MCMC in DAOPHOT-II

Sean K. Terry sean.terry@berkeley.edu

This is a guide for use of the modified version of the subroutine NSTAR.F which implements a Markov chain Monte Carlo (MCMC) routine for fitting stellar positions and fluxes. This manual assumes a prior installation of the base version of DAOPHOT-II¹ (Stetson 1987). Descriptions of each major section of the MCMC routine are given with example outputs. This guide includes only specific instructions for running the MCMC version of NSTAR.F. For instructions using any other DAOPHOT-II module, refer to the DAOPHOT-II User's Manual (DII-UM) when appropriate. Lastly, please cite Terry et al. (2021) [https://iopscience.iop.org/article/10.3847/1538-3881/abcc60] if you find this code useful in your research.

https://www.star.bris.ac.uk/~mbt/daophot/

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1 Installation

Adding this modified routine to the DAOPHOT-II workflow should be straightforward:

- 1. Move the file nstar-mcmc.f into the DAOPHOT-II source code directory.
- 2. Open the Makefile and <u>replace</u> the two instances of "nstar.o" with "nstar-mcmc.o". This will allow the user to run the command **NSTAR-MCMC** from within DAOPHOT-II.
- 3. Run make daophot (or sudo make daophot) in the source code directory. This should only take a few seconds as only the nstar-mcmc.o executable will need to be built.

Note: If the user simply adds "nstar-mcmc.o" to the Makefile instead of replacing "nstar.o" with "nstar-mcmc.o", the error "duplicate symbol in:nstar.o nstar-mcmc.o" will likely occur.

Once again, these installation steps assume that the user has previously (successfully) installed the entire DAOPHOT-II software package. When using the software, both the NSTAR and NSTAR-MCMC commands will run the modified version, however the default scheme/output is preserved and saved as an output file (i.e. the *.nst) output star list).

2 A Typical Run of NSTAR-MCMC

Before running **NSTAR-MCMC**, the user will need to have already produced a co-added master frame and run the stock <code>DAOPHOT-II</code> pipeline on the image through the following steps:

- ATTACH (DII-UM pg. 12)
- FIND (DII-UM pg. 20)
- PHOT (DII-UM pg. 25)
- PICK (DII-UM pg. 29)
- PSF (DII-UM pg. 29)
- GROUP (DII-UM pg. 36)

The user will also need to manually remove all irrelevant groups of stars from the .grp file, so that only the header information and the 1, 2, or 3-star group of interest remains. Below is an example .grp file with one remaining group (the group of interest):

3 1463 1463 -71.4 9700.00 18.750 5.000 40.00	0 10 000 1
	00 12.333 1
241 896.550 822.590 15.305 24.990 450 890.490 823.160 15.995 25.550	
(1) (2) (3) (4) (5)	

- (1) Star ID number.
- (2) X coordinate of stellar centroid.
- (3) Y coordinate of stellar centroid.
- (4) Instrumental magnitude.
- (5) Estimated modal sky value for the star (from PHOT).

From inside the working directory, follow the steps:

- I Run daophot from terminal/console. There will need to be a valid daophot.opt file that exists in the directory in order to properly initiate daophot.
- II Run ATTACH. Attach the stacked image to be analyzed.
- III Run **NSTAR-MCMC**. The user will first be prompted to give the .psf and .grp files (which were generated earlier). The third prompt will ask the user for a filename for the output .nst file. This output is the default file that **NSTAR** produces using the Newton-Raphson method (see DII-UM pg. 38 and sample .nst output table given in DII-UM pg. 73).

