Spring 2017 MAE3134: Final Exam

11 May 2017

Resources allowed:	Open notes/book, calculate	tor, ruler. No con	nputers or mobile devi	ices
Name:		GWID:		

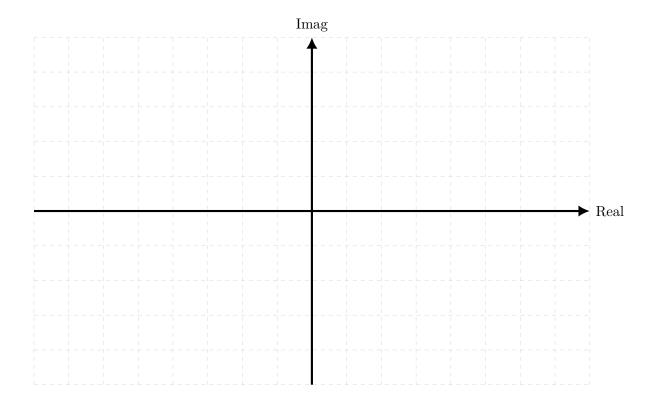
Prob. 1	Prob. 2	Prob. 3	Prob. 4	Prob. 5	Prob. 6	Prob. 7	Prob. 8	Total
10	5	20	20	20	10	10	5	100

Problem 1 Elon Musk, CEO of SpaceX and Tesla Motors, has a background in physics but unfortunately has never passed a Linear Dynamics course. His newest space vehicle must satisfy the following second order time response specifications for a unit step input:

- Percent Overshoot must be less than 5%,
- Peak time less than 1s,
- Settling Time less than 5 s.

Elon needs your help to choose a set of poles which will satisfy the specifications and save humanity from impending disaster.

- 1. On the s-plane, or complex plane, map out the acceptable regions where you could locate poles and meet the requirements.
- 2. Label the specifications lines and show your work.
- 3. Choose a set of poles that will meet the requirements.



Problem 2 The frequency response of two systems are shown in Figure 1. Using the plots, circle the correct descriptions: 469.75502pt

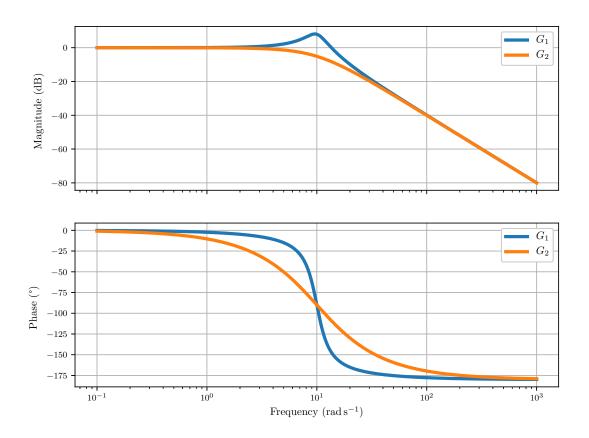


Figure 1: Frequency Response

- 1. Which of the following statements are true about the damping ratios of the two systems?
 - (a) The damping coefficients are the same.
 - (b) The damping coefficient of G_1 is greater than the damping coefficient of G_2 .
 - (c) The damping coefficient of G_2 is greater than the damping coefficient of G_1 .
 - (d) Not enough information to make any statements about the damping ratio.
- 2. Which of the following statements are true about the general form of G_1 ?
 - (a) It is a first order system.
 - (b) It must have two free s terms in the denominator since the phase ends at 180°.
 - (c) It must have two free s terms in the numerator since the final magnitude slope is $40 \,\mathrm{dB}$ per decade.
 - (d) None of the above.

Problem 3 The transfer functions of three systems are given as follows:

$$G_1 = \frac{1}{s^2 + 0.2s + 1},$$
 $G_2 = \frac{2s + 4}{s^2 + 0.5s + 4},$ $G_3 = \frac{-2s + 4}{s^2 + 0.5s + 4}.$

You should accomplish the following tasks:

- 1. Match each Bode plot shown in Figure 2a with the appropriate transfer function by indicating on each plot the correct transfer function (i.e. G_1 , G_2 , or G_3). Explain the reasoning that lead to your solution.
- 2. Match each response plot shown in Figure 2b with the correct transfer function by indicating on each plot the correct transfer function. The same input of $u = 2 \sin 2t$ is applied to each system. Explain the reasoning for your solution. Note: Figures 2a and 2b are not in the same order.

