

EECS4312 eHealth Project

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Revisions

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|------------------|----------|-------------------------------|
| December 8, 2015 | 1.0 | Initial requirements document |

Requirements Document: for Patient care eHealth System

Contents

| | |
|--|-----------|
| 1. System Overview | 5 |
| 2. Context Diagram | 6 |
| 3. Goals | 7 |
| 4. Monitored Events | 8 |
| 5. Controlled Variables | 9 |
| 6. E/R-descriptions | 10 |
| 6.1. Requirements Descriptions | 10 |
| 6.2. Environmental Descriptions | 10 |
| 7. Abstract variables needed for the Function Table | 11 |
| 8. Function Tables | 11 |
| 8.1. Function Table for eHealth | 13 |
| 8.2. Function Table for init | 13 |
| 8.3. Function Table for new_prescription(id, md, pt) | 14 |
| 8.4. Function Table for add_medicine(id, m, d) | 15 |
| 8.5. Function Table for remove_medicine(id, med) | 16 |
| 8.6. Function Table for add_interaction(id1, id2) | 17 |
| 9. Validation | 18 |
| 10. Acceptance Tests | 19 |
| A. eHealth PVS | 20 |

List of Figures

| | |
|---|----|
| 1. Context Diagram | 6 |
| 2. Abstract Variables used in Function Tables | 11 |
| 3. Table of errors and warnings | 12 |
| 4. Function Table for eHealth | 13 |
| 5. Function Table for init | 13 |
| 6. Function Table for new_prescription(id, doctor, patient) | 14 |

| | | |
|-----|---|----|
| 7. | Function Table for add_medicine(id, medicine, dose) | 15 |
| 8. | Function Table for remove_medicine(id, medicine) | 16 |
| 9. | Function Table for add_interaction(id1, id2) | 17 |
| 10. | Validated Isolette | 18 |
| 11. | First Acceptance Test | 19 |
| 12. | Second Acceptance Test | 20 |
| 13. | Second Acceptance Test | 29 |
| 14. | Second Acceptance Test | 30 |

List of Tables

| | | |
|----|--------------------------------|---|
| 1. | Monitored Events | 8 |
| 2. | Monitored Types | 9 |
| 3. | Controlled Variables | 9 |

1. System Overview

The System Under Development (SUD) is a eHealth prescriptions management prototype that will eventually be part of a much larger system that manages health prescription records for Ontario. This requirements document is specifically for this prototype that will keep track of prescriptions for patients so that dangerous interactions between medications can be controlled and checked.

To do this, the system will keep will maintain a database of physicians, medications, patients, and patient prescriptions, each with a unique identifier (ID). The system will also maintain records of dangerous interactions between medications. Interactions are defined as undesirable outcomes when certain pairs of medications are taken together. For this system, we are to track these interactions as well as prescriptions that contain medications that interact dangerously.

Physicians are classified either as generalists, or specialists in the database. Generalists are allowed to prescribe medications so long as they do not cause dangerous interactions. Specialists are given discretion in this case - they are allowed to prescribe medications that would cause dangerous reactions, though this is flagged by the system and displayed in a report.

2. Context Diagram

The System Under Description (SUD) is a computer *controller* to keep track of the physicians, patients, patient prescriptions, medications, and medication interactions. The monitored variables and controlled variables for this computer system can be found in Table 1 and Table 3 respectively.

The system must keep track of abstract state which isn't available to the user. For a list of the abstract states within the controller see Figure 2.