- IV Next the console will ask for the file name for the **full** mcmc chain output. This output file will contain the values for every step in the parameter space search (i.e. number of rows in this output file will equal total number of mcmc iterations).
- V Next the console will ask for the file name for the **accepted** mcmc chain output. This output file will contain only the values accepted by the mcmc algorithm (i.e. parameter values that give lower χ^2 in the minimization routine).
- VI The next prompt will ask for the file name for the **CHISQ_PIXEL** output. This output file will give the best-fit χ^2 /pix for the fitting box, which is a useful metric for checking the χ^2 distribution across the pixels that are being fit by the PSF model via MCMC. Appendix B gives an example figure for which the total χ^2 and χ^2 /pix is plotted as a function of radius from the PSF centroid.
- VII Next the console will ask for the file name for the **BEST_FIT** output. This output file will give the final best-fit parameters that give the minimized χ^2 as determined during the MCMC run. These best-fit values are also printed to the console at the end of the MCMC run.
- VIII The next prompt asks for either a 1-star, 2-star, or 3-star fit. After entering "1", "2", or "3" the total degrees of freedom (d.o.f) will be printed to the console. The d.o.f depends on the total number of pixels in the (pre-determined) fitting box, the number of fitting parameters, and fitting constraints (if any). The fitting parameters that contribute to the overall d.o.f are:
 - (a) 1-star fit: x, y, total flux.
 - (b) 2-star fit: x1, y1, x2, y2, flux ratio, total flux.
 - (c) 3-star fit: x1, y1, x2, y2, x3, y3, star 1-2 flux ratio, star 1-3 flux ratio, total flux.

For a 2-star MCMC run on a fitting box of 700 total pixels (with no fitting constraints applied), the total d.o.f = 700 + 6 - 0 = 706. Note that including constraints on any of the fitting parameters will additionally reduce the total d.o.f by the number of parameters being constrained. The fitting box and degrees of freedom are discussed further in Section 4.1, and fitting constraints are discussed in Appendix A.

- IX The next prompt asks the user for a pixel scale in units of mas/pix. The routine will use this pixel scale to calculate the separation between the stars (in units of milliarcsecond). The NIRC2 and OSIRIS instruments on the Keck telescopes have pixel scales of 9.942 mas/pixel. Since there is no separation measurement necessary for the 1-star fitting mode, this prompt is skipped in 1-star mode.
- X The next prompt asks the user for a "renormalization factor" (i.e. best-fit χ^2 divided by degrees of freedom). This is used for re-normalizing the χ^2 per degree of freedom (such that $\chi^2 \simeq 1$) in order to obtain more realistic error bars on the MCMC chains. If running the MCMC for the first time, this value should always equal 1.0. Near the end of the first run, the renormalization factor is computed and printed to the screen, this value should then be inputted by the user during the second MCMC run. The

renormalization factor will only be printed to the screen during the first MCMC run (i.e. when the initial value is set to 1.0).

- XI Next, the user is prompted for "Number of MCMC iterations". This is the total number of steps that the MCMC routine will attempt. It is usually true that the larger the iteration size, the longer the routine will take to run.
- XII The next prompt asks for pixel step size (or 'jump size' or 'jump function') for the MCMC routine. This step size dictates how large of a step the MCMC routine will make during its search through the 2D pixel parameter space. The magnitude of this value can vary quite substantially depending on the circumstances of the fitting, a useful metric is printed to the screen at this point which states that a good step size is one that gives an acceptance rate ($\frac{\text{accepted mcmc steps}}{\text{total proposed steps}}$) between 0.1-0.5.
- XIII The next prompt asks for flux step size. Similar to the previous description, this value determines how large of a step the MCMC routine will make during its search through the total flux parameter space.
- XIV The next prompt asks for initial guesses for the stellar positions of star 1, 2, and/or 3. The initial guess needs to be within the fitting box or an error will be thrown. Further, the MCMC fitting routine (in all three modes) expects the user-inputted stars to be in order of brightness (i.e. brightest to faintest). If there are multiple stars to be fit that have approximately the same brightness, the routine will still function properly. However, the user should verify that the best-fit individual stellar flux values are consistent with the best-fit total flux value (i.e. sum of the individual flux values equals the total flux value).

Note: If the user inputs an initial position outside of the pre-determined fitting box, a "segmentation fault – invalid memory reference" error will result.

