1)
a)
$$T(s) = \frac{16}{s^2 + 3s + 16}$$

1) $w_n = \sqrt{16} = 4$
 $g = \frac{3}{2w_n} = 0.3750$
 $T_p = \frac{1}{w_n \sqrt{1 + 8^2}} = 0.8472$
 $T_p = \frac{1}{w_n \sqrt{1 + 8^2}} = 0.8472$
 $T_p = \frac{1}{w_n \sqrt{1 + 8^2}} = 0.4176^2 + 1.0392 + 1$
 $T_s = \frac{1}{8w_n} = 2.667$

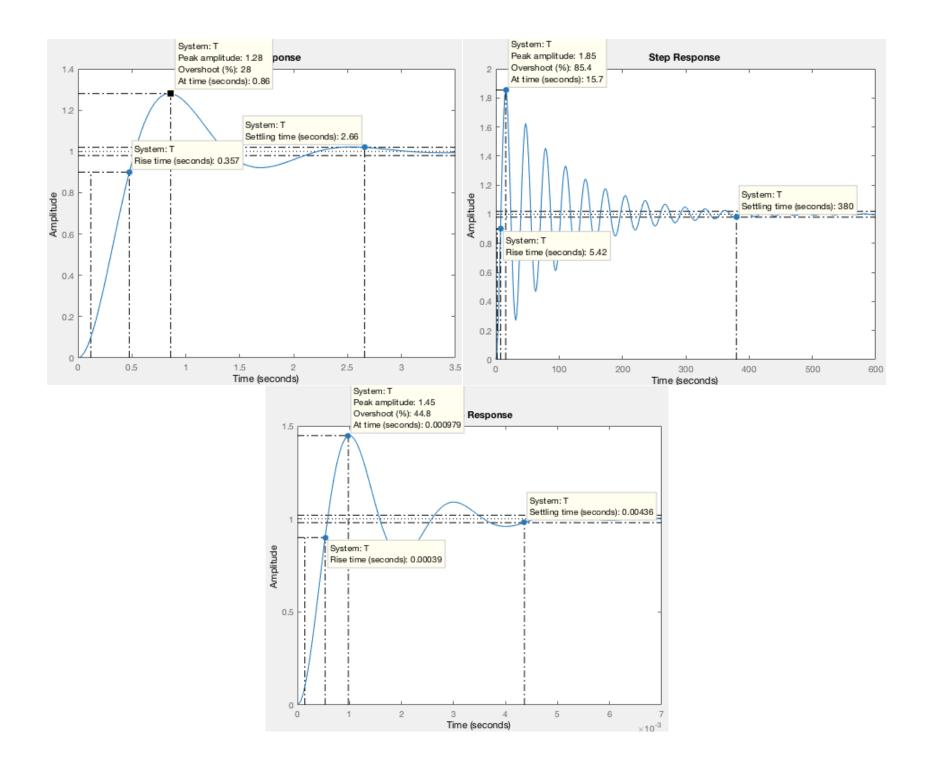
2) See MATLAB

9005 = $\exp(-\frac{8\pi}{41 - 8^2}) = 100 = 28.06\%$

b) $T(s) = \frac{0.04}{s^2 + 0.02s + 0.04}$

1) $w_n = \sqrt{0.02} = 0.2$
 $T_p = \frac{1}{w_n \sqrt{1 + 8^2}} = 15.7276$
 $T_s = \frac{1}{8w_n} = 400$
 $T_s = \frac{1}{8w_n} = 3.2404 \times 10^3$
 $T_s = \frac{1}{4w_n} = 3.2404 \times 10^3$
 $T_s = \frac{1}{4w_n} = 0.005$
 $T_s = \frac{1}{8w_n} = 0.005$

