weights = .02754514
 Iteration 4, max rel difference of raked weights = .00511347
 Iteration 5, max rel difference of raked weights = .00095888
 Iteration 6, max rel difference of raked weights = .00018036
 Iteration 7, max rel difference of raked weights = .00003391
 Iteration 8, max rel difference of raked weights = 6.377e-06
 Iteration 9, max rel difference of raked weights = 1.199e-06
 Iteration 10, max rel difference of raked weights = 2.254e-07
The worst relative discrepancy of 3.0e-08 is observed for race == 3
Target value = 20053682; achieved value = 20053682
Trimmed due to the upper absolute limit: 5 weights.
   Summary of the weight changes
                   Mean
                           Std. dev.
                                        Min
                                                              CV
Orig weights
                   11318
                               7304
                                          2000
                                                     79634
                                                              .6453
Raked weights
                   22055
                               18908
                                          4033
                                                    200000
                                                              .8573
                  2.1486
                                        0.9220
                                                   18,9828
Adjust factor
 char li rakedwgt3[]
  rakedwgt3[source]:
                               finalwgt
  rakedwgt3[objfcn]:
                              2.25435521346e-07
                              3.00266822363e-08
  rakedwgt3[maxctrl]:
  rakedwgt3[converged]:
                              1
  rakedwgt3[worstcat]:
                              3
  rakedwgt3[worstvar]:
                              race
  rakedwgt3[command]:
                               [pw=finalwgt], gen( rakedwgt3 ) ctotal( ACS2011_sex_age Census2011_region ...
  rakedwgt3[trimloabs]:
                               trimloabs(2000)
  rakedwgt3[trimhiabs]:
                               trimhiabs(200000)
  rakedwgt3[trimfrequency]:
                               sometimes
 rakedwgt3[hash1]:
                              2347674164
  rakedwgt3[mat3]:
                               Census2011_race
  rakedwgt3[over3]:
                              race
  rakedwgt3[totalof3]:
                               _one
  rakedwgt3[Census2011_race]: 7.48567503861e-09
                              Census2011_region
  rakedwgt3[mat2]:
  rakedwgt3[over2]:
                               region
  rakedwgt3[totalof2]:
                               _one
  rakedwgt3[Census2011_region]:
                               3.00266822363e-08
  rakedwgt3[mat1]:
                              ACS2011_sex_age
  rakedwgt3[over1]:
                               sex_age
  rakedwgt3[totalof1]:
                               _one
  rakedwgt3[ACS2011_sex_age]: 4.13778410340e-09
  rakedwgt3[note1]:
                              Raking controls used: ACS2011_sex_age Census2011_region Census2011_race
```

The following characteristics are stored with the newly created weight variable (see [P] **char**).

command The full command as typed by the user

matrix name The relative matrix difference from the corresponding

control total, see [D] functions

trimhiabs, trimloabs, Corresponding trimming options, if specified

 $\verb|trimhirel|, \verb|trimlorel|,$

trimfrequency

maxctrl the greatest mreldif between the targets and the achieved

weighted totals

objfcn the value of the relative weight change at exit converged whether ipfraking exited due to convergence (1)

vs. due to an increase in the objective function or reaching the limit on the number of iterations (0)

source weight variable specified as the [pw=] input

worstvar the variable in which the greatest discrepancy between

the targets and the achieved weighted totals

(maxctrl) was observed

worstcat the category of the worstvar variable in which the

greatest discrepancy was observed

For the control total matrices $\#=1,2,\ldots$, the following meta-information is stored.

mat# the name of the control total matrix
totalof# the multiplier variable (matrix' coleq
over# the margin associated with the matrix

(i.e., the categories represented by the columns)

Also, **ipfraking** stores the notes regarding the control matrices used, and which of the margins did not match the control totals, if any. See [D] **notes**.

2.3 Utility programs

The original package ipfraking provided two additional utility programs, mat2do and xls2row. An additional utility program whatsdeff was added to compute the design effects and margins of error, common tasks associated with describing survey weights. Specifically, the Transparency Initiative of the American Association for Public Opinion Research (AAPOR 2014) requires that

For probability samples, the estimates of sampling error will be reported, and the discussion will state whether or not the reported margins of sampling error or statistical analyses have been adjusted for the design effect due to weighting, clustering, or other factors.

```
whatsdeff weight\_variable\ [if]\ [in] , [ by(varlist) ]
```

The utility program whatsdeff calculates the apparent design effect due to unequal weighting, DEFF_{UWE} = $1 + CV_w^2 = 1 + r(Var)/(r(mean))^2$ from summarize

weight_variable. Additionally, it reports the effective sample size, $n/\text{DEFF}_{\text{UWE}}$, and also returns the margins of error for the sample proportions that estimate the population proportions of 10% and 50%.

- . webuse nhanes2, clear
- . whatsdeff finalwgt

| Group | Min | Mean | Max | CV | DEFF | N | N eff |
|---------|---------|----------|----------|--------|--------|-------|---------|
| Overall | 2000.00 | 11318.47 | 79634.00 | 0.6453 | 1.4164 | 10351 | 7307.97 |

. return list

scalars:

r(N) = 10351 r(M0E10) = .0068792766212984 r(M0E50) = .0114654610354974 r(Neff_Overall) = 7307.97435325364 r(DEFF_Overall) = 1.416397964696134

. whatsdeff finalwgt, by(sex)

| G | roup | Min | Mean | Max | CV | DEFF | N | N eff |
|-----|----------------|--------------------|----------------------|----------------------|------------------|------------------|--------------|--------------------|
| sex | Male Female | 2000.00 2130.00 | 11426.14 11221.12 | 79634.00 61534.00 | 0.6578 0.6333 | 1.4326 1.4010 | 4915 5436 | 3430.94 3880.01 |
| | Overall | 2000.00 | 11318.47 | 79634.00 | 0.6453 | 1.4164 | 10351 | 7307.97 |

. return list

scalars:

r(N) = 10351 r(M0E10) = .0068792766212984 r(M0E50) = .0114654610354974 r(Neff_Overall) = 7307.97435325364 r(DEFF_Overall) = 1.416397964696134 r(Neff_Female) = 3880.00710397866 r(DEFF_Female) = 1.40102836266093 r(Neff_Male) = 3430.938195872213 r(DEFF_Male) = 1.432552765279559

2.4 New programs in the package

Two new programs are added to the package: ipfraking_report and wgtcellcollapse, and are documented in the subsequent sections of this article. The former provides reports on the raked weights, including summaries of the unweighted data, data with the input weights, and data with the raked weights. The latter creates a mostly automated flow of collapsing weighting cells that are too detailed (and hence have low sample sizes).

3 Excel reports on raked weights: ipfraking_report

```
ipfraking_report using filename , raked_weight(varname) [
  matrices(namelist) by(varlist) xls replace force ]
```

The utility command ipfraking_report produces a detailed report describing the raked weights, and places it into *filename*.dta file (or, if xls option is specified, both *filename*.dta and *filename*.xls files).

Along the way, ipfraking_report runs a regression of the log raking ratio w_{3j}/w_{1j} on the calibration variables. This regression is expected to have R^2 very close to 1, and the regression coefficients provide insights regarding which categories received greater vs. smaller adjustments.

```
. ipfraking_report using rakedwgt3-report, raked_weight(rakedwgt3) replace by(_one) Margin variable sex_age (total variable: _one; categories: 11 12 13 21 22 23). Margin variable region (total variable: _one; categories: 1 2 3 4). Margin variable race (total variable: _one; categories: 1 2 3). Auxiliary variable _one (categories: 1).
```

| file rak | edwgt3-report.dta | saved |
|----------|-------------------|-------|
|----------|-------------------|-------|

| Source | SS | df | MS | | 01 01 000 | = 10,351 |
|----------|------------|----------|-----------|--------|-----------|-------------|
| | | | | | , | > 99999.00 |
| Model | 2086.13859 | 10 | 208.61385 | | = | = 0.0000 |
| Residual | .78315703 | 10,340 | .00007574 | 1 | uared | = 0.9996 |
| | | | | | R-squared | = 0.9996 |
| Total | 2086.92175 | 10,350 | .20163495 | 2 Root | MSE | = .0087 |
| | Г | | | | | |
| 000003 | Coef. | Std. Err | . t | P> t | [95% Conf | . Interval] |
| | | | | | | |
| sex_age | | | | | | |
| 11 | .0644365 | .0002775 | 232.21 | 0.000 | .0638925 | .0649804 |
| 12 | .4545577 | .0003154 | 1441.25 | 0.000 | .4539395 | .455176 |
| 13 | .6782466 | .0002804 | 2418.71 | 0.000 | .6776969 | .6787963 |
| 22 | .3966406 | .0003049 | 1300.84 | 0.000 | .3960429 | .3972383 |
| 23 | .7304392 | .0002726 | 2679.97 | 0.000 | .7299049 | .7309734 |
| | | | | | | |
| region | | | | | | |
| NE | 4455127 | .0002536 | -1756.49 | 0.000 | 4460099 | 4450155 |
| MW | 4428144 | .0002335 | -1896.53 | 0.000 | 4432721 | 4423567 |
| W | 6672675 | .0002407 | -2772.21 | 0.000 | 6677393 | 6667957 |
| | | | | | | |
| race | | | | | | |
| Black | .3360321 | .0002848 | 1180.08 | 0.000 | .3354739 | .3365902 |
| Other | 1.613276 | .0006303 | 2559.34 | 0.000 | 1.612041 | 1.614512 |
| | | | | | | |
| _cons | .5864801 | .0002455 | 2388.48 | 0.000 | .5859988 | .5869614 |
| | L | | | | | |

```
Raking adjustments for sex_age variable:
the smallest was 1.798 for category 21 (21)
the greatest was 3.732 for category 23 (23)
Raking adjustments for region variable (1=NE, 2=MW, 3=S, 4=W):
the smallest was 0.922 for category 4 (W)
the greatest was 1.798 for category 3 (S)
Raking adjustments for race variable (1=white, 2=black, 3=other):
the smallest was 1.798 for category 1 (White)
the greatest was 9.023 for category 3 (Other)
```

It looks like ipfraking had to work harder to adjust the weights of older females, and especially other race individuals.

3.1 Options of ipfraking_report

raked_weight(varname) specifies the name of the raked weight variable to create the report for. This is a required option.

matrices(namelist) specifies a list of matrices (formatted as the matrices supplied to ctotal() option of ipfraking) to produce weighting reports for. In particular, the variables and their categories are picked up from these matrices; and the control totals/proportions are compared to those defined by the weight being reported on.

by(varlist) specifies a list of additional variables for which the weights are to be tabulated in the raking weights report. The difference with the matrices() option is that the control totals for these variables may not be known (or may not be relevant). In particular, by(_one), where _one is identically one, will produce the overall report.

xls requests exporting the report to an Excel file.

replace specifies that the files produced by ipfraking_report (i.e., the .dta and the .xls file if xls option is specified) should be overwritten.

force requires that a variable that may be found repeatedly (between the calibration variables supplied originally to ipfraking, the variables found in the independent total matrices(), and the variables without the control totals provided in by() option) is processed every time it is encountered. (Otherwise, it is only processed once.)

3.2 Variables in the raking report

The raking report file contains the following variables.

| Variable name | Definition |
|---|--|
| | |
| ${	t Weight}_{	t L}{	t Variable}$ | The name of the weight variable, generate() |
| ${	t C_Total_Margin_Variable_Name}$ | The name of the control margin, |
| | rowname of the corresponding ctotal() matrix |
| C_Total_Margin_Variable_Label | The label of the control margin variable |
| Variable_Class | The role of the variable in the report: |
| | Raking margin: a variable used as a calibration margin |
| | (picked up automatically from the ctotal() |
| | matrix, provided meta option was specified) |
| | Other known target: supplied with matrices() |
| | option of ipfraking_report |
| | Auxiliary variable: additional variable supplied |
| | with by() option of ipfraking_report |
| C_Total_Arg_Variable_Name | The name of the multiplier variable |
| C_Total_Arg_Variable_Label | The label of the multiplier variable |

| Variable name | Definition |
|--------------------------------|--|
| C_Total_Margin_Category_Number | Numeric value of the control total category |
| C_Total_Margin_Category_Label | Label of the control total category |
| Category_Total_Target | The control total to be calibrated to |
| | (the specific entry in the ctotal() matrix) |
| Category_Total_Prop | Control total proportion |
| | (the ratio of the specific entry in the ctotal() |
| | matrix to the matrix total) |
| Unweighted_Count | Number of sample observations in the category |
| Unweighted_Prop | Unweighted proportion |
| Unweighted_Prop_Discrep | Difference Unweighted_Prop - Category_Total_Prop |
| Category_Total_SRCWGT | Weighted category total, with source weight |
| Category_Prop_SRCWGT | Weighted category proportion, with source weight |
| Category_Total_Discrep_SRCWGT | Difference Category_Total_SRCWGT - |
| | - Category_Total_Target |
| Category_Prop_Discrep_SRCWGT | Difference Category_Prop_SRCWGT - |
| | - Category_Total_Prop |
| Category_RelDiff_SRCWGT | reldif(Category_Total_SRCWGT, |
| | <pre>Category_Total_Target)</pre> |
| Overall_Total_SRCWGT | Sum of source weights |
| Source | The name of the matrix from which the totals |
| | were obtained |
| Comment | Placeholder for comments, to be entered during |
| | manual review |

For each of the input weights (SRCWGT suffix), raked weights (RKDWGT suffix) and raking ratio (the ratio of raked and input weights, RKDRATIO suffix), the following summaries are provided.

| Variable name | Definition |
|----------------------------------|--------------------------------------|
| Min_WEIGHT | Min of source weights |
| P25_WEIGHT | 25th percentile of source weights |
| P50_WEIGHT | Median of source weights |
| P75_WEIGHT | 75th percentile of source weights |
| ${	t Max}_{-}{	t WEIGHT}$ | Max of source weights |
| Mean_WEIGHT | Mean of source weights |
| $\mathtt{SD}_{-}\mathit{WEIGHT}$ | Standard deviation of source weights |
| DEFF_WEIGHT | Apparent UWE DEFF of source weights |

3.3 Example

| | C_Tota | ~y_Label | Categor~t | Categor | DEFF_SR~T | DEFF_RK~T |
|-----|---------|----------|-----------|-----------|-----------|-----------|
| 1. | sex_age | 11 | 41995394 | 41995394 | 1.2148059 | 1.6259899 |
| 2. | sex_age | 12 | 42148662 | 42148662 | 1.2462168 | 1.5716613 |
| 3. | sex_age | 13 | 26515340 | 26515340 | 1.2241095 | 1.5460785 |
| 4. | sex_age | 21 | 41164255 | 41164255 | 1.2325105 | 1.5639529 |
| 5. | sex_age | 22 | 43697440 | 43697440 | 1.1937826 | 1.5175312 |
| 6. | sex_age | 23 | 32773080 | 32773080 | 1.233902 | 1.664307 |
| 7. | region | NE | 40679030 | 40679030 | 1.3056639 | 1.3657837 |
| 8. | region | MW | 49205289 | 49205289 | 1.3475551 | 1.4909581 |
| 9. | region | S | 85024007 | 85024006 | 1.4950056 | 1.4912995 |
| 10. | region | W | 53385843 | 53385844 | 1.459859 | 2.3772667 |
| 11. | race | White | 1.784e+08 | 1.784e+08 | 1.4059259 | 1.4337901 |
| 12. | race | Black | 29856865 | 29856865 | 1.5173846 | 1.5092533 |
| 13. | race | Other | 20053682 | 20053682 | 1.3179136 | 1.2264706 |
| 14. | _one | 1 | | 2.283e+08 | 1.4164382 | 1.7349278 |

Functionality of ipfraking_report is aimed at manual quality control review, which typically involves (i) categories with raking factors that differ the most (in the output), and (ii) the resulting report file in Excel, although for some aspects of automated quality control, it can be useful, as well.

4 Collapsing weighting cells: wgtcellcollapse

An additional new component of **ipfraking** package is a tool to semi-automatically collapse weighting cells, in order to achieve a required minimal size of the weighting cell. (A typical recommendation is to have cells of size 30 to 50.)