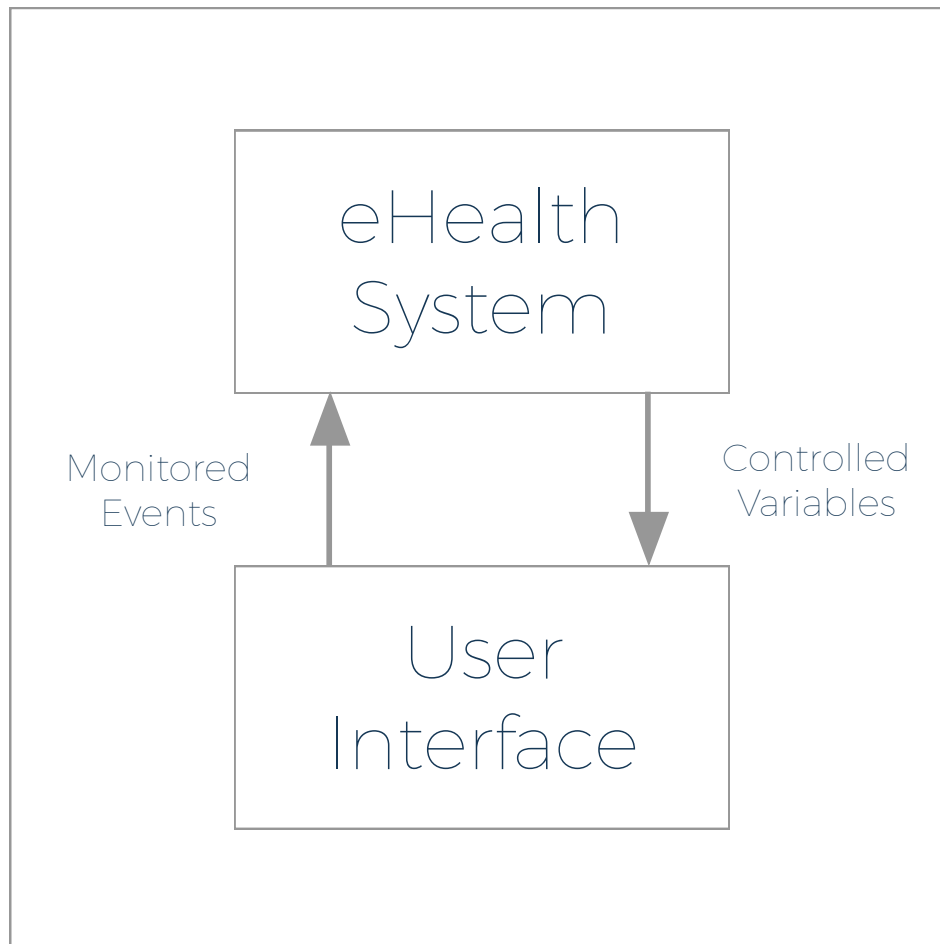


Figure 1: Context Diagram

3. Goals

The high-level goals (G) of the system are:

- G1 — The user should be able to add physicians of type {generalist, specialist} with unique IDs
- G2 — The user should be able to add patients with unique IDs
- G3 — The user should be able to add medications with unique names and IDs and a safe dosage range
- G4 — The user should be able to add prescriptions with a unique ID between a doctor and patient
- G5 — The user should be able to add interactions between medications
- G6 — Physicians should be able to prescribe medications with specific dosages, so long as the dosage is within the safe range
- G7 — A Physician must be a specialist to prescribe a medication to a patient when it would create a dangerous interaction with a different already prescribed medication - regardless of the prescription or physician the other medication exists in
- G8 — The system should be able to display a report of all patients prescribed a particular medication
- G9 — The system should be able to display a dangerous prescriptions report that lists all patients with dangerous prescriptions along with the particular medications prescribed to them that interact dangerously

4. Monitored Events

The monitored events are those which come through the user interface. The following monitored events will be available to the user.

| Name | Interpretation |
|---|--|
| add_physician(id: ID_MD; name: NAME; kind: PHYSICIAN_TYPE) | Add a Physician to the system |
| add_patient(id: ID_PT; name: NAME) | Add Patient to the system |
| add_medication(id: ID_MN; medicine: MEDICATION) | Add a medication to the system |
| add_interaction(id1:ID_MN;id2:ID_MN) | Add an interaction between two medications |
| new_prescription(id: ID_RX; doctor: ID_MD; patient: ID_PT) | Add a new prescription to the system |
| add_medicine(id: ID_RX; medicine:ID_MN; dose: VALUE) | Add a medicine to a prescription |
| remove_medicine(id: ID_RX; medicine:ID_MN) | Remove a medication from a prescription |
| prescriptions_q(medication_id: ID_MN) | List all patients prescribed the medication |
| dpr_q | Print out a dangerous prescription report |

Table 1: Monitored Events

| Name | Type | Interpretation |
|----------------|--|------------------------------------|
| PHYSICIAN_TYPE | {gn, sp} | Generalist or Specialist |
| MEDICATION | [name: NAME; kind: KIND; low: VALUE; hi: VALUE] | Name is unique. See following rows |
| KIND | {pill, liquid} | Pill or a liquid |
| DOSE | {mg, cc} | Milligrams or Cubic Centimetres |

Table 2: Monitored Types

5. Controlled Variables

The controlled variables represent what will be shown to the user.

| Name | Interpretation | Abstract State |
|---------------|--|----------------|
| Physicians | A list of all the Physicians currently within the system | See table 2 |
| Patients | A list of all the Patients currently in the system | See table 2 |
| Medications | A list of all the Medications currently within the system | See table 2 |
| Interactions | A list of all the Interactions currently within the system | See table 2 |
| Prescriptions | A list of all the Prescriptions within the system | See table 2 |
| Error | A message displaying the highest priority error, or ok | See table 2 |

Table 3: Controlled Variables

6. E/R-descriptions

6.1. Requirements Descriptions

| | | |
|------|---|--|
| REQ1 | The system will keep track of Physicians, Patients, Medications, Interactions, and Prescriptions | See Table 3 for list of abstract states. |
| REQ2 | A generalist cannot add a medicine to a prescription if that medicine leads to a dangerous interaction. | See Table 1 for adding medicine, and Table 3 for dangerous interactions. |
| REQ3 | An interaction cannot be added if a specialist has not prescribed at least one of the medications. | See Table 1 for adding interaction, and Table 3. |