2) See MATLAB



2)
$$T(s) = \frac{10.607}{5^2 + 0.9395 + 0.607}$$

384) see MATLAB

3&4) See MATLAB

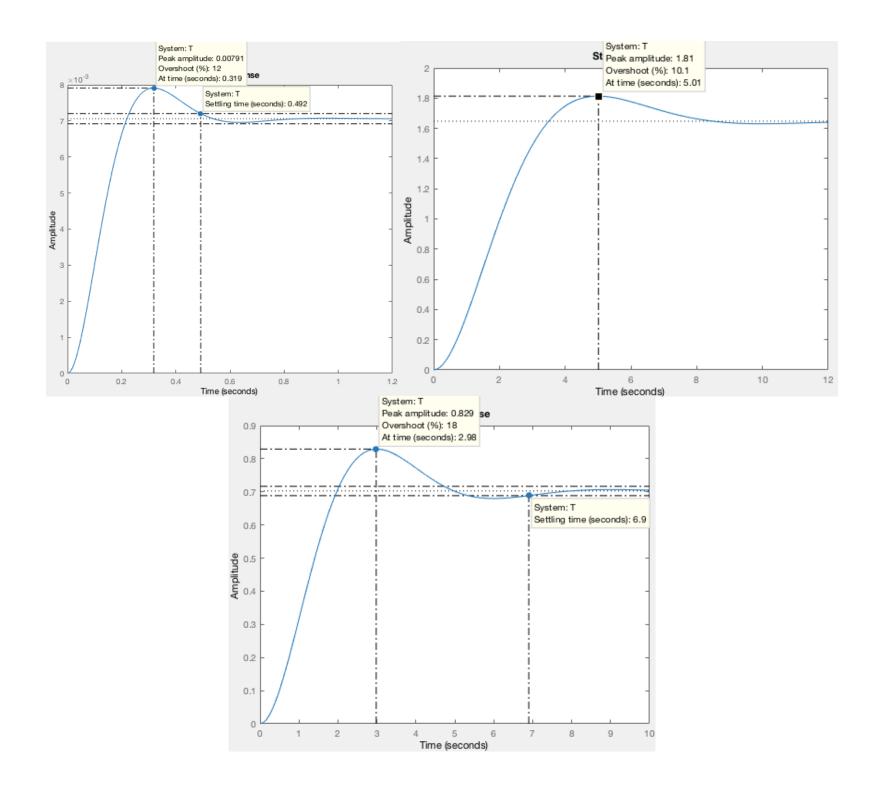
c)
$$T_s = 7s$$
 $T_p = 3s$ $w_n = \frac{4}{87s}$ $\rightarrow \frac{4}{87s} = \frac{7}{10} \frac{4}{10} = \frac{7}{10} \frac{2}{16} = \frac{7}{10} \frac{2}{10} = \frac{7}{10} = \frac{7}{10} \frac{2}{10} = \frac{7}{10} = \frac$

$$\mathcal{L} = \frac{-\ln(\%05/400)}{\sqrt{m^2 + \ln^2(\%05/400)}} = 0.56$$

$$W_n = \frac{4}{8T_8} = 11.9$$

$$W_d = W_n \sqrt{1-8^2} = 9.86$$

b)
$$\%05=10\%$$
 $T_p=5s$ $R = \frac{-\ln(\%05/300)}{\sqrt{\pi^2+\ln^2(\%05/300)}} = 0.59$
1) $w_n = \frac{1}{T_p} \sqrt{3-92} = 0.779$
 $w_n = \frac{1}{T_p} \sqrt{3-92} = 0.62$
 $w_n = \frac{1}{T_p} \sqrt{3-92} = 0.62$



a)
$$\frac{24}{R(s)} = \frac{24}{s^3 + 9s^2 + 26s + 24}$$
 \Rightarrow $c + 9c + 26c + 24c = 24r$
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 $c + 26c + 26c + 26c + 26c + 24c = 24r$
 $c + 26c + 26c$

$$\begin{bmatrix} \dot{x}_{1} \\ \dot{x}_{2} \\ \dot{x}_{3} \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x_{1} \\ x_{2} \\ x_{3} \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 24 \end{bmatrix} r$$

$$A$$

$$\dot{x} = A_x + B_C$$
 $c = [0]$
 $y = cx + Dr$
 $c = [0]$

b)
$$\frac{C(s)}{R(s)} = \frac{s^2 + 7s + 2}{s^3 + 9s^2 + 26s + 24}$$
 $= \frac{C(s)}{R(s)} = \frac{Z(s)}{R(s)} \cdot \frac{C(s)}{R(s)}$
state: $\frac{Z(s)}{R(s)} = \frac{1}{s^3 + 9s^2 + 26s + 24}$

