Updates to the ipfraking ecosystem

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Abstract. Kolenikov (2014) introduced the package **ipfraking** for iterative proportional fitting (raking) weight calibration procedures for complex survey designs. This article briefly describes the original package and updates to the core program, and documents additional programs that are used to support the process of creating survey weights in author's production code.

Keywords: st0001, survey, calibration, weights, raking

1 Introduction and background

Large scale social, behavioral and health data are often collected via complex survey designs that may involve stratification, multiple stages of selection and/or unequal probabilities of selection (Korn and Graubard 1995, 1999). In an ideal setting, varying probabilities of selection are accounted for by using the Horvitz-Thompson estimator of the totals (Horvitz and Thompson 1952; Thompson 1997), and the remaining sampling fluctuations can be further ironed out by post-stratification (Holt and Smith 1979). However, on top of the planned differences in probabilities of obtaining a response from a sampled unit, non-response is a practical problem that has been growing more acute in recent years (Groves et al. 2001; Pew Research Center 2012). The analysis weights that are provided along with the public use microdata by data collecting agencies are designed to account for unequal probabilities of selection, non-response, and other factors affecting imbalance between the population and the sample, thus making the analyses conducted on such microdata generalizable to the target population.

Earlier work (Kolenikov 2014) introduced a Stata package called **ipfraking** that implements calibration of survey weights to known control totals to ensure that the resulting weighted data are representative of the population of interest. The process of calibration is aimed at aligning the sample totals of the key variables with those known for the population as a whole. The remainder of this section provides a condensed treatment of estimation with survey data using calibrated weights; a full description was provided in the previous paper.

For a given finite population \mathcal{U} of units indexed i = 1, ..., N, the interests of survey statisticians often lie in estimating the population total of a variable Y:

$$T[Y] = \sum_{i \in \mathcal{U}} Y_i \tag{1}$$

A sample S of n units indexed by j = 1, ..., n is taken from U. If the probability to select the i-th unit is known to be π_i , then the probability weights, or design weights,

are given by the inverse probability of selection:

$$w_{di} = \pi_i^{-1} \tag{2}$$

where subscript d stands for design probabilities of selection. With these weights, an unbiased (design-based, non-parametric) estimator of the total (1) is (Horvitz and Thompson 1952)

$$t[y] = \sum_{j \in \mathcal{S}} \frac{y_j}{\pi_j} \equiv \sum_{j \in \mathcal{S}} w_{dj} y_j \tag{3}$$

Probability weights protect the end user from potentially informative sampling designs, in which the probabilities of selection are correlated with outcomes, and relieve the user from the need to fully account for the sampling design variables in their analysis, as is required in methods such as multilevel regression with post-stratification (Park et al. 2004). Design-based methods generally ensure that inference can be generalized to the finite population even when the statistical models used by analysts and researchers are not specified correctly (Pfeffermann 1993; Binder and Roberts 2003).

Often, survey statisticians have auxiliary information on the units in the frame, and such information can be included at the sampling stage to create more efficient designs. Unequal probabilities of selection are then controlled with probability weights, implemented as [pw=exp] in Stata (and can be permanently affixed to the data set with svyset command; see [SVY] svyset).

In many situations, however, usable information is not available beforehand, and may only appear in the collected data. For example, the census totals of the age and gender distribution of the population may exist, but age and gender of the sampled units is unknown until the survey measurement is taken on them. It is still possible to capitalize on this additional data by adjusting the weights in such a way that the reweighted data conforms to these known figures. The procedures to perform these reweighting steps are generally known as weight calibration (Deville and Särndal 1992; Deville et al. 1993; Kott 2006, 2009; Särndal 2007).

Suppose there are several variables, referred to as control variables, that are available for both the population and the sample (age groups, race, gender, educational attainment, etc.). Categorical variables are represented by the 0/1 category indicators, although Kolenikov and Hammer (2015) provide an illustrative example of how the counts of persons in each demographic category within a household (i.e., variables taking values $0, 1, 2, \ldots$) can be used to create person-level weights that are constant within households. Weight calibration aims at adjusting the weights via an iterative optimization so that the control totals for the control variables $\mathbf{x}_j = (x_{1j}, \ldots, x_{pj})$, obtained with the calibrated weights w_{cj} , align with the known population totals:

$$\sum_{j \in \mathcal{S}} w_{cj} \mathbf{x}_j = T[\mathbf{X}] \tag{4}$$

The population totals of the control variables in the right hand side of (4) are assumed to be known from a census or a higher quality survey. Deville and Särndal (1992) framed

the problem of finding a suitable set of weights as that of constrained optimization with the control equations (4) serving as constraints, and optimization targeted at making the discrepancy between the design weights w_{dj} and calibrated weights w_{cj} as close as possible, in a suitable sense.

The package ipfraking (Kolenikov 2014) implements a popular calibration algorithm, known as *iterative proportional fitting*, or *raking*, which consists of iterative updating (post-stratification) of each of the margins. (For an in-depth discussion of distinctions between raking and post-stratification, see Kolenikov (2016).) Since 2014, the continuing code development resulted in additional features that this update documents.

2 Updates to ipfraking program and package

Listed below is the full syntax of ipfraking. For description of options, please refer to Kolenikov (2014).

2.1 Syntax of ipfraking

```
ipfraking [if] [in] [weight], ctotal(matname [matname ...]) [
  generate(newvarname) replace double iterate(#) tolerance(#)
  ctrltolerance(#) trace nodivergence trimhiabs(#) trimhirel(#)
  trimloabs(#) trimlorel(#) trimfrequency(once|sometimes|often) double
  meta nograph ]
```

2.2 New features of ipfraking

The new features or functionality of ipfraking concerns reporting and diagnostics; an alternative functional form specification; and richer metadata stored in the characteristics of the weight variable.

Reporting of results and errors by ipfraking was improved in several directions. The discrepancy for the worst fitting category is now being reported. The number of trimmed observations is reported.

Using Example 3 from Kolenikov (2014) with trimming options, we have:

```
Iteration 5, max rel difference of raked weights = .00095888
Iteration 6, max rel difference of raked weights = .00018036
Iteration 7, max rel difference of raked weights = .00003391
Iteration 8, max rel difference of raked weights = 6.377e-06
Iteration 9, max rel difference of raked weights = 1.199e-06
Iteration 10, max rel difference of raked weights = 2.254e-07
The worst relative discrepancy of 3.0e-08 is observed for race == 3
Target value = 20053682; achieved value = 20053682
Trimmed due to the upper absolute limit: 5 weights.
```

Summary of the weight changes

```
Std. dev.
                                                               CV
                   Mean
                                         Min
                                                    Max
Orig weights
                   11318
                                7304
                                          2000
                                                     79634
                                                              . 6453
                   22055
                               18908
                                          4033
                                                    200000
Raked weights
                                                              .8573
Adjust factor
                  2.1486
                                        0.9220
                                                   18.9828
  char li rakedwgt3[]
  rakedwgt3[source]:
                               finalwgt
  rakedwgt3[objfcn]:
                               2.25435521346e-07
                               3.00266822363e-08
  rakedwgt3[maxctrl]:
  rakedwgt3[converged]:
                               1
  rakedwgt3[worstcat]:
                              3
  rakedwgt3[worstvar]:
                               [pw=finalwgt], gen( rakedwgt3 ) ctotal( ACS2011_sex_age Census2011_region ...
  rakedwgt3[command]:
  rakedwgt3[trimloabs]:
                               trimloabs(2000)
  rakedwgt3[trimhiabs]:
                               trimhiabs(200000)
  rakedwgt3[trimfrequency]:
                              sometimes
  rakedwgt3[hash1]:
                               2347674164
  rakedwgt3[mat3]:
                               Census2011_race
  rakedwgt3[over3]:
                              race
  rakedwgt3[totalof3]:
                               _one
  rakedwgt3[Census2011_race]: 7.48567503861e-09
  rakedwgt3[mat2]:
                               Census2011_region
  rakedwgt3[over2]:
                              region
  rakedwgt3[totalof2]:
                               _one
  rakedwgt3[Census2011_region]:
                               3.00266822363e-08
  rakedwgt3[mat1]:
                               ACS2011_sex_age
  rakedwgt3[over1]:
                               sex_age
  rakedwgt3[totalof1]:
                               _one
  rakedwgt3[ACS2011_sex_age]: 4.13778410340e-09
                               Raking controls used: ACS2011_sex_age Census2011_region Census2011_race
  rakedwgt3[note1]:
  rakedwgt3[note0]:
```

If ipfraking determines that the categories do not match in the control totals received from ctotals() and those found in the data, a full listing of categories is provided, and the categories not found in one or the other are explicitly shown. Using Example 2 of Kolenikov (2014), let us modify one of the variables to a nonsensical value:

```
_one:11 _one:12 _one:13 _one:15 _one:22 _one:23
This is what ACS2011_sex_age has that data don't:
   _one:21
This is what data have that ACS2011_sex_age doesn't:
   _one:15
r(111);
```

Option meta saves more information in characteristics of the calibrated weight variables that can be used in production diagnostics. The following characteristics are stored with the newly created weight variable (see [P] char).

command as typed by the user

matrix name The relative matrix difference from the corresponding

control total, see [D] functions

trimhiabs, trimloabs, Corresponding trimming options, if specified

trimhirel, trimlorel,

trimfrequency

maxctrl the greatest mreldif between the targets and the achieved

weighted totals

objfcn the value of the relative weight change at exit converged whether ipfraking exited due to convergence (1)

vs. due to an increase in the objective function or reaching the limit on the number of iterations (0)

source weight variable specified as the [pw=] input

worstvar the variable in which the greatest discrepancy between

the targets and the achieved weighted totals

(maxctrl) was observed

worstcat the category of the worstvar variable in which the

greatest discrepancy was observed

For the control total matrices $\#=1,2,\ldots$, the following meta-information is stored.

mat# the name of the control total matrix
totalof# the multiplier variable (matrix coleq)
over# the margin associated with the matrix

(i.e., the categories represented by the columns)

Also, **ipfraking** stores the notes regarding the control matrices used, and which of the margins did not match the control totals, if any. See [D] **notes**.