6.2. Environmental Descriptions

| | | |
|------|--|---|
| ENV4 | All input to the system will be constrained to the GUI grammar. | See Table 1 for the list possible monitored events. |
| ENV5 | A constraint by the grammar will ensure PHYSICIAN_TYPE is either a generalist or a specialist. | See Table 2 for PHYSICIAN_TYPE. |

Rationale: The operator interface for the nurse is designed in such a way that the increments of the input temperatures from the control interface must change by whole numbers.

| | | |
|------|--|-----------------------|
| ENV6 | The DOSE type will be constrained by the GUI grammar to be either mg, or cc. | See Table 2 for DOSE. |
|------|--|-----------------------|

| | | |
|------|---|-----------------------|
| ENV7 | The KIND type will be constrained by the GUI grammar to be either a pill or a liquid. | See Table 2 for KIND. |
|------|---|-----------------------|

7. Abstract variables needed for the Function Table

| Name | Interpredation | Purpose |
|------|---|--|
| mnid | The set of all medication ids | Keep track of all the medication ids in the system |
| ptid | The set of all patient ids | Keep track of all the patient ids in the system |
| mdid | The set of all doctor ids | Keep track of all the doctor ids in the system |
| rxid | The set of all prescription ids | Keep track of all the prescription ids in the system |
| mdpt | Relationship between Doctor and Patient | Keep track of the doctor and the patient |
| rx | Relation between doctor patient and medication | Keep track of all the medical prescriptions between doctor and patient in the system |
| prs | List of all prescriptions including dosage | Keep track of all the prescriptions in the system |
| di | Set of dangerous interactions between medications | Keep track of all the dangerous interactions in the system |
| gs | The kind of doctor | Keep track of all the type of doctor |
| dpi | The dangerous prescription report | Notify dangerous interactions, if they exist |

Figure 2: Abstract Variables used in Function Tables

8. Function Tables

| Name | Meaning |
|-------|--|
| err1 | physician id must be a positive integer |
| err2 | physician id already in use |
| err3 | name must start with a letter |
| err4 | patient id must be a positive integer |
| err5 | patient id already in use |
| err6 | name must start with a letter |
| err7 | medication id must be a positive integer |
| err8 | medication id already in use |
| err9 | medication name must start with a letter |
| err10 | medication name already in use |
| err11 | require $0 < \text{low-dose} \leq \text{hi-dose}$ |
| err12 | medication ids must be positive integers |
| err13 | medication ids must be different |
| err14 | medications with these ids must be registered |
| err15 | interaction already exists |
| err16 | first remove conflicting medicine prescribed by generalist |
| err17 | prescription id must be a positive integer |
| err18 | prescription id already in use |
| err19 | physician with this id not registered |
| err20 | patient with this id not registered |
| err21 | prescription already exists for this physician and patient |
| err22 | prescription with this id does not exist |
| err23 | medication id must be registered |
| err24 | medication is already prescribed |
| err25 | specialist is required to add a dangerous interaction |
| err26 | dose is outside allowed range |
| err27 | medication is not in the prescription |

Figure 3: Table of errors and warnings

8.1. Function Table for eHealth

| Monitored Inputs | | |
|------------------|--|-------------|
| $i = 0$ | | See Table 5 |
| $i > 0$ | <code>new_prescription(id, doctor, patient)</code> | See Table 6 |
| | <code>add_medicine(id, medicine, dose)</code> | See Table 7 |
| | <code>remove_medicine(id, medicine)</code> | See Table 8 |
| | <code>add_interaction(id1, id2)</code> | See Table 9 |

Figure 4: Function Table for eHealth

8.2. Function Table for init

error: *false*

| Abstract State | \neg error | error |
|----------------------|---------------------------------|-------|
| <code>mind(i)</code> | \emptyset | NC |
| <code>ptid(i)</code> | \emptyset | NC |
| <code>mdid(i)</code> | \emptyset | NC |
| <code>rxid(i)</code> | \emptyset | NC |
| <code>mn(i)</code> | \emptyset | NC |
| <code>mns(i)</code> | ε | NC |
| <code>mdpt(i)</code> | \emptyset | NC |
| <code>rx(i)</code> | ε | NC |
| <code>prs(i)</code> | ε | NC |
| <code>di(i)</code> | \emptyset | NC |
| <code>gs(i)</code> | $\emptyset \mapsto \varepsilon$ | NC |
| <code>dpr(i)</code> | $\emptyset \mapsto \varepsilon$ | NC |
| <code>r(i)</code> | ok | error |