XV After the initial position guesses, the user is prompted to enter an initial guess for the source (star-1) flux contribution to the total flux. For the trivial case of 1-star fitting, a good initial guess for this parameter is 1.0. For 2 and 3-star fitting, one can obtain an initial guess for this parameter by converting the instrumental magnitudes in the .grp file to fluxes and finding their individual contributions to the overall total flux. For example:

$$\frac{10^{(-0.4*m_1)}}{10^{(-0.4*m_1)} + 10^{(-0.4*m_2)}}$$

where m_1 and m_2 are the instrumental magnitudes of star-1 and star-2 respectively. If performing a 3-star fit, this prompt will be repeated for the 3rd star (also referred to as 'blend' star in the routine).

After the final flux contribution prompt(s), the routine will begin. A counter will print the current step at every 50,000 iterations. Once completed, the best fit parameters are printed to the console, which includes the χ^2 value for the best fit. The following screenshot shows

the terminal after the first run of a successful (2-star) fitting sequence:

```
Degrees of Freedom = 406
Pixel Scale (mas/pix):
.942
Renormalization Factor (type '1' if first time run):
Number of MCMC Iterations:
Step size pixel (goal: accept. rate -> 0.1 - 0.5):
Step size flux (goal: accept. rate -> 0.1 - 0.5):
Star 2 x,y:
213,1428
Star 1 Flux Contribution (star 1/(star1 + star2)):
Choose the BRIGHTER star!
           1199
52.9449997
Sky Avg: 52.9449997
Zeropoint Mag: 13.4010000
50000
  X1
1210.91370
                                                                                                                                                           CHI2
100.467575
                      Y1
1420.89087
                                                               Y2
1424.48743
                                                                                   SEP
56.892211709976195
                                                                                                                 F1
0.777228534
                                                                                                                                     F2
0.222771466
                                          1206.46277
   Done.
```

Before the final best-fit parameters are printed to the screen, two values are printed; the renormalization factor and the acceptance rate. As described in step XII, a reasonable acceptance rate should be between 0.1 and 0.5 (i.e. the fraction of proposed MCMC jumps that were accepted). This range is somewhat larger than the standard range used in order to get target probability densities that are locally Lipschitz (the standard practice is tuning the proposal distribution to get acceptance rates of 0.2 - 0.3). Testing has shown indistinguishable results with the marginally larger range, however the user should take note of acceptance rates and adjust accordingly for their specific circumstance. Finally, the renormalization factor printed to the screen should be used as the input factor during the 2nd iteration of MCMC fitting (see screenshot below).

```
1, 2, or 3 star fit:
2
Degrees of Freedom = 406
Pixel Scale (mas/pix):
9,942
Renormalization Factor (type '1' if first time run):
0,247
Number of MCMC Iterations:
100000
Step size pixel (goal: accept. rate -> 0.1 - 0.5):
0,02
Star 1 xy:
1210,1421
Star 2 xy:
1211,1428
Star 1 Flux Contribution (star 1/(star1 + star2)):
Choose the BRIGHTER star!
0,8
Pit box: 1199 1218 1413 1432
Sky Avg: 52,9449997
Zeropoint Mag: 13,4010000
50000
100000
Acceptance Rate = 0.3196100000000001
X1 Y1 X2 Y2 SEP F1 F2 CH12
1210,91284 1420.89062 1206.45715 1424.48120 56.891694972038273 0.777145565 0.222854435 406.782104
Done.
```

The above screenshot shows the terminal after the second run of a successful (2-star) fitting sequence. The input renormalization factor comes from the value that was calculated in iteration #1. The best-fit $\chi^2/\text{d.o.f}$ is now \sim 1, and errors derived from the MCMC chains are more realistic.

3 Description of Major Routines

3.1 Single Star MCMC

DAOPHOT-MCMC has functionality for fitting the position and flux for the trivial case of a single star. The star, of course, could actually be a binary or have a very close companion such that the separation is significantly smaller than some fraction of the FWHM, which would show no significant signal detected in the residual. For the purposes of this section, we will assume the star is indeed a single stellar object (point source).