Linear calibration (Case 1 of Deville and Särndal (1992)) is provided with linear option. The weights are calculated analytically:

$$w_{j,\text{lin}} = w_{dj}(1 + \mathbf{x}_j'\lambda), \quad \lambda = \left(\sum_{j \in \mathcal{S}} w_{dj}\mathbf{x}_j\mathbf{x}_j'\right)^{-1} (T[\mathbf{X}] - t[X])$$
 (5)

Since no iterative optimization is required, linear calibration works very fast. However it has an undesirable artefact of potentially producing negative weights, as the range of weights is not controlled. (As raking works by multiplying the currents weights by positive factors, if the input weights are all positive, the output weights will be positive as well.) Negative weights are not allowed by the official svy commands or commands that work with [pweights]. In many tasks, running linear weights first, pulling up the negative and small positive weights (replace weight = 1 if weight <= 1) and re-raking using the "proper" iterative proportional fitting runs faster than raking from scratch. An example of linearly calibrated weights is given below in Section 6.

2.3 Utility programs

The original package ipfraking provided additional utility programs: mat2do and xls2row. One of these utility programs, mat2do, was updated to provide the notimestamp option to omit the time stamps (which tend to unnecessarily throw off the project building and revision control systems).

This update provides two more utility programs, whatsdeff and totalmatrices.

Design effects

A new utility program whatsdeff was added to compute the unequal weighting design effects and margins of error, common tasks associated with describing survey weights. Specifically, the Transparency Initiative of the American Association for Public Opinion Research (AAPOR 2014) requires that

For probability samples, the estimates of sampling error will be reported, and the discussion will state whether or not the reported margins of sampling error or statistical analyses have been adjusted for the design effect due to weighting, clustering, or other factors.

$$\label{eq:whatsdeff} \ weight_variable\ \left[\ if\ \right]\ \left[\ in\ \right]\ \mbox{, [by(\it varlist)]}$$

The utility program whatsdeff calculates the apparent design effect due to unequal weighting,

$$DEFF_{UWE} = 1 + CV_w^2 = 1 + r(Var)/(r(mean))^2$$

using the returned values from summarize weight_variable (see help return). Additionally, it reports the effective sample size, $n/\text{DEFF}_{\text{UWE}}$, and also returns the margins of error for the sample proportions that estimate the population proportions of 10% and 50%.

- . webuse nhanes2, clear
- . whatsdeff finalwgt

Group	Min	Mean	Max	CV	DEFF	N	N eff
Overall	2000.00	11318.47	79634.00	0.6453	1.4164	10351	7307.97

. return list

```
scalars:
```

```
r(N) = 10351
r(M0E10) = .0068792766212984
r(M0E50) = .0114654610354974
r(Neff_Overall) = 7307.97435325364
r(DEFF_Overall) = 1.416397964696134
```

Design effects can also be broken down by a categorical variable:

. whatsdeff finalwgt, by(sex)

	Group	Min	Mean	Max	CV	DEFF	N	N eff
sex	Male Female	2000.00 2130.00	11426.14 11221.12	79634.00 61534.00	0.6578 0.6333	1.4326 1.4010	4915 5436	3430.94 3880.01
	Overall	2000.00	11318.47	79634.00	0.6453	1.4164	10351	7307.97

. return list

scalars:

```
r(N) = 10351
r(M0E10) = .0068792766212984
r(M0E50) = .0114654610354974
r(Neff_Overall) = 7307.97435325364
r(DEFF_Overall) = 1.416397964696134
r(Neff_Female) = 3880.0710397866
r(DEFF_Female) = 1.40102836266093
r(Neff_Male) = 3430.938195872213
r(DEFF_Male) = 1.432552765279559
```

The estimates of unequal weighting design effects that whatsdeff produces should be considered as a typical magnitude of a design effect. As pointed out by a referee, in many situations when survey variables are correlated with weights or with the variables that weight calibration is based upon, the actual design effects reported by postestimation command estat effect should be expected to be lower, provided that variance estimation methods take calibration into account properly (e.g., via replicate variance estimation, as described in Kolenikov (2010), or via svy, vce(calibrate) functionality of the official Stata svy suite available in Stata 15.1+ (Valliant and Dever 2017)). In other words, for most situations these estimates could be considered an upper bound on this design effect, since this calculation assumes that the weights are independent of the survey variable of descriptive interest.

Conversion of the matrices

A new program totalmatrices converts the control totals matrices between the formats expected by ipfraking and svycal (Valliant and Dever 2017).

```
totalmatrices matrix_list , [ svycal <u>ipfr</u>aking stub(name) replace ]
```

svycal checks that the supplied matrix or matrices are compatible with svycal specification of totals as a matrix.

ipfraking checks that the supplied matrix or matrices are compatible with ipfraking.

stub(name) provides the naming convention for the converted control total matrices. If the conversion is from ipfraking to svycal, one matrix whose name is supplied in the stub(...) option will be created. If the conversion is from svycal to ipfraking, matrices corresponding to each variable will be created and have their names set to concatenation of the stub and the variable name.

To convert several matrices from ipfraking format to a single matrix in svycal format:

```
. totalmatrices ACS2011_sex_age Census2011_region Census2011_race, ///

> ipfraking stub(alltotals) replace convert

It appears that the matrix ACS2011_sex_age is of ipfraking format.

It appears that the matrix Census2011_region is of ipfraking format.

It appears that the matrix Census2011_race is of ipfraking format.

You can now matrix list alltotals to check and then call svycal as:
    svycal [regress|rake] 11.sex_age 12.sex_age 13.sex_age 21.sex_age 2

> 2.sex_age 23.sex_age 1.region 2.region 3.region 4.region 1.race 2.ra

> ce 3.race [pw=finalwgt], generate(...) totals(alltotals) nocons

I suspect the following would be simpler and could work, too:
    svycal [regress|rake] ibn.sex_age ibn.region ibn.race [pw=finalwgt]

> , generate(...) totals(alltotals) nocons
```

To convert a single matrix compatible with svycal requirements for its totals(matname) format into a list of matrices compatible with ipfraking:

Note that at the moment, totalmatrices does not handle conversion of interactions, which is arguably one of the greatest strengths of svycal. As noted in section 7, for interactions to work out with ipfraking, standalone variables need to be created, and totalmatrices would rather have the user do that.

2.4 New programs in the package

Two new programs are added to the package: ipfraking_report and wgtcellcollapse, and are documented in the subsequent sections of this article. The former provides reports on the raked weights, including summaries of the unweighted data, data with the input weights, and with the calibrated weights. The latter creates a mostly automated flow of collapsing weighting cells that are too detailed (and hence have low sample sizes).

3 Excel reports on raked weights: ipfraking_report

```
ipfraking_report using filename , raked_weight(varname) [ matrices(namelist) by(varlist) xls replace force ]
```

The utility command ipfraking_report produces a detailed report describing the raked weights, and places it into *filename*.dta file (or, if xls option is specified, both *filename*.dta and *filename*.xls files).

Along the way, $ipfraking_report$ runs a regression of the log raking adjustment ratio on the calibration variables. This regression is expected to have R^2 equal to or very close to 1, and residual variance equal to or very close to zero. This naturally produces obscenely high t-test values, but the purpose of this regression is not in establishing "significance" of any variable in explaining the outcome (which we know to be predicted with near certainty). Instead, the regression coefficients provide insights regarding which categories received greater vs. smaller adjustments (which in turn indicate lower response or coverage rates for the corresponding population subgroups). Conversely, control variables that are associated with relatively similar adjustment factors may be contributing relatively little to the weight adjustment, and may be candidates for removal from the list of control totals.

The regression output, using Example 3 from Kolenikov (2014), is as follows.

```
. ipfraking_report using rakedwgt3-report, raked_weight(rakedwgt3) replace by(_one) Margin variable sex_age (total variable: _one; categories: 11 12 13 21 22 23). Margin variable region (total variable: _one; categories: 1 2 3 4). Margin variable race (total variable: _one; categories: 1 2 3). Auxiliary variable _one (categories: 1). file rakedwgt3-report.dta saved
```

Source	SS	df	MS	Number of obs		10,351
				F(10, 10340)	>	99999.00
Model	2086.13859	10	208.613859	Prob > F	=	0.0000
Residual	.78315703	10,340	.000075741	. R-squared	=	0.9996
				Adj R-squared	=	0.9996
Total	2086.92175	10,350	.201634952	Root MSE	=	.0087
000003	Coef.	Std. Err.	t	P> t [95% C	onf.	Interval]

000003	Coef.	Std. Err.	t	P> t	[95% Conf.	Interval]
sex_age						
11	.0644365	.0002775	232.21	0.000	.0638925	.0649804
12	.4545577	.0003154	1441.25	0.000	.4539395	.455176
13	.6782466	.0002804	2418.71	0.000	.6776969	.6787963
22	.3966406	.0003049	1300.84	0.000	.3960429	.3972383
23	.7304392	.0002726	2679.97	0.000	.7299049	.7309734
region						
NE	4455127	.0002536 -:	1756.49	0.000	4460099	4450155
MW	4428144	.0002335 -:	1896.53	0.000	4432721	4423567
W	6672675	.0002407 -	2772.21	0.000	6677393	6667957
race						
Black	.3360321	.0002848	1180.08	0.000	.3354739	.3365902

```
Other
                 1.613276
                             .0006303
                                     2559.34
                                                 0.000
                                                           1.612041
                                                                       1.614512
                 .5864801
                             .0002455
                                     2388.48
                                                 0.000
                                                           .5859988
                                                                        .5869614
       _cons
Raking adjustments for sex_age variable:
  the smallest was
                          1.798 for category 21 (21)
                          3.732 for category 23 (23)
  the greatest was
Raking adjustments for region variable (1=NE, 2=MW, 3=S, 4=W):
  the smallest was
                          0.922 for category 4 (W)
  the greatest was
                          1.798 for category 3 (S)
Raking adjustments for race variable (1=white, 2=black, 3=other):
  the smallest was
                          1.798 for category 1 (White)
                          9.023 for category 3 (Other)
  the greatest was
```

It looks like ipfraking had to make greater adjustments to the weights of older females (sex_age==23, i.e., sex==2 & age==3; the adjustment factor for this category was 3.732 vs. the low of 1.798 for young women), and especially other race individuals (the adjustment factor was 9.023, vs. 1.798 for the whites). The diagnostic value is in the differences in the adjustment factors with the same variable; since no attempt is being made to average across the population or the sample or to assign the "base" variable, the absolute reported values of the adjustment factors may not be meaningful. In the example above, 1.798 figures both as the greatest adjustment factor of the region variable, and as the lowest adjustment factor for the race the and sex-by-age interaction. As is easily seen from regression output, this value is the exponent of the intercept 1.798=exp(0.586). Since all of the "estimates" of the region specific coefficients are negative, the lowest reported value is less than this baseline value. Since all of the "estimates" of the race and sex-by-age indicators are positive, all the category-specific adjustment factors are greater than this baseline value. This is an interplay of the base categories, and the differences in the demographic composition within each category of a control total variable vis-a-vis other weighting variables.

