

* Slope intercept form of a line $\Rightarrow y = mx + c$ (1)

$$m = \tan \theta = \frac{a}{b}$$

* General forms to slope intercept form

$$ax + by + c = 0 \Rightarrow y = -\frac{a}{b}x - \frac{c}{b}$$

$$\omega_1 n_1 + \omega_2 n_2 + \omega_0 = 0$$

$$H \cdot P \rightarrow \omega_1 n_1 + \omega_2 n_2 + \omega_3 n_3 + \dots + \omega_d n_d + \omega_0 = 0 \rightarrow d \text{ dimensions.}$$

$$\Pi \rightarrow \omega^T n + b = 0$$

$\downarrow \leftarrow$
d-dim

$$* \text{ DOT product } \Rightarrow n_1 \cdot n_2 = (n_1 \mid n_2) \cos \theta = n_1^T n_2 = \sqrt{n_{11}^2 + n_{12}^2} \cdot \sqrt{n_{21}^2 + n_{22}^2} \cdot \cos \theta$$

$$\cos \theta = \frac{n_{11} n_{21} + n_{12} n_{22}}{\sqrt{n_{11}^2 + n_{12}^2} \sqrt{n_{21}^2 + n_{22}^2}} = \frac{n_1 \cdot n_2}{\|n_1\| \|n_2\|}$$

* DOT product of orthogonal vector is '0'.

$$* \begin{array}{l} \text{Diagram showing vectors } n \text{ and } \omega \text{ at origin } O. \\ \text{Angle between them is } \theta. \\ \text{Equation: } \|n\| \cos \theta + \omega_0 = 0 \\ \cos \theta = -\frac{\omega_0}{\|n\|} = \frac{a}{\|n\|} \end{array}$$

$$* \text{ Distance of plane to origin } \Rightarrow \frac{-\omega_0}{\|\omega\|}, \text{ or } \boxed{\frac{\text{dist}(O, \Pi)}{\|\omega\|}}$$

* +ve half space $\rightarrow \omega^T n_i + \omega_0 \geq 0 \rightarrow$ towards direction of ω .
 -ve half space $\rightarrow \omega^T n_i + \omega_0 < 0 \rightarrow$ opposite direction of ω .

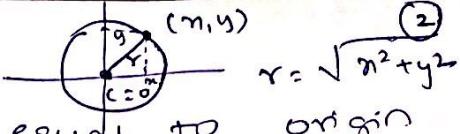
$$* \text{ Distance of point } n_i \text{ from plane } \omega^T n + \omega_0 = 0 \text{ is } \boxed{\frac{\omega^T n_i + \omega_0}{\|\omega\|}}$$

$$* \text{ Unit vector of any vector } \omega \Rightarrow \boxed{\frac{\omega}{\|\omega\|}} = \hat{\omega}$$

$$* \text{ Addition of vectors } \rightarrow \vec{ab} + \vec{bc} = \vec{ac}$$

Subtraction of vectors

$$\begin{bmatrix} n_1 \\ n_2 \\ n_3 \end{bmatrix} - \begin{bmatrix} y_1 \\ y_2 \\ y_3 \end{bmatrix} \Rightarrow n - y = \begin{bmatrix} n_1 - y_1 \\ n_2 - y_2 \\ \vdots \\ n_d - y_d \end{bmatrix}, n + y = \begin{bmatrix} n_1 + y_1 \\ n_2 + y_2 \\ \vdots \\ n_d + y_d \end{bmatrix}$$

- * equation of circle = $x^2 + y^2 = r^2$
- * equation of circle at centre not equal to origin

 $\Rightarrow \vec{OP} = \vec{OC} + \vec{CP} \Rightarrow \vec{r} = \vec{Ox} - \vec{Oc} \Rightarrow r = \sqrt{(x_1 - c_1)^2 + (x_2 - c_2)^2}$

* Point inside circle $\rightarrow ||n - c|| < r$, outside $\rightarrow ||n - c|| > r$ or
 on the circle $\rightarrow ||n - c|| = r$.

- * Ellipse equations $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ $\frac{x^2}{a^2} + \frac{y^2}{b^2} + \dots = 1$

- * Square area = a^2 , rectangle area = $a \times b$

CALCULUS FOR ML & AI

- * Domain of $f(n)$ \rightarrow set of possible values which a function can take.
- * Range of $f(n)$ \rightarrow values taken by function on y -axis.
- * $f(n)$ is continuous at 'a' if (i) $f(a)$ is defined at 'a'.