```
wgtcellcollapse task [if] [in], [task_options] where task is one of:

define to define collapsing rules explicitly sequence to create collapsing rules for a sequence of categories report to list the currently defined collapsing rules candidate to find rules applicable to a given category collapse to perform cell collapsing label to label collapsed cells using the original labels after wgtcellcollapse collapse
```

4.1 Syntax of wgtcellcollapse report

```
wgtcellcollapse report , <a href="mailto:varlist">var</a>iables(varlist) [ break ]
```

<u>var</u>iables(varlist) is the list of variables for which the collapsing rules are to be reported

break requires wgtcellcollapse report to exit with error when technical inconsistencies are encountered

4.2 Syntax of wgtcellcollapse define

```
wgtcellcollapse define , \underline{\text{var}}iables(varlist) [ from(numlist) to(#) label(string) max(#) clear ]
```

<u>var</u>iables(varlist) is the list of variables for which the collapsing rule can be used from(numlist) is the list of categories that can be collapsed according to this rule to(#) is the numeric value of the new, collapsed category

label(string) is the value label to be attached to the new, collapsed category max(#) overrides the automatically determined max value of the collapsed variable clear clears all the rules currently defined

Individual collapsing rules can be defined as follows.

```
clear
. set obs 4
number of observations (_N) was 0, now 4
. gen byte x = _n
. label define x_lbl 1 "One" 2 "Two" 3 "Three" 4 "Four"
. label values x x_lbl
. wgtcellcollapse define, var(x) from(1 2 3) to(123)
. wgtcellcollapse report, var(x)
Rule (1): collapse together
    x == 1 (One)
    x == 2 (Two)
    x == 3 (Three)
    into x == 123 (123)
    WARNING: unlabeled value x == 123
.
```

Note how break option of wgtcellcollapse report can be used to abort the execution when technical deficiencies in the rules or in the data are encountered. In this case, the label of the new category 123 was not defined, and this is considered a serious

enough deficiency to stop.

```
. wgtcellcollapse report, var(x) break
Rule (1): collapse together
 x == 1 (One)
 x == 2 (Two)
 x == 3 (Three)
 into x == 123 (123)
 ERROR: unlabeled value x == 123
assertion is false
r(9);
. wgtcellcollapse define, var(x) clear
. wgtcellcollapse define, var(x) from(1 2 3) to(123) label("One through three")
. wgtcellcollapse report, var(x) break
Rule (1): collapse together
 x == 1 (One)
 x == 2 (Two)
 x == 3 (Three)
 into x == 123 (One through three)
```

4.3 Syntax of wgtcellcollapse sequence

```
wgtcellcollapse sequence , variables(varlist) from(numlist) depth(\#)

variables(varlist) is the list of variables for which the collapsing rule can be used from(numlist) is the sequence of values from which the plausible subsequences can be constructed
```

depth(#) is the maximum number of the original categories that can be collapsed Moderate length sequences of collapsing categories can be defined as follows.

| S. Kolenikov | 15 |
|--------------|----|
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```
Rule (2): collapse together
 x == 2 (Two)
 x == 3 (Three)
 into x == 223 (Two to Three)
Rule (3): collapse together
 x == 3 (Three)
 x == 4 (Four)
  into x == 234 (Three to Four)
Rule (4): collapse together
 x == 1 (One)
 x == 2 (Two)
 x == 3 (Three)
 into x == 313 (One to Three)
Rule (5): collapse together
 x == 1 (One)
  x == 223 (Two to Three)
 into x == 313 (One to Three)
Rule (6): collapse together
 x == 3 (Three)
 x == 212 (One to Two)
  into x == 313 (One to Three)
Rule (7): collapse together
 x == 2 (Two)
 x == 3 (Three)
 x == 4 (Four)
  into x == 324 (Two to Four)
Rule (8): collapse together
 x == 2 (Two)
 x == 234 (Three to Four)
 into x == 324 (Two to Four)
Rule (9): collapse together
 x == 4 (Four)
 x == 223 (Two to Three)
 into x == 324 (Two to Four)
```

Note how wgtcellcollapse sequence automatically created labels for the collapsed cells.

When creating sequential collapses, wgtcellcollapse sequence uses the following mnemonics in creating the new categories:

- First comes the length of the collapsed subsequence (up to depth(#)).
- Then comes the starting value of the category in the subsequence (padded by zeroes as needed).
- Then comes the ending value of the category in the subsequence (padded by zeroes as needed).

In the example above, rules 7 through 9 lead to collapsing into the new category 324. This should be interpreted as "the subsequence of length 3 that starts with category 2 and ends with category 4". A numeric value of the collapsed category that reads like

50412 means "the subsequence of length 5 that starts with category 4 and ends with category 12". In that second example, wgtcellcollapse sequence padded the value of 4 with an additional zero, so that the length of resulting collapsed category value is always (of digits of the sequence length) + twice (of digits of the greatest source category).

Note that wgtcellcollapse sequence respects the order in which the categories are supplied in the from() option, and does not sort them. If the categories are supplied in the order 2, 4, 1 and 3, then wgtcellcollapse sequence would collapse 2 with 4, 4 with 1, and 1 with 3:

```
. wgtcellcollapse define, var(x) clear
. wgtcellcollapse sequence, var(x) from(2 4 1 3) depth(2)
. wgtcellcollapse report, var(x)
Rule (1): collapse together
    x == 2 (Two)
    x == 4 (Four)
    into x == 224 (Two to Four)
Rule (2): collapse together
    x == 4 (Four)
    x == 1 (One)
    into x == 241 (Four to One)
Rule (3): collapse together
    x == 1 (One)
    x == 3 (Three)
    into x == 213 (One to Three)
```

4.4 Syntax of wgtcellcollapse candidate

wgtcellcollapse candidate, variable(varname) category(#) [max#]
variable(varname) is the variable whose collapsing rules are to be searched
category(#) is the category for which the candidate rules are to be identified
max(#) is the maximum value of the categories in the candidate rules to be returned

The rules found are quietly returned through the mechanism of sreturn, see [P] return, as they are intended to stay in memory sufficiently long for wgtcellcollapse collapse to evaluate each rule. Going back to the example with sequential collapses of depth 3, we can identify the following candidates for categories 2, 212 (collapsed values of 1 and 2), and a non-existent category of 55:

(Continued on next page)

```
. wgtcellcollapse candidate, var(x) cat(2)
. sreturn list
macros:
           s(goodrule) : "1 2 4 7 8"
s(rule8) : "2:234=324"
              s(rule7) : "2:3:4=324"
              s(rule4) : "1:2:3=313"
              s(rule2) : "2:3=223"
              s(rule1) : "1:2=212"
                s(cat) : "2"
                  s(x) : "x"
. wgtcellcollapse candidate, var(x) cat(2) max(9)
. sreturn list
macros:
           s(goodrule) : "1 2 4 7"
              s(rule7) : "2:3:4=324"
              s(rule4) : "1:2:3=313"
              s(rule2) : "2:3=223"
              s(rule1) : "1:2=212"
                s(cat) : "2"
                  s(x) : "x"
. wgtcellcollapse candidate, var(x) cat(212)
. sreturn list
macros:
           s(goodrule): "6"
              s(rule6) : "3:212=313"
                s(cat): "212"
                  s(x) : "x"
. wgtcellcollapse candidate, var(x) cat(55)
. sreturn list
macros:
                s(cat) : "55"
                  s(x) : "x"
```

In the second call to the option max(9) was used to restrict the returned rules to the rules that deal with the original categories only (so rule 8 that involved a collapsed category 234 was omitted). In the third call, a list of rules that involve a collapsed category cat(212) was requested. Requests for nonexisting categories are not considered errors, but simply produce empty lists of "good rules"

4.5 Syntax of wgtcellcollapse label

```
wgtcellcollapse label , <u>var</u>iable(varname) [ verbose force ]

<u>var</u>iable(varname) is the collapsed variable to be labeled.

verbose outputs the labeling results. There may be a lot of output.

force instructs wgtcellcollapse label to only use categories present in the data.

Example is given in section 4.7 below.
```

4.6 Syntax of wgtcellcollapse collapse

```
wgtcellcollapse collapse [if][in], \underline{\text{var}}iables(varlist) mincellsize(\#) \underline{\text{sav}}ing(dofile\_name) [\underline{\text{gen}}erate(newvarname) replace append feed(varname) strict sort(varlist) run maxpass(\#) \underline{\text{maxcat}}egory(\#) \underline{\text{zer}}oes(numlist) greedy ]
```

<u>var</u>iables(varlist) provides the list of variables whose cells are to be collapsed. When more than one variable is specified, wgtcellcollapse collapse proceeds from right to left, i.e., first attempts to collapse the rightmost variable.

mincellsize(#) specifies the minimum cell size for the collapsed cells. For most weighting purposes, values of 30 to 50 can be recommended.

generate (newvarname) specifies the name of the collapsed variable to be created.

feed(varname) provides the name of an already existing collapsed variable.

strict modifies the behavior of wgtcellcollapse collapse so that only collapsing rules for which all participating categories have nonzero counts are utilized.

sort(varlist) sorts the data set before proceeding to collapse the cell. The default sort order is in terms of the values of the collapsed variable. A different sort order may produce a different set of collapsed cell when cells are tied on size.

maxpass(#) specifies the maximum number of passes through the data set. The default value is 10000.

<u>maxcategory(#)</u> is the maximum category value of the variable being collapsed. It is passed to the internal calls to wgtcellcollapse candidate, see above.

<u>zer</u>oes(numlist) provides a list of the categories of the collapsed variable that may have zero counts in the data.

greedy modifies the behavior wgtcellcollapse collapse to prefer the rules that collapse the maximum number of categories.

Options to deal with the do-file to write the collapsing code to:

<u>sav</u>ing(dofile_name) specifies the name of the do-file that will contain the cell collapsing code.

replace overwrites the do-file if one exists.

append appends the code to the existing do-file.

run specifies that the do-file created is run upon completion. This option is typically specified with most runs.

The primary intent of wgtcellcollapse collapse is to create the code that can be utilized for both the survey data file and the population targets data file that are assumed to have identically named variables. Thus it does not only manipulate the data in the memory and collapses the cells, but also produces the do-file code that can be recycled. To that effect, when a do-file is created with the replace and saving() options, the user needs to specify generate() option to provide the name of the collapsed variable; and when the said do-file is appended with the the append and saving() options, the name of that variable is provided with the feed() option.