The MCMC routine begins at a pixel location chosen by the user. The size of the fitting box is \sim 1.5x the FWHM of the PSF in both directions and is pre-determined by DAOPHOT-II before the iteration begins. The iteration proceeds by taking random steps (of step size defined by the user) in any direction and measuring the total flux (f_T) distribution:

$$f_T = f_1 \psi(i - x_1, j - y_1),$$

where f_1 is the fractional flux contribution from the single star (1.0 for a single-star fit), ψ is the two-dimensional empirical PSF, x_1 and y_1 are the initial pixel coordinates. A χ^2 value is also computed at each step in the chain. Once the routine is finished, the best-fit parameters are printed to the terminal screen (i.e. X1, Y1, Total Flux, χ^2). For the ideal case of 100% of the flux in the fitting box coming from the star (minus background), the best-fit total flux value would be 1.00. However, due to photon noise, imperfect PSF shape, and other sources of flux contamination (like an unresolved blend as mentioned earlier), this value may deviate from unity. The total flux calculation is rather simple; it is just the ratio of the total sum of each raw pixel value (minus background) and the total sum of the measured flux distribution at each pixel across the grid:

$$\frac{\sum_{i,j}^{n} P_{i,j} - s_{i,j}}{\sum_{i,j}^{n} f_1 \psi(i - x_1, j - y_1)},$$

where P is the raw pixel value and s is the background. Finally, the χ^2 minimization routine used for the fitting is given in section 4.5.

3.2 Dual Star MCMC

DAOPHOT-MCMC can simultaneously fit the positions, separations, and fluxes for a twostar blend. Similar to the single-star routine, the iteration begins at a user-defined pixel location (for both stars) inside the fitting box of $\sim 1.5 x$ FWHM, as well as an initial guess for the flux ratio of the stars. The iteration proceeds by taking random steps in any direction and any flux ratio. This flux ratio is an additional parameter to consider for the two stellar objects. The routine measures the total flux distribution at each step in the chain:

$$f_T = f_1 \psi(i - x_1, j - y_1) + (1 - f_1) \psi(i - x_2, j - y_2),$$

with the additional parameters as follows; $(1 - f_1)$ is the flux contribution from the second (fainter) star, x_2 and y_2 are the initial pixel positions for the second (fainter) star. Similar to the single-star fit, a χ^2 value is calculated at each step, and the best-fit parameters are printed to the screen once the routine has finished (i.e. X1, Y1, X2, Y2, Separation, Flux Ratio, Total Flux, χ^2). As mentioned in the previous section, the best-fit total flux may deviate from unity. The total flux is calculated similarly to the previous section:

$$\frac{\sum_{i,j}^{n} P_{i,j} - s_{i,j}}{\sum_{i,j}^{n} f_1 \psi(i - x_1, j - y_1) + (1 - f_1) \psi(i - x_2, j - y_2)},$$

where the additional parameters from the second (fainter) star are now included.

The separation between star-1 and star-2 is measured at each step in the chain, the calculation is very straightforward:

$$\Omega\sqrt{(x_1-x_2)^2+(y_1-y_2)^2},$$

where Ω is the pixel scale (mas/pixel). For the NIRC2 or OSIRIS instruments using adaptive optics (AO) on-board the Keck 10m telescopes, $\Omega = 9.942$ mas/pixel.

3.3 Triple Star MCMC

The third major function in DAOPHOT-MCMC is simultaneous fitting of three stars. The fitting will work on three blended stars, two blended stars and a nearby neighbor, or three nearby (non-blended) stars. Of course, factors like the star separations and flux ratios will influence the properties of the MCMC runs. Similar to the dual-star fitting scenario, if the stars have very small separations and similar fluxes (or large separation and very different fluxes), some difficulty may arise when attempting to accurately fit their positions.