3.1 Options of ipfraking_report

raked_weight(varname) specifies the name of the raked weight variable to create the report for. This is a required option.

matrices(namelist) specifies a list of matrices (formatted as the matrices supplied to ctotal() option of ipfraking) to produce weighting reports for. In particular, the variables and their categories are picked up from these matrices; and the control totals/proportions are compared to those defined by the weight being reported on.

by (varlist) specifies a list of additional variables for which the weights are to be tabulated in the raking weights report. The difference with the matrices() option is that the control totals for these variables may not be known (or may not be relevant). In particular, by (_one), where _one is identically one, will produce the overall report.

xls requests exporting the report to an Excel file.

replace specifies that the files produced by ipfraking_report (i.e., the .dta and the .xls file if xls option is specified) should be overwritten.

force requires that a variable that may be found repeatedly (between the calibration variables supplied originally to ipfraking, the variables found in the independent total matrices(), and the variables without the control totals provided in by() option) is processed every time it is encountered. (Otherwise, it is only processed once.)

3.2 Variables in the raking report

The raking report file contains the following variables.

(Continued on next page)

Variable name	Definition
Weight_Variable	The name of the weight variable, generate()
C_Total_Margin_Variable_Name	The name of the control margin,
_	rowname of the corresponding ctotal() matrix
C_Total_Margin_Variable_Label	The label of the control margin variable
Variable_Class	The role of the variable in the report:
	Raking margin: a variable used as a calibration margin
	(picked up automatically from the ctotal()
	matrix, provided meta option was specified)
	Other known target: supplied with matrices()
	option of ipfraking_report
	Auxiliary variable: additional variable supplied
	with by() option of ipfraking_report
C_Total_Arg_Variable_Name	The name of the multiplier variable
C_Total_Arg_Variable_Label	The label of the multiplier variable
C_Total_Margin_Category_Number	Numeric value of the control total category
C_Total_Margin_Category_Label	Label of the control total category
C_Total_Margin_Category_Cell	An indicator whether a weighting cell was
0=10001=101611=0000601	produced by collapsing categories
	using wgtcellcollapse
Category_Total_Target	The control total to be calibrated to
04006019_10041_141600	(the specific entry in the ctotal() matrix)
Category_Total_Prop	Control total proportion
0400801J_10041_110P	(the ratio of the specific entry in the ctotal()
	matrix to the matrix total)
Unweighted_Count	Number of sample observations in the category
Unweighted_Prop	Unweighted proportion
Unweighted_Prop_Discrep	Difference Unweighted_Prop - Category_Total_Prop
Category_Total_SRCWGT	Weighted category total, with input weight
Category_Prop_SRCWGT	Weighted category proportion, with input weight
Category_Total_Discrep_SRCWGT	Difference Category_Total_SRCWGT -
oatogory_rotar_bracker_browar	- Category_Total_Target
Category_Prop_Discrep_SRCWGT	Difference Category_Prop_SRCWGT -
oategory i rop_biserep_bitower	- Category_Total_Prop
Category_RelDiff_SRCWGT	reldif(Category_Total_SRCWGT,
Category TierDiff_Dicowdi	Category_Total_Target)
Overall_Total_SRCWGT	Sum of source weights
Source	The name of the matrix from which the totals
Dour 00	were obtained
Comment	Placeholder for comments, to be entered during
Comment	manual review
	manuar review

For each of the input weights (SRCWGT suffix), raked weights (RKDWGT suffix) and raking ratio (the ratio of raked and input weights, RKDRATIO suffix), the following summaries are provided.

Variable name	Definition
$\mathtt{Min}_{-}\mathit{WEIGHT}$	Min of the respective weight
P25_WEIGHT	25th percentile of the respective weights
P50_WEIGHT	Median of the respective weights
P75_WEIGHT	75th percentile of the respective weights
${ t Max}_{-}{ t WEIGHT}$	Max of the respective weights
Mean_WEIGHT	Mean of the respective weights
$\mathtt{SD}_ extit{WEIGHT}$	Standard deviation of the respective weights
DEFF_WEIGHT	Apparent UWE DEFF of the respective weights

3.3 Example

Continuing with the example of calibration by region, race, and sex-by-age interaction, a glimpse of the raking report looks as follows.

	C_Tota	~y_Label	Categor~t	Categor	DEFF_SR~T	DEFF_RK~T
1.	sex_age	11	41995394	41995394	1.2148059	1.6259899
2.	sex_age	12	42148662	42148662	1.2462168	1.5716613
3.	sex_age	13	26515340	26515340	1.2241095	1.5460785
4.	sex_age	21	41164255	41164255	1.2325105	1.5639529
5.	sex_age	22	43697440	43697440	1.1937826	1.5175312
6.	sex_age	23	32773080	32773080	1.233902	1.664307
7.	region	NE	40679030	40679030	1.3056639	1.3657837
8.	region	MW	49205289	49205289	1.3475551	1.4909581
9.	region	S	85024007	85024006	1.4950056	1.4912995
10.	region	W	53385843	53385844	1.459859	2.3772667
11.	race	White	1.784e+08	1.784e+08	1.4059259	1.4337901
12.	race	Black	29856865	29856865	1.5173846	1.5092533
13.	race	Other	20053682	20053682	1.3179136	1.2264706
14.	_one	1		2.283e+08	1.4164382	1.7349278

The last line, corresponding to the auxiliary variable _one identically equal to 1 (this variable was present in the data set as it was used by ipfraking as a multiplier), contains summaries for the sample as a whole. It is always recommended to include it (note the use of ipfraking_report, ... by(_one) option in the syntax in the previous section.)

Functionality of ipfraking_report is aimed at manual quality control, which typically involves (i) review of variables and categories with raking factors that differ the most (in the output such as that shown on page 9), and (ii) review of the resulting report file in Excel (e.g., for design effects and discrepancies between targets and achieved

totals).

4 Collapsing weighting cells: wgtcellcollapse

An additional new component of **ipfraking** package is a tool to semi-automatically collapse weighting cells, in order to achieve a required minimal size of the weighting cell. (A typical recommendation is to have cells of size at least 30 to 50.)

```
wgtcellcollapse task [if] [in], [task_options] where task is one of: define to define collapsing rules explicitly sequence to create collapsing rules for a sequence of categories report to list the currently defined collapsing rules candidate to find rules applicable to a given category collapse to perform cell collapsing label to label collapsed cells using the original labels after wgtcellcollapse collapse
```

4.1 Syntax of wgtcellcollapse report

```
wgtcellcollapse report , variables(varlist) [ break ]
```

<u>var</u>iables(varlist) is the list of variables for which the collapsing rules are to be reported

break requires wgtcellcollapse report to exit with error when technical inconsistencies are encountered

4.2 Syntax of wgtcellcollapse define

```
wgtcellcollapse define , \underline{\text{var}}iables(varlist) [ from(numlist) to(#) label(string) \max(\#) clear ]
```

variables(varlist) is the list of variables for which the collapsing rule can be used
from(numlist) is the list of categories that can be collapsed according to this rule
to(#) is the numeric value of the new, collapsed category
label(string) is the value label to be attached to the new, collapsed category

max(#) limits the values of the collapsed variable that can be used in a collapsing rule

clear clears all the rules currently defined

Let us demonstrate the two subcommands introduced so far with the following toy example.

```
. clear
.
. set obs 4
number of observations (_N) was 0, now 4
.
. gen byte x = _n
.
. label define x_lbl 1 "One" 2 "Two" 3 "Three" 4 "Four"
.
. label values x x_lbl
.
. wgtcellcollapse define, var(x) from(1 2 3) to(123)
.
. wgtcellcollapse report, var(x)
Rule (1): collapse together
    x == 1 (One)
    x == 2 (Two)
    x == 3 (Three)
    into x == 123 (123)
WARNING: unlabeled value x == 123
```

For automated quality control purposes, the break option of wgtcellcollapse report can be used to abort the execution when technical deficiencies in the rules or in the data are encountered. In the above example, the label of the new category 123 was not defined. Should the break option be specified, absence of the category label would be considered a serious enough deficiency to stop with an error:

```
. wgtcellcollapse report, var(x) break
Rule (1): collapse together
 x == 1 (One)
 x == 2 (Two)
 x == 3 (Three)
  into x == 123 (123)
 ERROR: unlabeled value x == 123
assertion is false
r(9);
. wgtcellcollapse define, var(x) clear
. wgtcellcollapse define, var(x) from(1 2 3) to(123) label("One through three")
. wgtcellcollapse report, var(x) break
Rule (1): collapse together
 x == 1 (One)
 x == 2 (Two)
 x == 3 (Three)
 into x == 123 (One through three)
```

