

# Brute Force Moving Average (MA) Smoother

Australian Wine Edition <3

In future workshops, we will use the actual high-level ITSMR functions used to implement this kind of smoother. However, these functions are *black boxes* in the sense that without diving into further documentation, it's not clear what they are doing *mathematically*. We'll recreate what's inside the black box now.

## Agenda

1. Load the data
2. Review the theoretical definition of an MA smoother
3. Create our own MA smoothing code
4. Calculate and examine the output at a few select times.

## 1) Loading the Data

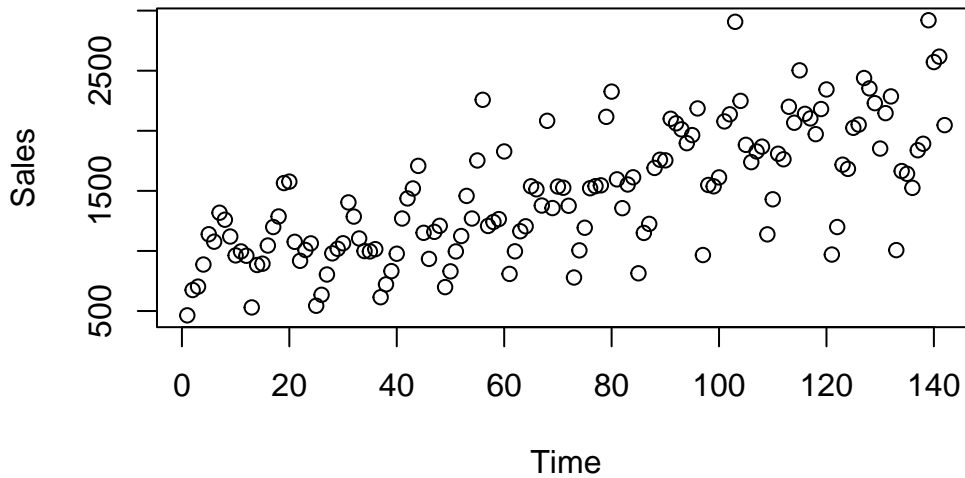
We'll use the Australian Wine Sales data. Recall that these data are dollar amounts, observed monthly from January 1980 to October 1991.

```
# load the ITSMR package which contains the wine dataset
library(itsmr)

# store the data as a spreadsheet with 2 columns: time (mo) and sales ($)
wine.data <- data.frame(Time = 1:142, Sales = wine)

# plot sales vs. time - Make sure time is the first column in the dataframe
plot(wine.data, main = "Australian Red Wine Sales")
```

## Australian Red Wine Sales



### 2) What's MA smoothing again?

At time  $t$ , we want to find  $\hat{m}_t$ : an estimate of the trend component  $m_t$ . The formula for an MA smoother with bandwidth  $q \geq 0$  is

$$\hat{m}_t = \frac{1}{2q+1} \sum_{j=-q}^q x_{t-j}$$

### 3) Making our own MA smoother for a fixed $t$

```
q <- 5           # choose bandwidth
t <- 10          # choose timepoint to estimate (the t in m_t)
x <- wine.data$Sales # this is our time series :)
```

Recall that the colon operator  $a:b$  concatenates (connects at the seams) integers ranging from  $a$  to  $b$ , inclusive. So to create the vector of  $t-j$  values for  $j \in \{-q, \dots, q\}$ , considering we've chosen  $t = 10$  and  $q = 5$ ,

$$\begin{bmatrix} t - (-q) \\ t - (-q + 1) \\ \vdots \\ t - (q - q) = t \\ \vdots \\ t - (q - 1) \\ t - q \end{bmatrix} = \begin{bmatrix} 10 - (-5) \\ 10 - (-4) \\ \vdots \\ 10 - 0 \\ \vdots \\ 10 - (4) \\ 10 - (5) \end{bmatrix} = \begin{bmatrix} 15 \\ 14 \\ \vdots \\ 10 \\ \vdots \\ 6 \\ 5 \end{bmatrix}$$

```
(t-(-q)): (t-q)
```

```
[1] 15 14 13 12 11 10 9 8 7 6 5
```

So our indices are correct. The corresponding data is

```
x[ (t-(-q)): (t-q) ]
```

```
[1] 894 883 530 960 996 963 1120 1260 1318 1077 1139
```

And the code representing the full RHS of the smoothing formula (part 2) is:

```
(1/(2*q+1)) * sum(x[ (t-(-q)): (t-q) ])
```