Just like before, the iteration begins at a user-defined pixel location (for all three stars) and initial guess for the flux ratios. The routine takes random steps in any direction and flux ratios (star1-2 and star1-3 flux ratios). The measurement of the total flux distribution at each step is:

$$f_T = f_1 \psi(i - x_1, j - y_1) + (1 - f_1 - f_3) \psi(i - x_2, j - y_2) + f_3 \psi(i - x_3, j - y_3),$$

where f_1 is the flux contribution from star 1, $(1 - f_1 - f_3)$ is the flux contribution from star 2, f_3 is the flux contribution from star 3, and x_3, y_3 are initial pixel values for star 3. Similar to the previous major routines, a χ^2 minimization routine is performed (i.e. section ??) and the best-fit parameters are printed to the screen when the process has finished.

The total flux for the three-star fitting is calculated as follows:

$$\frac{\sum_{i,j}^{n} P_{i,j} - s_{i,j}}{\sum_{i,j}^{n} f_1 \psi(i - x_1, j - y_1) + (1 - f_1 - f_3) \psi(i - x_2, j - y_2) + f_3 \psi(i - x_3, j - y_3)},$$

where the new factor in the denominator comes from the flux distribution of the third star. The new parameters that are calculated for three star fitting are: star 3's x,y position and flux contribution, and star 1-3 separation.

4 Description of Internal Functions

4.1 Degrees of Freedom

The degree of freedom (d.o.f) is calculated based on the following parameters:

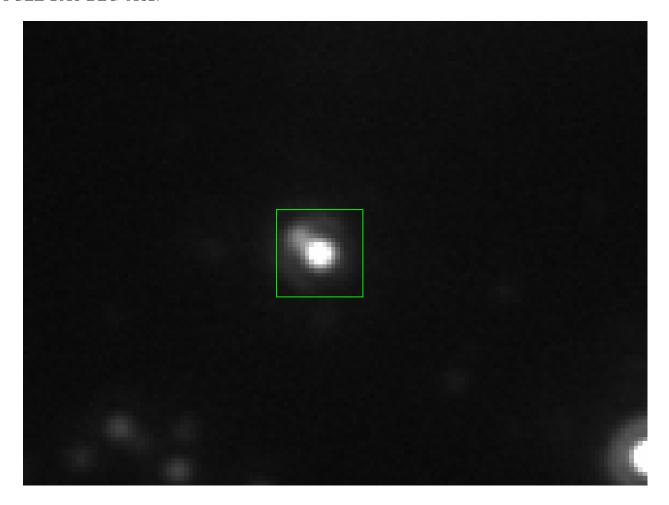
- Number of pixels
- Number of fitting parameters
- Number of fitting constraints

As described in Section 2, for a single star fit with zero constraints, the d.o.f = total pixels + 3. For a two-star fit this increases by 3 (total of 6 fitting parameters), and the d.o.f increases by 3 again for a three-star fit (total of 9 fitting parameters). The two main fitting constraints that are written into the program currently are constraints on the total flux and separation between the stars. These constraints are discussed in Appendix A.

NSTAR will automatically compute the size of the fitting box based on 1.5x the FWHM of the PSF for each star in the group. The fitting box will usually be a square grid of pixels, but can sometimes be rectangular depending on the separation amplitude and direction for two or three fitted stars in the box. The shape of the fitting box (square or rectangle) will not significantly impact any part of the MCMC or analysis thereafter. The total number of pixels in the fitting box can vary quite significantly (between a few hundred and few thousand) depending on the size of the PSF, the number of stars in the group and their separations. Finally, before the MCMC routine begins, the size of the fitting box is printed to the screen by: min_X, max_X, min_Y, max_Y. See screenshot below:

```
2, or 3 star fit:
Degrees of Freedom = 406
 Pixel Scale (mas/pix):
 Renormalization Factor (type '1' if first time run):
 Number of MCMC Iterations:
 Step size pixel (goal: accept. rate -> 0.1 - 0.5):
0.05
 Step size flux (goal: accept. rate -> 0.1 - 0.5):
0.05
 Star 1 x,y:
1210,1421
 Star 2 x,y:
1213,1428
 Star 1 Flux Contribution (star 1/(star1 + star2)):
 Choose the BRIGHTER star!
0.8
 Fit box:
                  1199
                              1218
                                           1413
                                                       1432
 Sky Avg:
            52.9449997
                  13.4010000
 Zeropoint Mag:
```

The following screenshot shows the target and an outline of the fitting box. The target consists of a blended source (brighter) star and lens (fainter) star for the mircolensing target OGLE-2013-BLG-0132.



