# Database Systems Lecture02 – Introduction to Relational Model

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### Relation

■ Relation = Table

# attributes (or columns)

	-			
ID	name	dept_name	salary	
10101	Srinivasan	Comp. Sci.	65000	
12121	Wu	Finance	90000	ŀ
15151	Mozart	Music	40000	,
22222	Einstein	Physics	95000	
32343	El Said	History	60000	ı
33456	Gold	Physics	87000	ı
45565	Katz	Comp. Sci.	75000	ı
58583	Califieri	History	62000	ı
76543	Singh	Finance	80000	ı
76766	Crick	Biology	72000	ı
83821	Brandt	Comp. Sci.	92000	1
98345	Kim	Elec. Eng.	80000	- 53

#### tuples

(or rows or records)

#### **Domain: Attribute Types**

- Domain is the <u>set of allowed values</u> for each attribute
  - Domain = data type + constraints
  - Eg. score domain: 0~100

Attribute values need to be atomic

Name_N_ID	Department
Alice 001	Comp. Sci.
Bob 002	Elec. Eng.
Charlie 003	NULL

Name	ID	Department
Alice	001	Comp. Sci.
Bob	002	Elec. Eng.
Charlie	003	NULL





■ The special value *null* is a member of every domain

#### Relation Schema and Instance

 $\blacksquare A_1, A_2, ..., A_n$  are **attributes** 

■  $R = (A_1, A_2, ..., A_n)$  is a **relation schema** Example:



instructor = (ID, name, dept name, salary)

a relation is an instance, i.e., a set of tuples

ID	name	dept_name	salary
10101	Srinivasan	Comp. Sci.	65000
12121	Wu	Finance	90000
15151	Mozart	Music	40000
22222	Einstein	Physics	95000
32343	El Said	History	60000
33456	Gold	Physics	87000



#### **Relations are Unordered**

- Order of tuples is irrelevant (tuples may be stored in an arbitrary order)
  - i.e., a relation is a set.
- Example: instructor relation with unordered tuples

ID	name	dept_name	salary
22222	Einstein	Physics	95000
12121	Wu	Finance	90000
32343	El Said	History	60000
45565	Katz	Comp. Sci.	75000
98345	Kim	Elec. Eng.	80000
76766	Crick	Biology	72000
10101	Srinivasan	Comp. Sci.	65000
58583	Califieri	History	62000
83821	Brandt	Comp. Sci.	92000
15151	Mozart	Music	40000
33456	Gold	Physics	87000
76543	Singh	Finance	80000

#### **Database**

- A database consists of multiple relations
- e.g.) a university database consists of

```
instructor relation
```

student relation

advisor relation

#### Key

• Q: What attribute plays the most significant role in the following relation?

Key attribute(s) uniquely identify a record in a table

ID	name	dept_name	salary
22222	Einstein	Physics	95000
12121	Wu	Finance	90000
32343	El Said	History	60000
45565	Katz	Comp. Sci.	75000
98345	Kim	Elec. Eng.	80000
76766	Crick	Biology	72000
10101	Srinivasan	Comp. Sci.	65000
58583	Califieri	History	62000
83821	Brandt	Comp. Sci.	92000
15151	Mozart	Music	40000
33456	Gold	Physics	87000
76543	Singh	Finance	80000

#### **Definition of Keys**

- Let K ⊆ R
- *K* is a **superkey** of *R* if values for *K* are sufficient to identify a unique tuple in relation *R*.
  - Example: {ID} and {ID,name} are both superkeys of instructor.

- Minimal superkey is called candidate key
  Example: {ID} is a candidate key for Instructor
- One of the candidate keys is selected to be the primary key.

#### **Relational Query Languages**

- Two mathematical Query Languages
  - Relational algebra
    - More operational
    - Useful for representing execution plans
  - Relational calculus
    - More declarative, i.e., describes what they want rather than how to compute it.
    - Rather theoretical, so not covered in this class
    - Eg. Find students whose SSN is 10.

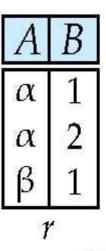
$$\{t \mid t \in STUDENT \land t[ssn] = 123\}$$

#### Relational Query Languages

- Relational operators
  - 5 fundamental relational operators
    - Union ( $\cup$ )
    - Selection ( $\sigma$ )
    - Projection  $(\Pi)$
    - Cartesian Product (x)
    - Set Difference (-)

# Union ( $\cup$ )

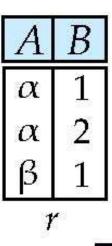
■ Relations r, s:



 $r \cup s$ :

# Set difference ( – )

■ Relations *r*, *s*:



$$egin{array}{c|c} A & B \\ \hline $\alpha$ & 2 \\ $\beta$ & 3 \\ \hline $s$ \\ \hline \end{array}$$

$$r-s$$
:

#### Selection ( $\sigma$ )

- Selection picks rows
- Relation r
- Select tuples with A=B and D > 5

$\boldsymbol{A}$	В	C	D
α	α	1	7
α	β	5	7
β	β	12	3
β	β	23	10

 $\bullet \quad \mathbf{O}_{A=B \land D>5} (r)$ 

A	В	C	D
α	α	1	7
β	β	23	10

#### Selection ( $\sigma$ ) - Example

■ Find 'Comp. Sci.'. major student named "Kim"

#### Student

ID	name	dept_name
10	Kim	Comp. Sci.
20	Lee	Biology
30	Kim	Electrical Eng.