(ii) $\lim_{n \rightarrow a^+} f(n) = \lim_{n \rightarrow a^-} f(n) = f(a)$ (iii) $\lim_{n \rightarrow a} f(n)$ exists.

- * $\left. \frac{d f(n)}{d n} \right|_{n=y} = \text{slope of } T_4$. if slope $> 0 \rightarrow$ curve is increasing
 slope $< 0 \rightarrow$ curve is decreasing

* $\tan \theta = \frac{\Delta y}{\Delta x}$, $\left. \frac{dy}{dx} \right|_{n=n_1} = \lim_{(n_2 - n_1) \rightarrow 0} \frac{y_2 - y_1}{x_2 - x_1} = \lim_{\Delta x \rightarrow 0} \frac{\Delta y}{\Delta x}$

- * Derivative of common functions:-

(i) $\frac{d n^n}{d n} = n \cdot n^{n-1}; n \neq 0, n - \text{rational number.}$

(ii) $\frac{d \log(n)}{d n} = 1/n$ (iii) $\frac{d (e^n)}{d n} = e^n$

$\left. \frac{d n }{d n} \right \Rightarrow$ $n > 0 \rightarrow +1$ $n < 0 \rightarrow -1$ $n = 0 \rightarrow \text{not defined}$ as $\lim_{n \rightarrow 0^+} \neq \lim_{n \rightarrow 0^-}$

- * Function is not differentiable at
 → where ever the graph or curve is non-smooth
 → where ever the function is discontinuous.

* Rules of differentiation:-

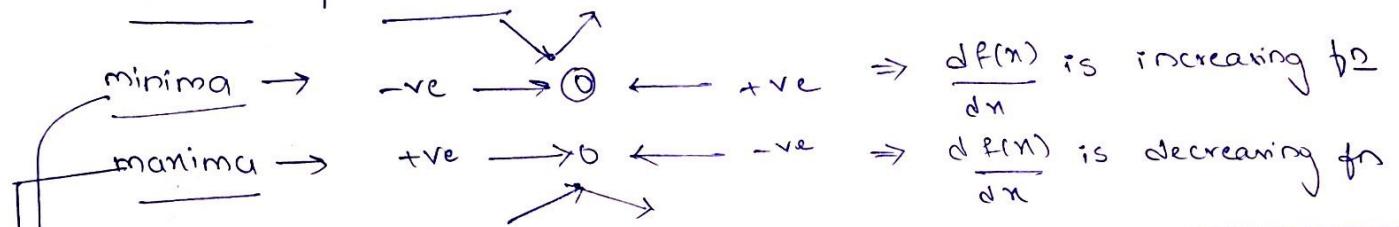
$$(i) \frac{d}{dx}(f(x) + g(x)) = \frac{df(x)}{dx} + \frac{dg(x)}{dx} \quad (ii) \frac{d}{dx}(\text{constant}) = 0$$

$$(iii) \text{Chain rule : } \frac{d f(g(x))}{dx} = f'(g(x)) \cdot g'(x)$$

$$(iv) \text{Product rule : } \frac{d}{dx} f(x) \cdot g(x) = f(x) \frac{dg}{dx} + g(x) \frac{df}{dx}$$

$$(v) \text{Quotient rule : } \frac{d}{dx} \left[\frac{f(x)}{g(x)} \right] = \frac{f'(x)g(x) - g'(x)f(x)}{[g(x)]^2}$$

* MAXIMA & MINIMA



$$\Rightarrow \frac{d}{dn} \left(\frac{df(x)}{dn} \right) > 0$$

$$\Rightarrow \frac{d}{dn} \left(\frac{df(x)}{dn} \right) < 0$$

Partial derivatives:-

$$z = x_1^2 + x_2^2 \Rightarrow \nabla z = \begin{bmatrix} \frac{\partial z}{\partial x_1} \\ \frac{\partial z}{\partial x_2} \end{bmatrix}$$

$$x = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$

$$\text{Let } z = f(x_1, x_2)$$

$$@ \text{Optima} \Rightarrow \nabla z = 0 \Rightarrow \nabla z = \begin{bmatrix} \frac{\partial z}{\partial x} \\ \frac{\partial z}{\partial y} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

→ we have special cases where the derivative of the function is '0' but it doesn't have either minima or maxima.

