

$x_1, x_2$

$$\text{Corr}[X, Y] = \frac{\text{Cov}[X, Y]}{\sqrt{\text{Var}[X] \text{Var}[Y]}}$$

$$\mu_{A_1} = 0$$

$$\mu_{A_2} = 0$$

$$x_{t=t_1, t_2} \rightarrow x_t = A_1 \cos(\omega t) + A_2 \sin(\omega t) \quad t \in \mathbb{Z}$$

$$\rightarrow P(x_2 | x_1)$$

$$\rightarrow P_2 x_1 = \underset{\uparrow}{a} x_1$$

$$P(Y|W) = \mu_Y + a^T(W - \mu_W)$$

$\Gamma a = \gamma$   
 Covariance matrix of predictors  $\rightarrow$  cov between  $Y, \text{ predictors}$

$$\text{Var}[x_1] a = \text{Cov}[x_2, x_1]$$

$$\left( \begin{smallmatrix} \Gamma \\ W \end{smallmatrix} \right)$$

$$a = \frac{\text{Cov}[x_2, x_1]}{\text{Var}[x_1]}$$

$$= \frac{\sqrt{\text{Var}[x_2] \text{Var}[x_1]}}{\sqrt{\text{Var}[x_1] \text{Var}[x_1]}} = \frac{\sqrt{\text{Var}[x_2] \text{Var}[x_1]}}{\text{Var}[x_1]}$$

$$\text{Cov}[x_2, x_1]$$

$$a = \hat{\rho}(x_1, x_2)$$

$$\text{Var}[A_i] = 1$$

$$\mu_{A_1}, \mu_{A_2} = 0$$

$$x_t = \underbrace{A_1}_{\text{unit variance}} \cos(\omega t) + \underbrace{A_2}_{\text{unit variance}} \sin(\omega t)$$

$$\text{Var}[aX] = a^2 \text{Var}[X]$$

$$E[aX] = aE[X]$$

$$\text{Var}[x_0] = \cos^2(\omega) \text{Var}[A_1] + \sin^2(\omega) \text{Var}[A_2]$$

$$= \cos^2(\omega) + \sin^2(\omega) = 1$$

$$\text{Cov}[x_2, x_1] = E[(A_1 \cos(\omega 2) + A_2 \sin(\omega 2))(A_1 \cos(\omega) + A_2 \sin(\omega))]$$

$$= \cos(2\omega) \cos(\omega) + \sin(2\omega) \sin(\omega) = \cos(\omega)$$

$$a = \cos(\omega)$$

$$P_1 x_2 = \underset{\downarrow}{a} x_1 = \cos(\omega) x_1$$

$$\text{Var}[Y] = a^T \gamma$$

$$\text{MSE}[P_2 x_1] = E[(x_2 - P_1 x_2)^2] = \text{Var}[x_2] - \cos(\omega) \text{Cov}[x_2, x_1]$$

$$= 1 - \cos^2(\omega)$$