The algorithm wgtcellcollapse collapse uses to identify the cells to be collapsed is a variation of greedy search. It first identifies the cells with the lowest (positive) counts; finds the candidate rules for the variable(s) to be collapsed; evaluates the counts of the collapsed cells across all these candidate rules; and uses the rule that produces the smallest size of the collapsed cell across all applicable rules. So when it finds several rules that are applicable to the cell being currently processed that has a size of 5, and the candidate rules produce cells of sizes 7, 10 and 15, wgtcellcollapse collapse will use the rule that produces the cell of size 7. The algorithm runs until all cells have sizes of at least mincellsize(#) or until maxpass(#) passes through the data are executed. It is a pretty dumb algorithm, actually, and it fails quite often. For that reason, a number of hooks are provided to modify its behavior. Section 4.7 will demonstrate the typical failures, and the ways to overcome them.

Hint 1. Since wgtcellcollapse collapse works with the sample data, it will not be able to identify categories that are not observed in the sample (e.g., rare categories), but may be present in the population. This will lead to errors at the raking stage, when the control total matrices have more categories than the data, forcing ipfraking to stop. To help with that, the option zeroes() allows the user to pass the categories of the variables that are known to exist in the population but not in the sample.

Hint 2. The behavior of wgtcellcollapse collapse, zeroes() may still not be satisfactory. As it evaluates the sample sizes of the collapsed cells across a number of candidate rules that involve zero cells, it will probably pick up the rule with lowest number, and that rule may as well leave some other candidate rules with zero cells untouched. This may create problems when wgtcellcollapse collapse returns to those untouched cells, and looks for the existing cells to collapse them with, creating collapsing rules with breaks in the sequences. To improve upon that behavior, option greedy makes wgtcellcollapse collapse look for a rule that has as many categories as possible, thus collapsing as many categories with zero counts in one swipe as it can.

Hint 3. Other than for dealing with zero cells, the option strict should be specified most of the times. It effectively makes sure that the candidate rules correspond to the actual data.

Hint 4. Sometimes, you see some combinations in the data that seem like a nobrainer to collapse. Well, they are nobrainers to you, but wgtcellcollapse collapse is not that smart. If you want to guarantee some specific combination of cells to be collapsed by wgtcellcollapse collapse, your best bet may be to explicitly identify them with the if condition, and specify some ridiculously large cell size like mincellsize(10000) so that wgtcellcollapse collapse makes every possible effort to collapse those cells. It will exit with a complaint that this size could not be achieved, but hopefully the cells

will be collapsed as needed.

4.7 Motivating example

Development of wgtcellcollapse was to address the need to collapse cells of the margin variables so that each cell has a minimum sample size; and to do so in a way that can be easily made consistent between the sample data and the population targets data. The problem arises when some of the target variables have dozens of categories, most of which have small counts. While the primary motivation comes from transportation surveys, the ideas are also applicable to other domains, e.g., continuous age variables or highly detailed race/ethnicity or region of origin categories in health or economic surveys.

The workflow of wgtcellcollapse is demonstrated with the following simulated data set of trips along a metro line composed of 21 stations:

- . use stations, clear
 . list station_id, sep(0)
- station_id 1. 1. Alewife 2. 2. Brookline 3. 8. Carmenton 4. 11. Dogville 18. East End 5. 6. 24. Framington 26. Grand Junction 7. 30. High Point 8. 36. Irvingtown 39. Johnsville 10. 11. 40. King Street 12. 44. Limerick 47. Moscow City 13. 49. Ninth Street 14. 15. 50. Ontario Lake 16. 53. Picadilly Square 17. 55. Queens Zoo 18. 60. Redline Circle 62. Silver Spring 19. 20. 68. Toledo Town 21. 69. Union Station

(Continued on next page)

Turnstile counts were collected at entrances and exits of the stations, producing the following population figures.

- . use trip_population, clear
- . table board_id daypart , c(sum num_pass) cellwidth(10) mi

| | | | daypart | | |
|-----------------------------|---------|--------|------------|-------|---------|
| board_id | AM Peak | Midday | PM Reverse | Night | Weekend |
| 1. Alewife | 1423 | 34 | 219 | 113 | 44 |
| Brookline | 7198 | 298 | 773 | 169 | 144 |
| 8. Carmenton | 19254 | 181 | 3739 | 872 | 422 |
| 11. Dogville | 12626 | 872 | 3476 | 769 | 1270 |
| 18. East End | 2470 | 143 | 1263 | 145 | 114 |
| 24. Framington | 634 | 50 | 1296 | 133 | 60 |
| 26. Grand Junction | 2208 | 233 | 439 | 88 | 166 |
| 30. High Point | 4319 | 424 | 3740 | 482 | 115 |
| 36. Irvingtown | 1221 | 34 | 444 | 30 | 167 |
| 39. Johnsville | 93 | 4 | 64 | 2 | 6 |
| 40. King Street | 398 | 46 | 76 | 11 | 13 |
| 44. Limerick | 1021 | 19 | 129 | 53 | 34 |
| 47. Moscow City | 3300 | 776 | 984 | 140 | 301 |
| 49. Ninth Street | 38 | 22 | 191 | 5 | 5 |
| 50. Ontario Lake | 606 | 22 | 80 | 18 | 23 |
| 53. Picadilly Square | 642 | 71 | 622 | 153 | 69 |
| 55. Queens Zoo | 331 | 23 | 174 | 15 | 19 |
| 60. Redline Circle | 270 | 4 | 63 | 13 | 3 |
| 62. Silver Spring | 3402 | 240 | 950 | 206 | 445 |
| 68. Toledo Town | 5085 | 61 | 744 | 272 | 112 |

. table alight_id daypart , c(sum num_pass) cellwidth(10) mi

| | | | daypart | | |
|----------------------|---------|--------|------------|-------|---------|
| alight_id | AM Peak | Midday | PM Reverse | Night | Weekend |
| 2. Brookline | 19 | | 3 | 2 | |
| 8. Carmenton | 492 | 18 | 56 | 23 | 15 |
| 11. Dogville | 2475 | 42 | 423 | 153 | 80 |
| 18. East End | 929 | 31 | 193 | 67 | 68 |
| 24. Framington | 404 | 13 | 91 | 28 | 27 |
| 26. Grand Junction | 576 | 20 | 147 | 42 | 41 |
| 30. High Point | 2189 | 89 | 560 | 165 | 167 |
| 36. Irvingtown | 288 | 10 | 91 | 21 | 18 |
| 39. Johnsville | 41 | | 11 | 2 | 1 |
| 40. King Street | 131 | 3 | 38 | 8 | 6 |
| 44. Limerick | 277 | 9 | 87 | 20 | 18 |
| 47. Moscow City | 1746 | 78 | 556 | 142 | 128 |
| 49. Ninth Street | 88 | 2 | 25 | 3 | 4 |
| 50. Ontario Lake | 232 | 11 | 70 | 14 | 14 |
| 53. Picadilly Square | 633 | 33 | 198 | 47 | 47 |
| 55. Queens Zoo | 230 | 10 | 71 | 13 | 14 |
| 60. Redline Circle | 90 | 2 | 26 | 3 | 4 |
| 62. Silver Spring | 1134 | 67 | 369 | 91 | 85 |
| 68. Toledo Town | 1372 | 81 | 444 | 112 | 118 |
| 69. Union Station | 53193 | 3038 | 16007 | 2733 | 2677 |

A survey was administered to a sample of the metro line users, with the following counts of cases collected.

As only 3654 surveys were collected from a total of 96783 riders, we would reasonably expect that things do not align quite well. We expect weighting to correct for at least a portion of that nonresponse. The data available for calibration includes the population turnstile counts listed above, and we will produce interactions of daypart and station that will serve as two weighting margins (one for the stations where the metro users boarded, and one for the stations where they got off).

First, we need to define the weighting rules. In this case, the stations are numbered sequentially, with the northernmost, say, station Alewife being number 3, and the southernmost station, Union Station, where everybody gets off to rush to their city jobs or attractions, being number 69. Below, we create a list of stations and provide it to wgtcellcollapse sequence. We would be collapsing stations along the line, with the expectation that travelers boarding or leaving at adjacent stations within the same day part are more similar to one another than the travelers boarding or leaving a particular station at different times of the day. Collapsing rules need to be defined for the daypart variable as well — mostly because wgtcellcollapse collapse expects all variables to have collapsing rules defined.

```
. use trip_sample, clear
. wgtcellcollapse sequence , var(daypart) from(2 3 4) depth(3)
. levelsof board_id, local(stations_on)
1 2 8 11 18 24 26 30 36 39 40 44 47 49 50 53 55 60 62 68
. levelsof alight_id, local(stations_off)
2 8 11 18 24 26 30 36 39 40 44 47 49 50 53 55 60 62 68 69
. local all_stations : list stations_on | stations_off
. * relies on stations being in sequential order!!!
. wgtcellcollapse sequence , var(board_id alight_id) from(`all_stations') depth(20)
. save trip_sample_rules, replace
file trip_sample_rules.dta saved
```

The number of collapsing rules for variables board_id and alight_id created by wgtcellcollapse sequence is 2961 each.

The first pass of cell collapse and raking

Let us say that we want to define weighting cells with at least 20 cases in each. We will thus start with weighting cells defined as station-by-daypart interaction, and collapsing stations within daypart to achieve the cell sizes of at least 20 cases. Here is what a simple run of wgtcellcollapse collapse might look like.

Table 1: Sample frequencies of the trips boardings and alightings.

- . use trip_sample, clear
- . table board_id daypart , c(freq) cellwidth(10) mi

| | | | daypart | | |
|----------------------|---------|--------|------------|-------|---------|
| board_id | AM Peak | Midday | PM Reverse | Night | Weekend |
| 1. Alewife | 46 | 4 | 11 | 7 | 3 |
| 2. Brookline | 236 | 4 | 35 | 6 | 7 |
| 8. Carmenton | 653 | 4 | 184 | 47 | 24 |
| 11. Dogville | 410 | 41 | 166 | 35 | 56 |
| 18. East End | 85 | 5 | 64 | 4 | 4 |
| 24. Framington | 30 | 3 | 74 | 3 | 1 |
| 26. Grand Junction | 72 | 13 | 23 | 5 | 6 |
| 30. High Point | 158 | 20 | 187 | 25 | 12 |
| 36. Irvingtown | 34 | 2 | 25 | 1 | 15 |
| 39. Johnsville | 5 | 1 | 1 | | |
| 40. King Street | 17 | 1 | 2 | | 1 |
| 44. Limerick | 28 | | 9 | 1 | 3 |
| 47. Moscow City | 94 | 31 | 49 | 7 | 13 |
| 49. Ninth Street | | | 9 | | |
| 50. Ontario Lake | 13 | 1 | 4 | 1 | 1 |
| 53. Picadilly Square | 23 | 4 | 35 | 7 | 5 |
| 55. Queens Zoo | 10 | 1 | 14 | | 2 |
| 60. Redline Circle | 13 | | 5 | | |
| 62. Silver Spring | 106 | 18 | 38 | 12 | 17 |
| 68. Toledo Town | 149 | 6 | 33 | 11 | 3 |
| | | | | | |