Figure 5: Function Table for init

8.3. Function Table for new_prescription(id, md, pt)

error: $\neg(id > 0 \wedge \neg rxid_1(id) \wedge md > 0 \wedge mdid_1(md) \wedge pt > 0 \wedge ptid_1(pt) \wedge mdpt_1(md, pt))$

| Abstract State | \neg error | error |
|----------------|--|-------|
| mind(i) | NC | NC |
| ptid(i) | NC | NC |
| mdid(i) | NC | NC |
| rxid(i) | $rxid_{-1} \cup \{id\}$ | NC |
| mn(i) | NC | NC |
| mns(i) | NC | NC |
| mdpt(i) | NC | NC |
| rx(i) | $rx_{-1} \upharpoonright (id \mapsto (md, pt))$ | NC |
| prs(i) | $prs_{-1} \upharpoonright (id \mapsto empty_prs(mnid_1))$ | NC |
| di(i) | NC | NC |
| gs(i) | NC | NC |
| dpr(i) | $dpr_{-1} \upharpoonright (id \mapsto \emptyset)$ | NC |
| r(i) | ok | error |

Figure 6: Function Table for new_prescription(id, doctor, patient)

8.4. Function Table for `add_medicine(id, m, d)`

error: $\neg(id > 0 \wedge \neg rxid_1(id) \wedge m > 0 \wedge mnid_1(m) \wedge pt > 0 has(m, prs_1(id)) \wedge sumthin \wedge isValidDose(m, d))$

| Abstract State | \neg error | error |
|----------------|--|-------|
| mind(i) | NC | NC |
| ptid(i) | NC | NC |
| mdid(i) | NC | NC |
| rxid(i) | NC | NC |
| mn(i) | NC | NC |
| mns(i) | NC | NC |
| mdpt(i) | NC | NC |
| rx(i) | NC | NC |
| prs(i) | $prs_{-1}(id) \upharpoonright (m \mapsto d)$ | NC |
| di(i) | NC | NC |
| gs(i) | NC | NC |
| dpr(i) | NC | NC |
| r(i) | ok | error |

Figure 7: Function Table for `add_medicine(id, medicine, dose)`

8.5. Function Table for `remove_medicine(id, med)`

error: $\neg(id > 0 \wedge \neg rxid_1(id) \wedge med > 0 \wedge mnid_1(med) \wedge prs_1(id)(med)'1 > 0)$

| Abstract State | \neg error | error |
|----------------|---|-------|
| mind(i) | NC | NC |
| ptid(i) | NC | NC |
| mdid(i) | NC | NC |
| rxid(i) | NC | NC |
| mn(i) | NC | NC |
| mns(i) | NC | NC |
| mdpt(i) | NC | NC |
| rx(i) | NC | NC |
| prs(i) | $prs_{-1} \upharpoonright (id \mapsto \varepsilon)$ | NC |
| di(i) | NC | NC |
| gs(i) | NC | NC |
| dpr(i) | NC | NC |
| r(i) | ok | error |

Figure 8: Function Table for `remove_medicine(id, medicine)`

8.6. Function Table for add_interaction(id1, id2)

error: $\neg(id1 > 0 \wedge id2 > 0 \wedge \neg id1 = id2 \wedge mnid_1(id1) \wedge mnid_1(id2) \wedge (\exists a : (prs_1(a)(id1)'1 > 0 \wedge sumin) \vee (prs_1(id)(med)'1 > 0 \wedge sumin)))$

| Abstract State | \neg error | error |
|----------------|---|-------|
| mind(i) | NC | NC |
| ptid(i) | NC | NC |
| mdid(i) | NC | NC |
| rxid(i) | NC | NC |
| mn(i) | NC | NC |
| mns(i) | NC | NC |
| mdpt(i) | NC | NC |
| rx(i) | NC | NC |
| prs(i) | NC | NC |
| di(i) | $di_{-1} \cup (id1, id2) \wedge di_1 \cup (id2, id1)$ | NC |
| gs(i) | NC | NC |
| dpr(i) | NC | NC |
| r(i) | ok | error |

Figure 9: Function Table for add_interaction(id1, id2)

