

	Formula	Exemplul
1.	$(u^n)' = n \cdot u^{n-1} \cdot u'$	$((\sin x)^5)' = 5 \cdot (\sin x)^4 \cdot (\sin x)' = 5 \cdot (\sin x)^4 \cdot \cos x$
2.	$(u^2)' = 2 \cdot u \cdot u'$	$(\ln^2 x)' = 2 \cdot \ln x \cdot (\ln x)' = 2 \cdot \ln x \cdot \frac{1}{x} = \frac{2 \ln x}{x}$
3.	$\left(\frac{1}{u}\right)' = -\frac{1}{u^2} \cdot u'$	$\left(\frac{1}{x^2 + 1}\right)' = -\frac{1}{(x^2 + 1)^2} \cdot (x^2 + 1)' = -\frac{2x}{(x^2 + 1)^2}$
4.	$(\sqrt{u})' = \frac{1}{2\sqrt{u}} \cdot u'$	$(\sqrt{x^2 + a^2})' = \frac{1}{2\sqrt{x^2 + a^2}} \cdot (x^2 + a^2)' = \frac{x}{\sqrt{x^2 + a^2}}$
5.	$(\sqrt[n]{u})' = \frac{1}{n \cdot \sqrt[n]{u^{n-1}}} \cdot u'$	$(\sqrt[5]{2x-3})' = \frac{1}{5 \cdot \sqrt[5]{(2x-3)^4}} \cdot (2x-3)' = \frac{2}{5 \cdot \sqrt[5]{(2x-3)^4}}$
6.	$(e^u)' = e^u \cdot u'$	$(e^{\arctg x})' = e^{\arctg x} \cdot (\arctg x)' = e^{\arctg x} \cdot \frac{1}{x^2 + 1}$
7.	$(a^u)' = a^u \cdot \ln a \cdot u'$	$(3^{\sqrt{x}})' = 3^{\sqrt{x}} \cdot \ln 3 \cdot (\sqrt{x})' = 3^{\sqrt{x}} \cdot \ln 3 \cdot \frac{1}{2\sqrt{x}}$
8.	$(\ln u)' = \frac{1}{u} \cdot u'$	$(\ln(\ln x))' = \frac{1}{\ln x} \cdot (\ln x)' = \frac{1}{\ln x} \cdot \frac{1}{x} = \frac{1}{x \ln x}$
9.	$(\log_a u)' = \frac{1}{u \cdot \ln a} \cdot u'$	$(\log_2(x^2 - x))' = \frac{1}{(x^2 - x) \cdot \ln 2} \cdot (x^2 - x)' = \frac{2x - 1}{\ln 2 \cdot (x^2 - x)}$
10.	$(\sin u)' = \cos u \cdot u'$	$(\sin e^x)' = \cos e^x \cdot (e^x)' = e^x \cdot \cos e^x$
11.	$(\cos u)' = -\sin u \cdot u'$	$(\cos(\sin x))' = -\sin(\sin x) \cdot (\sin x)' = -\sin(\sin x) \cdot \cos x$
12.	$(\operatorname{tg} u)' = \frac{1}{\cos^2 u} \cdot u'$	$(\operatorname{tg}(x^2 + 1))' = \frac{1}{\cos^2(x^2 + 1)} \cdot (x^2 + 1)' = \frac{2x}{\cos^2(x^2 + 1)}$
13.	$(\operatorname{ctg} u)' = -\frac{1}{\sin^2 u} \cdot u'$	$(\operatorname{ctg} \sqrt{x})' = -\frac{1}{\sin^2 \sqrt{x}} \cdot (\sqrt{x})' = -\frac{1}{\sin^2 \sqrt{x}} \cdot \frac{1}{2\sqrt{x}}$
14.	$(\arcsin u)' = \frac{1}{\sqrt{1 - u^2}} \cdot u'$	$(\arcsin x^2)' = \frac{1}{\sqrt{1 - (x^2)^2}} \cdot (x^2)' = \frac{2x}{\sqrt{1 - x^4}}$
15.	$(\arctg u)' = \frac{1}{u^2 + 1} \cdot u'$	$(\arctg(x + 1))' = \frac{1}{(x + 1)^2 + 1} \cdot (x + 1)' = \frac{1}{(x + 1)^2 + 1}$
16.	$(\arccos u)' = -\frac{1}{\sqrt{1 - u^2}} \cdot u'$	$(\arccos e^x)' = -\frac{1}{\sqrt{1 - (e^x)^2}} \cdot (e^x)' = -\frac{e^x}{\sqrt{1 - e^{2x}}}$
17.	$(\operatorname{arcctg} u)' = -\frac{1}{u^2 + 1} \cdot u'$	$(\operatorname{arcctg} x^3)' = -\frac{1}{(x^3)^2 + 1} \cdot (x^3)' = -\frac{3x^2}{x^6 + 1}$

