Medical Image Processing for Diagnostic Applications

Basic Principles of Tomography

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Topics

Tomography

Projection

Summary

Take Home Messages
Further Readings







Basic Principles of Tomography

τόμος ['tomos] \rightarrow slice

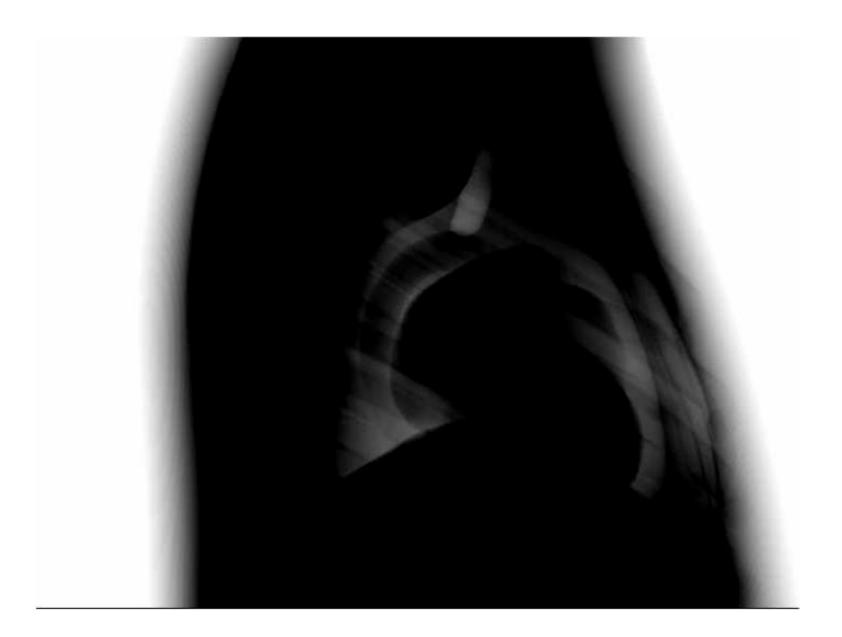


Figure 1: Single chest phantom projection

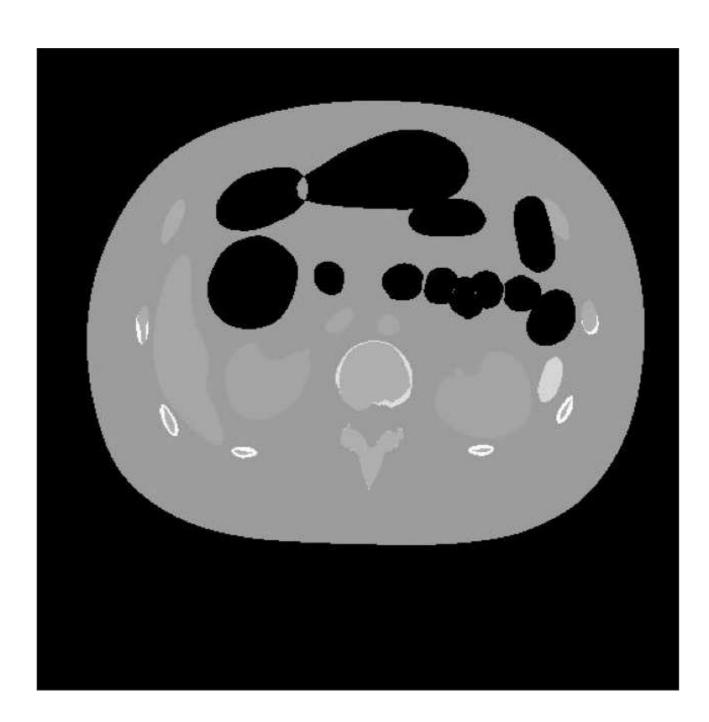


Figure 2: Slice view (click for video)







Basic Principles of Tomography

Idea: Observe the object of interest from multiple sides:

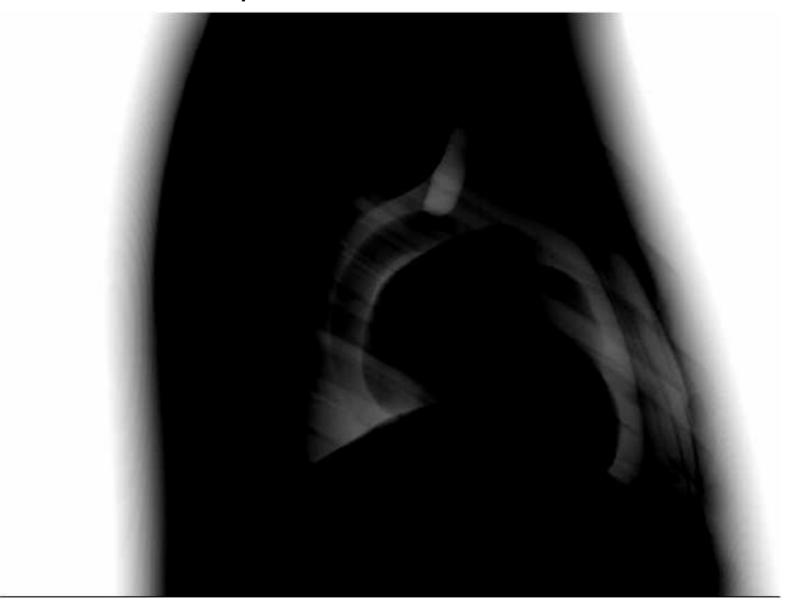


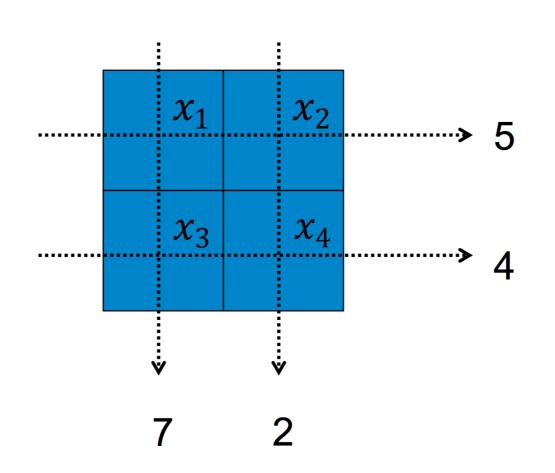
Figure 3: Multiple scan views (click for video)





Basic Principles of Tomography

Solve the puzzle:



$x_1+x_3=7$		$x_1 = 3$
$x_2+x_4=2$	\Rightarrow	$x_2 = 2$
$x_1+x_2=5$		$x_3 = 4$
$x_3+x_4=4$		$x_4 = 0$

- Usually, the problem size in CT is $512 \times 512 \times 512 = 134217728$.
- How can this problem be solved?







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Projection: X-ray Attenuation

