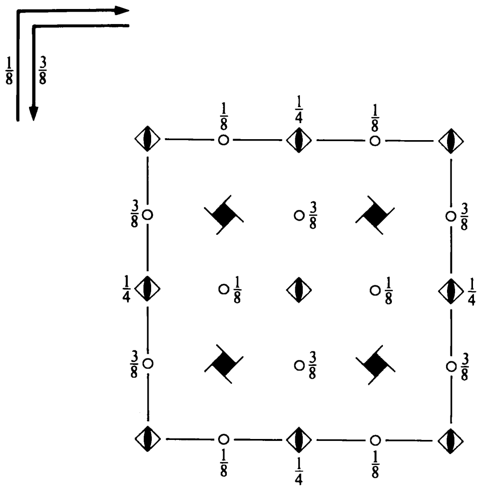
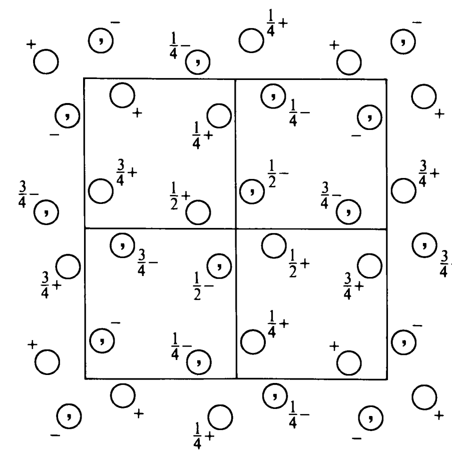
International Tables for Crystallography (2006). Vol. A, Space group 88, pp. 358–361.

$I4_1/a$ $\quad$ C_{4h}^6 $\quad$ $4/m$ $\quad$ Tetragonal

No. 88 $\quad$ $I4_1/a$ $\quad$ Patterson symmetry $I4/m$

ORIGIN CHOICE 1





Origin at $\bar{4}$, at $0,-\frac{1}{4},-\frac{1}{8}$ from $\bar{1}$

Asymmetric unit $\quad 0 \le x \le \frac{1}{4};\quad 0 \le y \le \frac{1}{4};\quad 0 \le z \le 1$

Symmetry operations

For $(0,0,0)+$ set

(1) 1	(2) $2(0,0,\frac{1}{2})\quad \frac{1}{4},\frac{1}{4},z$	(3) $4^+(0,0,\frac{1}{4})\quad -\frac{1}{4},\frac{1}{4},z$	(4) $4^-(0,0,\frac{3}{4})\quad \frac{1}{4},-\frac{1}{4},z$
(5) $\bar{1}\quad 0,\frac{1}{4},\frac{1}{8}$	(6) $a\quad x,y,\frac{3}{8}$	(7) $\bar{4}^+\ 0,0,z;\ 0,0,0$	(8) $\bar{4}^-\ 0,\frac{1}{2},z;\ 0,\frac{1}{2},\frac{1}{4}$

For $(\frac{1}{2},\frac{1}{2},\frac{1}{2})+$ set

(1) $t(\frac{1}{2},\frac{1}{2},\frac{1}{2})$	(2) $2\quad 0,0,z$	(3) $4^+(0,0,\frac{3}{4})\quad \frac{1}{4},\frac{1}{4},z$	(4) $4^-(0,0,\frac{1}{4})\quad \frac{1}{4},\frac{1}{4},z$
(5) $\bar{1}\quad \frac{1}{4},0,\frac{3}{8}$	(6) $b\quad x,y,\frac{1}{8}$	(7) $\bar{4}^+\ \frac{1}{2},0,z;\ \frac{1}{2},0,\frac{1}{4}$	(8) $\bar{4}^-\ 0,0,z;\ 0,0,0$

Generators selected (1); $t(1,0,0)$; $t(0,1,0)$; $t(0,0,1)$; $t(\frac{1}{2},\frac{1}{2},\frac{1}{2})$; (2); (3); (5)