#### 4) Calculating $\hat{m}_t$

For  $t = 10$ :

```
# Calculate and Store
hat.m10 <- (1/(2*q+1)) * sum(x[ (t-(-q)): (t-q) ])

# Print (you must print it if you want it to show up in the Quarto output)
hat.m10
```

```
[1] 1012.727
```

For  $t = 11$  through to  $t = 15$ , we can compute  $\hat{m}_t$  manually (obviously, in practice, we would write a function returning a vector, but we're doing it manually now for the sake of demonstration.)

```

hat.m11 <- (1/(2*q+1)) * sum(x[ (11-(-q)):(11-q) ])
hat.m12 <- (1/(2*q+1)) * sum(x[ (12-(-q)):(12-q) ])
hat.m13 <- (1/(2*q+1)) * sum(x[ (13-(-q)):(13-q) ])
hat.m14 <- (1/(2*q+1)) * sum(x[ (14-(-q)):(14-q) ])
hat.m15 <- (1/(2*q+1)) * sum(x[ (15-(-q)):(15-q) ])

my.MA <- c(hat.m10, hat.m11, hat.m12, hat.m13, hat.m14, hat.m15)

check <- smooth.ma(wine,5)[10:15] # ITSMR function: should be the same as ours

```

Let's plot our results over the original data in that time-region, and compare it to the results from the ITSMR package's built-in function.

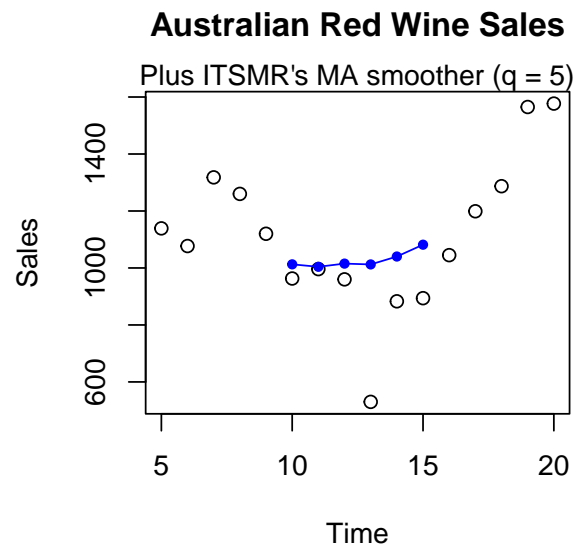
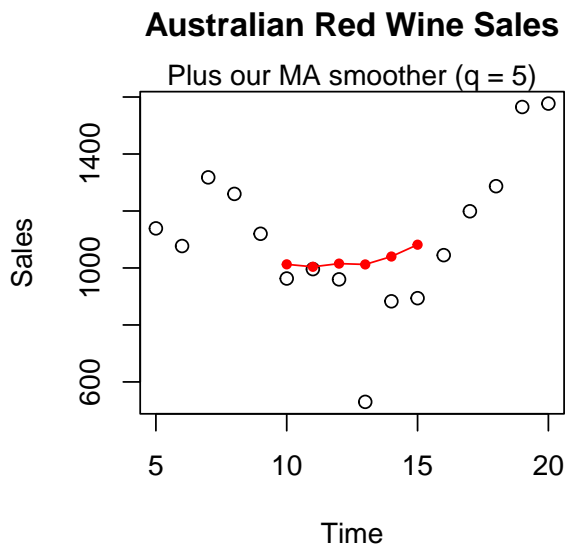
```

par(mfrow = c(1,2), mar = c(4,4,4,1)) # puts 2 plots side-by-side

## --- PLOT 1
# Only shows region surrounding timepoints we've estimated
plot(wine.data[5:20,],
     ylim = range(x[5:20],my.MA),          # Makes it all fit in plot window
     main = "Australian Red Wine Sales")
mtext("Plus our MA smoother (q = 5)")      # Adds a subtitle
lines(10:15, my.MA,
     col = "red", type = "o", pch = 20)   # Adds our home-made MA

## --- PLOT 2
# Same plot as before, but with the ITSMR output highlighted
plot(wine.data[5:20,],
     ylim = range(x[5:20],my.MA),          # Makes it all fit in plot window
     main = "Australian Red Wine Sales")
mtext("Plus ITSMR's MA smoother (q = 5)")  # Adds a subtitle
lines(10:15, check,
     col = "blue", type = "o", pch = 20)  # Adds ITSMR function's output

```



### Questions for you to think about

Does this look right?

Why do you think  $\hat{m}_t$  has this shape, in this region?

Was the smoother “effective?” What would that mean?

Consider how you would write a function to smooth an entire time series, similarly to the `smoo.ma()` function. (You might want to use loops, vector arithmetic, or `apply()` functions)