4.3 Syntax of wgtcellcollapse sequence

```
\verb|wgtcellcollapse sequence |, | \underline{var} \\ iables(|\mathit{varlist}|) | \\ from(|\mathit{numlist}|) | \\ depth(\#)
```

variables(varlist) is the list of variables for which the collapsing rule can be used
from(numlist) is the sequence of values from which the plausible subsequences can be
constructed

depth(#) is the maximum number of the original categories that can be collapsed

Continuing with the toy example introduced above, here is an example of moderate length sequences to collapse categories:

```
. clear
. set obs 4
number of observations (_N) was 0, now 4
. gen byte x = _n
. label define x_lbl 1 "One" 2 "Two" 3 "Three" 4 "Four"
. label values x x_lbl
. wgtcellcollapse sequence, var(x) from(1 2 3 4) depth(3)
. wgtcellcollapse report, var(x)
Rule (1): collapse together
  x == 1 \text{ (One)}
  x == 2 (Two)
  into x == 212 (One to Two)
Rule (2): collapse together
  x == 2 (Two)
  x == 3 (Three)
  into x == 223 (Two to Three)
Rule (3): collapse together
  x == 3 (Three)
  x == 4 \text{ (Four)}
  into x == 234 (Three to Four)
Rule (4): collapse together
  x == 1 (One)
  x == 2 (Two)
  x == 3 (Three)
  into x == 313 (One to Three)
Rule (5): collapse together
  x == 1 (One)
  x == 223 (Two to Three)
  into x == 313 (One to Three)
Rule (6): collapse together
  x == 3 (Three)
  x == 212 (One to Two)
  into x == 313 (One to Three)
```

(Continued on next page)

```
Rule (7): collapse together

x == 2 (Two)

x == 3 (Three)

x == 4 (Four)

into x == 324 (Two to Four)

Rule (8): collapse together

x == 2 (Two)

x == 234 (Three to Four)

into x == 324 (Two to Four)

Rule (9): collapse together

x == 4 (Four)

x == 223 (Two to Three)

into x == 324 (Two to Four)
```

Note how wgtcellcollapse sequence automatically created labels for the collapsed cells.

When creating sequential collapses, wgtcellcollapse sequence uses the following conventions in assigning the values the new collapsed categories:

- First comes the length of the collapsed subsequence (up to depth(#)).
- Then comes the starting value of the category in the subsequence (padded by zeroes as needed).
- Then comes the ending value of the category in the subsequence (padded by zeroes as needed).

In the example above, rules 7 through 9 lead to collapsing into the new category 324, which stands for "the subsequence of length 3 that starts with category 2 and ends with category 4". A numeric value of the collapsed category that reads like 50412 means "the subsequence of length 5 that starts with category 4 and ends with category 12". In that second example, wgtcellcollapse sequence padded the value of 4 with an additional zero, so that the length of resulting collapsed category value is always (of digits of the sequence length) + twice (of digits of the greatest source category).

Note that wgtcellcollapse sequence respects the order in which the categories are supplied in the from() option, and does not sort them. If the categories are supplied in the order 2, 4, 1 and 3, then wgtcellcollapse sequence would collapse 2 with 4, 4 with 1, and 1 with 3:

```
. wgtcellcollapse define, var(x) clear
. wgtcellcollapse sequence, var(x) from(2 4 1 3) depth(2)
. wgtcellcollapse report, var(x)
Rule (1): collapse together
    x == 2 (Two)
    x == 4 (Four)
    into x == 224 (Two to Four)
Rule (2): collapse together
```

```
x == 4 (Four)
x == 1 (One)
into x == 241 (Four to One)
Rule (3): collapse together
x == 1 (One)
x == 3 (Three)
into x == 213 (One to Three)
```

4.4 Syntax of wgtcellcollapse candidate

```
wgtcellcollapse candidate, variable(varname) category(#) [ max#]
variable(varname) is the variable whose collapsing rules are to be searched
category(#) is the category for which the candidate rules are to be identified
max(#) is the maximum value of the categories in the candidate rules to be returned
```

The rules found are quietly returned through the mechanism of sreturn, see [P] return, as they are intended to stay in memory sufficiently long for wgtcellcollapse collapse to evaluate each rule. Going back to the example from the previous section with sequential collapses of depth 3, we can identify the following candidates for categories 2, 212 (collapsed values of 1 and 2), and a non-existent category of 55:

```
. wgtcellcollapse candidate, var(x) cat(2)
. sreturn list
macros:
           s(goodrule) : "1 2 4 7 8"
              s(rule8) : "2:234=324"
              s(rule7) : "2:3:4=324"
              s(rule4) : "1:2:3=313"
              s(rule2) : "2:3=223"
              s(rule1) : "1:2=212"
                s(cat) : "2"
                  s(x) : "x"
. wgtcellcollapse candidate, var(x) cat(2) max(9)
. sreturn list
macros:
           s(goodrule) : "1 2 4 7"
              s(rule7) : "2:3:4=324"
              s(rule4) : "1:2:3=313"
              s(rule2) : "2:3=223"
              s(rule1) : "1:2=212"
                s(cat) : "2"
                  s(x) : "x"
```

(Continued on next page)

In the second call to the option max(9) was used to restrict the returned rules to the rules that deal with the original categories only (so rule 8 that involved a collapsed category 234 was omitted). It relies on the naming conventions described in the previous section: any of the collapsed cells would have 3-digit values. In the third call, a list of rules that involve a collapsed category cat(212) was requested. Requests for nonexisting categories are not considered errors, but simply produce empty lists of "good rules".

4.5 Syntax of wgtcellcollapse label

```
wgtcellcollapse label , <u>var</u>iable(varname) [ verbose force ]

<u>var</u>iable(varname) is the collapsed variable to be labeled.

verbose outputs the labeling results. There may be a lot of output.

force instructs wgtcellcollapse label to only use categories present in the data.
```

.6 Syntax of wgtcellcollapse collapse

An example is given in section 5.2 below.

```
wgtcellcollapse collapse [if][in], variables(varlist) mincellsize(#)
    saving(dofile_name) [ generate(newvarname) replace append
    feed(varname) strict sort(varlist) run maxpass(#) maxcategory(#)
    zeroes(numlist) greedy ]
```

<u>var</u>iables(varlist) provides the list of variables whose cells are to be collapsed. When more than one variable is specified, wgtcellcollapse collapse proceeds from right to left, i.e., first attempts to collapse the rightmost variable.

mincellsize(#) specifies the minimum cell size for the collapsed cells. For most weighting purposes, values of 30 to 50 can be recommended.

generate (newvarname) specifies the name of the collapsed variable to be created.

feed(varname) provides the name of an already existing collapsed variable.

strict modifies the behavior of wgtcellcollapse collapse so that only collapsing rules for which all participating categories have nonzero counts are utilized.

sort(varlist) sorts the data set before proceeding to collapse the cell. The default sort order is in terms of the values of the collapsed variable. A different sort order may produce a different set of collapsed cell when cells are tied on size.

maxpass(#) specifies the maximum number of passes through the data set. The default value is 10000.

<u>maxcategory</u>(#) is the maximum category value of the variable being collapsed. It is passed to the internal calls to wgtcellcollapse candidate, see above.

<u>zer</u>oes(numlist) provides a list of the categories of the collapsed variable that may have zero counts in the data.

greedy modifies the behavior wgtcellcollapse collapse to prefer the rules that collapse the maximum number of categories.

Options to deal with the do-file to write the collapsing code to:

<u>saving(dofile_name)</u> specifies the name of the do-file that will contain the cell collapsing code.

replace overwrites the do-file if one exists.

append appends the code to the existing do-file.

run specifies that the do-file created is run upon completion. This option is typically specified with most runs.

The primary intent of wgtcellcollapse collapse is to create the code that can be utilized in both a survey data file and a population targets data file that are assumed to have identically named variables. Thus it does not only manipulate the data in the memory and collapses the cells, but also produces the do-file code that can be recycled in automated weight production. To that effect, when a do-file is created with the replace and saving() options, the user needs to specify generate() option to provide the name of the collapsed variable; and when the said do-file is appended with the the append and saving() options, the name of that variable is provided with the feed() option.

The algorithm by which wgtcellcollapse collapse identifies the cells to be collapsed uses a variation of greedy search. It first identifies the cells with the lowest (positive) counts; finds the candidate rules for the variable(s) to be collapsed; evaluates the counts of the collapsed cells across all these candidate rules; and uses the rule that produces the smallest size of the collapsed cell across all applicable rules. So when it finds several rules that are applicable to the cell being currently processed that has a size of 5, and the candidate rules produce cells of sizes 7, 10 and 15, wgtcellcollapse

collapse will use the rule that produces the cell of size 7. The algorithm runs until all cells have sizes of at least mincellsize(#) or until maxpass(#) passes through the data are executed. In real world situations with messy data, this basic algorithm often produces inconsistent results, generally because it fails to identify empty cells, or fully track the cells that have already been collapsed. For that reason, a number of options are provided to modify its behavior. Section 5 demonstrates a worked out example.

