## MAE 3134: Final Exam

**Problem 1** The frequency response of two systems are shown in Figure 1. Using the plots, circle the correct descriptions:

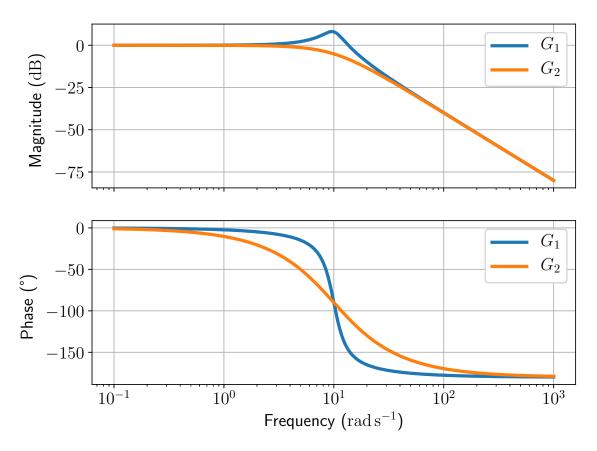


Figure 1: Frequency Response

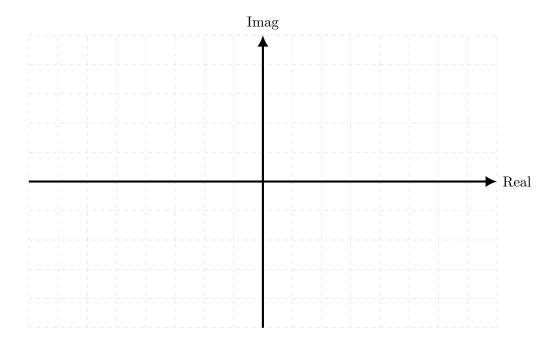
- 1. Which of the following statements are true about the damping ratios of the two systems?
  - (a) The damping coefficients are the same.
  - (b) The damping coefficient of  $G_1$  is greater than the damping coefficient of  $G_2$ .
  - (c) The damping coefficient of  $G_2$  is greater than the damping coefficient of  $G_1$ .
  - (d) Not enough information to make any statements about the damping ratio.
- 2. Which of the following statements are true about the general form of  $G_1$ ?
  - (a) It is a first order system.
  - (b) It must have two free s terms in the denominator since the phase ends at 180°.
  - (c) It must have two free s terms in the numerator since the final magnitude slope is  $40\,\mathrm{dB}$  per decade.
  - (d) None of the above.

**Problem 2** Elon Musk, CEO of SpaceX and Tesla Motors, has a background in physics but unfortunately has never passed a Linear Dynamics course. His newest space vehicle must satisfy the following second order time response specifications for a unit step input:

- Percent Overshoot must be less than 5%,
- Rise time less than 1s,
- Settling Time less than 5 s.

Elon needs your help to choose a set of poles which will satisfy the specifications and save humanity from impending disaster.

- 1. On the s-plane, or complex plane, map out the acceptable regions where you could locate poles and meet the requirements.
- 2. Label the specifications lines and show your work.
- 3. Choose a set of poles that will meet the requirements.



 $\textbf{Problem 3} \quad \text{List at least two advantages of state-space or "modern control" techniques as compared to "classical control" approaches.$ 

**Problem 4** The transfer functions of three systems are given as follows:

$$G_1 = \frac{1}{s^2 + 0.2s + 1}, \qquad G_2 = \frac{2s + 4}{s^2 + 0.5s + 4}, \qquad G_3 = \frac{-2s + 4}{s^2 + 0.5s + 4}.$$
 (1)

You should accomplish the following tasks:

1. Figure 2 shows the Bode plots associated with these transfer functions. Match each plot with the appropriate transfer function by indicating on each plot the correct transfer function (i.e.  $G_1$ ,  $G_2$ , or  $G_3$ ). Explain your reasoning that lead to your solution.

2.

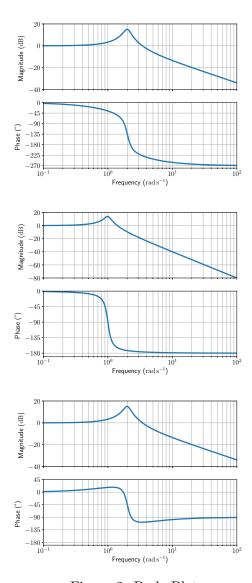


Figure 2: Bode Plots