. table alight_id daypart , c(freq) cellwidth(10) mi

| Weekend |
|-----------|
| Weekend . |
| . 1 |
| 1 |
| |
| 5 |
| 4 |
| 2 |
| 1 |
| 8 |
| 2 |
| |
| |
| 2 |
| 6 |
| |
| 1 |
| 2 |
| |
| |
| 9 |
| 7 |
| 123 |
| |

```
replace dpston1 = 2023940 if inlist(dpston1, 2000039, 2000040)
Pass 1 through the data..
 smallest count = 1 in the cell
                                      2000050
  Invoking rule 50:53=25053
 replace dpston1 = 2025053 if inlist(dpston1, 2000050, 2000053)
Pass 2 through the data...
                                      2000055
 smallest count = 1 in the cell
 Invoking rule 55:25053=35055
 replace dpston1 = 2035055 if inlist(dpston1, 2000055, 2025053)
Pass 3 through the data...
  smallest count = 1 in the cell
 Invoking rule 39:40=23940
 replace dpston1 = 3023940 if inlist(dpston1, 3000039, 3000040)
 (output omitted)
Pass 35 through the data...
 smallest count = 11 in the cell
                                       5031826
  Invoking rule 30:31826=41830
  replace dpston1 = 5041830 if inlist(dpston1, 5000030, 5031826)
Pass 36 through the data...
                                       2065068
  smallest count = 12 in the cell
  WARNING: could not find any rules to collapse dpston1 == 2065068
Pass 37 through the data...
  smallest count = 12 in the cell
                                       3033944
  Invoking rule 26:23036:33944=62644
 replace dpston1 = 3062644 if inlist(dpston1, 3000026, 3023036, 3033944)
  (output omitted)
Pass 38 through the data...
  smallest count = 13 in the cell
                                       1000050
 Invoking rule 50:53=25053
 replace dpston1 = 1025053 if inlist(dpston1, 1000050, 1000053)
  (output omitted)
Pass 43 through the data...
 smallest count = 14 in the cell
                                       3000055
 Invoking rule 53:55=25355
 replace dpston1 = 3025355 if inlist(dpston1, 3000053, 3000055)
Pass 44 through the data...
  smallest count = 15 in the cell
                                       5104068
  WARNING: could not find any rules to collapse dpston1 == 5104068
Pass 45 through the data...
  smallest count = 17 in the cell
                                       5000062
 Invoking rule 11:18:24:26:30:36:39:40:44:47:49:50:53:55:60:62=161162
 replace dpston1 = 5161162 if inlist(dpston1, 5000011, 5000018, 5000024, 5000026, 5
> 000030, 5000036, 5000039, 5000040, 5000044, 5000047, 5000049, 5000050, 5000053, 50
> 00055, 5000060, 5000062)
Pass 46 through the data...
  smallest count = 18 in the cell
                                       2000062
  Invoking rule 30:36:39:40:44:47:49:50:53:55:60:62=123062
 replace dpston1 = 2123062 if inlist(dpston1, 2000030, 2000036, 2000039, 2000040, 2
> 000044, 2000047, 2000049, 2000050, 2000053, 2000055, 2000060, 2000062)
Pass 47 through the data...
  smallest count = 18 in the cell
                                       3054960
 Invoking rule 62:54960=64962
 replace dpston1 = 3064962 if inlist(dpston1, 3000062, 3054960)
Pass 48 through the data...
                                       1023940
  smallest count = 22 in the cell
 Done collapsing! Exiting...
. return list
scalars:
```

```
r(arg_min_id) = 1023940
                r(min) = 22
macros:
            r(cfailed): "2065068.5104068"
             r(failed) : "2065068 5104068"
. wgtcellcollapse collapse, variables(daypart alight_id) mincellsize(20) ///
          generate(dpstoff1) saving(dpstoff1.do) replace run
Pass 0 through the data...
 smallest count = 1 in the cell
                                      1000002
  Invoking rule 2:8=20208
 replace dpstoff1 = 1020208 if inlist(dpstoff1, 1000002, 1000008)
Pass 1 through the data...
 smallest count = 1 in the cell
                                      2000008
  Invoking rule 8:11=20811
  replace dpstoff1 = 2020811 if inlist(dpstoff1, 2000008, 2000011)
Pass 2 through the data...
                                      2000018
  smallest count = 1 in the cell
  Invoking rule 18:24=21824
 replace dpstoff1 = 2021824 if inlist(dpstoff1, 2000018, 2000024)
  (output omitted)
Pass 37 through the data...
  smallest count = 7 in the cell
                                      5000068
 Invoking rule 62:68=26268
 replace dpstoff1 = 5026268 if inlist(dpstoff1, 5000062, 5000068)
Pass 38 through the data...
                                      2044753
  smallest count = 8 in the cell
  WARNING: could not find any rules to collapse dpstoff1 == 2044753
Pass 39 through the data...
                                      4053647
  smallest count = 8 in the cell
  Invoking rule 30:53647=63047
 replace dpstoff1 = 4063047 if inlist(dpstoff1, 4000030, 4053647)
  (output omitted)
Pass 44 through the data...
  smallest count = 10 in the cell
                                       4041126
  Invoking rule 41126:63047=101147
  replace dpstoff1 = 4101147 if inlist(dpstoff1, 4041126, 4063047)
Pass 45 through the data...
                                       4055368
  smallest count = 10 in the cell
  WARNING: could not find any rules to collapse dpstoff1 == 4055368
Pass 46 through the data...
  smallest count = 12 in the cell
                                       1020208
  Invoking rule 20208:21118:24=50224
  replace dpstoff1 = 1050224 if inlist(dpstoff1, 1020208, 1021118, 1000024)
  (output omitted)
Pass 52 through the data...
  smallest count = 15 in the cell
                                       3044955
  Invoking rule 44955:60:62=64962
  replace dpstoff1 = 3064962 if inlist(dpstoff1, 3044955, 3000060, 3000062)
Pass 53 through the data...
                                       5026268
  smallest count = 16 in the cell
  Invoking rule 69:26268=36269
 replace dpstoff1 = 5036269 if inlist(dpstoff1, 5000069, 5026268)
Pass 54 through the data...
  smallest count = 22 in the cell
                                       3000047
 Done collapsing! Exiting...
. return list
scalars:
```

```
r(arg_min_id) = 3000047
r(min) = 22
macros:
r(cfailed) : "2044753,4055368"
r(failed) : "2044753 4055368"
```

The collapsed values of the variables dpston (DayPart-STation-ON) and dpstoff (DayPart-STation-OFF) combine the values of the parent variables. The value of dpston==1000001 indicates daypart==1 and station ID 1. The value of dpston==2023940, the very first collapsed cell, indicates daypart==2 and sequence of two stations from 39 to 40. The value of dpston==3064960 indicates daypart==3 and sequence of six stations from 49 to 60.

Note that wgtcellcollapse returns a list of the cells that it could not collapse in r(failed) macro (and a comma delimited list, in f(cfailed)). These returned values should be used in production code by making an assert (Gould 2003) that these macros are empty. While we know that some cell counts are less than 20, we will ignore the issue for the moment, as there are bigger concerns with the collapsed cells at the moment, as will become clear once we follow through with the workflow and attempt raking.

From the above run, wgtcellcollapse produced two files, one for each weighting margin, called dpston.do and dpstoff.do. An interested reader is welcome to list them; they contain long sequences of replace commands to perform the cell collapsing. The point of creating these is that they can be run on the population data to create identical categories:

| Over | Total | Std. Err. | [95% Conf. | Interval] |
|--------------|-------|-----------|------------|-----------|
| num_pass | | | | |
| 1000001 | 1423 | 967.7508 | -476.9595 | 3322.959 |
| 1000002 | 7198 | 4895.91 | -2414.011 | 16810.01 |
| (output omit | ted) | | | |
| 5104068 | 270 | 116.7702 | 40.74822 | 499.2518 |
| 5161162 | 1723 | 909.6551 | -62.90172 | 3508.902 |

| 28 | Raking survey data: updates |
|----|-----------------------------|
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```
. total num_pass , over(dpstoff1)
Total estimation
                                   Number of obs
                                                              719
      1000011: dpstoff1 = 1000011
      1000018: dpstoff1 = 1000018
  (output\ omitted)
      5000060: dpstoff1 = 5000060
      5036269: dpstoff1 = 5036269
      5140853: dpstoff1 = 5140853
        Over
                     Total
                             Std. Err.
                                            [95% Conf. Interval]
num_pass
     1000011
                      2475
                             1468.807
                                           -408.6691
                                                         5358.669
     1000018
                       929
                             360.7303
                                            220.7878
                                                        1637.212
  (output omitted)
     5000060
                                    2
                                            .0734531
                                                        7.926547
     5036269
                      2880
                             980.8909
                                            954.2428
                                                         4805.757
     5140853
                       634
                             139.2172
                                            360.6787
                                                        907.3213
```

- . matrix dpstoff1 = e(b)
- . matrix coleq dpstoff1 = _one
- . matrix rownames dpstoff1 = dpstoff1

We can then go back to the sample data and try creating raked weights:

```
. use trip_sample, clear
. run dpston1
. run dpstoff1
. gen byte _one = 1
. ipfraking [pw=_one], ctotal(dpston1 dpstoff1) gen(raked_weight1)
categories of dpston1 do not match in the control dpston1 and in the data (nolab opt
> ion)
This is what dpston1 gives:
  _one:1000001 _one:1000002 _one:1000008 _one:1000011 _one:1000018 _one:1000024 _one
> :1000026 _one:1000030 _one:1000036 _one:1000044 _one:1000047 _one:1000049 _one:100
> 0062 _one:1000068 _one:1023940 _one:1025053 _one:1025560 _one:2000011 _one:2065068
> _one:2070126 _one:2110847 _one:2123062 _one:3000008 _one:3000011 _one:3000018 _on
> e:3000024 _one:3000030 _one:3000036 _one:3000047 _one:3000068 _one:3020102 _one:30
> 25355 _one:3062644 _one:3064962 _one:4030108 _one:4041830 _one:4084768 _one:413115
> 3 _one:5030108 _one:5041830 _one:5053647 _one:5104068 _one:5161162
This is what I found in data:
  _one:1000001 _one:1000002 _one:1000008 _one:1000011 _one:1000018 _one:1000024 _one
> :1000026 _one:1000030 _one:1000036 _one:1000044 _one:1000047 _one:1000062 _one:100
> 0068 _one:1023940 _one:1025053 _one:1025560 _one:2000011 _one:2065068 _one:2070126
> _one:2110847 _one:2123062 _one:3000008 _one:3000011 _one:3000018 _one:3000024 _on
> e:3000030 _one:3000036 _one:3000047 _one:3000068 _one:3020102 _one:3025355 _one:30
> 62644 _one:3064962 _one:4030108 _one:4041830 _one:4084768 _one:4131153 _one:503010
> 8 _one:5041830 _one:5053647 _one:5104068 _one:5161162
This is what dpston1 has that data don't:
  one:1000049
This is what data have that dpston1 doesn't:
  <none>
r(111);
```

```
. ipfraking [pw=_one], ctotal(dpstoff1 dpston1) gen(raked_weight1)
categories of dpstoff1 do not match in the control dpstoff1 and in the data (nolab o
> ption)
This is what dostoff1 gives:
  _one:1000011 _one:1000018 _one:1000030 _one:1000047 _one:1000068 _one:1000069 _one
> :1025355 _one:1043644 _one:1060226 _one:1064962 _one:2044753 _one:2190869 _one:300
> 0002 _one:3000047 _one:3000068 _one:3000069 _one:3050826 _one:3053044 _one:3064962
> _one:4000002 _one:4000008 _one:4000049 _one:4055368 _one:4075069 _one:4101147 _on
> e:5000055 _one:5000060 _one:5036269 _one:5140853
This is what I found in data:
  _one:1000011 _one:1000018 _one:1000030 _one:1000047 _one:1000068 _one:1000069 _one
> :1025355 _one:1043644 _one:1060226 _one:1064962 _one:2044753 _one:2190869 _one:300
> 0047 _one:3000068 _one:3000069 _one:3050826 _one:3053044 _one:3064962 _one:4055368
  _one:4075069 _one:4101147 _one:5036269 _one:5140853
This is what dpstoff1 has that data don't:
  _one:3000002 _one:4000002 _one:4000008 _one:4000049 _one:5000055 _one:5000060
This is what data have that dpstoff1 doesn't:
  <none>
r(111);
```

We see that raking failed, because survey nonresponse wiped out some of the smaller stations from the sample. (Note also the informative error message with diagnostics of missing categories produced by <code>ipfraking</code>. This is a functionality added since the first 2010 publication in *The Stata Journal*. The message lists the categories found in the data, in the control totals, and in the mismatch.) We should have suspected as much from the full output of the population control totals, where e.g. the line for <code>dpstoff==5000060</code> showed only 4 alightings at station Redline Circle (60) on the weekends.

The second pass of cell collapse and raking: zeroes() option

Having identified the issue, we can overcome it with zeroes() option of wgtcellcollapse collapse whose purpose is specifically to add missing categories. This option provides the list of stations that may have zero sample counts in a given daypart. For instance, notice that the sample registers only one alighting at Brookline (2) in AM Peak daypart, even though there are passengers exiting in other dayparts. All in all, wgtcellcollapse needs to be made aware of the zero sample boardings at Johnsville (39), King Street (40), Limerick (44), Ninth Street (49), Queens Zoo (55) and Redline Circle (60); as well as zero alightings at Brookline (2), Carmenton (8), Irvingtown (36), Johnsville (39), King Street (40), Limerick (44), Moscow City (47), Ninth Street (49), Ontario Lake (50), Queens Zoo (55), Redline Circle (60), and Silver Spring (62).

(Continued on next page)

