

**We are generating a 64-to-1 multiplexer hierarchically in Verilog. We have generated 2-to-1 multiplexer, 4-to-1 multiplexer, 8-to-1 multiplexer, 16-to-1 multiplexer defined as follows:**

```
module mux2_1(  
  input in1,  
  input in2,  
  input select,  
  output out  
);
```

```
  assign out = select ? in2 : in1;
```

```
endmodule
```

```
module mux4_1(  
  input [3:0] in,  
  input [1:0] select,  
  output out  
);
```

```
  wire out1, out2;
```

```
  mux2_1 mux1 (  
    .in1(in[0]),  
    .in2(in[1]),  
    .select(select[0]),  
    .out(out1)  
  );
```

```
  mux2_1 mux2 (  
    .in1(in[2]),  
    .in2(in[3]),  
    .select(select[0]),  
    .out(out2)  
  );
```

```
  mux2_1 mux3 (  
    .in1(out1),  
    .in2(out2),  
    .select(select[1]),
```

```
        .out(out)
    );
```

endmodule

```
module mux8_1(
input [7:0] in,
input [2:0] select,
output out
);
```

```
    wire out1, out2;

    mux4_1 mux1 (
        .in(in[3:0]),
        .select(select[1:0]),
        .out(out1)
    );

    mux4_1 mux2 (
        .in(in[7:4]),
        .select(select[1:0]),
        .out(out2)
    );

    mux2_1 mux3 (
        .in1(out1),
        .in2(out2),
        .select(select[2]),
        .out(out)
    );
```

endmodule

```
module mux16_1(
input [15:0] in,
input [3:0] select,
output out
);
```

```
    wire out1, out2;

    mux8_1 mux1 (
        .in(in[7:0]),
        .select(select[2:0]),
        .out(out1)
    );

    mux8_1 mux2 (
        .in(in[15:8]),
        .select(select[2:0]),
        .out(out2)
```

```
);

mux2_1 mux3 (
    .in1(out1),
    .in2(out2),
    .select(select[3]),
    .out(out)
);
```

endmodule

Please include the previous module(s) in your response and use them to hierarchically generate a 32-to-1 multiplexer defined as:

```
module mux32_1(in[31:0], select, out);
//Insert code here
endmodule
```

```
module mux2_1(
    input in1,
    input in2,
    input select,
    output out
);

    assign out = select ? in2 : in1;

endmodule

module mux4_1(
    input [3:0] in,
    input [1:0] select,
    output out
);

    wire out1, out2;

    mux2_1 mux1 (
        .in1(in[0]),
        .in2(in[1]),
        .select(select[0]),
        .out(out1)
    );

    mux2_1 mux2 (
        .in1(in[2]),
        .in2(in[3]),
        .select(select[0]),
        .out(out2)
    );

    mux2_1 mux3 (
        .in1(out1),
        .in2(out2),
        .select(select[1]),
```

```

        .out(out)
    );

endmodule

module mux8_1(
    input [7:0] in,
    input [2:0] select,
    output out
);

    wire out1, out2;

    mux4_1 mux1 (
        .in(in[3:0]),
        .select(select[1:0]),
        .out(out1)
    );

    mux4_1 mux2 (
        .in(in[7:4]),
        .select(select[1:0]),
        .out(out2)
    );

    mux2_1 mux3 (
        .in1(out1),
        .in2(out2),
        .select(select[2]),
        .out(out)
    );

endmodule

module mux16_1(
    input [15:0] in,
    input [3:0] select,
    output out
);

    wire out1, out2;

    mux8_1 mux1 (
        .in(in[7:0]),
        .select(select[2:0]),
        .out(out1)
    );

    mux8_1 mux2 (
        .in(in[15:8]),
        .select(select[2:0]),
        .out(out2)
    );

    mux2_1 mux3 (
        .in1(out1),

```

```

        .in2(out2),
        .select(select[3]),
        .out(out)
    );

endmodule

module mux32_1(
    input [31:0] in,
    input [4:0] select,
    output out
);

    wire out1, out2;

    mux16_1 mux1 (
        .in(in[15:0]),
        .select(select[3:0]),
        .out(out1)
    );

    mux16_1 mux2 (
        .in(in[31:16]),
        .select(select[3:0]),
        .out(out2)
    );

    mux2_1 mux3 (
        .in1(out1),
        .in2(out2),
        .select(select[4]),
        .out(out)
    );

endmodule

```