#### Projection (Π)

- Projection picks columns and removes duplicates
- Relation *r*:

A	В	C
α	10	1
α	20	1
β	30	1
β	40	2

- Select A and C
  - Projection
  - Π<sub>A,C</sub> (r)

#### Projection (Π) - Example

- Find ID of 'Comp. Sci.'. major students.
  - Hint: relational operators can be cascaded

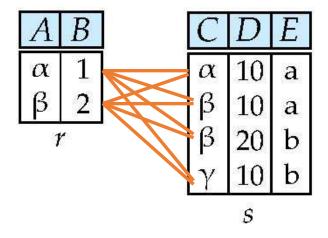
ID	name	dept_name
10	Kim	Comp. Sci.
20	Lee	Biology
30	Kim	Electrical Eng.

■ 
$$\Pi_{ID}(\sigma_{dept\_name = 'Comp. Sci.'}$$
 (Student))

#### Cartesian Product (x)

Cartesian Product generates all possible pairs

■ Relations *r, s*:



r x s:

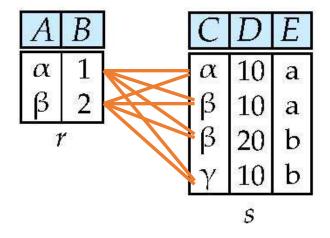


works as in nested loops:
 for each row i in r
 for each row j in s
 output i,j

#### Cartesian Product (x)

Cartesian Product generates all possible pairs

■ Relations *r, s*:



r x s:

A	В	C	D	E
α	1	α	10	a
α	1	β	10	a
$\alpha$	1	β	20	b
α	1	γ	10	b
β	2	α	10	a
β	2	β	10	a
β	2	β	20	b
β	2	γ	10	b

works as in nested loops:
 for each row i in r
 for each row j in s
 output i,j

■ Find name of students who take course 'swe3003'

Student

ID	name	dept_name
10	Kim	Comp. Sci.
20	Lee	Biology

ID	c_id	grade
10	swe2021	А
20	swe3003	В
30	sw4016	Α

Take

ID	name	dept_name	ID	c_id	grade
10	Kim	Comp. Sci.	10	swe2021	А
10	Kim	Comp. Sci.	20	swe3003	В
10	Kim	Comp. Sci.	30	sw4016	А
20	Lee	Biology	10	swe2021	А
20	Lee	Biology	20	swe3003	В
20	Lee	Biology	30	sw4016	А

Student x Take

■ Find name of students who take course 'swe3003'

Student

ID	name	dept_name
10	Kim	Comp. Sci.
20	Lee	Biology

ID	c_id	grade
10	swe2021	Α
20	swe3003	В
30	sw4016	Α

	ID	name	dept_name	ID	c_id	grade	
	10	Kim	Comp. Sci.	10	swe2021	А	
_	10	Kim	Comp. Sci.	20	swe3003	В	
	10	Kim	Comp. Sci.	30	sw4016	A	
	20	100	Riology	10	swo2021	Δ	
	20	Loo	Diology	20	3WCZOZI	D	
	20	Lee	Biology	20	swe3003	В	
	20	Lee	Biology	30	sw4016	A	

$$\sigma_{\text{Student.ID=Take.ID}}$$
 (Student x Take)

■ Find name of students who take course 'swe3003'

Student

ID	name	dept_name
10	Kim	Comp. Sci.
20	Lee	Biology
•••		

ID	c_id	grade
10	swe2021	А
20	swe3003	В
30	sw4016	Α

ID	name	dept_name	ID	c_id	grade	
10	Kim	Comp. Sci.	10	swe2021	A	
		'				
10	Kim	Comp. Sci.	20	swe3003	В	
10	Kim	Comp. Sci.	30	sw4016	A	
		'				
20	Lee	Biology	10	swe2021	A	
20	Lee	Biology	20	swe3003	В	
20	Lee	Biology	30	sw4016	A	
)	)	biology		344 10 10		

$$\sigma_{\text{Student.ID=Take.ID} \land c_{\text{id='swe}3003}}$$
, (Student x Take)