Integrale nedefinite

1	$\int 1 \, dx = \int dx = x + \mathcal{C}$	
2	$\int x^n \, dx = \frac{x^{n+1}}{n+1} + \mathcal{C}$	$\int u^n(x) \cdot u'(x) \, dx = \frac{u^{n+1}(x)}{n+1} + \mathcal{C}$
3	$\int e^x \, dx = e^x + \mathcal{C}$	$\int e^{u(x)} \cdot u'(x) \, dx = e^{u(x)} + \mathcal{C}$
4	$\int a^x \, dx = \frac{a^x}{\ln a} + \mathcal{C}$	$\int a^{u(x)} \cdot u'(x) \, dx = \frac{a^{u(x)}}{\ln a} + \mathcal{C}$
5	$\int \frac{1}{x} \, dx = \ln x + \mathcal{C}$	$\int \frac{1}{u(x)} \cdot u'(x) \, dx = \ln u(x) + \mathcal{C}$
6	$\int \frac{1}{x^2 - a^2} \, dx = \frac{1}{2a} \ln \left \frac{x-a}{x+a} \right + \mathcal{C}$	$\int \frac{1}{u^2(x) - a^2} \cdot u'(x) \, dx = \frac{1}{2a} \ln \left \frac{u(x)-a}{u(x)+a} \right + \mathcal{C}$
7	$\int \frac{1}{x^2 + a^2} \, dx = \frac{1}{a} \operatorname{arctg} \frac{x}{a} + \mathcal{C}$	$\int \frac{1}{u^2(x) + a^2} \cdot u'(x) \, dx = \frac{1}{a} \operatorname{arctg} \frac{u(x)}{a} + \mathcal{C}$
8	$\int \frac{1}{\sqrt{x^2 - a^2}} \, dx = \ln \left x + \sqrt{x^2 - a^2} \right + \mathcal{C}$	$\int \frac{1}{\sqrt{u^2(x) - a^2}} \cdot u'(x) \, dx = \ln \left u(x) + \sqrt{u^2(x) - a^2} \right + \mathcal{C}$
9	$\int \frac{1}{\sqrt{x^2 + a^2}} \, dx = \ln \left(x + \sqrt{x^2 + a^2} \right) + \mathcal{C}$	$\int \frac{1}{\sqrt{u^2(x) + a^2}} \cdot u'(x) \, dx = \ln \left(u(x) + \sqrt{u^2(x) + a^2} \right) + \mathcal{C}$
10	$\int \frac{1}{\sqrt{a^2 - x^2}} \, dx = \arcsin \frac{x}{a} + \mathcal{C}$	$\int \frac{1}{\sqrt{a^2 - u^2(x)}} \cdot u'(x) \, dx = \arcsin \frac{u(x)}{a} + \mathcal{C}$
11	$\int \sin x \, dx = -\cos x + \mathcal{C}$	$\int \sin u(x) \cdot u'(x) \, dx = -\cos u(x) + \mathcal{C}$
12	$\int \cos x \, dx = \sin x + \mathcal{C}$	$\int \cos u(x) \cdot u'(x) \, dx = \sin u(x) + \mathcal{C}$
13	$\int \operatorname{tg} x \, dx = -\ln \cos x + \mathcal{C}$	$\int \operatorname{tg} u(x) \cdot u'(x) \, dx = -\ln \cos u(x) + \mathcal{C}$
14	$\int \operatorname{ctg} x \, dx = \ln \sin x + \mathcal{C}$	$\int \operatorname{ctg} u(x) \cdot u'(x) \, dx = \ln \sin u(x) + \mathcal{C}$
15	$\int \frac{1}{\sin^2 x} \, dx = -\operatorname{ctg} x + \mathcal{C}$	$\int \frac{1}{\sin^2 u(x)} \cdot u'(x) \, dx = -\operatorname{ctg} u(x) + \mathcal{C}$
16	$\int \frac{1}{\cos^2 x} \, dx = \operatorname{tg} x + \mathcal{C}$	$\int \frac{1}{\cos^2 u(x)} \cdot u'(x) \, dx = \operatorname{tg} u(x) + \mathcal{C}$