9. Validation

todo

```

***
*** top (23:34:28 11/15/2015)
*** Generated by proveit - ProofLite-6.0.9 (3/14/14)
*** Trusted Oracles
*** MetiTarski: MetiTarski Theorem Prover via PVS proof rule metit
***

Proof summary for theory top
  Theory totals: 0 formulas, 0 attempted, 0 succeeded (0.00 s)

Proof summary for theory Time
  r2d_TCC1.....proved - complete [shostak](0.23 s)
  d2r_TCC1.....proved - complete [shostak](0.03 s)
  held_for_TCC1.....proved - complete [shostak](0.08 s)
  Theory totals: 3 formulas, 3 attempted, 3 succeeded (0.33 s)

Proof summary for theory isolette
  c_md_ft_TCC1.....proved - complete [shostak](0.03 s)
  c_md_ft_TCC2.....proved - complete [shostak](0.03 s)
  c_md_ft_TCC3.....proved - complete [shostak](0.05 s)
  c_md_ft_TCC4.....proved - complete [shostak](0.10 s)
  c_md_ft_TCC5.....proved - complete [shostak](0.06 s)
  c_md_ft_TCC6.....proved - complete [shostak](0.03 s)
  c_md_ft_TCC7.....proved - complete [shostak](0.02 s)
  c_md_ft_TCC8.....proved - complete [shostak](0.02 s)
  c_md_ft_TCC9.....proved - complete [shostak](0.02 s)
  c_td_ft_TCC1.....proved - complete [shostak](0.01 s)
  c_hc_ft_TCC1.....proved - complete [shostak](0.07 s)
  c_hc_ft_TCC2.....proved - complete [shostak](0.11 s)
  c_hc_ft_TCC3.....proved - complete [shostak](0.07 s)
  c_hc_ft_TCC4.....proved - complete [shostak](0.05 s)
  c_hc_ft_TCC5.....proved - complete [shostak](0.03 s)
  c_al_ft_TCC1.....proved - complete [shostak](0.03 s)
  c_al_ft_TCC2.....proved - complete [shostak](0.04 s)
  c_al_ft_TCC3.....proved - complete [shostak](0.00 s)
  c_al_ft_TCC4.....proved - complete [shostak](0.07 s)
  c_al_ft_TCC5.....proved - complete [shostak](0.04 s)
  c_al_ft_TCC6.....proved - complete [shostak](0.03 s)
  inv_hc_holds.....proved - complete [shostak](0.34 s)
  inv_al_holds.....proved - complete [shostak](2.71 s)
  Theory totals: 23 formulas, 23 attempted, 23 succeeded (3.98 s)

Grand Totals: 26 proofs, 26 attempted, 26 succeeded (4.32 s)

```

Figure 10: Validated Isolette

10. Acceptance Tests

```
at1.txt
add_physician      (1, "Mayo", specialist)
add_patient        (3, "Dora")
add_patient        (1, "Drew")
add_medication     (1, ["Wafarin", pill, 1.0, 6.0])
add_medication     (3, ["caffeine", liquid, 1.0, 16.0])
add_medication     (2, ["acetaminophen", liquid, 1.0, 25.5])
add_interaction    (2,3)
add_interaction    (1,2)
new_prescription   (2, 1, 3)
new_prescription   (1, 1, 1)
dpr_q
add_medicine       (1, 1, 5.5)
add_medicine       (1, 2, 5.5)
add_medicine       (1, 3, 5.5)
add_medicine       (2, 2, 5.5)
add_medicine       (2, 3, 5.5)
add_medicine       (2, 1, 5.5)
prescriptions_q(1)
```

Figure 11: First Acceptance Test

```

-- at2.txt
add_physician      (1, "Mayo", specialist)
add_patient        (3, "Drew")
add_patient        (1, "Helen")
add_medication     (1, ["Wafarin", pill, 1.0, 6.0])
add_medication     (3, ["caffeine", liquid, 1.0, 16.0])
add_medication     (2, ["acetaminophen", liquid, 1.0, 25.5])
add_interaction    (1,2)
add_interaction    (1,3)
add_interaction    (2,3)
new_prescription   (2, 1, 3)
new_prescription   (1, 1, 1)
add_medicine       (1, 1, 5.5)
add_medicine       (1, 2, 5.5)
add_medicine       (1, 3, 5.5)
add_medicine       (2, 2, 5.5)
add_medicine       (2, 3, 5.5)
add_medicine       (2, 1, 5.5)
dpr_q
remove_medicine(2,1)
remove_medicine(2,2)
remove_medicine(2,3)
add_medicine       (1, 1, 5.5)
add_medicine       (1, 2, 5.5)
add_medicine       (1, 3, 5.5)
dpr_q

```

Figure 12: Second Acceptance Test

A. eHealth PVS

```

% This is a partial theory to help you get started encoding your
% function tables in PVS for the eHealth project.
% This theory type checks but the function tables are
% not valid as the requirements have not been properly elicited.
% Furthermore the function tables do not respect our format
% as completeness and disjointness is circumvented by the
% ELSE keyword. You may not use the ELSE keyword in function tables
% for this project.
% You are not required to prove any invariants.
% Nevertheless, we show you below how to prove some simple