Find name of students who take course 'swe3003'

Student

ID	name	dept_name
10	Kim	Comp. Sci.
20	Lee	Biology

ID	c_id	grade
10	swe2021	А
20	swe3003	В
30	sw4016	Α

ID		name	dep	t_name	ID	c_id		grade
10		Kim	Con	ъ. Sci.	10	swe2	2021	A
1(	)	Kim	Con	<del>np. Sci.</del>	20	swe	8003	B
10	)	Kim	Con	<del>ıp. Sci.</del>	30	sw4(	)16	A
20		Lee	Biol	<del>ogy</del>	10	swe2	021	A
20		Lee	Biol		20	swe	3003	В
2(		Lee	Biol	ogy	30	sw4(	)16	A

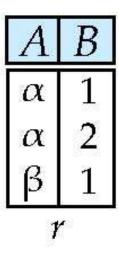
$$\Pi_{\text{name}}$$
 ( $\sigma_{\text{Student.ID=Take.ID}} \wedge c_{\text{id='swe3003'}}$  (Student x Take))

#### 5 relational operators are enough! But,

- 5 fundamental relational operators are enough to write any query
  - Union (∪)
  - Selection (σ)
  - Projection  $(\Pi)$
  - Cartesian Product (x)
  - Set Difference (-)
- But, derived operators, for convenience
  - Set intersection ( ∩ )
  - Join (⋈)
  - Rename ( $\rho$ )
  - Division (÷)
  - Group by (G)

# Set Intersection of two relations ( ∩ )

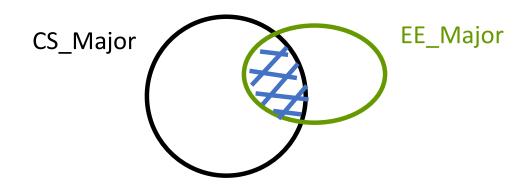
■ Relation *r, s*:



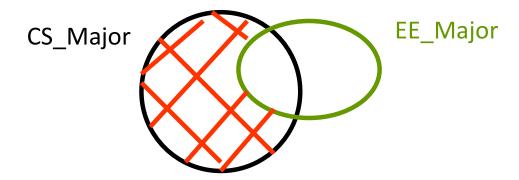
$$egin{array}{c|c} A & B \\ \hline $\alpha$ & 2 \\ $\beta$ & 3 \\ \hline $s$ \\ \hline \end{array}$$

$$r \cap s$$

#### **Observation**



CS\_Major ∩ EE\_Major =CS\_Major − (CS\_Major − EE\_Major)



So,  $\cap$  is not fundamental

#### Natural Join ( ⋈ )

- Natural Join
  - R  $\bowtie$  S =  $\prod_{\text{R.a. R.b.}} ... (\sigma_{\text{R.a=S.a} \land \text{R.b=S.b} \land} ... (\text{R x S}))$
  - For each pair of tuples  $t_R$  from R and  $t_S$  from S,
  - If  $t_R$  and  $t_S$  have the same values on common attributes, add a tuple t to the result, where
    - t has the same value as  $t_R$
    - t has the same value as  $t_s$
    - Drop duplicate attributes

#### Natural Join ( ⋈ ) - Example

Find name of students who take course 'swe3003'

Student

ID	name	dept_name
10	Kim	Comp. Sci.
20	Lee	Biology
30	Kim	Electrical Eng.

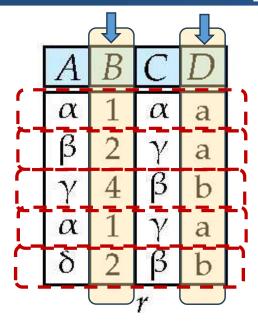
ID	c_id	grade
10	swe2021	Α
20	swe3003	В
30	sw4016	Α

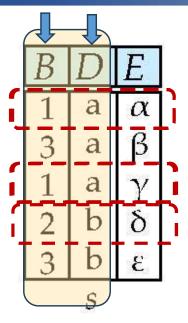
		_							
ı	ID		name	dep	t_name	c_ic		8	grade
	<del>10</del>		Kim	Con	<del>ıp. Sci.</del>		2021	_	λ
2	20		Lee	Biol	ogy	swe	3003	ı	3
	30		Kim	Elec	trical Eng.		4016	_	λ
		•				•			

$$\Pi_{\text{name}}$$
 ( $\sigma_{\text{c_id='swe3003'}}$  (Student  $\bowtie$  Take))

#### Natural Join with multiple common attributes

■ Relations r, s:





**Natural Join** 

 $r \bowtie s$ 

A	В	C	D	Ε
α	1	α	a	α
$\alpha$	1	α	a	γ
$\alpha$	1	γ	a	α
α	1	γ	a	γ
δ	2	β	b	δ

#### rename ( $\rho$ )

$$ho_{AFTER}(BEFORE)$$

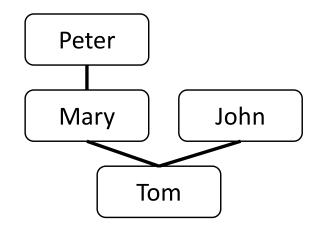
**Q**: why?