Positions

Multiplicity, Wyckoff letter, Site symmetry			Coordinates				Reflection conditions
			$(0,0,0)+$ $(\frac{1}{2},\frac{1}{2},\frac{1}{2})+$				General:
16	f	1	(1) x,y,z (5) $\bar{x},\bar{y}+\frac{1}{2},\bar{z}+\frac{1}{4}$	(2) $\bar{x}+\frac{1}{2},\bar{y}+\frac{1}{2},z+\frac{1}{2}$ (6) $x+\frac{1}{2},y,\bar{z}+\frac{3}{4}$	(3) $\bar{y},x+\frac{1}{2},z+\frac{1}{4}$ (7) $y,\bar{x},\bar{z}$	(4) $y+\frac{1}{2},\bar{x},z+\frac{3}{4}$ (8) $\bar{y}+\frac{1}{2},x+\frac{1}{2},\bar{z}+\frac{1}{2}$	hkl : $h+k+l=2n$ $hk0$: $h,k=2n$ $0kl$: $k+l=2n$ hhl : $l=2n$ $00l$: $l=4n$ $h00$: $h=2n$ $h\bar{h}0$: $h=2n$
							Special: as above, plus
8	e	$2\,.\,.$	$0,0,z$	$0,\frac{1}{2},z+\frac{1}{4}$	$0,\frac{1}{2},\bar{z}+\frac{1}{4}$	$0,0,\bar{z}$	hkl : $l=2n+1$ or $2h+l=4n$
8	d	$\bar{1}$	$0,\frac{1}{4},\frac{5}{8}$	$\frac{1}{2},\frac{1}{4},\frac{1}{8}$	$\frac{3}{4},\frac{1}{2},\frac{7}{8}$	$\frac{3}{4},0,\frac{3}{8}$	hkl : $l=2n+1$ or $h,k=2n$, $h+k+l=4n$
8	c	$\bar{1}$	$0,\frac{1}{4},\frac{1}{8}$	$\frac{1}{2},\frac{1}{4},\frac{5}{8}$	$\frac{3}{4},\frac{1}{2},\frac{3}{8}$	$\frac{3}{4},0,\frac{7}{8}$	
4	b	$\bar{4}\,.\,.$	$0,0,\frac{1}{2}$	$0,\frac{1}{2},\frac{3}{4}$			hkl : $l=2n+1$ or $2h+l=4n$
4	a	$\bar{4}\,.\,.$	$0,0,0$	$0,\frac{1}{2},\frac{1}{4}$			

Symmetry of special projections

Along [001] $p4$
$\mathbf{a}'=\frac{1}{2}\mathbf{a}$ $\mathbf{b}'=\frac{1}{2}\mathbf{b}$
Origin at $0,0,z$

Along [100] $c2mm$
$\mathbf{a}'=\mathbf{b}$ $\mathbf{b}'=\mathbf{c}$
Origin at $x,0,\frac{3}{8}$

Along [110] $p2mg$
$\mathbf{a}'=\frac{1}{2}(-\mathbf{a}+\mathbf{b})$ $\mathbf{b}'=\frac{1}{2}\mathbf{c}$
Origin at $x,x+\frac{1}{4},\frac{1}{8}$

Maximal non-isomorphic subgroups

I [2] $I\bar{4}$ (82) (1; 2; 7; 8)+
[2] $I4_1$ (80) (1; 2; 3; 4)+
[2] $I2/a$ ($C2/c$, 15) (1; 2; 5; 6)+

IIa none

IIb none

Maximal isomorphic subgroups of lowest index

IIc [3] $I4_1/a$ ($\mathbf{c}'=3\mathbf{c}$) (88); [5] $I4_1/a$ ($\mathbf{a}'=\mathbf{a}+2\mathbf{b},\mathbf{b}'=-2\mathbf{a}+\mathbf{b}$ or $\mathbf{a}'=\mathbf{a}-2\mathbf{b},\mathbf{b}'=2\mathbf{a}+\mathbf{b}$) (88)

Minimal non-isomorphic supergroups

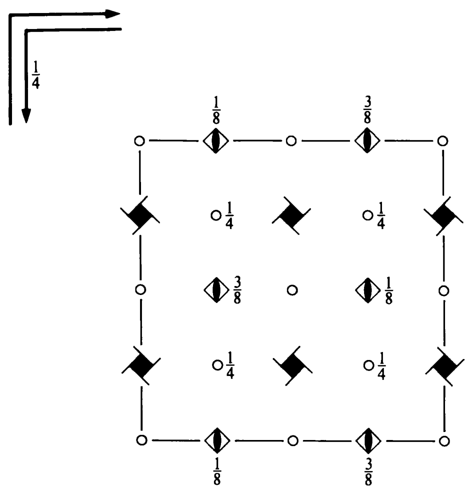
I [2] $I4_1/amd$ (141); [2] $I4_1/acd$ (142)

