

Assignment No. 05



Title of the Assignment :
Design n-queens matrix having first queen placed. Use backtracking to place remaining queens to generate the final n-queen's matrix.

Objective of the Assignment :
Students should be able to understand and solve n-Queen problem and understand basics of backtracking.

Prerequisite :

1. Basic of Python or Java Programming
2. Concept of backtracking method
3. N-Queen Problem

Theory :

Introduction to Backtracking :

- Many problems are difficult to solve algorithmically. Backtracking makes it possible to solve at least some large instances of difficult combinatorial problems.

What is backtracking?

Backtracking is finding the solution of a problem whereby the solution depends on the previous steps taken.



In backtracking, we first take a step & then we see if step taken is correct or not i.e., whether it will give a correct answer or not.

Thus, the general steps of backtracking are:

- Start with a sub-solution
- Check if this sub-solution will lead to the solution or not.
- If not, then come back and change the sub-solution. Continue again.

Applications of Backtracking :

- N Queens Problem
- Sum of subsets Problem
- Graph coloring
- Hamiltonian cycles.

N queens on $N \times N$ chessboard

N-queens Problem :

A classic combinational problem is to place n queens on an $n \times n$ chess board so that no two attack i.e., no two queens are on the same row, column or diagonal.

```
# Python3 program to solve
# Problem using backtracking
global N
N = 4
def printSolution(board):
    for i in range(N):
        for j in range(N):
            print(board[i][j], end = " ")
        print()
# A utility function to check
# if a queen can be placed on board[row][col]
# Note that this function is called when
# there is no queen already placed in column
# So we need to check only
# attacking queens
def isSafe(board, row, col):
    # Check this row on left side
    for i in range(col):
        if board[row][i] == 1:
            return False
    # Check upper diagonal
    for i, j in zip(range(row, -1, -1), range(col, -1, -1)):
        if board[i][j] == 1:
            return False
    # Check lower diagonal
    for i, j in zip(range(row, N, 1), range(col, -1, -1)):
        if board[i][j] == 1:
            return False
    return True
def solveNQUtil(board, col):
    # base case: If all queens
    # are placed then return true
    if col == N:
        return True
    # Consider this column
    # and try to place queen in
    # this column in all rows
    for i in range(N):
        if isSafe(board, i, col):
            # Place this queen in board[i][col]
            board[i][col] = 1
            # recur to place rest of
            # queens
            if solveNQUtil(board, col + 1):
                return True
            # If placing queen in
            # board[i][col]
            # doesn't lead to a solution
            # then remove queen from
            # board[i][col]
            board[i][col] = 0
            # if the queen can not
            # be placed in this
            # column then
            return False
```




Algorithm :

- ①. Start in the leftmost column.
- ②. If all queens are place return true.
- ③. Try all rows in the current column.
- ④. If all rows have been tried & nothing worked return false to trigger backtracking.

4-Queen Problem :

Problem : Given 4×4 chessboard, arrange four queens in a way, such that no two queens attack each other.

	1	2	3	4
1				
2				
3				
4				

4×4 chessboard

All possible solutions for 4-queen are shown in fig.

	1	2	3	4
1		Q ₁		
2				Q ₂
3	Q ₃			
4			Q ₄	

Fig. (a): solution-1

	1	2	3	4
1			Q ₁	
2	Q ₂			
3				Q ₃
4		Q ₄		

Fig. (b): solution-2



Conclusion :

In this way we have explored Concept of Backtracking and solve n-queen problem using backtracking method.

~~Backtracking~~

1					
2					
3					
4					

4x4 chessboard

All possible solutions for n-queen are shown in fig.

1					
2					
3					
4					

Fig. (a) : (a) solution

1					
2					
3					
4					

Fig. (b) : (b) solution