```
. use trip_sample_rules, clear
. wgtcellcollapse collapse, variables(daypart board_id) mincellsize(20) ///
         zeroes(39 40 44 49 55 60) ///
          generate(dpston2) saving(dpston2.do) replace run
Pass 0 through the data...
 smallest count = 1 in the cell
Processing zero cells...
 Invoking rule 49:50=24950 to collapse zero cells
 replace dpston2 = 1024950 if inlist(dpston2, 1000049, 1000050)
Pass 0 through the data...
 smallest count = 1 in the cell
                                      2000039
 Invoking rule 40:44=24044 to collapse zero cells
 replace dpston2 = 2024044 if inlist(dpston2, 2000040, 2000044)
Pass 0 through the data...
 smallest count = 1 in the cell
                                      2000039
 Invoking rule 49:50=24950 to collapse zero cells
  replace dpston2 = 2024950 if inlist(dpston2, 2000049, 2000050)
Pass 0 through the data...
                                      2000039
  smallest count = 1 in the cell
  Invoking rule 55:60=25560 to collapse zero cells
 replace dpston2 = 2025560 if inlist(dpston2, 2000055, 2000060)
Pass 0 through the data...
 smallest count = 1 in the cell
                                      2000039
 Invoking rule 36:39=23639 to collapse zero cells
 replace dpston2 = 4023639 if inlist(dpston2, 4000036, 4000039)
Pass 0 through the data...
  smallest count = 1 in the cell
                                      2000039
 Invoking rule 40:44=24044 to collapse zero cells
 replace dpston2 = 4024044 if inlist(dpston2, 4000040, 4000044)
Pass 0 through the data...
 smallest count = 1 in the cell
                                     2000039
 Invoking rule 49:50=24950 to collapse zero cells
 replace dpston2 = 4024950 if inlist(dpston2, 4000049, 4000050)
Pass 0 through the data...
 smallest count = 1 in the cell
 Invoking rule 53:55=25355 to collapse zero cells
 replace dpston2 = 4025355 if inlist(dpston2, 4000053, 4000055)
Pass 0 through the data...
                                      2000039
 smallest count = 1 in the cell
  Invoking rule 24950:53:55:60=54960 to collapse zero cells
 replace dpston2 = 4054960 if inlist(dpston2, 4024950, 4000053, 4000055, 4000060)
Pass 0 through the data...
  smallest count = 1 in the cell
                                      2000039
 Invoking rule 39:40=23940 to collapse zero cells
 replace dpston2 = 5023940 if inlist(dpston2, 5000039, 5000040)
Pass 0 through the data...
  smallest count = 1 in the cell
                                      2000039
  Invoking rule 49:50=24950 to collapse zero cells
 replace dpston2 = 5024950 if inlist(dpston2, 5000049, 5000050)
Pass 0 through the data...
 smallest count = 1 in the cell
                                      2000039
 Invoking rule 24950:25355:60=54960 to collapse zero cells
 replace dpston2 = 5054960 if inlist(dpston2, 5024950, 5025355, 5000060)
Pass 0 through the data...
  smallest count = 1 in the cell
                                      2000039
Pass 12 through the data...
 smallest count = 1 in the cell
                                      2000039
 Invoking rule 39:24044=33944
 replace dpston2 = 2033944 if inlist(dpston2, 2000039, 2024044)
```

```
(output omitted)
Pass 44 through the data...
  smallest count = 10 in the cell
                                       5020102
  Invoking rule 8:20102=30108
  replace dpston2 = 5030108 if inlist(dpston2, 5000008, 5020102)
Pass 45 through the data...
  smallest count = 10 in the cell
                                       5055368
  WARNING: could not find any rules to collapse dpston2 == 5055368
Pass 46 through the data...
  smallest count = 11 in the cell
                                       2100844
  Invoking rule 47:100844=110847
 replace dpston2 = 2110847 if inlist(dpston2, 2000047, 2100844)
  (output omitted)
Pass 57 through the data...
  smallest count = 18 in the cell
                                       3054960
  Invoking rule 62:54960=64962
  replace dpston2 = 3064962 if inlist(dpston2, 3000062, 3054960)
Pass 58 through the data...
  smallest count = 18 in the cell
                                       4055368
  WARNING: could not find any rules to collapse dpston2 == 4055368
Pass 59 through the data...
  smallest count = 20 in the cell
                                       2000030
  Done collapsing! Exiting...
. return list
scalars:
         r(arg_min_id) = 2000030
                r(min) = 20
macros:
            r(cfailed) : "5055368,4055368"
             r(failed): "5055368 4055368"
. wgtcellcollapse collapse, variables(daypart alight_id) mincellsize(20) ///
          zeroes(2 8 36 39 40 44 47 49 50 55 60 62) ///
          generate(dpstoff2) saving(dpstoff2.do) replace run
Pass 0 through the data...
 smallest count = 1 in the cell
                                      1000002
Processing zero cells...
  Invoking rule 39:40=23940 to collapse zero cells
  replace dpstoff2 = 1023940 if inlist(dpstoff2, 1000039, 1000040)
Pass 0 through the data...
  smallest count = 1 in the cell
                                      1000002
  Invoking rule 2:8=20208 to collapse zero cells
  replace dpstoff2 = 2020208 if inlist(dpstoff2, 2000002, 2000008)
Pass 0 through the data...
                                      1000002
  smallest count = 1 in the cell
  Invoking rule 30:36=23036 to collapse zero cells
  replace dpstoff2 = 2023036 if inlist(dpstoff2, 2000030, 2000036)
Pass 0 through the data...
  smallest count = 1 in the cell
  Invoking rule 26:30:36:39=42639 to collapse zero cells
 replace dpstoff2 = 2042639 if inlist(dpstoff2, 2000026, 2000030, 2000036, 2000039)
  (output omitted)
Pass 0 through the data...
  smallest count = 1 in the cell
                                      1000002
  Invoking rule 24950:53:55:60=54960 to collapse zero cells
  replace dpstoff2 = 5054960 if inlist(dpstoff2, 5024950, 5000053, 5000055, 5000060)
Pass 0 through the data...
```

```
smallest count = 1 in the cell
                                      1000002
Pass 24 through the data...
  smallest count = 1 in the cell
                                      1000002
  Invoking rule 2:8=20208
  replace dpstoff2 = 1020208 if inlist(dpstoff2, 1000002, 1000008)
  (output omitted)
Pass 50 through the data...
  smallest count = 3 in the cell
                                      5022426
  Invoking rule 18:22426=31826
  replace dpstoff2 = 5031826 if inlist(dpstoff2, 5000018, 5022426)
Pass 51 through the data...
                                      2023036
  smallest count = 4 in the cell
  WARNING: could not find any rules to collapse dpstoff2 == 2023036
Pass 52 through the data...
  smallest count = 4 in the cell
                                      2110244
  WARNING: could not find any rules to collapse dpstoff2 == 2110244
Pass 53 through the data...
  smallest count = 4 in the cell
                                      4031826
  Invoking rule 30211:31826=60226
 replace dpstoff2 = 4060226 if inlist(dpstoff2, 4030211, 4031826)
Pass 54 through the data...
  smallest count = 4 in the cell
                                      5043644
  Invoking rule 43644:64760=103660
 replace dpstoff2 = 5103660 if inlist(dpstoff2, 5043644, 5064760)
Pass 55 through the data...
 smallest count = 5 in the cell
                                      1000060
  Invoking rule 24950:25355:60=54960
  replace dpstoff2 = 1054960 if inlist(dpstoff2, 1024950, 1025355, 1000060)
Pass 56 through the data...
  smallest count = 5 in the cell
                                      2074968
  Invoking rule 72647:74968=142668
 replace dpstoff2 = 2142668 if inlist(dpstoff2, 2072647, 2074968)
Pass 57 through the data...
  smallest count = 5 in the cell
                                      3025560
  Invoking rule 34953:25560=54960
 replace dpstoff2 = 3054960 if inlist(dpstoff2, 3034953, 3025560)
Pass 58 through the data...
  smallest count = 6 in the cell
                                      1000055
  Invoking rule 53:55=25355
  replace dpstoff2 = 1025355 if inlist(dpstoff2, 1000053, 1000055)
  (output omitted)
Pass 67 through the data...
  smallest count = 10 in the cell
                                       4060226
  Invoking rule 30:60226=70230
  replace dpstoff2 = 4070230 if inlist(dpstoff2, 4000030, 4060226)
Pass 68 through the data...
  smallest count = 11 in the cell
                                       5103660
  WARNING: could not find any rules to collapse dpstoff2 == 5103660
Pass 69 through the data...
  smallest count = 12 in the cell
  Invoking rule 20208:21118:24=50224
  replace dpstoff2 = 1050224 if inlist(dpstoff2, 1020208, 1021118, 1000024)
  (output omitted)
```

(Continued on next page)

```
Pass 76 through the data...
 smallest count = 15 in the cell
                                       3054960
  Invoking rule 62:54960=64962
 replace dpstoff2 = 3064962 if inlist(dpstoff2, 3000062, 3054960)
Pass 77 through the data...
                                       4070230
 smallest count = 21 in the cell
 Done collapsing! Exiting...
. return list
scalars:
        r(arg_min_id) =
                          4070230
               r(min) =
                          21
macros:
            r(cfailed): "2023036,2110244,5103660"
             r(failed): "2023036 2110244 5103660"
```

We will continue to disregard the cell counts of insufficient size for the time being. Running the resulting do-files dpston.do and dpstoff.do on the population data to create control totals, and providing these control totals to ipfraking program produces an apparently successful raking result:

```
. use trip_sample, clear
. run dpston2
. run dpstoff2
. gen byte _one = 1
. ipfraking [pw=_one], ctotal(dpston2 dpstoff2) gen(raked_weight2)
 Iteration 1, max rel difference of raked weights = 36.208881
Iteration 2, max rel difference of raked weights = .05484732
 Iteration 3, max rel difference of raked weights = .0055794
 Iteration 4, max rel difference of raked weights = .00053851
Iteration 5, max rel difference of raked weights = .00005171
 Iteration 6, max rel difference of raked weights = 4.962e-06
Iteration 7, max rel difference of raked weights = 4.762e-07
The worst relative discrepancy of 3.9e-08 is observed for dpstoff2 == 5180262
                      483; achieved value =
                                                    483
Target value =
  Summary of the weight changes
                           Std. dev.
                                                               CV
                   Mean
                                         Min
                                                    Max
Orig weights
                                   0
                                             1
                                                         1
                                                                 0
Raked weights
                  26.487
                             5.9013
                                        8.1096
                                                    37.001
                                                              . 2228
Adjust factor
                 26.4869
                                        8.1096
                                                   37.0014
 whatsdeff raked_weight2
  Group
              Min
                          Mean
                                       Max
                                                    CV
                                                             DEFF
                                                                        N
                                                                               N eff
                                         37.00
                 8.11
                             26.49
                                                  0.2228
                                                            1.0496
                                                                       3654
                                                                              3481.24
  Overall
```

Note the use of utility program whatsdeff to compute the design effect due to unequal weighting; see section 2.3. The problem of zero cells appeared to have been solved: each and every population combination of daypart and station is properly reflected in control total categories, and there are

The weighting cells, however, are still not without problems. Consider this cross-

tab of original and collapsed stations (the first part of the *if* expression identifies the daypart, AM Peak; the second part identifies collapsed stations, given the nomenclature of dpstoff variable described on page 4.7 as the concatenation of the first variable of the interaction, daypart; the length of the collapsed sequence, and its starting and end points; station numbers take up to two characters, and hence the collapsed values would use categories of alight_id like 20102, and mod by 100*100 would be greater than the maximum two-digit number, 99).

| | | | - | | |
|----------------------|---------|-------------|-------------|---------|-------|
| | Long | g ID of the | interaction | n | |
| alight_id | 1025355 | 1043644 | 1060226 | 1064962 | Total |
| 2. Brookline | 0 | 0 | 1 | 0 | 1 |
| 8. Carmenton | 0 | 0 | 11 | 0 | 11 |
| 24. Framington | 0 | 0 | 15 | 0 | 15 |
| 26. Grand Junction | 0 | 0 | 15 | 0 | 15 |
| 36. Irvingtown | 0 | 9 | 0 | 0 | 9 |
| 39. Johnsville | 0 | 3 | 0 | 0 | 3 |
| 44. Limerick | 0 | 13 | 0 | 0 | 13 |
| 49. Ninth Street | 0 | 0 | 0 | 3 | 3 |
| 50. Ontario Lake | 0 | 0 | 0 | 2 | 2 |
| 53. Picadilly Square | 23 | 0 | 0 | 0 | 23 |
| 55. Queens Zoo | 6 | 0 | 0 | 0 | 6 |
| 60. Redline Circle | 0 | 0 | 0 | 5 | 5 |
| 62. Silver Spring | 0 | 0 | 0 | 49 | 49 |
| | | | | | |

. tab alight_id dpstoff2 if daypart == 1 & mod(dpstoff2,100*100)>99

To human eye, it is obvious that Picadilly Square (53) and Queens Zoo (55) should have been a part of the six-station sequence 1064962 spanning from Ninth Street (49) to Silver Spring (62). Instead, wgtcellcollapse decided to separate these two stations out into their own cell. How did that happen? The logic of wgtcellcollapse is to collapse categories in such a way as to produce the result with the smallest possible count. Thus, within AM Peak daypart, the sequence of collapsing steps was as follows.

59

155

29

Total

- **Pass 0** The zero cells were collapsed first: Johnsville (39) and King Street (40) resulting in an intermediate cell of size 3.
- Pass 24 The smallest cell of size 1 (Brookline (2)) was collapsed with its neighbor (Carmenton (8)) resulting in an intermediate cell of size 12.
- Pass 38 The smallest cell of size 2 (Ontario Lake (50)) was collapsed with its neighbor (Ninth Street (49)) resulting in an intermediate cell of size 5.
- Pass 47 The smallest cell of size 3, collapsed Johnsville (39) and King Street (40), was further collapsed with its neighbor Irvingtown (36) resulting in an intermediate cell of size.
- Pass 55 The smallest cell of size 5, Redline Circle (60), was collapsed by a three-way rule with a duo Picadilly Square (53) + Queens Zoo (55), which actually was empty, and a small cell Ontario Lake (50) + Ninth Street (49), resulting in an intermediate cell of size 10.

Let us look at that last step in more detail. At this stage, Redline Circle (60) with 5 exiting passengers in the sample could be collapsed with:

- 1. Silver Spring (62), to form a cell of size 54;
- 2. Queens Zoo (55), to form a cell of size 11;
- 3. a sequence of Picadilly Square (53) and Queens Zoo (55), to form a cell of size 34;
- 4. ... and a number of other options

However, at pass 55, wgtcellcollapse picked the rule 24950:25355:60=54960 which, at the time it was processed, had a count of 5 in the cell 24950, a count of zero in the cell 25355, and a count of 5 in the original station Redline Circle (60). (Note that the cell 25355 would actually form later at pass 58.) The problem lies with the zero count of the ghost of the cell 25355.

To overcome this problem, wgtcellcollapse have a strict option that only allows the rules that have a non-zero count in every component of the rule (so the problematic rule 24950:25355:60=54960 would not be a legal one under that restriction). As is easily seen, this option directly contradicts the zeroes() option, and that necessitates separate runs.

The third pass of cell collapse and raking: strict and feed options

We will separate the two runs of wgtcellcollapse into a run that only deals with zeroes, and another run that deals with everything else. To prevent wgtcellcollapse from any further merges, mincellsize(1) can be specified in the first run. As the relevant variables will have already been created by the first run, the option to pass the variable name to be further modified is feed(). To make sure that the relevant variable exists in the data set, the option run instructs wgtcellcollapse to run the do-file it just created, thus creating or modifying the collapsed cell variable. Finally, instead of specifying replace to overwrite the do-files that wgtcellcollapse creates, we need to specify append to keep adding to these files.