$$\dot{x} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -24 & -26 & -9 \end{bmatrix} \times + \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} \cap$$

output:
$$\frac{C(s)}{Z(s)} = s^2 + 7s + 2 \Rightarrow C(s) = (s^2 + 7s + 2)Z$$

$$C = \frac{1}{2} + 7\frac{1}{2} + 2Z \qquad \times_1 = Z \qquad \times_2 = \frac{1}{2} \qquad \times_3 = \frac{1}{2} \qquad y = C = \times_3 + 7\times_2 + 2\times_4$$

$$y = \begin{bmatrix} 2 & 7 & 1 \end{bmatrix} \times$$

c)
$$G(s) = \frac{2s+1}{s^2+7s+9}$$

state:
$$\frac{Z(s)}{R(s)} = \frac{1}{s^2 + 7s + 9}$$
 \Rightarrow $\frac{1}{2} + 7z + 9z = \Gamma$ $x_1 = Z$ $x_2 = z$ $x_1 = X_2$ $x_2 = -9x_1 - 7x_2 + \Gamma$ $\begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -9 & -7 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} \Gamma$

output:
$$\frac{C(s)}{2(s)} = 2s + 1 \rightarrow C(s) = (2s + 1)Z \rightarrow c = 2z + Z$$

 $x_3 = Z$ $x_2 = t$ $c = y = 2x_2 + x_3$
 $y = [1 2] \times$

```
%---- Problem 1 Part a ----
clear
close all
s = tf('s');
T = 16/(s^2+3*s+16);
step(T)
wn = sqrt(16);
damp = 3/(2*wn);
Ts = 4/(damp*wn);
Tp = pi/(wn*sqrt(1-damp^2));
Tr = (1/wn)*(1.76*damp^3-0.417*damp^2+1.039*damp+1);
OS = exp(-(damp*pi/sqrt(1-damp^2)))*100;
%---- Problem 1 Part b -----
clear
close all
s = tf('s');
T = 0.04/(s^2+0.02*s+0.04);
step(T)
wn = sqrt(0.04);
damp = 0.02/(2*wn);
Ts = 4/(damp*wn);
Tp = pi/(wn*sqrt(1-damp^2));
Tr = (1/wn)*(1.76*damp^3-0.417*damp^2+1.039*damp+1);
OS = exp(-(damp*pi/sqrt(1-damp^2)))*100;
%---- Problem 1 Part c ----
clear
close all
s = tf('s');
T = (1.05*10^7)/(s^2+(1.6*10^3*s)+(1.05*10^7));
step(T)
wn = sqrt(1.05*10^7);
damp = (1.6*10^3)/(2*wn);
Ts = 4/(damp*wn);
Tp = pi/(wn*sqrt(1-damp^2));
Tr = (1/wn)*(1.76*damp^3-0.417*damp^2+1.039*damp+1);
OS = exp(-(damp*pi/sqrt(1-damp^2)))*100;
```

```
%----- Problem 2 Part a -----
clear
close all
s = tf('s');
T = 1/(s^2+13.3*s+141.6);
step(T)
```

```
%---- Problem 2 Part b ----
clear
close all
s = tf('s');
T = 1/(s^2+0.919*s+0.607);
step(T)
```

```
%---- Problem 2 Part c ----
clear
close all

s = tf('s');
T = 1/(s^2+1.143*s+1.423);

step(T)
```

```
%---- Problem 4 Part a ----
clear

syms s

A = [0 1 0; 0 0 1; -1 -2 -3];
B = [10; 0; 0];
C = [1 0 0];
D = 0;

Phi = inv(s*eye(3)-A);
T = C*Phi*B+D;
[n,d] = ss2tf(A, B, C, D);
```

```
%----- Problem 4 Part b -----
clear

syms s

A = [-4 -1.5; 4 0];
B = [2; 0];
C = [1.5 0.625];
D = 0;

Phi = inv(s*eye(2)-A);

T = C*Phi*B+D;

[n,d] = ss2tf(A, B, C, D);
```