

Radhakrishnan S, Ph.D.

Department of Science and Humanities

Unit I: Review of concepts leading to Quantum Mechanics



Week #1

- **Cl#1** Review of Electric and magnetic fields
- Cl#2 EM Wave equation
- Cl#3 Energy transported by EM Waves
- Cl#4 Max Planck's Black Body Radiation equation

Unit I: Review of concepts leading to Quantum Mechanics



- >Suggested Reading
 - 1. Fundamentals of Physics, Resnik and Halliday, Chapters 22,29, 32
 - 2. NCERT Physics Book I grade 12 Chapters 1,4,6
- > Reference Videos
 - 1. https://nptel.ac.in/courses/108/106/108106073/

Unit I: Review of concepts leading to Quantum Mechanics



Class #1

- Review of Electric and magnetic fields
- Concept of the Nabla operator ∇
- Gradient, Divergence and Curl Operations
- Divergence and curl of fields

Concepts of Electric fields

Electric Charges

- Electric charges can be isolated
- The potential at any point x from the charge

•
$$V_x = \frac{Q}{4\pi\varepsilon_0} \times \frac{1}{x}$$

• The electric field due to a point charge

•
$$E_{x} = \frac{Q}{4\pi\varepsilon_{0}} \times \frac{1}{x^{2}}$$

• The electric field in terms of the potential

•
$$E_x = -\frac{dV_x}{dx}$$

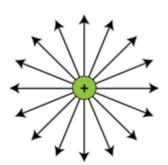


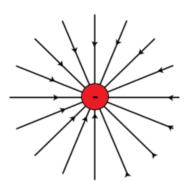
Concepts of Electric fields



Electric fields can be visualized through the electric flux lines

Electric field lines from positive and negative charges



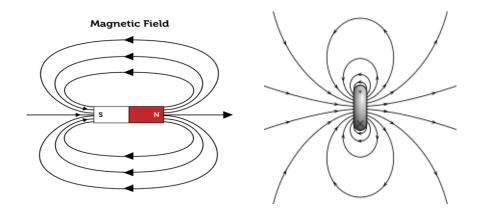


Concepts of Magnetic fields

Magnetic dipoles

- Magnetic mono poles do not exist
- Fields can be expressed in terms of the flux lines
- Flux lines are continuous from the north pole to the south pole

Magnetic field lines of a magnetic dipole

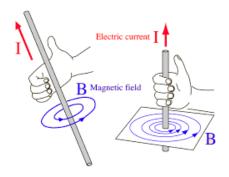


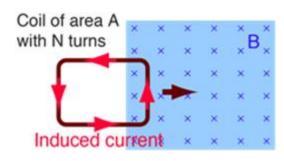


Electric and Magnetic fields

- Magnetism and magnetic fields are due to moving charges
- Electric currents are also due to moving charges

Interplay of electric currents and Magnetic fields





Ampere's law

Faraday's law

Images courtesy Hyperphysics, Wikipedia



Del or Nabla operator $-\overrightarrow{\nabla}$

The Nabla operator is a differential vector operator

$$ightharpoonup \overrightarrow{\nabla} = \hat{\imath} \frac{\partial}{\partial x} + \hat{\jmath} \frac{\partial}{\partial y} + \hat{k} \frac{\partial}{\partial z}$$
 Del operator

$$ightharpoonup \overrightarrow{\nabla}.\overrightarrow{\nabla} = \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2} = \nabla^2$$
 Laplacian operator

$$ightharpoonup \overrightarrow{\nabla} imes (\overrightarrow{\nabla} imes A) = \overrightarrow{\nabla} (\overrightarrow{\nabla} . A) - \nabla^2 A$$
 Vector identity



Operations with Del or Nabla operator - ∇

Operations with the Nabla operator (del operator)

- $ightharpoonup \overrightarrow{\nabla}$ operates on a scalar to give a vector
 - Gradient of the scalar
- \triangleright The dot product (.) of ∇ with a vector gives a scalar
 - Divergence of the vector
- \triangleright The cross product (x) of ∇ with a vector gives a vector
 - Curl of the vector



Gradient of a scalar field

Gradient of a scalar V(xyz)

$$grad V = \nabla V = \hat{\iota} \frac{\partial V_x}{\partial x} + \hat{J} \frac{\partial V_y}{\partial y} + \hat{k} \frac{\partial V_z}{\partial z}$$

The gradient of a scalar field gives a vector

Gradient gives the rate of change of the property at any point and the direction gives the direction in which the change is maximum

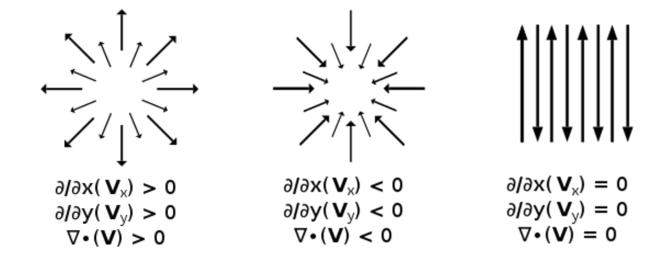


Divergence of a vector field

Divergence of a vector
$$\vec{V} = \hat{\imath}V_x + \hat{\jmath}V_y + \hat{k}V_z$$

$$Div V = \nabla \cdot V = \frac{\partial V_x}{\partial x} + \frac{\partial V_y}{\partial v} + \frac{\partial V_z}{\partial z}$$

The divergence of a vector field gives a scalar

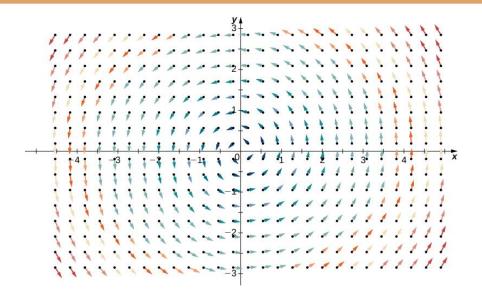




Curl of a vector field

$$curl A = \nabla \times A = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ A_x & A_y & A_z \end{vmatrix}$$

The curl of a vector is another vector



Images courtesy Hyperphysics, Wikipedia



Class 1. Quiz ...

The concepts which are correct are....

- 1. Electric monopoles do not exist
- 2. Magnetic dipoles exist
- 3. Magnetic monopoles do not exist
- 4. Electric dipoles can be observed in systems
- 5. Magnetic lines of force are divergent
- 6. Electric flux lines are always divergent





THANK YOU

Radhakrishnan S, Ph.D.

Professor, Department of Science and Humanities

sradhakrishnan@pes.edu

+91 80 21722683 Extn 759