```

```
% invariants as part of the state as TCCs. See fields inv1 and
% inv2 in the STATE record using the unit ADT. You may omit these
% invariants in the state if you choose, but they do help to ensure
% the correct requirements if kept.
% Note that we show a change of state using the override WITH
% operator so that any part of the state not overridden is left
% unchanged.
```

```
ehealth: THEORY
```

```
BEGIN
```

```
delta: posreal % sampling time
```

```
IMPORTING Time[delta]
```

```
IMPORTING structures@Unit_adt
```

```
i: VAR DTIME
```

```
% Definition of an empty function
```

```
emptyfun [T, U : TYPE] (x : {x : T | FALSE}) : RECURSIVE U =
  emptyfun(x)
```

```
  MEASURE (LAMBDA (x : {x : T | FALSE}) : 1)
```

```
ID_MD: TYPE+ = int %physicians
```

```
ID_PT: TYPE+ = int %patients
```

```
ID_RX: TYPE+ = int %prescriptions
```

```
ID_MN: TYPE+ = int %medications
```

```
% Physician type
```

```
GS: TYPE+ = {gn, sp}
```

```
UNIT: TYPE+ = {cc, mg}
```

```
DOSE: TYPE = [nnreal, UNIT]
```

```
NAME: TYPE+
```

```
KIND: TYPE+ = {pill, liquid}
```

```
MEDICINE: TYPE = [name:NAME, kind:KIND, low:nnreal, hi:nnreal]
```

```
COMMAND : DATATYPE
```

```
BEGIN
```

```
  m_np(id:ID_RX, md: ID_MD, pt: ID_PT): np?
```

```
  m_ai(id1:ID_MN, id2:ID_MN): ai?
```

```
  m_am(id:ID_RX, med:ID_MN, dose:DOSE): am?
```

```
  m_rm(id:ID_RX, med: ID_MN): rm?
```

```
END COMMAND
```

```

cmd: VAR [POS_DTIME -> COMMAND]

invariant (p : bool) : TYPE = { x : Unit | p }
    % unit : { x : Unit | 2 is even }
    % (type correct IFF: 2 is even [ x := unit ]
    % ... 2 is even
    % TRUE
    %
    % unit : { x : Unit | 3 is even }
    % (type correct IFF: 3 is even [x := unit]
    % ... 3 is even
    % FALSE
    %
    % { x : Unit | p } = IF p THEN {unit} ELSE {} ENDIF

has [T : TYPE] (m : T, p : [T -> DOSE]) : bool = p(m) `1 > 0
    % does prescription p have a non-zero dose of m?

% Have to place the state in a record
STATE: TYPE =
    [#
        mnid: set[ID_MN] % medication ids
        , ptid: set[ID_PT] % patient ids
        , mdid: set[ID_MD] % doctor ids
        , rxid: set[ID_RX] % prescription ids
        , mdpt: set[[mdid],(ptid)] % (doctor, patient) care relation
        , rx: [(rxid) -> (mdpt)] % care to rx ids, needs to be a bijection
        , prs: [(rxid) -> [(mnid) -> DOSE]] % prescriptions
        , di: set[[mnid], (mnid)] % dangerous interactions, invariant needed?
        , gs: [(mdid) -> GS] % kind of doctor
        , dpr : [(rxid) -> set[[mnid], (mnid)]]
        %, inv1 : invariant( FORALL (x : (mnid)): NOT di((x,x)) )
            % irreflexivity
        %, inv2 : invariant( FORALL (x,y : (mnid)): di((x,y)) <=> di((y,x)) )
            % symmetry
    #]

PRES (s : STATE) : TYPE = [(s`mnid) -> DOSE]
    % type of PRESCRIPTIONS for a given state

% would prescriptions p0 and p1 cause dangerous interactions

```

```

    % if they were prescribed to the same patient?
interact (s : STATE)(p0, p1 : PRES (s)) : bool =
    EXISTS (m0,m1 : (s`mnid)):
        s`di((m0,m1))
        AND has(m0,p0)
        AND has(m1,p1)

    % given state s, does medication m1 cause a problem
    % for the patient of prescription p0?
interactWith (s: STATE)(p0 : PRES (s), m1 : (s`mnid)) : bool =
    EXISTS (m0 : (s`mnid)): s`di((m0,m1)) AND has(m0,p0)

    medicine: MEDICINE
isValidDose(s : STATE)(m : ID_MN, d : DOSE) :
bool = d`1 > 0 AND d`1 > medicine`3 AND medicine`4 > d`1
    % is d a valid dose of medication m?
    % kept abstract; will need a counterpart in the state
    % in order to be refined

prsOfPt (s: STATE)(p: (s`ptid)) : set [(s`rxid)] =
    { r : (s`rxid) | s`rx(r)`2 = p }

ptOf (s: STATE)(r : (s`rxid)) : (s`ptid) = s`rx(r)`2

mdOf (s: STATE)(r : (s`rxid)) : (s`mdid) = s`rx(r)`1

s: VAR [ DTIME -> STATE ]

empty_prs (mdns : set[ID_MN])(m : (mdns)) : DOSE = (0, mg)

init_mdid: set[ID_MD]
init_gs: [(init_mdid) -> GS]
init_mnid: set[ID_MN]
init_ptid: set[ID_PT]
init_rxid: set[ID_RX]
init_dpr: [(init_rxid) -> set[[init_mnid), (init_mnid)]]]
init_prs: [(init_rxid) -> [(init_mnid) -> DOSE]]

init_state : STATE =
    (# mnid := init_mnid
    , ptid := init_ptid