Those are called 'SADDLE POINTS' ex:- $f(x) = x^3$ at $x=0$

$$z = x^2 - y^2 \text{ at } x=0, y=0$$

→ Gradient descent $\Rightarrow n_1 = n_0 + \alpha \left(-\frac{\partial f}{\partial n} \right)_{n=n_0}$ (4)

$n_0 \uparrow y_0$ (randomly pick) tve constant \rightarrow learning rate.

$\exists f(n, y) \rightarrow n_1 = n_0 + \alpha \left(-\frac{\partial f}{\partial n} \right)_{n_0, y_0}, y_1 = y_0 + \alpha \left(-\frac{\partial f}{\partial y} \right)_{n_0, y_0}$

→ repeat till $\left(\frac{\partial f}{\partial n} \right)_{n_1, y_1}$ & $\left(\frac{\partial f}{\partial y} \right)_{n_1, y_1}$ are close to zero.

KEY words and identifiers

→ reserved words in python, cannot be used as variables, functions, classes and other identifiers.

→ 35 keywords. * import keyword, keyword.kwlist.

→ identifier identifies classes, functions, variables etc;

→ identifier → allows (a-z), (A-Z), (0-9), (-)

→ cannot begin with → digit

→ keyword cannot be used as identifier.

→ Comment → #, multiline comment, """ - """, "''' - "'''.

↳ do not come under the category of statements.

→ system to access docstring → (classname.__doc__).

→ ''' → used for multiline statements.

→ pr(id(x)) → prints the storage location of x.

→ Intervals [-5, 256] → all variables with similar value direct to same location, outside [-5, 256] → variables with similar values direct to different locations.

* type() → to know which class a variable/value belong to
→ type(a)

* isinstance() → to check if a given object belong to particular class → (isinstance(1+2j, complex))

Mutable → lists, dictionaries, sets

immutable → integers, floats, booleans, strings, tuples

→ set is unordered collection of unique elements.

(5)

→ sets do not allow repetition, slicing.

Output formating:-

print("The value is a is {} and b is {}".format(a,b))

print("The value is a is {} and b is {}".format(a,b))

print("The value is a is {} and b is {}".format(a=2, b=3))

print("The value is a is {} and b is {}".format(0, b=3))

operators:-

Arithmetic :- addition(+), subtraction(-), multiplication(*), division(/).

modulo division(%), floor division(/), exponent (**)

Comparison :- >, <, ==, !=, >=, <=

Logical :- and, or, not Bitwise :- &(and), |(or), NOT(~), XOR(^),

Bitwise rightshift(>>), Bitwise left shift(<<) Assignment :- =, +=,

-=, *=, /=, **= Identity operators :- is, is not (pointing to same location)

Membership :- in & not in (dict → it checks key values)

* The 'else' block of while loop runs only if the test expression is returning 'False' and if there is no break statement.

* Iterating over a sequence is called traversal.

* range(start, stop, step) → not store values in memory, just remember, start, stop, step.

* For loop can have an optional 'else' - executed if the items in the sequence used in for loop is exhausted. When

break is used, else is ignored.

lists:- (i) `len(A)` → length of list (6)

(ii) `list insert`:- `lst.insert(2, "three")` → will add element 4, at location 3.

(iii) `list remove`:- `lst.remove("two")` → it will remove first occurrence of 'two'.
→ Error when "two" not present in lst.

(iv) `list append`:- `lst.append("five")` → will append at the last.
`lst.append([1st2])` → [list1, ~~list2~~, list2] → appends the list
list2 as is to list1

(v) `list extend`:- `list1.append(list2)` → [list1, list2] → adds list2 directly to
`list1.extend(list2)` → [list1, list2] → adds elements to
list2.

(vi) `list delete`:- `lst.pop(i)` → index value
,

(vii) `list reverse`:- `lst.reverse()` → print(lst) → it will be reversed

(viii) `list sort()` :- sorts the original list itself. default - ASC
`list.sort()` → reverse

(ix) `list sorted()` :- returns the copy of sorted list. → True
`sorted(list)` → False for desc

NOTE:- whenever we want to sort a list make sure all elements belong to some datatype.