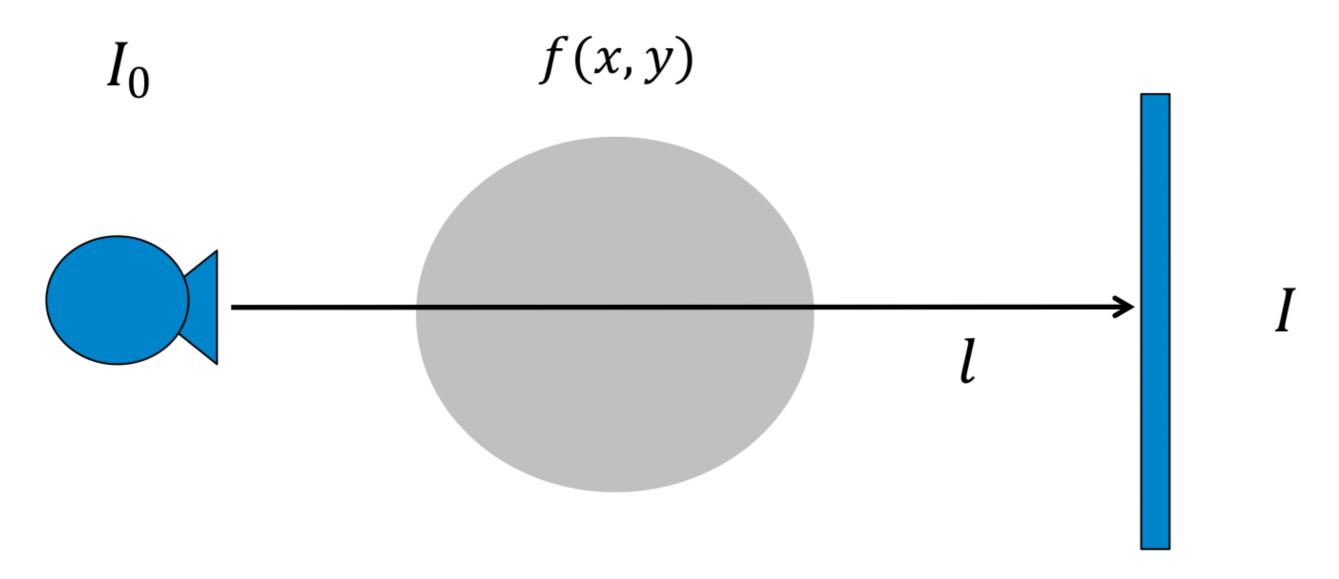


Figure 4: Beer–Lambert law: $I = I_0 e^{-(\int f(x,y) dI)}$







Projection: Physical Observations

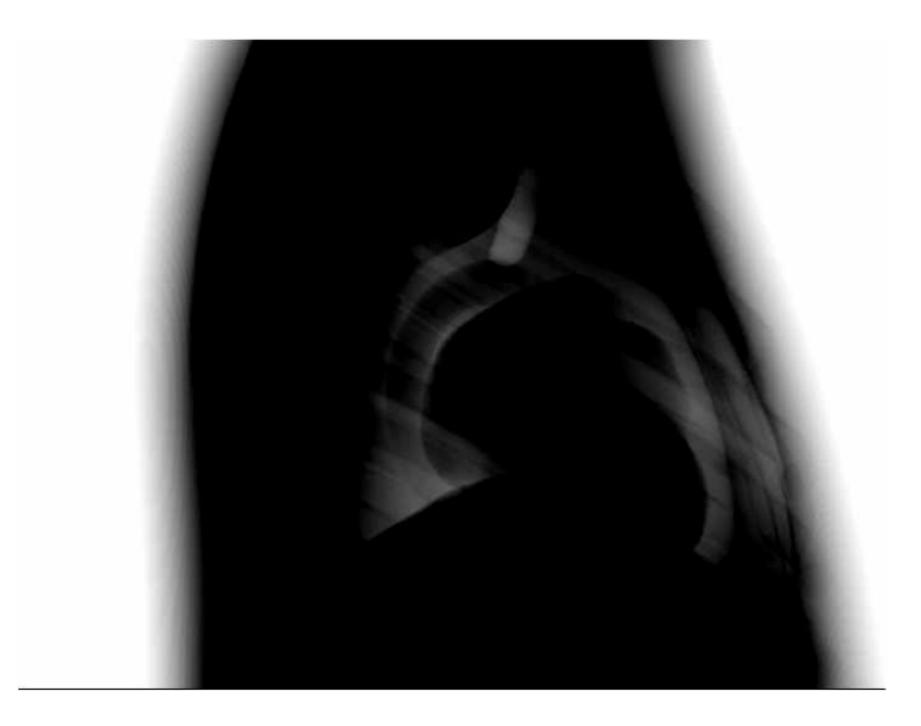


Figure 5: Observed projection signal (click for video)







Projection: Physical Observations



Figure 6: Line integral data (click for video)







Projection Formation



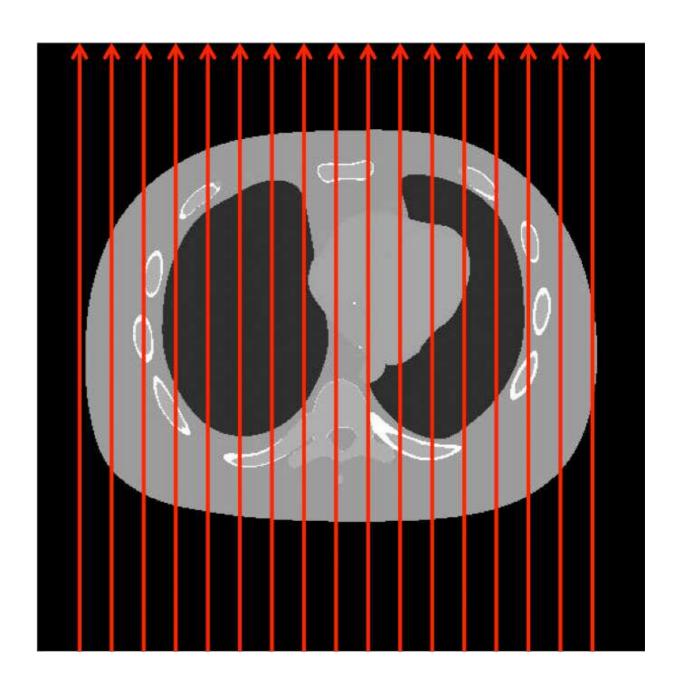


Figure 7: Slice by slice projection (left), projection ray scheme (right)







Projection: Mathematical Formulation

$$p(s,\theta) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} f(x,y) \delta(x \cos \theta + y \sin \theta - s) dx dy$$

