

## Unit's Digit

1. What is the unit's digit of the number  $19^{78} + 35^{39} + 43^{67}$ ?  
(a) 1 (b) 2 (c) 3 (d) 4
2. What is the unit's digit of the number  $23^{34} \times 34^{57} \times 57^{61}$ ?  
(a) 9 (b) 8 (c) 7 (d) 6
3. Aman wrote product of all natural numbers from 1 to 997 on a board. Naman came and erased all the multiples of 5. Find the unit's digit of the remaining number.  
(a) 6 (b) 7 (c) 8 (d) None of these
4. What is the unit's digit of the product of first 40 odd natural numbers?  
(a) 5 (b) 7 (c) 9 (d) Cannot be determined
5. Let us define function  $f(x)$  such that  $f(x)$  = Unit digit of  $x$ .  
Also,  $A = f(42^{78})$ ,  $B = f(45^{26})$ ,  $C = f(18^{39})$ , then which of the following is true?  
(a)  $A > B > C$  (b)  $A > C > B$  (c)  $B > C > A$  (d)  $B > A > C$
6. Find the unit's digit of  $N$ , where  $N = 16^{16!} + 17^{17!} + 18^{18!}$   
(a) 2 (b) 3 (c) 4 (d) 5
7. Rahim wrote a number  $A$  such that  $A = (xyz)^{4k+2}$ , where  $x, y, z$  and  $k$  are positive integers. For how many values of  $z$ , will the number  $A$  have unit's digit as 1?  
(a) 0 (b) 1 (c) 2 (d) 3
8. Devraj took a six digit number ending in 4 and raised it to an even power greater than 1000. He then took the number 12 and raised it to a power which leaves the remainder 2 when divided by 8. If he now multiplies both the numbers, what will be the unit's digit of the number he so obtained?  
(a) 3 (b) 4 (c) 5 (d) 6
9. The last digits in the expansion of the numbers  $(584a)^{149}$  and  $(584a)^{151}$  are 8 and 2 respectively. What can be said about the value of  $a$ ?  
(a)  $a = 8$  (b)  $a = 6$  (c)  $a = 4$  (d)  $a = 2$
10. What is the unit's digit of the number  $1! + 2! + 3! + 4! + 5! + \dots + 20!$ ?  
(a) 1 (b) 3 (c) 5 (d) 7
12. Find the unit's digit of the number  $(17^{33})^{67}$   
(a) 2 (b) 3 (c) 4 (d) 5
13. If the unit's digit of a number  $N = (1258a)^b$  remains  $a$  for all the values of  $b$ , then which of the following is true?  
(a) The number of values of  $a$  can be 2 (b) The number of values of  $a$  can be 3  
(c) The number of values of  $a$  can be 4 (d) The number of values of  $a$  can be 5
14. Let us define  $a_k$  = Unit's digit of  $[(15b)^k]$ . If  $a_1 + a_2 + a_3 + a_4 = 24$ , what is the value of  $b$ ?  
(a) 4 (b) 6 (c) 8 (d) None of these

## Factorial

1. Find the number of zeroes at the end of  $58!$

- (a) 10                      (b) 11                      (c) 12                      (d) 13

2. What power of 7 will divide  $80!$  exactly?

- (a) 11                      (b) 12                      (c) 13                      (d) 14

3. What power of 35 will divide  $62!$  exactly?

- (a) 9                      (b) 10                      (c) 11                      (d) 12

4. Which of the following cannot be the number of zeroes at the end of any factorial?

- (a) 26                      (c) 27                      (c) 28                      (d) 29

5. What will be the number of zeroes at the end of  $(36!)^{4!}$

- (a) 96                      (b) 168                      (c) 192                      (d) None of these

6. Find the number of zeroes at the end in the expression  $125 \times 64 + 25 \times 8 + 35 \times 12$

- (a) 0                      (b) 1                      (c) 2                      (d) 3

7. Find the maximum value of  $n$  for which the expression  $\frac{52!}{105^n}$  is an integer.

- (a) 8                      (b) 12                      (c) 23                      (d) 32

8. Kashish took a number  $N$  such that  $N!$  has 31 zeroes at the end. Also, the number  $N$  is a prime number. What is the sum of digits of the number  $N$ ?

- (a) 9                      (b) 10                      (c) 11                      (d) Data Inadequate

9. If  $490! = 7^p \times q$ , where  $q$  is not a multiple of 7, then find the value of  $p$ .

- (a) 79                      (b) 80                      (c) 81                      (d) 82

10. If  $N = (4!)^{4!} \times (6!)^{6!} \times (8!)^{8!} \times (10!)^{10!}$ , then find the number of zeroes at the end of  $N$

- (a)  $6! + 8! + 10!$                       (b)  $2 \times 6! + 8! + 10!$                       (c)  $6! + 2 \times 8! + 10!$                       (d)  $6! + 8! + 2 \times 10!$

11. If in the previous question, all  $\times$  are replaced by  $+$ , then the number of zeroes at the end of  $N$  will be.....

- (a)  $6! + 8! + 2 \times 10!$                       (b) 0                      (c)  $4!$                       (d) None of these

12.  $A =$  Product of first 50 multiples of 2.

$B =$  Product of first 8 multiples of 5

Find the number of zeroes at the end of  $A/B$ .

- (a) 3                      (b) 4                      (c) 5                      (d) 6