→ we can have multiple reference to list and when reference object changes, main object also changes.

→ str. `split(',')` → used to split a string using ',' - result in list.

Slicing → list [start(included) : stop(excluded) : step]

NOTE:- '+' is like 'extend' → [1, 2, 3] + [3, 4] ⇒ [1, 2, 3, 3, 4]

(x) `Count` :- `list.Count(element)` → counts # the element in list.

→ list comprehension examples:

* `newlist = [i**2 for i in list]` * `list2 = [i for i in list if i >= 0]`

* `list3 = [(i, i**2) for i in range(10)]`

→ nested list Comprehensions:

* `list = [[row[i] for row in matrix] for i in range(4)]`

Tuples:- mutable object inside tuple (immutable object) can be changed.

- * when we have only one element in tuple we need to use (element,) → like the datatype of that object will be of element.
- * '+' → concatenation of tuples → $(1, 2, 3) + (4, 5, 6) = (1, 2, 3, 4, 5, 6)$
- * del → we can use "del tuple" to delete tuple.
- * count() → tuple.count(1) → gives count of '1' in tuple.
- * index() → tuple.index(3) → gives index of first occurrence of '3' if '3' not present then error.
- * sorted() → Here sort() → doesn't work, only sorted(tuple) works.
- * max(), min() → gives max & min, but same datatype elements.

Sets:- unordered collection of unique items.

set.add(): adds single element → set.add(1)

set.update

set.update(): adds multiple elements → set.update([1, 2, 3, 4], [1, 2, 3, 4], {1, 2, 3})

→ NOTE:- cannot use dict in set.

Removal of elements from set:-

set.discard(3) → removes '3' - when element not present no error

set.remove(3) → removes '3' - when element not present error
(unlike list & tuple) throws error when set is

set.pop() → takes no argument, and removes random element, empty

set.clear() → removes all elements.

Set Operations:

Union: set1 | set2 (or) set1.union(set2)

intersection: set1.intersection(set2) (or) set1 & set2

difference: set1.difference(set2) (or) set1 - set2 a = [1, 2, 3], b = [3, 4]
a - b = [1, 2]

symmetric diff: set1.symmetric_difference(set2) (or) set1 ^ set2
a ^ b = [1, 2, 4]

; issubset(): set1.issubset(set2)

Frozenset(): - As tuples are the immutable lists, Frozensets are the immutable sets. → created by frozenset(). (8)

* frozenset() → supports copy(), difference(), intersection(), isdisjoint(), issubset(), is superset(), symmetric_difference() and union().
→ does not support → add or remove elements.

Dictionary(): - Dictionary key should be hashable. (list & sets cannot be used as keys in Dictionary)

→ Access(): dict['key'] or dict.get('key') → NO 'key' then error.

→ Add / modify(): dict['key'] = value

arbitrary items removes all
↑ ↑

→ Deletion / removal(): dict.pop('key') / dict.popitem() / dict.clear()
del dict['key']

Methods():

→ copy() → dict.copy() → returns copy of dict.

→ fromkeys() → a = {} . fromkeys(['a', 'b'], 0) creates a dict.

→ keys() → a.keys() → returns key of a. as list

→ values() → a.values() → returns all the values as list

→ items() → a.items() → returns all key-value pairs as a list of tuples.

→ dir() → to display a list of available methods.

Dictionary comprehensions():

(i) a = {k:v for k,v in d.items() if v>2} → creating new dict

(ii) d = {k+'c': v*2 for k,v in d.items() if v>2} → perform operations while creating.

String: - *String is a sequence of unicode characters. ⑦
→ all * strings are immutable - that is making changes to the existing values is not possible.

* + → concatenation * '*' - repetition

String methods

- (i) `upper()` → upper values (converts)
(ii) `lower()` → lower values (converts)
(iii) `split()` → str.split(^{splitwith('')})
(iv) `join()` → ' '.join(['a', 'b']) = 'a b'
 ↑ returns '-' if 'H' is not present
(v) `find()` → 'Hing'.find('H') = 0 (No replace()) - 'Hing'.replace("H", "D")
(vi) `reversed()` → reversed(str) → reverses the string
(vii) ~~sort()~~ → ~~str.sort()~~ →

Functions :-

- * avoids the repetition of code and make it reusable.
- * when returns is not done, function returns 'None'.
- * scope of variable is the portion of the programs upto which a variable gets recognised.
- * The lifetime of the variable inside a function is as long as the function executes.