A: The same table is used multiple times

# rename ( $\rho$ )

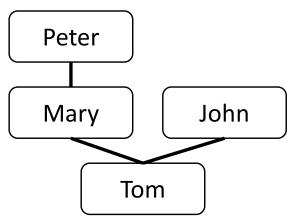
find the grand-parents of 'Tom', given PC(parent-id, child-id)

parent	child
Mary	Tom
Peter	Mary
John	Tom



#### rename ( $\rho$ )

find the grand-parents of 'Tom', given PC(parent-id, child-id)



parent	child
Mary	Tom
Peter	Mary
John	Tom

parent	child
Mary	Tom
Peter	Mary
John	Tom

• We need two different names for the same table hence, the 'rename' op.

$$\sigma_{\,\text{PC1.child=PC.parent}}$$
 (  $\rho_{\text{PC1}}$  (PC) x PC )

#### Division (÷)

Useful for expressing queries like:
Find students who have taken all CS courses.

- Suppose R has 2 attributes (x,y) and S has (y).
- Then  $R \div S$  returns the set of x's that match all y values in S.
- **Example:** R = Friend(x,y). S = set of 10 students.
  - Then  $R \div S$  returns the set of all x's that are friends with all 10 students.

# Division (÷) - Example

■ Find ID of students who take all 'Comp. Sci' courses

Take

ID	c_id
10	swe3003
10	ece2031
20	swe3003
20	swe4021
20	ece2031
30	swe3003
30	swe4021

dept_name	c_id
Comp. Sci.	swe3003
Comp. Sci	swe4021
Electrical Eng.	ece2031

Course

$$\Pi_{\text{c_id}} \sigma_{\text{dept_name= 'Comp. Sci.'}}$$
 (Course)

c\_id swe3003 swe4021

$$Take \div (\Pi_{c_id} \sigma_{dept_name='Comp. Sci.'}, (Course))$$

ID	
20	
30	

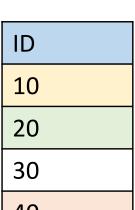
### Division (÷) - Example

Find ID of students who work on all projects of S#

R

ID	proj_no
10	p1
10	p2
10	р3
10	p4
20	p1
20	p2
30	p2
40	p2
40	p4

proj_no
p2
<b>S</b> 1



proj_no
p2
p4
52

D	
.0	
20	ID
0	10
0	40

proj_no	
p1	
p2	
p4	
<b>S</b> 3	

ID 10

#### **Observations**

■ Division (÷) is reverse of cartesian product

It can be derived from the 5 fundamental operators

$$r \div s = \pi_{(R-S)}(r) - \pi_{(R-S)}[(\pi_{(R-S)}(r) \times s) - r]$$

### Let's practice using the following schema

- branch (branch-name, branch-city, assets)
- customer (customer-name, customer-street, customer-only)
- account (account-number, branch-name, balance)
- loan (loan-number, branch-name, amount)
- depositor (customer-name, account-number)
- borrower (customer-name, loan-number)

#### **Example Queries in Relational Algebra**

loan (loan-number, branch-name, amount)

Find all attributes of loans of over \$1200

$$\sigma_{amount > 1200}$$
 (loan)

■ Find the loan number for each loan of an amount greater than \$1200

$$\prod_{loan-number} (\sigma_{amount > 1200} (loan))$$

#### Example Queries in Relational Algebra

depositor (customer-name, account-number)

borrower (customer-name, loan-number)

Find the names of all customers who have a loan, an account, or both, from the bank

$$\prod_{\text{customer-name}}$$
 (borrower)  $\cup \prod_{\text{customer-name}}$  (depositor)

Find the names of all customers who have a loan and an account at bank.

$$\prod_{\text{customer-name}}$$
 (borrower)  $\cap \prod_{\text{customer-name}}$  (depositor)

#### **Example Queries in Relational Algebra**

loan (loan-number, branch-name, amount) borrower (customer-name, loan-number) depositor (customer-name, account-number)

■ Find the names of customers who have a loan at Suwon branch.

$$\prod_{customer-name} (\sigma_{branch-name="Suwon"} (borrower \bowtie loan)))$$

Find the names of all customers who have a loan at the Suwon branch but do not have an account at any branch of the bank.

$$\prod_{customer-name} (\sigma_{branch-name = "Suwon"} (borrower \bowtie loan))$$

$$- \prod_{customer-name} (depositor)$$