```
. use trip_sample_rules, clear
 wgtcellcollapse collapse, variables(daypart board_id) mincellsize(1) ///
          zeroes(39 40 44 49 55 60) ///
          generate(dpston3) saving(dpston3.do) replace run
Pass 0 through the data..
 smallest count = 1 in the cell
                                      2000039
Processing zero cells..
  Invoking rule 49:50=24950 to collapse zero cells
  replace dpston3 = 1024950 if inlist(dpston3, 1000049, 1000050)
Pass 0 through the data...
  smallest count = 1 in the cell
                                      2000039
  Invoking rule 40:44=24044 to collapse zero cells
  replace dpston3 = 2024044 if inlist(dpston3, 2000040, 2000044)
  (output omitted)
```

```
Pass 0 through the data...
  smallest count = 1 in the cell
                                      2000039
  Invoking rule 24950:25355:60=54960 to collapse zero cells
 replace dpston3 = 5054960 if inlist(dpston3, 5024950, 5025355, 5000060)
Pass 0 through the data...
  smallest count = 1 in the cell
                                      2000039
Pass 12 through the data...
 smallest count = 1 in the cell
                                      2000039
 Done collapsing! Exiting...
. wgtcellcollapse collapse, variables(daypart board_id) mincellsize(20) ///
          strict feed(dpston3) saving(dpston3.do) append run
Pass 12 through the data...
  smallest count = 1 in the cell
                                      2000039
  Invoking rule 39:24044=33944
 replace dpston3 = 2033944 if inlist(dpston3, 2000039, 2024044)
  (output omitted)
Pass 40 through the data...
  smallest count = 6 in the cell
                                      4000002
  Invoking rule 1:2=20102
 replace dpston3 = 4020102 if inlist(dpston3, 4000001, 4000002)
Pass 41 through the data...
  smallest count = 7 in the cell
                                      4025355
  WARNING: could not find any rules to collapse dpston3 == 4025355
Pass 42 through the data...
  smallest count = 7 in the cell
                                      5025355
  WARNING: could not find any rules to collapse dpston3 == 5025355
Pass 43 through the data...
  smallest count = 8 in the cell
                                      2021824
  Invoking rule 26:21824=31826
 replace dpston3 = 2031826 if inlist(dpston3, 2000026, 2021824)
  (output omitted)
Pass 57 through the data...
  smallest count = 19 in the cell
                                       3025560
  Invoking rule 62:25560=35562
  replace dpston3 = 3035562 if inlist(dpston3, 3000062, 3025560)
Pass 58 through the data...
  smallest count = 20 in the cell
                                       5026268
 Done collapsing! Exiting...
. wgtcellcollapse collapse, variables(daypart alight_id) mincellsize(1) ///
          zeroes(2 8 36 39 40 44 47 49 50 55 60 62) ///
          generate(dpstoff3) saving(dpstoff3.do) replace run
Pass 0 through the data...
  smallest count = 1 in the cell
Processing zero cells...
  Invoking rule 39:40=23940 to collapse zero cells
 replace dpstoff3 = 1023940 if inlist(dpstoff3, 1000039, 1000040)
Pass 0 through the data...
  smallest count = 1 in the cell
                                      1000002
  Invoking rule 2:8=20208 to collapse zero cells
 replace dpstoff3 = 2020208 if inlist(dpstoff3, 2000002, 2000008)
Pass 0 through the data...
  smallest count = 1 in the cell
                                      1000002
  Invoking rule 30:36=23036 to collapse zero cells
 replace dpstoff3 = 2023036 if inlist(dpstoff3, 2000030, 2000036)
Pass 0 through the data...
  smallest count = 1 in the cell
                                      1000002
```

```
Invoking rule 26:30:36:39=42639 to collapse zero cells
  replace dpstoff3 = 2042639 if inlist(dpstoff3, 2000026, 2000030, 2000036, 2000039)
Pass 0 through the data...
  smallest count = 1 in the cell
                                      1000002
  Invoking rule 24:26:30:36:39:40=62440 to collapse zero cells
 replace dpstoff3 = 2062440 if inlist(dpstoff3, 2000024, 2000026, 2000030, 2000036,
> 2000039, 2000040)
Pass 0 through the data...
  smallest count = 1 in the cell
                                      1000002
  Invoking rule 44:62440=72444 to collapse zero cells
 replace dpstoff3 = 2072444 if inlist(dpstoff3, 2000044, 2062440)
  (output omitted)
Pass 0 through the data...
                                      1000002
  smallest count = 1 in the cell
  Invoking rule 24950:53:55:60=54960 to collapse zero cells
 replace dpstoff3 = 5054960 if inlist(dpstoff3, 5024950, 5000053, 5000055, 5000060)
Pass 0 through the data...
  smallest count = 1 in the cell
                                      1000002
Pass 24 through the data...
  smallest count = 1 in the cell
                                      1000002
  Done collapsing! Exiting...
. wgtcellcollapse collapse, variables(daypart alight_id) mincellsize(20) ///
          strict feed(dpstoff3) saving(dpstoff3.do) append run
Pass 24 through the data...
  smallest count = 1 in the cell
                                      1000002
  Invoking rule 2:8=20208
  replace dpstoff3 = 1020208 if inlist(dpstoff3, 1000002, 1000008)
Pass 25 through the data...
                                      2000011
  smallest count = 1 in the cell
  Invoking rule 11:18=21118
 replace dpstoff3 = 2021118 if inlist(dpstoff3, 2000011, 2000018)
  (output omitted)
Pass 46 through the data...
  smallest count = 2 in the cell
                                      5023639
  Invoking rule 23639:24044=43644
  replace dpstoff3 = 5043644 if inlist(dpstoff3, 5023639, 5024044)
Pass 47 through the data...
                                      5025355
  smallest count = 2 in the cell
  WARNING: could not find any rules to collapse dpstoff3 == 5025355
  (output omitted)
Pass 51 through the data...
  smallest count = 4 in the cell
                                      2023036
  WARNING: could not find any rules to collapse dpstoff3 == 2023036
Pass 52 through the data...
  smallest count = 4 in the cell
                                      2110244
  Invoking rule 47:110244=120247
  replace dpstoff3 = 2120247 if inlist(dpstoff3, 2000047, 2110244)
  (output omitted)
Pass 76 through the data...
  smallest count = 16 in the cell
                                       5026268
  Invoking rule 170260:26268=190268
 replace dpstoff3 = 5190268 if inlist(dpstoff3, 5170260, 5026268)
Pass 77 through the data...
  smallest count = 21 in the cell
                                       4070230
  Done collapsing! Exiting...
```

The result still isn't satisfactory, as some collapsed cells still overlap:

| . tab | alight_id | dpstoff3 | if | daypart == | 2 | & mod | (dpstoff3,100*100)>99 |
|-------|-----------|----------|----|------------|---|-------|-----------------------|
|-------|-----------|----------|----|------------|---|-------|-----------------------|

| | Long ID | | | |
|----------------------|---------|---------|---------|-------|
| alight_id | 2023036 | 2042639 | 2200269 | Total |
| 8. Carmenton | 0 | 0 | 1 | 1 |
| 11. Dogville | Ö | 0 | 1 | 1 |
| 18. East End | 0 | 0 | 1 | 1 |
| 24. Framington | 0 | 0 | 1 | 1 |
| 26. Grand Junction | 0 | 2 | 0 | 2 |
| 30. High Point | 4 | 0 | 0 | 4 |
| 47. Moscow City | 0 | 0 | 6 | 6 |
| 49. Ninth Street | 0 | 0 | 1 | 1 |
| 53. Picadilly Square | 0 | 0 | 1 | 1 |
| 68. Toledo Town | 0 | 0 | 3 | 3 |
| 69. Union Station | 0 | 0 | 138 | 138 |
| Total | 4 | 2 | 153 | 159 |

This overlap can be traced back to the collapsing of zero cells: first, the cell 2023036 came to being by a reasonable, at its face, collapsing of the zero cell Irvingtown (36) with non-zero cell High Point (30); and then the cell 2042639 came to being by a long overreach for the zero cell Johnsville (39) to be collapsed with a non-zero cell Grand Junction (26).

The fourth pass of cell collapse and raking: greedy and maxcat() options

The next improvement I am going to demonstrate is to fix the problem of weak performance in collapsing the zero cells with an additional option greedy. It modifies behavior of wgtcellcollapse to require that, among the possible candidate rules with the lowest count, the rule with the greatest number of components is preferred. That way, the long streaks of zeroes from Irvingtown (36) to Limerick (44) in midday part could be collapsed simultaneously into one cell. To support this option, and avoid complex collapses of zero cells with the already defined cells, option maxcategory() specifies the greatest value of a component of a rule. By specifying maxcategory(99), we can instruct wgtcellcollapse to only use rules that deal with individual stations (that have category numbers from 1 to 69, and thus are below 99), and do not use the rules that involve collapsed cells (which would have numbers of at least 20102 for the collapsed cell Alewife (1) and Brookline (2)). In the first run, those collapsed cells will always be empty ghosts, and they should not be used in defining how the cells be collapsed.

Note also that with the greedy option, one would want to specify the zeroes somewhere in the middle of the streak, and possibly across multiple categories of the interacting variable. In our example, specifying (zeroes(36) would collapse the midday streak of zero counts, but the need to collapse the zeroes in the night and the weekend dayparts would still remain, necessitating something like zeroes(40) — which, in turn, will likely create overlapping artifacts in the midday section. However, specifying zeroes(40) without (zeroes(36) would take care of all the streaks observed in Table 1.

```
. use trip_sample_rules, clear
 wgtcellcollapse collapse, variables(daypart board_id) mincellsize(1) ///
          zeroes(39 44 49 60) greedy maxcategory(99) ///
          generate(dpston4) saving(dpston4.do) replace run
Pass 0 through the data...
 smallest count = 1 in the cell
                                      2000039
Processing zero cells...
  Invoking rule 49:50=24950 to collapse zero cells
  replace dpston4 = 1024950 if inlist(dpston4, 1000049, 1000050)
Pass 0 through the data...
  smallest count = 1 in the cell
                                      2000039
  Invoking rule 40:44=24044 to collapse zero cells
 replace dpston4 = 2024044 if inlist(dpston4, 2000040, 2000044)
Pass 0 through the data...
  smallest count = 1 in the cell
  Invoking rule 49:50=24950 to collapse zero cells
  replace dpston4 = 2024950 if inlist(dpston4, 2000049, 2000050)
  (output omitted)
Pass 0 through the data...
  smallest count = 1 in the cell
                                      2000039
  Invoking rule 55:60=25560 to collapse zero cells
  replace dpston4 = 5025560 if inlist(dpston4, 5000055, 5000060)
Pass 0 through the data...
  smallest count = 1 in the cell
                                      2000039
Pass 10 through the data...
  smallest count = 1 in the cell
                                      2000039
  Done collapsing! Exiting...
. wgtcellcollapse collapse, variables(daypart board_id) mincellsize(20) ///
          strict feed(dpston4) saving(dpston4.do) append run
Pass 10 through the data...
  smallest count = 1 in the cell
                                      2000039
  Invoking rule 39:24044=33944
 replace dpston4 = 2033944 if inlist(dpston4, 2000039, 2024044)
Pass 11 through the data...
  smallest count = 1 in the cell
                                      2024950
  Invoking rule 53:24950=34953
 replace dpston4 = 2034953 if inlist(dpston4, 2000053, 2024950)
Pass 12 through the data...
  smallest count = 1 in the cell
                                      2025560
  Invoking rule 34953:25560=54960
  replace dpston4 = 2054960 if inlist(dpston4, 2034953, 2025560)
Pass 13 through the data...
  smallest count = 1 in the cell
                                      3000039
  Invoking rule 39:40=23940
 replace dpston4 = 3023940 if inlist(dpston4, 3000039, 3000040)
  (output omitted)
Pass 55 through the data...
  smallest count = 19 in the cell
                                       3025560
  Invoking rule 62:25560=35562
 replace dpston4 = 3035562 if inlist(dpston4, 3000062, 3025560)
Pass 56 through the data...
  smallest count = 20 in the cell
                                       5026268
  Done collapsing! Exiting...
. assert "`r(failed)'" == ""
                          (Continued on next page)
```