Built in functions:-

- * `abs()` - absolute value , `all()` - takes an iterable and returns true if all elements are 'true' else returns 'false'. NOTE:- empty list always true.
- * `divmod()` → $\text{divmod}(9, 2) = \begin{pmatrix} 4 \\ 1 \end{pmatrix}$ ↑ Quotient remainder
- * `enumerate()` → `enumerate(list, number)` → returns tuple with index starting from 'number' and 1st elements.
- * `filter()` :- The filter() method constructs an iterator from elements of an iterable for which a function returns 'true'.
`filter(function, iterable)`

* Filter function will loop the input iterator and pass each element of the iterator through the function and creates an iterator with only those ~~functions~~ elements that do not return None, when passed through the function.

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isinstance() :- isinstance() function checks if the object (first argument) is an instance or subclass of class-name class (second argument). ∴ isinstance (object, class-name)

map() :- map (function-name, iterable-name)

→ map will apply the function 'function-name' to each and every element in the iterable 'iterable-name'. The result would be of map class. If we want to get the result in the form of list (or) a tuple (or) a set. Then we have to apply the list() (or) tuple() (or) set() functions on the map function output.

reduce() :-

* reduce() function is for performing some computation on a list and returning the result.

* It applies a rolling computation to sequential values pairs in a list.

From functools import reduce

```
def multiply(n,y):  
    return n*y.
```

```
product = reduce(multiply, list)
```

FUNCTION ARGUMENTS:-

(1)

(i) Default arguments: assigning a default value to the function argument, when a value is passed in the function call, default argument value is replaced else else default is used.

e.g:- def a(c=b='12'): → a() → op-k op-ij:
return b

NOTE:- At the time of function definition and function call we must make sure that non-default arguments come first and then the default arguments.

(ii) KEY WORD ARGUMENTS:-

- * we should use **kwargs - if we want to handle named arguments.
- * **kwargs is considered a dictionary and access is by using keys. access by kwargs[key].

(iii) ARBITRARY ARGUMENTS:-

- * *args → represent arbitrary arguments. we don't know how many arguments can be given them by index or looping. tuple(*args).

RULES OF ARGUMENTS:-

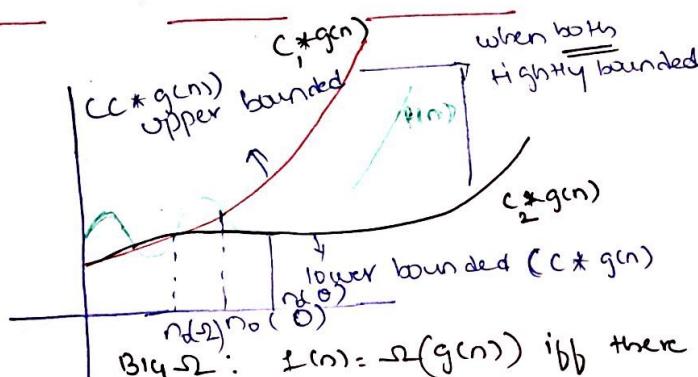
- * Keyword arguments must follow positional arguments if any.

INSERTION SORT:-

- (i) two subarrays unsorted & sorted (ii) each element in unsorted subarray compared with sorted subarray and inserted in appropriate position.

- * Insertion sort is an "inplace" algorithm. as it consumes the constant amount of additional memory irrespective of the ilp size.
- * Insertion sort is an stable sorting algorithm as the initial order of the same key value is retained even after sorting using an sorting algorithm.
- * Insertion sort is an online sorting algorithm as it can sort the data that is given to us over time.
- * Insertion sort time complexity: Best case: $O(n)$ worst case: $O(n^2)$
space complexity: $O(1)$

BIG O, Θ , Ω , \mathcal{O} , ω :-



BIG-O: $f(n) = O(g(n))$ iff there exists a no, c s.t
 $0 \leq c * g(n) \leq f(n)$ for all $n \geq n_0$

BIG O: $f(n) = O(g(n))$ if and only if there exists some n_0 and c such that $0 \leq f(n) \leq c * g(n)$ for all $n \geq n_0$.