- Hint 1. Since wgtcellcollapse collapse works with the sample data, it will not be able to identify categories that are not observed in the sample (e.g., rare categories missing because of unit nonresponse), but may be present in the population. This will lead to errors at the raking stage, when the control total matrices have more categories than the data, forcing ipfraking to stop. (See page 4 for the output ipfraking provides in this situation.) To help with that, the option zeroes() allows the user to pass the categories of the variables that are known to exist in the population but not in the sample.
- Hint 2. The behavior of wgtcellcollapse collapse, zeroes() leads to undesirable artifacts when collapsing long streaks of sequential zeroes. While the edge zero cells would be collapsed with their non-zero neighbors, the zero cell in between may end up being collapsed with some far-away cells, creating collapsing rules with breaks in the sequences. To improve upon that behavior, option greedy makes wgtcellcollapse collapse look for a rule that combines as many cells as possible, thus collapsing as many categories with zero counts in one pass as it can.
- Hint 3. Other than for dealing with zero cells, the option strict should be specified most of the time. It ensures that each cell in a candidate rule being evaluated has some data in it.
- Hint 4. If you want to guarantee some specific combination of cells to be collapsed by wgtcellcollapse collapse, the most reliable way is to explicitly identify them with the if condition, and specify a very large cell size like mincellsize(10000) so that wgtcellcollapse collapse makes every possible effort to collapse those cells. Since the resulting cell(s) will fall short of that size, the program will exit with a complaint that this size could not be achieved, but hopefully the cells will be collapsed as needed.
- Hint 5. If any of the cells fail to reach the requires sizes, the problematic value are returned to the user in the r(failed) macro as a space delimited list, and in the r(cfailed), as a comma-delimited list. The content of the r(failed) macro can be used in code that could read

```
foreach c in `r(failed)´ {
    ...
    * run some diagnostics for each category that failed
    list ... if collapsed_variable == `c´
    ...
}
```

while the content of the the r(cfailed) macro can be used in code that could read

```
list ... if inlist(collapsed_variable,`r(cfailed)`)
```

Also, these returned values should be used in production code by using the assert command (Gould 2003) to ascertain that these macros are empty (i.e., no errors were encountered):

```
assert "`r(failed)'" == ""
```

A referee noted that wgtcellcollapse could also have utility in preparing for hotdeck imputation procedures. The textbook versions of hotdeck procedures impute missing data by assuming a MAR model (Rubin 1976) with conditioning on a set of categorical variables, i.e., cells of a multivariate table. Akin to weighting procedures, hotdeck procedures are more stable with larger cells, so cell collapsing is often recommended to achieve minimal cell sizes (with an understanding of the bias-vs-variance tradeoff built into these collapsing decisions). For a review of the hotdeck and related imputation methods, see Andridge and Little (2010).

5 Extended motivating example

The primary purpose of developing wgtcellcollapse and adding it to the ipfraking suite was to address the need to collapse cells of the margin variables so that each cell has a minimum sample size; and to do so in a way that can be easily made consistent between a sample data and the population targets data. The problem arises when some of the target variables have dozens of categories, most of which have small counts. Example where such needs arise include:

- transportation surveys, where many stations will have low counts of boardings and/or alightings;
- country of origin variables in household surveys, where most countries will have very low counts;
- continuous age variables which can be collapsed into age groups differently for different values of race or sex.

The workflow of wgtcellcollapse is demonstrated with the following simulated transportation data set of trips along a commuter metro line composed of 21 stations:

- . use stations, clear
 . list station_id, sep(0)

8.	30. High Point
9.	36. Irvingtown
10.	39. Johnsville
11.	40. King Street
12.	44. Limerick
13.	47. Moscow City
14.	49. Ninth Street
15.	50. Ontario Lake
16.	53. Picadilly Square
17.	55. Queens Zoo
18.	60. Redline Circle
19.	62. Silver Spring
20.	68. Toledo Town
21.	69. Union Station

Suppose turnstile counts were collected at entrances (board_id) and exits (alight_id) of these stations, producing the following population figures.

. use trip_population, clear

. table board_id daypart , c(sum num_pass) cellwidth(10) mi

		daypart			
Weekend	Night	PM Reverse	Midday	AM Peak	board_id
44	113	219	34	1423	1. Alewife
144	169	773	298	7198	2. Brookline
422	872	3739	181	19254	8. Carmenton
1270	769	3476	872	12626	11. Dogville
114	145	1263	143	2470	18. East End
60	133	1296	50	634	24. Framington
166	88	439	233	2208	26. Grand Junction
115	482	3740	424	4319	30. High Point
167	30	444	34	1221	36. Irvingtown
6	2	64	4	93	39. Johnsville
13	11	76	46	398	40. King Street
34	53	129	19	1021	44. Limerick
301	140	984	776	3300	47. Moscow City
5	5	191	22	38	49. Ninth Street
23	18	80	22	606	50. Ontario Lake
69	153	622	71	642	53. Picadilly Square
19	15	174	23	331	55. Queens Zoo
3	13	63	4	270	60. Redline Circle
445	206	950	240	3402	62. Silver Spring
112	272	744	61	5085	68. Toledo Town

. table alight_id daypart , c(sum num_pass) cellwidth(10) mi

alight_id	AM Peak	Midday	daypart PM Reverse	Night	Weekend
2. Brookline	19		3	2	
8. Carmenton	492	18	56	23	15
11. Dogville	2475	42	423	153	80
18. East End	929	31	193	67	68
24. Framington	404	13	91	28	27
26. Grand Junction	576	20	147	42	41

30. High Point	2189	89	560	165	167
36. Irvingtown	288	10	91	21	18
39. Johnsville	41		11	2	1
40. King Street	131	3	38	8	6
44. Limerick	277	9	87	20	18
47. Moscow City	1746	78	556	142	128
49. Ninth Street	88	2	25	3	4
50. Ontario Lake	232	11	70	14	14
53. Picadilly Square	633	33	198	47	47
55. Queens Zoo	230	10	71	13	14
60. Redline Circle	90	2	26	3	4
62. Silver Spring	1134	67	369	91	85
68. Toledo Town	1372	81	444	112	118
69. Union Station	53193	3038	16007	2733	2677

Most people ride the train to the last station, with much smaller traffic at other population centers.

Suppose a survey was administered to a sample of the metro line users, with the following counts of cases collected.

- . use trip_sample, clear
- . table board_id daypart , c(freq) cellwidth(10) mi

			daypart		
board_id	AM Peak	Midday	PM Reverse	Night	Weekend
1. Alewife	46	4	11	7	3
Brookline	236	4	35	6	7
8. Carmenton	653	4	184	47	24
11. Dogville	410	41	166	35	56
18. East End	85	5	64	4	4
24. Framington	30	3	74	3	1
26. Grand Junction	72	13	23	5	6
30. High Point	158	20	187	25	12
36. Irvingtown	34	2	25	1	15
39. Johnsville	5	1	1		•
40. King Street	17	1	2		1
44. Limerick	28		9	1	3
47. Moscow City	94	31	49	7	13
49. Ninth Street			9		
50. Ontario Lake	13	1	4	1	1
53. Picadilly Square	23	4	35	7	5
55. Queens Zoo	10	1	14		2
60. Redline Circle	13		5		
62. Silver Spring	106	18	38	12	17
68. Toledo Town	149	6	33	11	3

. table alight_id daypart , c(freq) cellwidth(10) mi

alight_id	AM Peak	Midday	daypart PM Reverse	Night	Weekend
2. Brookline	1				
8. Carmenton	11	1	1	•	1
11. Dogville	85	1	14	6	5

18. East End	36	1	18	1	4
24. Framington	15	1	2	2	2
26. Grand Junction	15	2	8	1	1
30. High Point	73	4	22	11	8
36. Irvingtown	9		4	2	2
39. Johnsville	3		1		•
40. King Street			3		•
44. Limerick	13		2		2
47. Moscow City	81	6	22	6	6
49. Ninth Street	3	1	1		•
50. Ontario Lake	2		1	2	1
53. Picadilly Square	23	1	8	3	2
55. Queens Zoo	6		5	1	•
60. Redline Circle	5				•
62. Silver Spring	49		19	3	9
68. Toledo Town	43	3	24	6	7
69. Union Station	1,709	138	813	128	123

As only 3654 surveys were collected from a total of 96783 riders, we would reasonably expect that there is a need for weighting and nonresponse adjustment. The data available for calibration includes the population turnstile counts listed above. We will produce interactions of the day part and the station that will serve as two weighting margins (one for the stations where the metro users boarded, and one for the stations where they got off).

First, we need to define the weighting rules. In this case, the stations are numbered sequentially, with the northernmost, say, station Alewife being number 3, and the southernmost station, Union Station, where everybody gets off to rush to their city jobs or attractions, being number 69. Below, we create a list of stations and provide it to wgtcellcollapse sequence. We would be collapsing stations along the line, with the expectation that travelers boarding or leaving at adjacent stations within the same day part are more similar to one another than the travelers boarding or leaving a particular station at different times of the day. Collapsing rules need to be defined for the daypart variable as well — mostly because wgtcellcollapse collapse expects all variables to have collapsing rules defined.

```
. use trip_sample, clear
. wgtcellcollapse sequence , var(daypart) from(2 3 4) depth(3)
. levelsof board_id, local(stations_on)
1 2 8 11 18 24 26 30 36 39 40 44 47 49 50 53 55 60 62 68
. levelsof alight_id, local(stations_off)
2 8 11 18 24 26 30 36 39 40 44 47 49 50 53 55 60 62 68 69
. local all_stations : list stations_on | stations_off
. * relies on stations being in sequential order!!!
. wgtcellcollapse sequence , var(board_id alight_id) from(`all_stations') depth(20)
. save trip_sample_rules, replace
file trip_sample_rules.dta saved
```

The syntax above relies on the stations being in the sequential order, which is how the output of levelsof is organized. Otherwise, the internal numeric identifiers of the stations would need to be supplied in the order in which the trains run through them. The number of collapsing rules for variables board_id and alight_id created by wgtcellcollapse sequence is 2961 each.