```
wgtcellcollapse collapse, variables(daypart alight_id) mincellsize(1) ///
        zeroes(2 40 49 50 60) greedy maxcategory(99) ///
          generate(dpstoff4) saving(dpstoff4.do) replace run
Pass 0 through the data...
 smallest count = 1 in the cell
Processing zero cells...
  Invoking rule 39:40=23940 to collapse zero cells
 replace dpstoff4 = 1023940 if inlist(dpstoff4, 1000039, 1000040)
Pass 0 through the data...
 smallest count = 1 in the cell
                                      1000002
 Invoking rule 1:2:8=30108 to collapse zero cells
 replace dpstoff4 = 2030108 if inlist(dpstoff4, 2000001, 2000002, 2000008)
  (output omitted)
Pass 0 through the data...
 smallest count = 1 in the cell
                                      1000002
 Invoking rule 49:50=24950 to collapse zero cells
 replace dpstoff4 = 5024950 if inlist(dpstoff4, 5000049, 5000050)
Pass 0 through the data...
 smallest count = 1 in the cell
                                      1000002
 Invoking rule 49:50:53:55:60=54960 to collapse zero cells
 replace dpstoff4 = 5054960 if inlist(dpstoff4, 5000049, 5000050, 5000053, 5000055,
> 5000060)
Pass 0 through the data...
 smallest count = 1 in the cell
                                      1000002
Pass 14 through the data...
 smallest count = 1 in the cell
                                      1000002
 Done collapsing! Exiting...
. wgtcellcollapse collapse, variables(daypart alight_id) mincellsize(20) ///
         strict feed(dpstoff4) saving(dpstoff4.do) append run
Pass 14 through the data...
 smallest count = 1 in the cell
                                      1000002
 Invoking rule 2:8=20208
 replace dpstoff4 = 1020208 if inlist(dpstoff4, 1000002, 1000008)
Pass 15 through the data...
 smallest count = 1 in the cell
                                      2000011
 Invoking rule 11:18=21118
 replace dpstoff4 = 2021118 if inlist(dpstoff4, 2000011, 2000018)
Pass 16 through the data...
 smallest count = 1 in the cell
                                      2000024
 Invoking rule 24:26=22426
 replace dpstoff4 = 2022426 if inlist(dpstoff4, 2000024, 2000026)
  (output omitted)
Pass 65 through the data...
 smallest count = 18 in the cell
                                       5074968
  Invoking rule 69:74968=84969
 replace dpstoff4 = 5084969 if inlist(dpstoff4, 5000069, 5074968)
Pass 66 through the data...
 smallest count = 21 in the cell
                                       2200168
 Done collapsing! Exiting...
. assert "`r(failed)'" == ""
```

We have finally been able to produce a clean collapse of everything! Note the use of assert "'r(failed)' =="" in the above code snippet to make sure that all cells have the minimal required size of 20.

As a very minor point, we can see some room for improvement in collapsing the cells on the weekend:

| . tab alight_id dpstoff4 if daypart == 5 & mod(dpstoff4,100*100) | . tab | alight id | dpstoff4 | if | davpart | == 5 | & | mod(dpstoff4.100*100)>99 |
|--|-------|-----------|----------|----|---------|------|---|--------------------------|
|--|-------|-----------|----------|----|---------|------|---|--------------------------|

| | Long ID of the | | | | |
|----------------------|----------------|---------|-------|--|--|
| | intera | ction | | | |
| alight_id | 5084969 | 5150150 | Total | | |
| 8. Carmenton | 0 | 1 | 1 | | |
| 11. Dogville | 0 | 5 | 5 | | |
| 18. East End | 0 | 4 | 4 | | |
| 24. Framington | 0 | 2 | 2 | | |
| 26. Grand Junction | 0 | 1 | 1 | | |
| 30. High Point | 0 | 8 | 8 | | |
| 36. Irvingtown | 0 | 2 | 2 | | |
| 44. Limerick | 0 | 2 | 2 | | |
| 47. Moscow City | 0 | 6 | 6 | | |
| 50. Ontario Lake | 0 | 1 | 1 | | |
| 53. Picadilly Square | 2 | 0 | 2 | | |
| 62. Silver Spring | 9 | 0 | 9 | | |
| 68. Toledo Town | 7 | 0 | 7 | | |
| 69. Union Station | 123 | 0 | 123 | | |
| Total | 141 | 32 | 173 | | |

Instead of two cells with sizes 141 and 32, it seems like we could produce three cells, with Union Station (69) being its own cell, and everything else split somewhere in the middle.

The fifth pass of cell collapse and raking: if conditions

We will now code the collapsing cells for that day part "by hand", and we will put those custom coded cells upfront before the main run. (Some special treatment had to be given to the zero cells to avoid overlapping cells around Ninth Street (49) for the night and weekend day parts; without the separation, it is getting collapsed in a long overreach all the way up to Redline Circle (60).)

```
. use trip_sample_rules, clear
. wgtcellcollapse collapse, variables(daypart board_id) mincellsize(1) ///
         zeroes(39 44 49 60) greedy maxcategory(99) ///
          generate(dpston5) saving(dpston5.do) replace run
Pass 0 through the data...
                                      2000039
 smallest count = 1 in the cell
Processing zero cells...
 Invoking rule 49:50=24950 to collapse zero cells
 replace dpston5 = 1024950 if inlist(dpston5, 1000049, 1000050)
Pass 0 through the data...
 smallest count = 1 in the cell
                                      2000039
 Invoking rule 40:44=24044 to collapse zero cells
 replace dpston5 = 2024044 if inlist(dpston5, 2000040, 2000044)
Pass 0 through the data...
 smallest count = 1 in the cell
  Invoking rule 49:50=24950 to collapse zero cells
 replace dpston5 = 2024950 if inlist(dpston5, 2000049, 2000050)
```

```
(output omitted)
Pass 0 through the data...
  smallest count = 1 in the cell
                                      2000039
  Invoking rule 55:60=25560 to collapse zero cells
  replace dpston5 = 5025560 if inlist(dpston5, 5000055, 5000060)
Pass 0 through the data...
  smallest count = 1 in the cell
                                      2000039
Pass 10 through the data...
  smallest count = 1 in the cell
                                      2000039
  Done collapsing! Exiting...
. wgtcellcollapse collapse, variables(daypart board_id) mincellsize(20) ///
          strict feed(dpston5) saving(dpston5.do) append run
Pass 10 through the data...
  smallest count = 1 in the cell
                                      2000039
 Invoking rule 39:24044=33944
  replace dpston5 = 2033944 if inlist(dpston5, 2000039, 2024044)
Pass 11 through the data...
  smallest count = 1 in the cell
                                      2024950
  Invoking rule 53:24950=34953
  replace dpston5 = 2034953 if inlist(dpston5, 2000053, 2024950)
  (output omitted)
Pass 55 through the data...
  smallest count = 19 in the cell
                                       3025560
  Invoking rule 62:25560=35562
  replace dpston5 = 3035562 if inlist(dpston5, 3000062, 3025560)
Pass 56 through the data...
  smallest count = 20 in the cell
                                       5026268
  Done collapsing! Exiting...
. assert "`r(failed)'" == ""
 wgtcellcollapse collapse, variables(daypart alight_id) mincellsize(1) ///
          zeroes(2 40 60) greedy maxcategory(99) ///
          generate(dpstoff5) saving(dpstoff5.do) replace run
Pass 0 through the data...
  smallest count = 1 in the cell
                                      1000002
Processing zero cells...
  Invoking rule 39:40=23940 to collapse zero cells
  replace dpstoff5 = 1023940 if inlist(dpstoff5, 1000039, 1000040)
Pass 0 through the data...
  smallest count = 1 in the cell
                                      1000002
  Invoking rule 1:2:8=30108 to collapse zero cells
  replace dpstoff5 = 2030108 if inlist(dpstoff5, 2000001, 2000002, 2000008)
Pass 0 through the data...
  smallest count = 1 in the cell
                                      1000002
  Invoking rule 30:36:39:40:44=53044 to collapse zero cells
  replace dpstoff5 = 2053044 if inlist(dpstoff5, 2000030, 2000036, 2000039, 2000040,
 2000044)
  (output omitted)
Pass 0 through the data...
  smallest count = 1 in the cell
                                      1000002
  Invoking rule 53:55:60=35360 to collapse zero cells
  replace dpstoff5 = 5035360 if inlist(dpstoff5, 5000053, 5000055, 5000060)
Pass 0 through the data...
  smallest count = 1 in the cell
                                      1000002
Pass 12 through the data...
  smallest count = 1 in the cell
                                      1000002
  Done collapsing! Exiting...
```

```
. wgtcellcollapse collapse if inlist(daypart,4,5) & inrange(alight_id,49,50), ///
          variables(daypart alight_id) mincellsize(1) ///
          \verb|feed(dpstoff5)| zeroes(49)| maxcategory(99)| saving(dpstoff5.do)| append run|
Pass 12 through the data...
 smallest count = 1 in the cell
Processing zero cells...
  Invoking rule 49:50=24950 to collapse zero cells
 replace dpstoff5 = 4024950 if inlist(dpstoff5, 4000049, 4000050)
Pass 12 through the data...
  smallest count = 1 in the cell
                                      1000002
  Invoking rule 49:50=24950 to collapse zero cells
 replace dpstoff5 = 5024950 if inlist(dpstoff5, 5000049, 5000050)
Pass 12 through the data...
  smallest count = 1 in the cell
                                      1000002
Pass 14 through the data...
  smallest count = 1 in the cell
                                      5024950
  Done collapsing! Exiting...
. * special cells for weekend
. wgtcellcollapse collapse if daypart==5 & inrange(alight_id,1,36), ///
          variables(daypart alight_id) mincellsize(50) ///
          strict feed(dpstoff5) saving(dpstoff5.do) append run
Pass 14 through the data...
  smallest count = 1 in the cell
                                      5000026
  Invoking rule 24:26=22426
 replace dpstoff5 = 5022426 if inlist(dpstoff5, 5000024, 5000026)
Pass 15 through the data...
  smallest count = 1 in the cell
  Invoking rule 11:30108=40111
  replace dpstoff5 = 5040111 if inlist(dpstoff5, 5000011, 5030108)
Pass 16 through the data...
  smallest count = 2 in the cell
                                      5033640
  Invoking rule 30:33640=43040
 replace dpstoff5 = 5043040 if inlist(dpstoff5, 5000030, 5033640)
Pass 17 through the data...
  smallest count = 3 in the cell
                                      5022426
  Invoking rule 18:22426=31826
 replace dpstoff5 = 5031826 if inlist(dpstoff5, 5000018, 5022426)
Pass 18 through the data...
  smallest count = 6 in the cell
                                      5040111
  Invoking rule 40111:31826=70126
  replace dpstoff5 = 5070126 if inlist(dpstoff5, 5040111, 5031826)
Pass 19 through the data...
  smallest count = 10 in the cell
                                       5043040
  Invoking rule 70126:43040=110140
 replace dpstoff5 = 5110140 if inlist(dpstoff5, 5070126, 5043040)
Pass 20 through the data...
  smallest count = 23 in the cell
  WARNING: could not find any rules to collapse dpstoff5 == 5110140
Pass 21 through the data...
  smallest count = .i in the cell
                                       1000002
 Done collapsing! Exiting...
```

(Continued on next page)