```

```

, mdid := init_mdid
, rxid := init_rxid
, mdpt := emptyset
, rx := emptyfun
, prs := init_prs
, di := emptyset
, gs := init_gs
, dpr := init_dpr
% , inv1 := unit
% , inv2 := unit
#)

% new_prescription (id: ID_RX; doctor: ID_MD; patient: ID_PT)
%   prescription id must be a positive integer
%   prescription id already in use
%   physician id must be a positive integer
%   physician with this id not registered
%   patient id must be a positive integer
%   patient with this id not registered
%   prescription already exists for this physician and patient
np_ft(id:ID_RX, md: ID_MD, pt: ID_PT)(s)(i): bool =
COND
  id > 0
  AND NOT rxid_ (id)
  AND md > 0
  AND mdid_ (md)
  AND pt > 0
  AND ptid_ (pt)
  AND mdpt_ (md, pt) ->
    s(i) = s(i-1) WITH [ rxid := add(id,rxid_)
                        , rx  := rx_ WITH [id := (md,pt)]
                        , prs := prs_ WITH [id := empty_prs(mnid_) ]
                        , dpr := dpr_ WITH [id := emptyset ]
                        ] ,
  NOT (id > 0
  AND NOT rxid_ (id)
  AND md > 0
  AND mdid_ (md)
  AND pt > 0
  AND ptid_ (pt)
  AND mdpt_ (md, pt))

```



```

        -> s(i) = s(i-1)
ENDCOND
where
    rxid_ = s(i-1) `rxid
    ,mdid_ = s(i-1) `mdid
    ,ptid_ = s(i-1) `ptid
    ,mdpt_ = s(i-1) `mdpt
    ,rx_   = s(i-1) `rx
    ,dpr_  = s(i-1) `dpr
    ,mnid_ = s(i-1) `mnid
    ,prs_  = s(i-1) `prs

% add_medicine (id: ID_RX; medicine:ID_MN; dose: VALUE)
%   prescription id must be a positive integer
%   prescription with this id does not exist
%   medication id must be a positive integer
%   medication id must be registered
%   medication is already prescribed
%   specialist is required to add a dangerous interaction
%   dose is outside allowed range
am_ft(id:ID_RX, m: ID_MN, d: DOSE)(s)(i): bool =
COND
    id > 0 AND NOT rxid_ (id)
    AND m > 0 AND mnid_ (m)
    AND NOT has(m,prs_ (id))
    AND (EXISTS (r : (prsOfPt_ (ptOf_ (id)))): interactWith_ (prs_(r),m))
        % does medication m introduce an interaction?
        % if so, is doctor 'md' a specialist?
    AND isValidDose_ (m,d)
        -> s(i) = s(i-1) WITH [ prs := prs_ WITH [id := prs_(id) WITH [m := d] ]
        % s_ WITH [ prs := s_ `prs | id -> (s_ `prs.id | m -> d) ]
    , ELSE
        -> s(i) = s(i-1)
ENDCOND
where
    rxid_ = s(i-1) `rxid
    ,mnid_ = s(i-1) `mnid
    ,prs_  = s(i-1) `prs
    ,mdOf_ = mdOf(s(i-1))
    ,ptOf_ = ptOf(s(i-1))
    ,interactWith_ = interactWith(s(i-1))

```

```

,prsOfPt_ = prsOfPt(s(i-1))
,isValidDose_ = isValidDose(s(i-1))

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%% FUN FUN FUNCTION TABLES %%
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

%add_interaction (id1:ID_MN;id2:ID_MN)
%   medication ids must be positive integers
%   medication ids must be different
%   medications with these ids must be registered
%   interaction already exists
%   first remove conflicting medicine prescribed by generalist
ai_ft(id1:ID_MN, id2:ID_MN)(s)(i): bool = COND
  id1 > 0 AND id2 > 0
  AND NOT (id1 = id2)
  AND member(id1, mnid_ )
  AND member(id2, mnid_ )
  AND NOT member((id1,id2), di_ )
  AND NOT (EXISTS (a: ID_RX, b: ID_MD, c: ID_PT):
    ((prs_ (a)(id1)`1 > 0 AND (rx_ (a) = (b,c) AND gs_ (b) = sp ))
    OR (prs_ (a)(id2)`1 > 0 AND (rx_ (a) = (b,c) AND gs_ (b) = sp)))
  AND NOT (member((id1, id2), di_ )
    OR member((id2, id1), di_ ))
  -> s(i) = s(i-1) WITH [
    di := add((id1, id2), di_ )
    ,di := add((id2, id1), di_ )
    % ,dpr := dpr_ WITH []
  ],
  NOT (
    id1 > 0
    AND id2 > 0
    AND NOT (id1 = id2)
    AND member(id1, mnid_ )
    AND member(id2, mnid_ )
    AND NOT (EXISTS (a: ID_RX, b: ID_MD, c: ID_PT):
      ((prs_ (a)(id1)`1 > 0 AND (rx_ (a) = (b,c) AND gs_ (b) = sp ))
      OR (prs_ (a)(id2)`1 > 0 AND (rx_ (a) = (b,c) AND gs_ (b) = sp)))
    AND NOT (member((id1, id2), di_ )
      OR member((id2, id1), di_ ))