Below we present the final syntax to produce the collapsed cells. A more detailed version of the paper, available upon request from the author, describes the process of building the syntax through trial and (mostly) error. A reader who plans to thoroughly utilize wgtcellcollapse should read the full description.

```
. use trip_sample_rules, clear
. * (1) Run 1
. wgtcellcollapse collapse, variables(daypart board_id) mincellsize(1) ///
          zeroes(39 44 49 60) greedy maxcategory(99) ///
          generate(dpston5) saving(dpston5.do) replace run
  (output omitted)
. * (2) Run 2
. wgtcellcollapse collapse, variables(daypart board_id) mincellsize(20) ///
          strict feed(dpston5) saving(dpston5.do) append run
  (output omitted)
. assert "`r(failed)'" == ""
. * (3) Run 3
. wgtcellcollapse collapse, variables(daypart alight_id) mincellsize(1) ///
          zeroes(2 40 60) greedy maxcategory(99) ///
          generate(dpstoff5) saving(dpstoff5.do) replace run
Pass 0 through the data...
 smallest count = 1 in the cell
Processing zero cells...
  Invoking rule 39:40=23940 to collapse zero cells
  replace dpstoff5 = 1023940 if inlist(dpstoff5, 1000039, 1000040)
Pass 0 through the data...
  smallest count = 1 in the cell
                                      1000002
  Invoking rule 1:2:8=30108 to collapse zero cells
 replace dpstoff5 = 2030108 if inlist(dpstoff5, 2000001, 2000002, 2000008)
Pass 0 through the data...
  smallest count = 1 in the cell
                                      1000002
  Invoking rule 30:36:39:40:44=53044 to collapse zero cells
  replace dpstoff5 = 2053044 if inlist(dpstoff5, 2000030, 2000036, 2000039, 2000040,
> 2000044)
  (output omitted)
Pass 0 through the data...
  smallest count = 1 in the cell
                                      1000002
  Invoking rule 53:55:60=35360 to collapse zero cells
  replace dpstoff5 = 5035360 if inlist(dpstoff5, 5000053, 5000055, 5000060)
Pass 0 through the data...
  smallest count = 1 in the cell
                                      1000002
Pass 12 through the data...
  smallest count = 1 in the cell
                                      1000002
 Done collapsing! Exiting...
. wgtcellcollapse collapse if inlist(daypart,4,5) & inrange(alight_id,49,50), ///
          variables(daypart alight_id) mincellsize(1) ///
          feed(dpstoff5) zeroes(49) maxcategory(99) saving(dpstoff5.do) append run
Pass 12 through the data...
  smallest count = 1 in the cell
                                      1000002
Processing zero cells...
```

```
Invoking rule 49:50=24950 to collapse zero cells
  replace dpstoff5 = 4024950 if inlist(dpstoff5, 4000049, 4000050)
Pass 12 through the data...
  smallest count = 1 in the cell
                                      1000002
  Invoking rule 49:50=24950 to collapse zero cells
 replace dpstoff5 = 5024950 if inlist(dpstoff5, 5000049, 5000050)
Pass 12 through the data...
  smallest count = 1 in the cell
                                      1000002
Pass 14 through the data...
  smallest count = 1 in the cell
                                      5024950
  Done collapsing! Exiting...
. * (5) Run 5
. * special cells for weekend
. wgtcellcollapse collapse if daypart==5 & inrange(alight_id,1,36), ///
          variables(daypart alight_id) mincellsize(50) ///
          strict feed(dpstoff5) saving(dpstoff5.do) append run
Pass 14 through the data...
 smallest count = 1 in the cell
                                      5000026
  Invoking rule 24:26=22426
  replace dpstoff5 = 5022426 if inlist(dpstoff5, 5000024, 5000026)
Pass 15 through the data...
  smallest count = 1 in the cell
                                      5030108
  Invoking rule 11:30108=40111
 replace dpstoff5 = 5040111 if inlist(dpstoff5, 5000011, 5030108)
  (output omitted)
Pass 19 through the data...
  smallest count = 10 in the cell
                                       5043040
  Invoking rule 70126:43040=110140
  replace dpstoff5 = 5110140 if inlist(dpstoff5, 5070126, 5043040)
Pass 20 through the data...
  smallest count = 23 in the cell
                                       5110140
  WARNING: could not find any rules to collapse dpstoff5 == 5110140
Pass 21 through the data...
 smallest count = .i in the cell
                                       1000002
  Done collapsing! Exiting...
. * (6) Run 6
. wgtcellcollapse collapse if daypart==5 & inrange(alight_id,44,68), ///
          variables(daypart alight_id) mincellsize(50) ///
          strict feed(dpstoff5) saving(dpstoff5.do) append run
Pass 20 through the data...
  smallest count = 1 in the cell
                                      5024950
  Invoking rule 24950:35360=54960
 replace dpstoff5 = 5054960 if inlist(dpstoff5, 5024950, 5035360)
Pass 21 through the data...
  smallest count = 2 in the cell
                                      5000044
  Invoking rule 44:47=24447
 replace dpstoff5 = 5024447 if inlist(dpstoff5, 5000044, 5000047)
  (output omitted)
Pass 25 through the data...
  smallest count = 27 in the cell
                                       5094468
  WARNING: could not find any rules to collapse dpstoff5 == 5094468
Pass 26 through the data...
                                       1000002
  smallest count = .i in the cell
 Done collapsing! Exiting...
. * (7) Run 7
. * all other cells
. wgtcellcollapse collapse, variables(daypart alight_id) mincellsize(20) ///
          strict feed(dpstoff5) saving(dpstoff5.do) append run
```

```
Pass 25 through the data...
  smallest count = 1 in the cell
                                      1000002
 Invoking rule 2:8=20208
 replace dpstoff5 = 1020208 if inlist(dpstoff5, 1000002, 1000008)
Pass 26 through the data...
                                      2000011
 smallest count = 1 in the cell
  Invoking rule 11:18=21118
 replace dpstoff5 = 2021118 if inlist(dpstoff5, 2000011, 2000018)
  (output omitted)
Pass 64 through the data...
 smallest count = 15 in the cell
                                       3054960
 Invoking rule 62:54960=64962
 replace dpstoff5 = 3064962 if inlist(dpstoff5, 3000062, 3054960)
Pass 65 through the data...
  smallest count = 21 in the cell
                                        2200168
 Done collapsing! Exiting...
. assert "`r(failed)'" == ""
```

Each pass identified the smallest cell count, the cell where this low count is found, the rule that can be used to collapse this cell with some other cell (see more on determination of what wgtcellcollapse believes to be the best rule below), and Stata code that can be used to apply this collapsing rule.

The collapsed values of the variables dpston (DayPart-STation-ON) and dpstoff (DayPart-STation-OFF) combine the values of the parent variables. The value of dpston==1000003 indicates the combination of categories daypart==1 and station number 3. The value of dpston==1023940 indicates daypart==1 and sequence of two stations from 39 to 40. The value of dpston==2053044 indicates daypart==2 and sequence of five stations from 30 to 44.

The first call to wgtcellcollapse uses the options generate() and replace to create a new variable and a new do-file, while subsequent calls feed() this variable back, and append additional cell collapsing code to the existing do-file.

The zeroes() option of wgtcellcollapse collapse specified in calls 1, 3 and 4 notified wgtcellcollapse that there are values of alight_id that are never observed. (Riders get on the train on these stations, and exit in small numbers; but no completed surveys were obtained.) The mincellsize(1) option effectively instructed wgtcellcollapse to exit once all of these zero cells are identified and merged with non-zero cells. The maxcategory(99) option restricts collapsing rules to only those that involve individual stations. It relies on the convention that all the individual station IDs are less than 99, and all of the collapsed values are at least 20102 (i.e., the first two stations merged together, forming a cell of size 2 that stretched from 01 to 02). Without these options, wgtcellcollapse would be allowed to pick up one of the previously collapsed cells. It seems safer to collapse stations with zero count to only one station though.

The use of the subsampling conditions like if daypart==5 inrange(alight_id,1,36) in calls 5 and 6 effectively specifies one specific collapsing cell that the algorithm could not otherwise identify. A higher target value mincellsize(50) is used in conjunction,

to make sure that the algorithm does not exit prematurely. The special missing value .i that appears in the smallest count report, as opposed to the actual counts in other runs, is used internally to stop wgtcellcollapse after all of the relevant cases selected by the *if* conditions have been processed.

The use of greedy option in call 3 made it possible to collapse the streak of zero counts in the mid-day part from 36. Irvington to 44. Limerick. Without it, each individual zero count station would be paired with a non-missing station, which leads to cells that overlap in space.

After all zero counts stations are processed, the strict option should almost always be specified, as is done in runs 2, 5, 6 and 7. It prevents wgtcellcollapse from picking up rules that may have skipped categories in them. In other words, it ensures that the collapsed cells are contiguous.

The resulting cells satisfy the sample size requirements of at least 20 cases per cell:

```
. bysort dpston5: assert _N >= 20
. bysort dpstoff5: assert _N >= 20
```

5.1 Pipeline to raking

As its output, wgtcellcollapse produced two files, one for each weighting margin, called dpston.do and dpstoff.do. An interested reader is welcome to type them; they contain long sequences of replace commands to perform the cell collapsing. These do-files are intended to be run on both the sample and the population data to create identical collapsed categories and produce consistent matrices of the population control totals for ipfraking.

```
. use trip_population, clear
. run dpston5.do
. total num_pass , over(dpston5)
Total estimation
                                   Number of obs
                                                              719
      1000001: dpston5 = 1000001
      1000002: dpston5 = 1000002
  (output omitted)
      5000011: dpston5 = 5000011
      5026268: dpston5 = 5026268
      5030108: dpston5 = 5030108
      5051836: dpston5 = 5051836
      5093960: dpston5 = 5093960
        Over
                     Total
                             Std. Err.
                                            [95% Conf. Interval]
num_pass
     1000001
                      1423
                             967.7508
                                           -476.9595
                                                        3322.959
     1000002
                                           -2414.011
                                                        16810.01
                      7198
                              4895.91
  (output omitted)
     5000011
                      1270
                              834.301
                                            -367.961
                                                        2907.961
     5026268
                       557
                             364.4324
                                           -158.4805
                                                        1272.481
```

```
5030108
                       263.2061
                                                  1126.746
                 610
                                     93.25444
                                                 1045.225
5051836
                 622
                       215.5712
                                     198.7749
5093960
                 473
                       261.8954
                                    -41.17225
                                                 987.1723
```

- . matrix dpston5 = e(b)
- . matrix coleq dpston5 = _one
- . matrix rownames dpston5 = dpston5
- . run dpstoff5.do
- . total num_pass , over(dpstoff5)