BIG Ω : $f(n) = \Omega(g(n))$ iff there exists some n_0, c_1, c_2 s.t $0 \leq c_1 * g(n) \leq f(n) \leq c_2 * g(n)$ for all $n \geq n_0$.

NOTE: if $f(n) = \Theta(g(n))$ then $f(n) = O(g(n))$ & $f(n) = \Omega(g(n))$

small O :- $f(n) = O(g(n))$ for some c.

small ω :- $f(n) = \omega(g(n))$ for all c.

small Ω :- $f(n) = \Omega(g(n))$ for all c.

alternate def:- $f(n) = O(g(n))$ iff $\lim_{n \rightarrow \infty} \frac{f(n)}{g(n)} = 0$

small ω :- definition -1:- $f(n) = \omega(g(n))$ iff $g(n) = O(f(n))$

definition 2: $f(n) = \omega(g(n))$ iff $\forall c > 0 \exists n_0 > 0$ s.t $0 \leq c * g(n) < f(n) \forall n \geq n_0$

definition 3: $f(n) = \omega(g(n))$ iff $\lim_{n \rightarrow \infty} \frac{f(n)}{g(n)} = \infty$

NOTE: $O, \Theta, \Omega, o, \omega$ → are called asymptotic notations.

* mathematical operators to understand the relationship b/w $O, \Theta, \Omega, o, \omega$

$$(i) f(n) = O(g(n)) \rightarrow f \leq g$$

$$(iii) f(n) = \Theta(g(n)) \rightarrow f = g$$

$$(ii) f(n) = \Omega(g(n)) \rightarrow f \geq g$$

$$(iv) f(n) = o(g(n)) \rightarrow f < g$$

$$(v) f(n) = \omega(g(n)) \rightarrow f > g$$

- transitive property :- If $f(n) = \Theta(\Omega(\omega(g(n))))$ & $g(n) = \Theta(\Omega(\omega(h(n))))$ then
 $f(n) = \Theta(\Omega(\omega(h(n))))$ - holds for all asymptotic notations
- Reflexive relationship :- $f(n) = \Omega(\Omega(f(n))) \Rightarrow f(n) \leq f(n)$ - holds for $(O\Theta\Omega)$
- Symmetric relationship :- $f(n) = \Theta(g(n))$ iff $g(n) = \Theta(f(n))$ | $f=g$ iff $g=f$.
- Transpose symmetry :- $f(n) = O(g(n))$ iff $g(n) = \Omega(f(n))$ | $f \leq g$ iff $g \geq f$.
 $f(n) = o(g(n))$ iff $g(n) = \omega(f(n))$ | $f < g$ iff $g > f$.

NOTE :- TRICHOTOMY DOES NOT HOLD FOR ASYMPTOTIC NOTATIONS. (i.e. a/b are # then any of these $a=b$, $a>b$, $a<b$ are true)

ORDERS OF COMMON FUNCTIONS :-

$O(1)$	$O(\log \log n)$	$O(\log n)$	$O((\log n)^c)$	$O(n^c)$	$O(n)$	$O(n \log^* n)$	\sim
constant	$\frac{1}{\log}$ double log	\log	$c > 1$ poly log	$c < 1$ fraction pow	linear	$n \log^* n$	
$O(n \log n) = O(\log n!)$	$O(n^2)$	$O(n^c)$	$c > 2$ polynomial	$\ln(a_1 c) = e^{(c+O(1))(\ln n)^c}$	$(\ln \ln n)^{1-\alpha}$		
log linear, quasilinear	quadratic						L Notation
$< O(c^n)$	$< O(n!)$						
$c > 1$ exponentials	factorial						

NOTE :- If $f(n) = a_0 + a_1 n + a_2 n^2 + \dots + a_m n^m$, $f(n)$ is polynomial of degree 'm'.
then $f(n) = O(n^m)$; $O(n^{m+1})$; $O(n^{m+k})$ where $k \geq 0$
 $f(n) = \Omega(n^m)$; $\Omega(n^{m-1})$; $\Omega(n^{m-k})$ where $k \geq 0$
 $f(n) = \Theta(n^m)$.

