

Prob of being defective = 0.05

Prob. of Being functional = 0.95

(a) exactly 20 bulb are defective

$$P(x=20) = {}^{500}C_{20} (0.05)^{20} \times (0.95)^{480}$$

using Binomial

$$P(x) = {}^nC_x p^x q^{n-x}$$

$$P(x=20) = 0.052$$

(b) at least 10 bulbs are defective

$$P(x \geq 10) = 1 - P(x < 10) = 1 - P(x \leq 9)$$

$$\therefore P(x \geq 10) = 1 - \frac{4.6 \times 10^{-4}}{\text{using calculator}}$$

$$P(x \geq 10) = 0.99$$

(c) at max 15 defective bulbs

$$P(x > 15) = 1 - P(x \leq 15)$$

$$= 1 - 0.0198$$

$$P(x > 15) = 0.98$$

(d) expected no. of defective bulb in Batch of 500.

$$\begin{aligned} \text{Expected no. of defective bulbs} &= n \times \text{Prob of being defective} \\ &= 500 \times 0.05 \end{aligned}$$

$$n_{\text{defective}} = 25$$