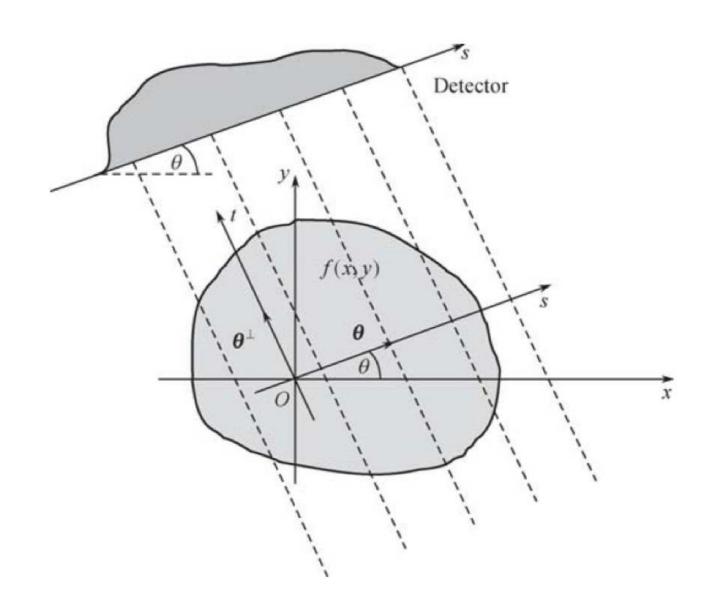


Figure 8: Parallel beam geometry (Zeng, 2009)







Projection: Example Point Object

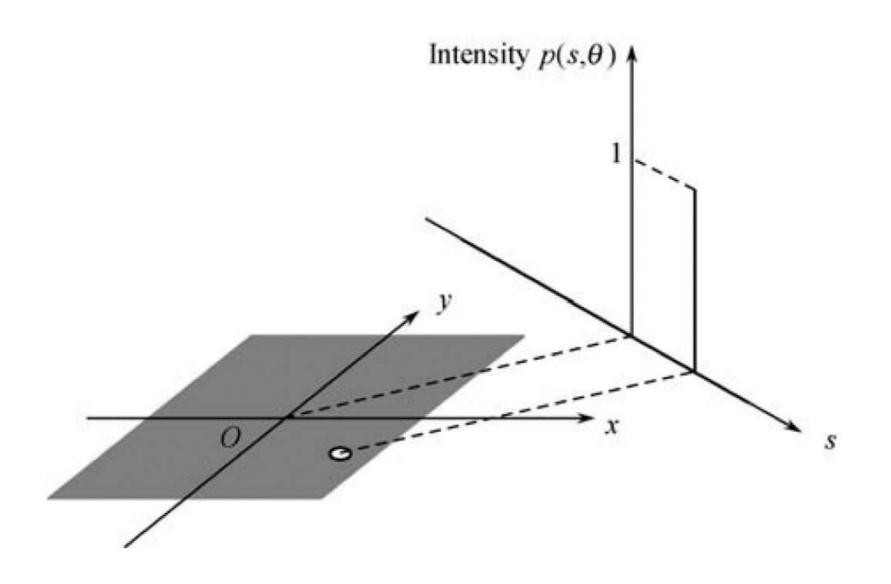


Figure 9: Intensity profile of a point object (Zeng, 2009)







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Take Home Messages

- Tomography is looking through an object from several angles and recombining the projection views back to a 3-D volume of the object.
- 3-D data is usually represented as a stack of slices.
- The Beer-Lambert law describes the attenuation of X-rays on their path through an object.
- A single projection can be regarded as the integral of projections of every point inside the object.







Further Readings

Students learning about reconstruction should have a look at one of the following books:

- Gengsheng Lawrence Zeng. Medical Image Reconstruction A Conceptual Tutorial. Springer-Verlag Berlin Heidelberg, 2010. DOI: 10.1007/978-3-642-05368-9
- Avinash C. Kak and Malcolm Slaney. Principles of Computerized Tomographic Imaging. Classics in Applied Mathematics. Accessed: 21. November 2016. Society of Industrial and Applied Mathematics, 2001. DOI: 10.1137/1.9780898719277. URL: http://www.slaney.org/pct/
- Thorsten Buzug. Computed Tomography: From Photon Statistics to Modern Cone-Beam CT. Springer Berlin Heidelberg, 2008. DOI: 10.1007/978-3-540-39408-2
- Willi A. Kalender. Computed Tomography: Fundamentals, System Technology, Image Quality, Applications. 3rd ed. Publicis Publishing, July 2011