Geometric series :- $s_n = \frac{a_1(1-r^n)}{(1-r)}$, $r \neq 1$ where n is # of terms, a_1 first term, r is the common ratio.
finik \uparrow geometric series $r = \frac{a_2}{a_1}$ n^{th} term - $a_1 r^{n-1}$

→ infinite geometric series having ratios with an absolute value
less than one, → else no sum. Use the formula $\boxed{s = \frac{a_1}{1-r}}$

Arithmetic progression :- terms in the sequence are said to increase by a common difference 'd'. n^{th} term $\rightarrow a + (n-1)d$, sum $= \frac{n}{2} [2a + (n-1)d]$

sum of n natural numbers $\rightarrow \frac{n(n+1)}{2}$

sum of squares of n # $\rightarrow \frac{n(n+1)(2n+1)}{6}$

sums of n # $\rightarrow \left[\frac{n(n+1)}{2} \right]^2$

* Divide & conquer \rightarrow dividing large problem to small subproblems (divide) (4)
and combine them in some form to solve the larger problems (conquer).

\rightarrow recursion is popular choice.

	iterative	recursive
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$a^b \rightarrow$	time complexity	$O(b)$	$O(\log b)$
	space complexity	$O(1)$	$O(\log b)$

\rightarrow two types of dynamic programming

(i) top down DP \rightarrow recursion + bsp (memoization) \rightarrow top-down

(ii) bottom up DP \rightarrow iteration + bsp (tabulation) Bottom up better to use
itter recur

\rightarrow Fibonacci - time complexity $O(n)$ $O(2^n)$
space complexity $O(n)$ $O(1)$ + call stack

\rightarrow Longest common subsequence itter recur $n \rightarrow \text{len}(a), n \rightarrow \text{len}(b)$
 $O(m \times n)$ 2^b $b \in \max(m, n)$

\rightarrow Merge sort \rightarrow Best case time complexity } $O(n \log n)$
worst case time complexity }
Best case space complexity } $O(n)$.
worst case space complexity }

Note:- merge sort is the external sorting algorithm

\rightarrow Linear search :- worst case time complexity $- O(n)$
best case time complexity $- O(1)$
worst & best case space complex $- O(1)$

\rightarrow Binary search :- works only on sorted arrays
worst case time complexity $- O(\log n)$ or $\Theta(\log n)$
best case time complexity $- O(1)$
worst & best case space complex $- O(1)$ or $\Theta(1)$

* matrix multiplication \rightarrow time complexity recurrence $\Omega(2^n)$ Iterative $O(n^3)$

* subset sum problem \rightarrow Brute force $- 2^n$
DP $- O(n \times \text{sum})$. if $\text{sum} = 2^n$ the DP is waste

* matrix multiplication \rightarrow Optimal substructure

$$m[i,j] = \begin{cases} 0 & \text{if } i > j \\ \min_{1 \leq k < j} m[i,k] + m[k+1,j] + p_{i-1} \times p_k \times p_j & \text{if } i \leq j. \end{cases}$$

* subset sum problem \rightarrow false if $n > 0$ & $\text{sum} > 0$
true if $\text{sum} = 0$
 $s(n-1, \text{sum})$ (or) $s(n-1, \text{sum} - \text{arr}[n])$.

Lambda functions:- # lamb = lambda x: x*2 ; print(lamb(5)) 15

Use with filter:- evenlist = list(filter(lambda x: (x%2 == 0), [1,2,3,4,5]))

UX with map:- maplist = list(map(lambda x: x**2, list))

UX with reduce:- reduces = reduce(lambda x,y: x*y, list)

- * Irrespective of whether an exception occurs or not, the 'finally' block gets executed.
- * When no exception occurs in try then only else will be executed.

Multi Threading & Multiprocessing:-

Multiprocessing:- from multiprocessing import process, Queue.

start() → Start the process, join() → combine the processes

→ thread: light weight process with faster context switching

→ from threading import thread.

→ GIL - Global Interpreter Lock, Python's memory management is not thread safe.

Joblib:- simple parallel computing library in python : from joblib import parallel, delayed

SQL:-

DML: insert, update, delete
call, explain call, lock

DDL: create, alter, truncate
drop, modify, comment, rename

DQL: select

set

DCL: grant, revoke , TCL - commit, savepoint, Roll Back, set transaction, constraint