Proprietăți ale funcțiilor trigonometrice	
Mărginirea	
$-1 \leq \sin x \leq 1, \forall x \in \mathbb{R}$	$-1 \leq \cos x \leq 1, \forall x \in \mathbb{R}$
Paritatea	
$\sin(-x) = -\sin x$	$\operatorname{tg}(-x) = -\operatorname{tg} x$
$\cos(-x) = \cos x$	$\operatorname{ctg}(-x) = -\operatorname{ctg} x$
<i>Observație! cos este funcției pară, sin, tg, ctg funcții impare</i>	
Periodicitatea	
$\sin(x + 2k\pi) = \sin x, \forall x \in \mathbb{R}, k \in \mathbb{Z}$	$\operatorname{tg}(x + k\pi) = \operatorname{tg} x, \forall x \in \mathbb{R} \setminus \left(\frac{\pi}{2} + \mathbb{Z}\pi\right), k \in \mathbb{Z}$
$\cos(x + 2k\pi) = \cos x, \forall x \in \mathbb{R}, k \in \mathbb{Z}$	$\operatorname{ctg}(x + k\pi) = \operatorname{ctg} x, \forall x \in \mathbb{R} \setminus (\mathbb{Z}\pi), k \in \mathbb{Z}$

Formule trigonometrice	
Formula fundamentală a trigonometriei	
$\sin^2 x + \cos^2 x = 1, \forall x \in \mathbb{R}$	
$\sin(90^\circ - x) = \cos x$	$\sin(180^\circ - x) = \sin x$
$\cos(90^\circ - x) = \sin x$	$\cos(180^\circ - x) = -\cos x$
$\sin(a + b) = \sin a \cos b + \cos a \sin b$	$\sin(a - b) = \sin a \cos b - \cos a \sin b$
$\cos(a + b) = \cos a \cos b - \sin a \sin b$	$\cos(a - b) = \cos a \cos b + \sin a \sin b$
$\sin 2x = 2 \sin x \cos x$	$\cos 2x = \cos^2 x - \sin^2 x$
$\cos 2x = 2 \cos^2 x - 1$	$\cos 2x = 1 - 2 \sin^2 x$
$\operatorname{tg} x = \frac{\sin x}{\cos x}$	$\operatorname{ctg} x = \frac{\cos x}{\sin x}$

$\operatorname{tg}(a + b) = \frac{\operatorname{tg} a + \operatorname{tg} b}{1 - \operatorname{tg} a \operatorname{tg} b}$	$\operatorname{tg}(a - b) = \frac{\operatorname{tg} a - \operatorname{tg} b}{1 + \operatorname{tg} a \operatorname{tg} b}$
$\operatorname{tg} 2x = \frac{2 \operatorname{tg} x}{1 - \operatorname{tg}^2 x}$	$\operatorname{tg} \frac{x}{2} = \frac{\sin x}{1 + \cos x}$
$\sin x = \frac{2 \operatorname{tg} \frac{x}{2}}{1 + \operatorname{tg}^2 \frac{x}{2}}$	$\cos x = \frac{1 - \operatorname{tg}^2 \frac{x}{2}}{1 + \operatorname{tg}^2 \frac{x}{2}}$
Transformarea unor sume în produs	
$\sin a + \sin b = 2 \sin \frac{a+b}{2} \cdot \cos \frac{a-b}{2}$	$\cos a + \cos b = 2 \cos \frac{a+b}{2} \cdot \cos \frac{a-b}{2}$
$\sin a - \sin b = 2 \sin \frac{a-b}{2} \cdot \cos \frac{a+b}{2}$	$\cos a - \cos b = -2 \sin \frac{a+b}{2} \cdot \sin \frac{a-b}{2}$