```

```

    ) -> s(i) = s(i-1)
ENDCOND
where
  di_   = s(i-1) `di
  ,dpr_ = s(i-1) `dpr
  ,mnid_ = s(i-1) `mnid
  ,prs_ = s(i-1) `prs
  ,rx_ = s(i-1) `rx
  ,mdpt_ = s(i-1) `mdpt
  ,gs_ = s(i-1) `gs

%remove_medicine (id: ID_RX; medicine: ID_MN)
%   prescription id must be a positive integer
%   prescription with this id does not exist
%   medication id must be a positive integer
%   medication id must be registered
%   medication is not in the prescription
rm_ft(id: ID_RX, med: ID_MN) (s) (i): bool = COND
  id > 0
  AND rxid_ (id)
  AND med > 0
  AND mnid_ (med)
  AND prs_ (id) (med) `1 > 0
  -> s(i) = s(i-1) WITH [
    prs := prs_ WITH [id := emptyfun]
  ],
  NOT (
    id > 0
    AND rxid_ (id)
    AND med > 0
    AND mnid_ (med)
    AND prs_ (id) (med) `1 > 0
  ) -> s(i) = s(i-1)
ENDCOND
where
  rxid_ = s(i-1) `rxid
  ,dpr_ = s(i-1) `dpr
  ,mnid_ = s(i-1) `mnid
  ,prs_ = s(i-1) `prs

```

```
ehealth_ft(cmd)(s)(i): bool = COND
  i = 0 -> s(0) = init_state,
  i > 0 ->
    CASES cmd(i) OF
      m_np(id, md, pt): np_ft(id, md, pt)(s)(i),
      m_ai(id1, id2): ai_ft(id1, id2)(s)(i),
      m_am(id, med, dose): am_ft(id, med, dose)(s)(i),
      m_rm(id, med): rm_ft(id, med)(s)(i)
    ENDCASES
ENDCOND

END ehealth
```

```
-- at3.txt\  
add_physician      (1, "Mayo", specialist)  
add_physician      (2, "Mayo", specialist)  
add_physician      (3, "Mayo", generalist)  
  
add_patient        (3, "Drew")  
add_patient        (1, "Drew")  
  
add_medication      (1, ["Wafarin", pill, 1.0, 6.0])  
add_medication      (2, ["acetaminophen", liquid, 1.0, 25.5])  
  
new_prescription    (2, 1, 3)  
new_prescription    (4, 3, 1)  
new_prescription    (1, 1, 1)  
  
new_prescription    (3, 2, 3)  
  
add_medicine        (1, 1, 5.5)  
add_medicine        (1, 2, 5.5)  
  
add_medicine        (4, 2, 5.5)  
  
add_medicine        (2, 2, 5.5)  
add_medicine        (2, 1, 5.5)  
  
add_medicine        (3, 1, 5.5)  
add_medicine        (3, 2, 5.5)  
  
-- error cases  
-- add_physician  
add_physician      (-1, "Mayo", specialist)  
add_physician      (1, "Mayo", specialist)  
add_physician      (6, "99Yo", specialist)  
  
-- add_patient  
add_patient        (-1, "Drew")  
add_patient        (1, "Drew")  
add_patient        (7, "76rew")  
  
-- add_medication  
add_medication      (-1, ["Wafarin", pill, 1.0, 6.0])  
add_medication      (1, ["Wafarin", pill, 1.0, 6.0])  
add_medication      (6, ["23afarin", pill, 1.0, 6.0])  
add_medication      (7, ["Wafarin", pill, 1.0, 6.0])  
add_medication      (8, ["Wafarin", pill, 6.0, 1.0])
```

Figure 13: Second Acceptance Test

```
dpr_q
-- add_interaction
add_interaction    (1,-2)
add_interaction    (1,1)
add_interaction    (7,9)
add_interaction    (1,2)
add_interaction    (1,2)
add_interaction    (2,1)
dpr_q

-- new_prescription
new_prescription   (-3, 2, 3)
new_prescription   (4, 2, 3)
new_prescription   (5, -2, 3)
new_prescription   (6, 2, 3)
new_prescription   (7, 2,-3)
new_prescription   (8, 2, 3)
new_prescription   (3, 20, 3)
new_prescription   (3, 2, 30)

-- add_medicine
add_medicine        (-2, 1, 5.5)
add_medicine        (2, -1, 5.5)
add_medicine        (2, 100, 5.5)
add_medicine        (2, 1, 5.5)
add_medicine        (2, 1, 5.5)
add_medicine        (2, 100, 55.00)

prescriptions_q(-1000)
prescriptions_q(1000)
```

Figure 14: Second Acceptance Test