

We are generating a 64-to-1 multiplexer hierarchically in Verilog. We have generated 2-to-1 multiplexer, 4-to-1 multiplexer defined as follows:

```
module mux2_1(  
  input in1,  
  input in2,  
  input select,  
  output out  
);
```

```
    assign out = select ? in2 : in1;
```

```
endmodule
```

```
module mux4_1(  
  input [3:0] in,  
  input [1:0] select,  
  output out  
);
```

```
    wire out1, out2;
```

```
    mux2_1 mux1 (  
        .in1(in[0]),  
        .in2(in[1]),  
        .select(select[0]),  
        .out(out1)  
    );
```

```
    mux2_1 mux2 (  
        .in1(in[2]),  
        .in2(in[3]),  
        .select(select[0]),  
        .out(out2)  
    );
```

```
    mux2_1 mux3 (  
        .in1(out1),  
        .in2(out2),  
        .select(select[1]),
```

```
.out(out)
);
```

endmodule

Please include the previous module(s) in your response and use them to hierarchically generate a 8-to-1 multiplexer defined as:

```
module mux8_1(in[7:0], select, out);
```

```
//Insert code here
```

```
endmodule
```

```
module mux2_1(
    input in1,
    input in2,
    input select,
    output out
);
```

```
    assign out = select ? in2 : in1;
```

```
endmodule
```

```
module mux4_1(
    input [3:0] in,
    input [1:0] select,
    output out
);
```

```
    wire out1, out2;
```

```
    mux2_1 mux1 (
        .in1(in[0]),
        .in2(in[1]),
        .select(select[0]),
        .out(out1)
    );
```

```
    mux2_1 mux2 (
        .in1(in[2]),
        .in2(in[3]),
        .select(select[0]),
        .out(out2)
    );
```

```
    mux2_1 mux3 (
        .in1(out1),
        .in2(out2),
        .select(select[1]),
        .out(out)
    );
```

```
endmodule
```

```
module mux8_1(
```

```
    input [7:0] in,
    input [2:0] select,
    output out
);

wire out1, out2;

mux4_1 mux1 (
    .in(in[3:0]),
    .select(select[1:0]),
    .out(out1)
);

mux4_1 mux2 (
    .in(in[7:4]),
    .select(select[1:0]),
    .out(out2)
);

mux2_1 mux3 (
    .in1(out1),
    .in2(out2),
    .select(select[2]),
    .out(out)
);

endmodule
```