There are a total of 400 pixels inside the fitting box.

4.2 Separation

The separation between the stars (in two-star or three-star fit) is *not* considered a fitting parameter. It is simply the calculation that was presented earlier in Section 3.2:

$$\Omega\sqrt{(x_1-x_2)^2+(y_1-y_2)^2},$$

where Ω is the user-defined pixel scale (in mas/pix) described earlier. For each step in the MCMC chain, the separation is calculated using the central positions of each star in the group. The positions are denoted $x_1, y_1, x_2, y_2, x_3, y_3$, and the calculated separations are denoted "S1-2_SEP" for the separation between star '1' and star '2', and "S1-3_SEP" for the separation between star '1' and star '3'. With this information, it is trivial to calculate the separation between star '2' and star '3'. As mentioned earlier, the general guideline is to

consider star '1' as the brightest, star '2' as the intermediate, and star '3' as the faintest in the group (for a three-star fitting).

4.3 Flux Ratios (Contributions to total flux)

The flux contribution parameter describes the ratio between the flux value for each star and the total flux). Upon initialization of the MCMC, the user will need to give an initial guess for the flux ratio for 'star 1' (i.e. brighter star), and for the three-star fit will also need to supply an initial guess for 'star 3' flux ratio (i.e. faintest star). As described earlier in Section 3.2, a first guess for the flux contributions can be determined from the .grp file that provides the aperture photometry for the stars in the group. There is also a *Python* script in the /Example directory that will quickly calculate the flux ratio's based on the magnitudes from the .grp file.

The best-fit fluxes will be printed to the screen when the routine finishes. For a one-star fit, this value should be very close to 1.0. For two-star and three-star fits, the flux fractions for all fitted stars are printed to the screen and labeled 'F1', 'F2', and 'F3'. The sum of each flux value will equal approximately 1. To get the flux ratio between star 3 and star 1 for example, one simply needs to divide F3 by F1 $(F_{31} = \frac{F3}{F1})$.

4.4 Total Flux

The total flux calculation was presented in Section's 3.1, 3.2, and 3.3 and is used in all three fitting runs. In the absence of various sources of noise, undetectable effects (unresolved companion, PSF wings of neighboring stars falling inside the fit box, etc), or sky/background variation inside the fit box, the total flux for the single-star fit should always equal 1.0. Because of variations in the PSF from image to image, drawing the uncertainty in total flux from the MCMC distribution will likely result in underestimated error bars. The Jackknife method (presented in Bhattacharya et al. 2021 and Terry et al. 2021) can account for these PSF variations and is likely a more reasonable method for estimating the errors on the total flux.

4.5 χ^2 Minimization

DAOPHOT-MCMC employs the Metropolis-Hastings (MH) algorithm on the 3 , 6 , or 9-dimensional parameter space for the one-star, two-star, or three-star scenarios respectively. For each step in the chain, the following is computed:

$$\chi^2 = \sum_{i,j} \left[\frac{1}{\sigma} \{ P_{i,j} - s_* - f_1 \psi(i - x_1, j - y_1) - (1 - f_1) \psi(i - x_2, j - y_2) \} \right]^2,$$

where $P_{i,j}$ is the intensity at pixel i, j, σ is the uncertainty in pixel intensity, and s_* is the background flux. The procedure for minimizing this value follows the MH method, and the best-fit minimum χ^2 is then printed to screen when the run has finished.