```
wgtcellcollapse collapse if daypart==5 & inrange(alight_id,44,68), ///
         variables(daypart alight_id) mincellsize(50) ///
          strict feed(dpstoff5) saving(dpstoff5.do) append run
Pass 20 through the data...
 smallest count = 1 in the cell
 Invoking rule 24950:35360=54960
 replace dpstoff5 = 5054960 if inlist(dpstoff5, 5024950, 5035360)
Pass 21 through the data...
                                      5000044
  smallest count = 2 in the cell
  Invoking rule 44:47=24447
 replace dpstoff5 = 5024447 if inlist(dpstoff5, 5000044, 5000047)
Pass 22 through the data...
                                      5054960
 smallest count = 3 in the cell
  Invoking rule 24447:54960=74460
 replace dpstoff5 = 5074460 if inlist(dpstoff5, 5024447, 5054960)
Pass 23 through the data...
  smallest count = 7 in the cell
                                      5000068
 Invoking rule 62:68=26268
 replace dpstoff5 = 5026268 if inlist(dpstoff5, 5000062, 5000068)
Pass 24 through the data...
  smallest count = 11 in the cell
                                       5074460
  Invoking rule 74460:26268=94468
 replace dpstoff5 = 5094468 if inlist(dpstoff5, 5074460, 5026268)
Pass 25 through the data...
  smallest count = 27 in the cell
  WARNING: could not find any rules to collapse dpstoff5 == 5094468
Pass 26 through the data...
 smallest count = .i in the cell
                                       1000002
 Done collapsing! Exiting...
. * all other cells
. wgtcellcollapse collapse, variables(daypart alight_id) mincellsize(20) ///
          strict feed(dpstoff5) saving(dpstoff5.do) append run
Pass 25 through the data...
  smallest count = 1 in the cell
                                      1000002
  Invoking rule 2:8=20208
 replace dpstoff5 = 1020208 if inlist(dpstoff5, 1000002, 1000008)
Pass 26 through the data...
  smallest count = 1 in the cell
                                      2000011
  Invoking rule 11:18=21118
 replace dpstoff5 = 2021118 if inlist(dpstoff5, 2000011, 2000018)
  (output omitted)
Pass 64 through the data...
                                       3054960
  smallest count = 15 in the cell
  Invoking rule 62:54960=64962
 replace dpstoff5 = 3064962 if inlist(dpstoff5, 3000062, 3054960)
Pass 65 through the data...
  smallest count = 21 in the cell
                                       2200168
 Done collapsing! Exiting...
. assert "`r(failed)'" == ""
```

The special missing value .i that appears in the smallest count report is used internally to stop wgtcellcollapse after all of the relevant cases selected by the *if* conditions have been processed.

Checking on the last improvement, we see how the manual resolution succeeded:

| <pre>. tab alight_id dpstoff5 if daypart == 5</pre> |
|---|
|---|

| | Interactions of daypart | | | | | |
|----------------------|-------------------------|-----------|------------|-------|--|--|
| | alight_id, | with some | collapsing | | | |
| alight_id | 5000069 | 5094468 | 5110140 | Total | | |
| 8. Carmenton | 0 | 0 | 1 | 1 | | |
| 11. Dogville | 0 | 0 | 5 | 5 | | |
| 18. East End | 0 | 0 | 4 | 4 | | |
| 24. Framington | 0 | 0 | 2 | 2 | | |
| 26. Grand Junction | 0 | 0 | 1 | 1 | | |
| 30. High Point | 0 | 0 | 8 | 8 | | |
| 36. Irvingtown | 0 | 0 | 2 | 2 | | |
| 44. Limerick | 0 | 2 | 0 | 2 | | |
| 47. Moscow City | 0 | 6 | 0 | 6 | | |
| 50. Ontario Lake | 0 | 1 | 0 | 1 | | |
| 53. Picadilly Square | 0 | 2 | 0 | 2 | | |
| 62. Silver Spring | 0 | 9 | 0 | 9 | | |
| 68. Toledo Town | 0 | 7 | 0 | 7 | | |
| 69. Union Station | 123 | 0 | 0 | 123 | | |
| Total | 123 | 27 | 23 | 173 | | |

The resulting do-files can now be applied to producing control totals, and eventually to raking:

| Over | Total | Std. Err. | [95% Conf. Inter | rval] |
|--------------|-------|-----------|------------------|-------|
| num_pass | | | | |
| 1000001 | 1423 | 967.7508 | -476.9595 3322 | 2.959 |
| 1000002 | 7198 | 4895.91 | -2414.011 1681 | 10.01 |
| (output omit | ted) | | | |
| 5000011 | 1270 | 834.301 | -367.961 2907 | 7.961 |
| 5026268 | 557 | 364.4324 | -158.4805 1272 | 2.481 |
| 5030108 | 610 | 263.2061 | 93.25444 1126 | 3.746 |
| 5051836 | 622 | 215.5712 | 198.7749 1045 | 5.225 |
| 5093960 | 473 | 261.8954 | -41.17225 987. | .1723 |

- . matrix dpston5 = e(b)
- . matrix coleq dpston5 = _one
- . matrix rownames dpston5 = dpston5
- . run dpstoff5.do

. total num_pass , over(dpstoff5)

Total estimation Number of obs = 719

1000018: dpstoff5 = 1000018 1000030: dpstoff5 = 1000030

(output omitted)

5000069: dpstoff5 = 5000069 5094468: dpstoff5 = 5094468 5110140: dpstoff5 = 5110140

| Over | Total | Std. Err. | [95% Conf. | Interval] |
|--------------|-------|-----------|------------|-----------|
| num_pass | | | | |
| 1000018 | 929 | 360.7303 | 220.7878 | 1637.212 |
| 1000030 | 2189 | 868.0319 | 484.8161 | 3893.184 |
| (output omit | ted) | | | |
| 5000069 | 2677 | 895.7917 | 918.316 | 4435.684 |
| 5094468 | 432 | 87.57763 | 260.0612 | 603.9388 |
| 5110140 | 423 | 120.0254 | 187.3574 | 658.6426 |

- . matrix dpstoff5 = e(b)
- . matrix coleq dpstoff5 = _one
- . matrix rownames dpstoff5 = dpstoff5
- . use trip_sample_rules, clear
- . run dpston5
- . run dpstoff5
- . gen byte _one = 1
- . ipfraking [pw=_one], ctotal(dpston5 dpstoff5) gen(raked_weight5)

Iteration 1, max rel difference of raked weights = 37.856256

Iteration 2, max rel difference of raked weights = .06404821

Iteration 3, max rel difference of raked weights = .00891802

Iteration 4, max rel difference of raked weights = .00128619

Iteration 5, max rel difference of raked weights = .00018966

Iteration 6, max rel difference of raked weights = .00002818

Iteration 7, max rel difference of raked weights = 4.198e-06 Iteration 8, max rel difference of raked weights = 6.257e-07

The worst relative discrepancy of 7.8e-08 is observed for dpstoff5 == 5110140

Target value = 423; achieved value = 423

Summary of the weight changes

| | Mean | Std. dev. | Min | Max | CV |
|---------------|---------|-----------|---------|---------|-------|
| Orig weights | 1 | 0 | 1 | 1 | 0 |
| Raked weights | 26.487 | 5.754 | 13.174 | 38.634 | .2172 |
| Adjust factor | 26.4869 | | 13.1743 | 38.6339 | |

. whatsdeff raked_weight5

| Group | Min | Mean | Max | CV | DEFF | N | N eff |
|---------|-------|-------|-------|--------|--------|------|---------|
| Overall | 13.17 | 26.49 | 38.63 | 0.2172 | 1.0472 | 3654 | 3489.37 |

Informative labels

As the final touch, let us consider the variety of labels that can be attached to the resulting collapsed cells.

```
. wgtcellcollapse label, var(dpston5)
(language default renamed unlabeled_ccells)
(language numbered_ccells now current language)
(language texted_ccells now current language)
To attach the numeric labels (of the kind "dpston5==1000001"), type:
   label language numbered_ccells
To attach the text labels (of the kind "dpston5==AM Peak; 1. Alewife"), type:
   label language texted_ccells
The original state, which is also the current state, is:
   label language unlabeled_ccells
. wgtcellcollapse label, var(dpstoff5)
To attach the numeric labels (of the kind "dpstoff5==1000018"), type:
   label language numbered_ccells
To attach the text labels (of the kind "dpstoff5==AM Peak; 18. East End"), type:
   label language texted_ccells
The original state, which is also the current state, is:
   label language unlabeled_ccells
. label language numbered_ccells
. tab dpstoff5 if daypart==5
```

| Long ID of the interaction | Freq. | Percent | Cum. |
|--|-----------------|-------------------------|--------------------------|
| daypart==5, alight_id==69 daypart==5, alight_id==94468 daypart==5, alight_id==110140 | 123 27 23 | 71.10 15.61 13.29 | 71.10 86.71 100.00 |
| Total | 173 | 100.00 | |

- . label language texted_ccells
- . tab dpstoff5 if daypart==5

| Long ID of the interaction | Freq. | Percent | Cum. |
|---|-----------------|-------------------------|--------------------------|
| Weekend; 69. Union Station Weekend; 44. Limerick to 68. Toledo Tow Weekend; 1. Alewife to 40. King Street | 123 27 23 | 71.10 15.61 13.29 | 71.10 86.71 100.00 |
| Total | 173 | 100.00 | |

- . label language unlabeled_ccells
- . tab dpstoff5 if daypart==5

| Interaction s of daypart alight_id, with some collapsing | Freq. | Percent | Cum. |
|--|-----------------|-------------------------|--------------------------|
| 5000069 5094468 5110140 | 123 27 23 | 71.10 15.61 13.29 | 71.10 86.71 100.00 |
| Total | 173 | 100.00 | |

Using the mechanics of labels in multiple languages, wgtcellcollapse label defines three "languages" to describe the cells. The language numbered_ccells may be convenient for debugging purposes in fine-tuning the collapsing algorithms, while the language texted_ccells would prove useful for ipfraking_report in creating human-readable labels.

5 Linear calibrated weights

Using the existing example, let me demonstrate the linear calibration option of ipfraking.

```
. set rmsg on
r; t=0.00 14:59:22
. ipfraking [pw=_one], ctotal(dpston5 dpstoff5) nograph gen(raked_weight5)
Iteration 1, max rel difference of raked weights = 37.856256
Iteration 2, max rel difference of raked weights = .06404821
 Iteration 3, max rel difference of raked weights = .00891802
Iteration 4, max rel difference of raked weights = .00128619
Iteration 5, max rel difference of raked weights = .00018966
Iteration 6, max rel difference of raked weights = .00002818
Iteration 7, max rel difference of raked weights = 4.198e-06
Iteration 8, max rel difference of raked weights = 6.257e-07
The worst relative discrepancy of 7.8e-08 is observed for dpstoff5 == 5110140
Target value =
                     423; achieved value =
  Summary of the weight changes
             Mean Std. dev.
                                       Min
                                                  Max
                                                            CV
```

| | | Dour dorr | | | ٠. |
|-----------------|---------|-----------|---------|---------|-------|
| Orig weights | 1 | 0 | 1 | 1 | 0 |
| Raked weights | 26.487 | 5.754 | 13.174 | 38.634 | .2172 |
| Adjust factor | 26.4869 | | 13.1743 | 38.6339 | |
| r; t=2.16 14:59 | 9:24 | | | | |

. ipfraking [pw=_one], ctotal(dpston5 dpstoff5) nograph gen(raked_weight51) linear Linear calibration

The worst relative discrepancy of 1.8e-14 is observed for dpstoff5 == 5110140 Target value = 423; achieved value = 423

Summary of the weight changes

| | Mean | Std. dev. | Min | Max | CV |
|-----------------|---------|-----------|---------|---------|-------|
| Orig weights | 1 | 0 | 1 | 1 | 0 |
| Raked weights | 26.487 | 5.7523 | 12.518 | 38.204 | .2172 |
| Adjust factor | 26.4869 | | 12.5178 | 38.2040 | |
| r; t=0.63 14:59 | 9:25 | | | | |

- . set rmsg off
- . label variable raked_weight51 "Linear calibrated weights"
- . compare raked_weight5 raked_weight51

| | | | difference — | | |
|--|-------|-----------|--------------|-----------|--|
| | count | minimum | average | maximum | |
| raked_w~5 <raked_~51< td=""><td>1896</td><td>-1.813144</td><td>0476911</td><td>-3.11e-11</td></raked_~51<> | 1896 | -1.813144 | 0476911 | -3.11e-11 | |
| raked_w~5>raked_~51 | 1758 | 2.18e-09 | .0514348 | 2.405758 | |
| jointly defined | 3654 | -1.813144 | 3.21e-10 | 2.405758 | |

total 3654

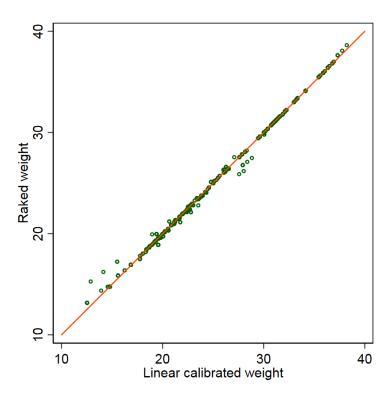


Figure 1: Linear and raked weights

The speed advantages of linear calibration are quite clear (0.63 seconds vs. 2.16 seconds), and raking convergence of raking in 8 iterations is lighting-fast, in author's experience; it is not unusual to see dozens and hundreds of iterations, especially when higher order interactions with many cells and subtle correlations between them are being used as raking margins. The weights are very similar to one another, with the lowest of the linearly calibrated weights being slightly smaller than comparable raked weights. As mentioned before, in the extreme situations, linearly calibrated weights may become negative.

Acknowledgements

The author is grateful to Jason Brinkley and Tom Guterbock for bug reports and functionality suggestions. The opinions stated in this paper are of the author only, and do not represent the position of Abt Associates.

6 References

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About the author

Stanislav (Stas) Kolenikov is a Senior Scientist at Abt Associates. His work involves applications of statistical methods in data collection for public opinion research, public health, transportation, and other disciplines that utilize collection of survey data. Within survey methodology, his expertise includes advanced sampling techniques, survey weighting, calibration, missing data imputation, variance estimation, nonresponse analysis and adjustment, small area estimation, and mode effects. Besides survey statistics, Stas has extensive experience developing and applying statistical methods in social sciences, with focus on structural equation modeling and microeconometrics. He has been writing Stata programs since 1998 when Stata was version 5.