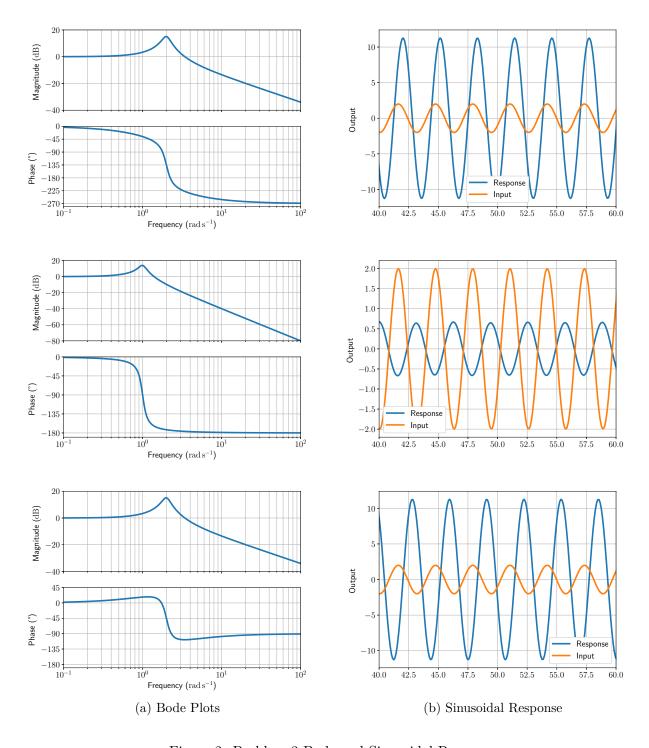
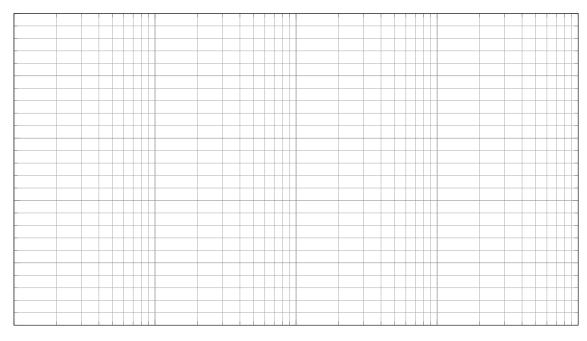


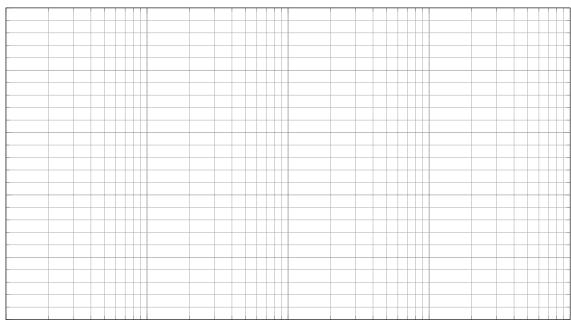
Figure 2: Problem 3 Bode and Sinusoidal Responses

Problem 4 A transfer function is defined as

$$G(s) = \frac{500(s+40)}{s^2 + 8s + 25}.$$

- 1. Draw the asymptotic Bode plots for this system.
- 2. What is the steady state output for an input of $u = 5 \sin 25t$?





Problem 5 Given the state space representation is defined as

$$\dot{\boldsymbol{x}} = A\boldsymbol{x} + B\boldsymbol{u},$$
$$\boldsymbol{y} = C\boldsymbol{x} + D\boldsymbol{u},$$

DERIVE the expression for the transfer function $\frac{Y(x)}{U(s)}$.

 $\textbf{Problem 6} \quad \text{List at least two advantages of state-space or "modern control" techniques as compared to "classical control" approaches.$

Problem 7 For the electrical system in Figure 4:

- 1. Find the differential equations for the system.
- 2. Find the state space representation of the system with your state vector defined as

$$\boldsymbol{x} = \begin{bmatrix} q_1 & i_1 & q_2 & i_2 \end{bmatrix}^T,$$

where q_1, i_1 represent the charge and current in the left loop while q_2, i_2 represent the charge and current in the right loop. The output is defined as

$$y = \begin{bmatrix} q_1 & q_2 \end{bmatrix}^T.$$

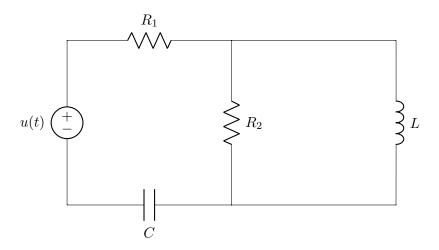


Figure 4: Electrical Circuit

Problem 8 Consider the electrical circuit shown in Figure 5:

- 1. Find the differential equations which govern the behavior of the electrical system.
- 2. Construct the state space representation of the system. Assume the desired output is the charge in the system.
- 3. Find the output response of the system assuming zero initial conditions and a step input of $u(t)=24\,\mathrm{V}$

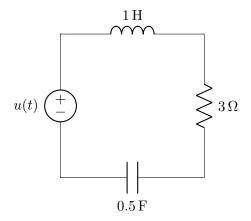


Figure 5: Electrical Circuit