4.5.1 Renormalization

The renormalization factor is implemented in order to obtain more realistic error bars on the MCMC chains. This is achieved by dividing the 'un-renormalized' best-fit minimum χ^2 by the d.o.f from the initial run of NSTAR-MCMC, which results in $\chi^2/d.o.f \sim 1.0$. I'll note that this is a standard technique in the microlensing field; I am not specifically using a reduce χ^2 to distinguish models. I use the difference between the χ^2 values, and only use the renormalization to scale that difference.

While it has been argued that including the errorbar scaling factor as a model parameter while fitting the model to the data may be a better approach, there are some potentially significant drawbacks. First, the idea of scaling the error bars while fitting could erroneously increase the chances of overfitting. The scaling factor for one data set can be driven very large and hide the fact that a given data set doesn't fit the model. Second, including the errorbar scaling as a model parameter while fitting may require one to define a prior on the proposal distribution P(x) in order to allow the MCMC to converge. In this case it would likely be more beneficial to build a new likelihood, and use an uninformative prior. A future update to the code may include a different approach to recaling the errorbars, however the author does not expect any change to significantly impact the MCMC results.

A Fitting Constraints

There are currently two main parameters that can be constrained; the total flux and the separation. At present, the only way to implement these constraints is by manually editing the source code. There are several lines inside NSTAR-MCMC.F that are commented to show where the expression is for implementing the constraint(s). These constraints have the following forms.

For constraining the flux:

$$\chi^2 = \sum_{i,j} \{ (f_1 \psi(i - x_1, j - y_1) - (1 - f_1) \psi(i - x_2, j - y_2) - F_C) / \sigma_{F_C} \}^2$$

where F_C and σ_{F_C} are the flux constraint and uncertainty on the flux constraint, respectively.

Similarly, for constraining the separation:

$$\chi^2 = \sum_{i,j} \left\{ (\Omega \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2} - S_C) / \sigma_{S_C} \right\}^2$$

where S_C and σ_{S_C} are the separation constraint and uncertainty on the separation constraint, respectively. As mentioned earlier, Ω is the user-defined pixel scale (in mas/pix).

Again, if one intends to place constraints on either of these quantities, one must edit the *nstar-mcmc.f* source code and recompile/build.

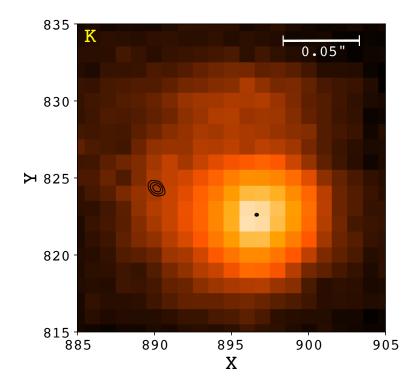
B Example Outputs / Figures / Tables

The following outputs are from the DAOPHOT-MCMC analysis of the microlensing target MOA-2009-BLG-319 (Terry et al. 2021).

The following table shows the first several lines from the "mcmc_fit.dat" output file:

X1	Y1	X2	Y2	SEP	F_RATIO	F_TOTAL	F1	F2	CHISQ
896.000000	822.000000	890.000000	824.000000	62.8787308	0.880000055	0.949538827	0.835594237	0.113944605	476.541962
896.178772	821.930115	889.810486	823.843506	66.1095428	0.886963248	0.949477732	0.842151880	0.107325882	453.851593
896.145813	821.969910	889.947937	824.038330	64.9601669	0.893375695	0.949382246	0.848155022	0.101227224	440.780151
896.152771	821.977234	890.033081	824.092590	64.3742294	0.895395815	0.949335396	0.850030959	9.93044525E- 02	435.635895
896.248108	822.114014	890.158264	824.058105	63.5555038	0.901857197	0.949421048	0.856242180	9.31788459E-02	351.118225
896.308533	822.161804	890.163208	824.139771	64.1835709	0.902112067	0.949595094	0.856641173	9.29538980E- 02	317.609924

Using the "2star-contour.py" Python script (https://github.com/skterry/DAOPHOT-MCMC/tree/master/Example/Output/2star-contour.py) to plot the contour intervals for both stars on top of the stellar image gives the follow figure:

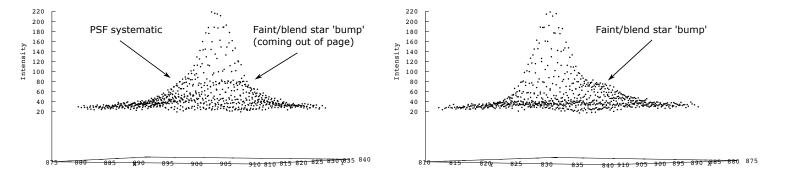


Caption: Best fit MCMC contours (68.3%, 99.5%, 99.7%) for the two blended stellar positions, over-plotted on the K band image of the target. The fainter star contributes $\sim 15\%$ of flux to the total blend. Figure from Terry et al. 2021 (https://arxiv.org/abs/2009.08461).

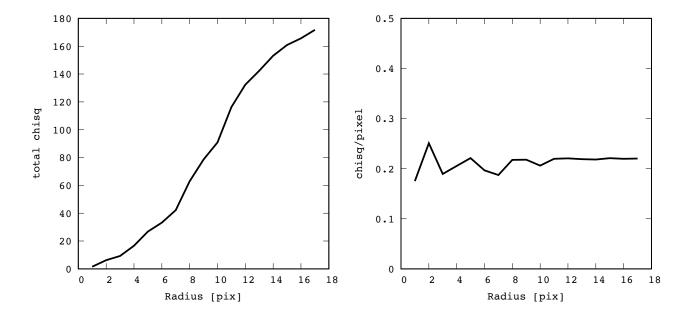
The second file that is printed out, "chisq_pixel.dat":

X	Y	CHISQ	PIX_INTENSITY
879	811	0.343843967	29.9540348
879	812	4.09128983E-03	27.9113522
879	813	2.59341728E-02	27.8329487
879	814	0.226609126	24.6133747
879	815	0.639254093	23.6851978
879	816	1.21737766	22.3830376

This table is very straightforward, it can be used to plot the variation in pixel intensities across the grid, or a diagnostic test for the stability of the PSF model as fitted to the stellar position(s).



Caption: 3-D plots of pixel intensities across the grid. Panels are rotated (45° about z-axis) to show a systematic feature from the PSF model, and a real feature from the blended faint star.



Caption: Diagnostic plots for chisq as a function of pixel radius (i.e. pixels from peak centroid).

5 Change Log

- 2023 November 4: Several bug fixes (d.o.f., chi2pix table).
- 2023 April 12: v1.5.0 release.
- 2023 April 10: Adjusted how flux values are reported for better clarity. Update to User Manual, post_analysis scripts, misc scripts. Minor bug fixes.
- 2023 April 2: Built-in renormalization factor calculation printed to screen (at the end of first MCMC run only).
- 2021 October 30: Added support for creating/saving *.mcmc/*.chi2pix/*.bf outputs for Jackknife method (v1.4.0 release). Deprecated "chisq_pixel.dat" output.
- 2021 May 13: Update references to Bhattacharya et al. 2021 and Terry et al. 2021.
- 2020 November 9: Add appendix B to user manual, add headers to "chisq_pixel.dat" output.
- 2020 October 22: v1.3.0 release.
- 2020 October 16: Bug fixes from ref. report (c.f. Terry et al. 2021).
- 2020 July 16: Added separation and flux constraint (commented out by default).
- 2020 July 7: χ^2 renormalization implemented (v1.2.0 release).
- 2020 July 2: Fix dimension size to match pre-determined gridsize via ALLOCATABLE.
- 2020 June 30: Added column headers to raw MCMC output file.
- 2020 June 26: Fix bug printing star(1-2) separation and star(1-3) separation for triple-star MCMC.
- 2020 June 10: Cleaner printing of best-fit parameters to the terminal, minor bug fix in degree of freedom (d.o.f) calculation (v1.1 release).
- 2020 May 30: Added functionality for 3-star fitting, minor bug fixes.
- 2020 May 15: v1.0.0 release.