719 Total estimation Number of obs =

1000018: dpstoff5 = 1000018 1000030: dpstoff5 = 1000030

(output omitted)

5000069: dpstoff5 = 5000069 5094468: dpstoff5 = 50944685110140: dpstoff5 = 5110140

Over	Total	Std. Err.	[95% Conf. In	nterval]
num_pass				
1000018	929	360.7303	220.7878	1637.212
1000030	2189	868.0319	484.8161	3893.184
(output omit	ted)			
5000069	2677	895.7917	918.316	1435.684
5094468	432	87.57763	260.0612	303.9388
5110140	423	120.0254	187.3574	558.6426

- . matrix dpstoff5 = e(b)
- . matrix coleq dpstoff5 = _one
- . matrix rownames dpstoff5 = dpstoff5
- . use trip_sample_rules, clear
- . run dpston5
- . run dpstoff5
- . gen byte _one = 1
- . ipfraking [pw=_one], ctotal(dpston5 dpstoff5) gen(raked_weight5)

Iteration 1, max rel difference of raked weights = 37.856256

Iteration 2, max rel difference of raked weights = .06404821

Iteration 3, max rel difference of raked weights = .00891802

Iteration 4, max rel difference of raked weights = .00128619

Iteration 5, max rel difference of raked weights = .00018966

Iteration 6, max rel difference of raked weights = .00002818

Iteration 7, max rel difference of raked weights = 4.198e-06

Iteration 8, max rel difference of raked weights = 6.257e-07The worst relative discrepancy of 7.8e-08 is observed for dpstoff5 == 5110140

423; achieved value = Target value =

Summary of the weight changes

	Mean	Std. dev.	Min	Max	CV
Orig weights	1	0	1	1	0
Raked weights	26.487	5.754	13.174	38.634	.2172
Adjust factor	26.4869		13.1743	38.6339	

. whatsdeff raked_weight5

Group	Min	Mean	Max	CV	DEFF	N	N eff
Overall	13.17	26.49	38.63	0.2172	1.0472	3654	3489.37

5.2 Informative labels

Once the collapsing rules are finalized, several types of category labels can be attached to the resulting collapsed cells. Using the mechanics of labels in multiple languages (see [R] label language), wgtcellcollapse label defines three "languages" to describe the cells. The language numbered_ccells may be convenient for debugging purposes in fine-tuning the collapsing algorithms, while the language texted_ccells would prove useful for ipfraking_report in creating human-readable labels. (In Stata SMCL output, the label language instructions are clickable, so the user does not have to copy and paste the command, but can click it instead.)

```
. wgtcellcollapse label, var(dpston5)
(language default renamed unlabeled_ccells)
(language numbered_ccells now current language)
(language texted_ccells now current language)
To attach the numeric labels (of the kind "dpston5==1000001"), type:
   label language numbered_ccells
To attach the text labels (of the kind "dpston5==AM Peak; 1. Alewife"), type:
  label language texted_ccells
The original state, which is also the current state, is:
   label language unlabeled_ccells
. wgtcellcollapse label, var(dpstoff5)
To attach the numeric labels (of the kind "dpstoff5==1000018"), type:
   label language numbered_ccells
To attach the text labels (of the kind "dpstoff5==AM Peak; 18. East End"), type:
  label language texted_ccells
The original state, which is also the current state, is:
   label language unlabeled_ccells
. label language numbered_ccells
. tab dpstoff5 if daypart==5
```

Long ID of the interaction	Freq.	Percent	Cum.
daypart==5, alight_id==69 daypart==5, alight_id==94468 daypart==5, alight_id==110140	123 27 23	71.10 15.61 13.29	71.10 86.71 100.00
Total	173	100.00	

- . label language texted_ccells
- . tab dpstoff5 if daypart==5

	Long ID of the interaction	Freq.	Percent	Cum.
•	Weekend; 69. Union Station Limerick to 68. Toledo Tow Alewife to 40. King Street	123 27 23	71.10 15.61 13.29	71.10 86.71 100.00
	Total	173	100.00	

. label language $unlabeled_ccells$

. tab dpstoii	15 11	daypart	==5	
Interaction				
s of				
daypart				
alight_id,				
with some				
collapsing		Freq.	Percent	Cum.
5000069		123	71.10	71.10
5094468		27	15.61	86.71
5110140		23	13.29	100.00
Total		173	100.00	

6 Linear calibrated weights

r; t=2.16 14:59:24

tab dnataffE if dammant---

Using the final set of collapsed categories in the simulated transportation data example, let us demonstrate the linear calibration option of **ipfraking**, added since Kolenikov (2014). In mathematical terms, linear weights explicitly solve the minimization problem of finding a set of weights $\{w_{li}, i = 1, ..., n\}$, where the subscript l stands for linear calibration, such that

$$\sum_{i=1}^{n} \frac{(w_{li} - w_{di})^2}{w_{di}} \to \min$$
 (6)

Deville and Särndal (1992) and Särndal et al. (1992) provide explicit treatment of the problem and the resulting analytical expressions coded in ipfraking, linear. The main advantage of linear weight calibration is a much faster computing time. To demonstrate it, we will time the output by using the immediate timing results, set rmsg on (see [R] set).

```
. set rmsg on
r; t=0.00 14:59:22
. ipfraking [pw=_one], ctotal(dpston5 dpstoff5) nograph gen(raked_weight5)
 Iteration 1, max rel difference of raked weights = 37.856256
 Iteration 2, max rel difference of raked weights = .06404821
 Iteration 3, max rel difference of raked weights = .00891802
 Iteration 4, max rel difference of raked weights = .00128619
 Iteration 5, max rel difference of raked weights = .00018966
 Iteration 6, max rel difference of raked weights = .00002818
 Iteration 7, max rel difference of raked weights = 4.198e-06
 Iteration 8, max rel difference of raked weights = 6.257e-07
The worst relative discrepancy of 7.8e-08 is observed for dpstoff5 == 5110140
Target value =
                      423; achieved value =
                                                    423
   Summary of the weight changes
                                                               {\tt CV}
                   Mean
                           Std. dev.
                                         Min
                                                    Max
Orig weights
                       1
                                   0
                                             1
                                                         1
                                                                 0
Raked weights
                  26.487
                               5.754
                                        13.174
                                                    38.634
                                                              .2172
Adjust factor
                 26.4869
                                       13,1743
                                                   38.6339
```

. ipfraking [pw=_one], ctotal(dpston5 dpstoff5) nograph gen(raked_weight51) linear Linear calibration

The worst relative discrepancy of 1.8e-14 is observed for dpstoff5 == 5110140 Target value = 423; achieved value = 423

Summary of the weight changes

	Mean	Std. dev.	Min	Max	CA
Orig weights	1	0	1	1	0
Raked weights	26.487	5.7523	12.518	38.204	.2172
Adjust factor	26.4869		12.5178	38.2040	
r; t=0.63 14:59	9:25				

- . set rmsg off
- . label variable raked_weight51 "Linear calibrated weights"
- . compare raked_weight5 raked_weight51

	count	minimum	difference average	maximum
raked_w~5 <raked_~51 raked_w~5="">raked_~51</raked_~51>	1896 1758	-1.813144 2.18e-09	0476911 .0514348	-3.11e-11 2.405758
jointly defined	3654	-1.813144	3.21e-10	2.405758
total	3654			

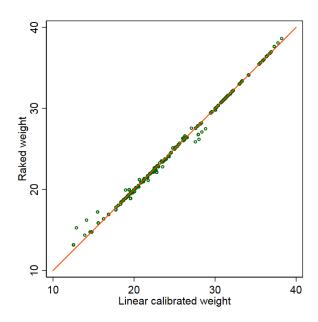


Figure 1: Linear and raked weights

The speed advantages of linear calibration are quite clear (0.63 seconds vs. 2.16 seconds), even though raking convergence in 8 iterations is quite fast, in author's experience. It is not unusual to see dozens iterations, and when higher order interactions are being used as raking margins, subtle correlations between the cells arise, slowing down convergence and requiring hundreds of iterations. Linear calibrated and raked weights are very similar to one another, as Figure 1 demonstrates, albeit the lowest of the linearly calibrated weights are slightly smaller than comparable raked weights. The weights produced by linear and raking calibration methods should be expected to agree in general, but the match along the diagonal line of the plot should not be expected to be ideal.

As mentioned before, in the extreme situations, linearly calibrated weights may become negative, which creates additional issues. First, Stata's svy commands or estimation commands with pweight specifications do not accept negative weights, and produce error messages when such weights are encountered. (This is not a bug, but indeed a welcome behavior.) Second, negative weights are typically difficult to interpret; within a common, although not technically accurate, interpretation of sampling weights as the number of population units that a sampled unit represents, it is puzzling to find a negative number of such population units. The way the author uses the linear calibration functionality of ipfraking is to produce "preliminary" sets of weights. If the weights at the low end satisfy the natural range restriction (greater than 0, so as not to produce input data check errors with estimation commands; or sometimes greater than 1, so as to satisfy the "number of population units" interpretation that is often desirable), these weights can be "accepted" as final. If they do not, ipfraking can be called with trimming syntax such as trimloabs(1). The linear weights can then be used as a starting point to accelerate convergence using from() option of ipfraking.

While the general theory of calibrated estimation (Deville and Särndal 1992) ensures that linear calibrated weights (analyzed as Case 1 in that paper) and raked weights (Case 2) are asymptotically equivalent, this equivalence implicitly requires that the scales of the population control matrices are identical. In practice, different control total variables may come from different sources, and some sources may have either different populations to which they can technically be generalized, or come at different scales such as proportions vs. population totals. Nearly every dual frame random digit dialing survey of the general U.S. population that the present author had dealt with would use the American Community Survey data for demographic variables (that would come with the desirable population scaling), and National Health Interview Survey data for phone use variables (cell phone only, landline only, both, or none) that would come in the form of proportions. While the raking version of ipfraking would not have any difficulty incorporating both (with the caveat that the final scale of weights will be determined by the *last* variable in the ctotal() list), the linear version of weights would try to find a middle point between the population totals that are on the scale of millions, and proportions that are on the scale of about 1. The results would likely be quite strange.

7 Other packages with similar functionality

There is a number of other packages that provide similar basic functionality (i.e., raked weights, with or without trimming). Kolenikov (2014) provided comparisons with survwgt (Winter 2002), ipfweight (Bergmann 2011), maxentropy (Wittenberg 2010), and reported that the weights produced by these packages were identical within numeric accuracy.

Yet another weight calibration package that was published simultaneously with Kolenikov (2014) was sreweight (Pacifico 2014). It implements a full range of objective functions from Deville and Särndal (1992), and does so faster than ipfraking as the core iterative functionality is implemented in Mata. Finally, Stata 15.1 now provides svycal command, undocumented at the time of the writing of this paper, although described and exemplified in detail in Valliant and Dever (2017). Compared to svycal, the core functionality of ipfraking provides a richer set of trimming specifications. The author compared the weights produced by ipfraking with those produced by sreweight and svycal in the case of basic raking procedure without trimming, and they agree within numeric accuracy:

. compare rakedwgt2 rakedwgt2a

	count	minimum	difference average	maximum
rakedwgt2 <rakedw~2a rakedwgt2>rakedw~2a</rakedw~2a 	6843 3508	0057653 1.56e-07	0001227 .0002394	-3.27e-06 .0038718
jointly defined	10351	0057653	1.70e-13	.0038718
total	10351			

. assert reldif(rakedwgt2, rakedwgt2a) < c(epsfloat)</pre>

Weights produced by ipfraking also agree with those produced by R package survey (Lumley 2010, 2018), namely survey::calibrate(...,calfun="raking") function, and those produced by SAS raking macro RAKE_AND_TRIM() (Izrael et al. 2017). When trimming options are specified, the results from different packages diverge, as trimming operations appear to be implemented differently in each package.

It is somewhat unfortunate that so much effort has gone into replicating the functionality by the different authors. The primary distinction of the current **ipfraking** package is the rich ecosystem that goes along with it, aimed, in its totality, at producing survey weights by a survey organization in a way that is efficient, robust and flexible from coding perspective.

As a practicing survey statistician who needs to experiment with the weights a lot, the present author believes that ipfraking is easier to experiment with than svycal or sreweight, for several reasons. First, ipfraking relies on the control totals being

carried over from svy: total with minimal modifications such as renaming row and column names; passing control totals is more cumbersome with other packages. Second, ipfraking produces detailed diagnostics of problems and oddities it encounters along the way, assisting the survey statistician in assessing whether the resulting weights are satisfactory.

For relatively simpler tasks of producing replicate weights and calibrating them at the same time, **survwgt** provides a much easier syntax. Coding the task with **ipfraking** or any other package would require explicit cycles.

From code development perspective, the present author believes that relying on matching the order of control totals and variables, as required by all other user-contributed packages, creates a potential for errors that are easy to make and difficult to catch. If you supplied 20 control totals and 19 variables, at which position in the list should the 20th missing variable be?? With either ipfraking and the official svycal, the risk that a control total figure would be associated with a wrong category of the control total variable is much lower, as they pair the values and the categories in a single object (via the names attached to the control total matrices) or explicit syntax value.variable = # specification of svycal. (The matrix naming is different between ipfraking and svycal, though, so a conversion tool, totalmatrices, is provided in this update.)

Additionally, ipfraking can incorporate variables that sum up to different totals, e.g., totals from different sources or from different years, or totals and proportions, in case unified data are not available, with the side effect of producing weights whose totals agree with the *last* control total variable. Without trimming, doing so ensures that *proportions* for each calibration variables are satisfied. As maxentropy, sreweight and svycal produce weights by optimization, with the goal of satisfying all totals simultaneously, it is unclear what the properties of the resulting weight would be when the control totals differ between variables, and whether the resulting weights would produce marginal proportions that agree between the control totals and calibrated weights.

Compared to ipfraking, the official svycal command handles interactions far more graciously, and consistently with the Stata user experience of using factor variables in regression models (see [U] Factor variables). It creates the necessary interactions internally on the fly, while ipfraking requires explicit generation of interaction variables.

Finally, of all the Stata weight calibration packages, ipfraking is unique in offering the possibility of using multipliers other than 0 and 1 (i.e., category dummies).

In the end of the day, the choice of the package is a matter of personal preference, package familiarity, and coding style.

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are of the author only, and do not represent the position of Abt Associates.

8 References

- AAPOR. 2014. AAPOR Terms and Conditions for Transparency Certification. The American Association for Public Opinion Research. Available at http://www.aapor.org/AAPOR_Main/media/MainSiteFiles/TI-Terms-and-Conditions-10-4-17.pdf.
- Andridge, R. R., and R. J. Little. 2010. A Review of Hot Deck Imputation for Survey Non-response. *International statistical review* 78(1): 40–64.
- Bergmann, M. 2011. IPFWEIGHT: Stata module to create adjustment weights for surveys. Statistical Software Components, Boston College Department of Economics. RePEc:boc:bocode:s457353.
- Binder, D. A., and G. R. Roberts. 2003. Design-based and Model-based Methods for Estimating Model Parameters. In *Analysis of Survey Data*, ed. R. L. Chambers and C. J. Skinner, chap. 3. New York: John Wiley & Sons.
- Deville, J. C., and C. E. Särndal. 1992. Calibration Estimators in Survey Sampling. Journal of the American Statistical Association 87(418): 376–382.
- Deville, J. C., C. E. Särndal, and O. Sautory. 1993. Generalized Raking Procedures in Survey Sampling. *Journal of the American Statistical Association* 88(423): 1013–1020.
- Gould, W. 2003. Stata tip 3: How to be assertive. Stata Journal 3(4).
- Groves, R. M., D. A. Dillman, J. L. Eltinge, and R. J. A. Little. 2001. Survey Nonresponse. Wiley Series in Survey Methodology, Wiley-Interscience.
- Holt, D., and T. M. F. Smith. 1979. Post Stratification. Journal of the Royal Statistical Society, Series A 142(1): 33–46.
- Horvitz, D. G., and D. J. Thompson. 1952. A Generalization of Sampling Without Replacement From a Finite Universe. *Journal of the American Statistical Association* 47(260): 663–685.
- Izrael, D., M. P. Battaglia, A. A. Battaglia, and S. W. Ball. 2017. You Do Not Have To Step On The Same Rake: SAS Raking Macro—Generation IV. In SAS Global Forum. Available at https://support.sas.com/resources/papers/proceedings17/0470-2017-poster.pdf.
- Kolenikov, S. 2010. Resampling inference with complex survey data. The Stata Journal 10: 165–199.
- ——. 2014. Calibrating survey data using iterative proportional fitting. The Stata Journal 14(1): 22–59.

- ______. 2016. Post-stratification or non-response adjustment? Survey Practice 9(3). Available at http://www.surveypractice.org/index.php/SurveyPractice/article/view/315.
- Kolenikov, S., and H. Hammer. 2015. Simultaneous Raking of Survey Weights at Multiple Levels. Survey Methods: Insights from the Field Special issue on Weighting: Practical Issues and How to Approach. Retrieved from https://surveyinsights.org/?p=5099.
- Korn, E. L., and B. I. Graubard. 1995. Analysis of Large Health Surveys: Accounting for the Sampling Design. *Journal of the Royal Statistical Society, Series A* 158(2): 263–295.
- ———. 1999. Analysis of Health Surveys. John Wiley and Sons.
- Kott, P. S. 2006. Using Calibration Weighting to Adjust for Nonresponse and Coverage Errors. Survey Methodology 32(2): 133–142.
- ———. 2009. Calibration Weighting: Combining Probability Samples and Linear Prediction Models. In Sample Surveys: Inference and Analysis, ed. D. Pfeffermann and C. R. Rao, vol. 29B of Handbook of Statistics, chap. 25. Oxford, UK: Elsevier.
- Lumley, T. S. 2010. Complex Surveys: A Guide to Analysis Using R (Wiley Series in Survey Methodology). New York: Wiley.
- ——. 2018. Package 'survey', v. 3.34. Available at http://r-survey.r-forge.r-project.org/survey/.
- Pacifico, D. 2014. sreweight: A Stata command to reweight survey data to external totals. The Stata Journal 14(1): 4–21.
- Park, D. K., A. Gelman, and J. Bafumi. 2004. Bayesian Multilevel Estimation with Post-stratification: State-Level Estimates from National Polls. *Political Analysis* 12(4): 375–385.
- Pew Research Center. 2012. Assessing the Representativeness of Public Opinion Surveys. Technical report, Pew Research Center for People and Press. Available at http://www.people-press.org/files/legacy-pdf/Assessing the Representativeness of Public Opinion Surveys.pdf.
- Pfeffermann, D. 1993. The role of sampling weights when modeling survey data. *International Statistical Review* 61: 317–337.
- Rubin, D. B. 1976. Inference and missing data. Biometrika 63(3): 581–592.
- Särndal, C.-E. 2007. The calibration approach in survey theory and practice. Survey Methodology 33(2): 99–119.
- Särndal, C.-E., B. Swensson, and J. Wretman. 1992. *Model Assisted Survey Sampling*. New York: Springer.

Thompson, M. E. 1997. Theory of Sample Surveys, vol. 74 of Monographs on Statistics and Applied Probability. New York: Chapman & Hall/CRC.

- Valliant, R., and J. Dever. 2017. Survey Weights: A Step-by-step Guide to Calculation. College Station, TX: Stata Press.
- Winter, N. 2002. SURVWGT: Stata module to create and manipulate survey weights. Statistical Software Components, Boston College Department of Economics. RePEc:boc:bocode:s427503.
- Wittenberg, M. 2010. An introduction to maximum entropy and minimum cross-entropy estimation using Stata. *Stata Journal* 10(3): 315–330.

About the author

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