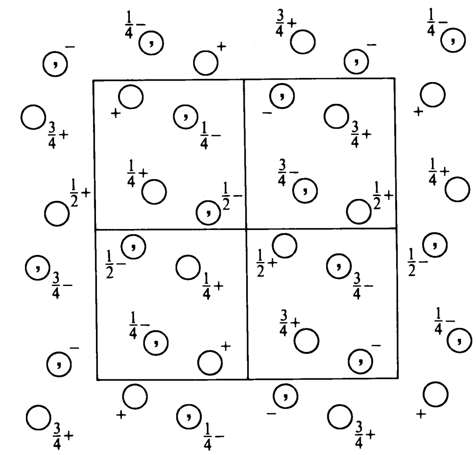
II [2] $C4_2/a$ ($\mathbf{c}'=\frac{1}{2}\mathbf{c}$) ($P4_2/n$, 86)

$I4_1/a$ $\quad C_{4h}^6$ $\quad 4/m$ $\quad$ Tetragonal

No. 88 $\quad I4_1/a$ $\quad$ Patterson symmetry $I4/m$

ORIGIN CHOICE 2





Origin at $\bar{1}$ on glide plane b, at $0, \frac{1}{4}, \frac{1}{8}$ from $\bar{4}$

Asymmetric unit $\quad 0 \le x \le \frac{1}{4}; \quad 0 \le y \le \frac{1}{4}; \quad 0 \le z \le 1$

Symmetry operations

For $(0,0,0)+$ set

(1) 1	(2) $2(0,0,\frac{1}{2})\quad \frac{1}{4},0,z$	(3) $4^+(0,0,\frac{1}{4})\quad \frac{1}{4},\frac{1}{2},z$	(4) $4^-(0,0,\frac{3}{4})\quad \frac{3}{4},0,z$
(5) $\bar{1}\quad 0,0,0$	(6) $a\quad x,y,\frac{1}{4}$	(7) $\bar{4}^+\quad \frac{1}{2},\frac{1}{4},z;\ \ \frac{1}{2},\frac{1}{4},\frac{3}{8}$	(8) $\bar{4}^-\quad 0,\frac{1}{4},z;\ \ 0,\frac{1}{4},\frac{1}{8}$

For $(\frac{1}{2},\frac{1}{2},\frac{1}{2})+$ set

(1) $t(\frac{1}{2},\frac{1}{2},\frac{1}{2})$	(2) $2\quad 0,\frac{1}{4},z$	(3) $4^+(0,0,\frac{3}{4})\quad -\frac{1}{4},\frac{1}{2},z$	(4) $4^-(0,0,\frac{1}{4})\quad \frac{1}{4},0,z$
(5) $\bar{1}\quad \frac{1}{4},\frac{1}{4},\frac{1}{4}$	(6) $b\quad x,y,0$	(7) $\bar{4}^+\quad \frac{1}{2},-\frac{1}{4},z;\ \ \frac{1}{2},-\frac{1}{4},\frac{1}{8}$	(8) $\bar{4}^-\quad 0,\frac{3}{4},z;\ \ 0,\frac{3}{4},\frac{3}{8}$

Generators selected (1); $t(1,0,0)$; $t(0,1,0)$; $t(0,0,1)$; $t(\frac{1}{2},\frac{1}{2},\frac{1}{2})$; (2); (3); (5)

Positions

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			$(0,0,0)+$ $(\frac{1}{2},\frac{1}{2},\frac{1}{2})+$				General:
16	f	1	(1) x,y,z	(2) $\bar{x}+\frac{1}{2},\bar{y},z+\frac{1}{2}$	(3) $\bar{y}+\frac{3}{4},x+\frac{1}{4},z+\frac{1}{4}$	(4) $y+\frac{3}{4},\bar{x}+\frac{3}{4},z+\frac{3}{4}$	hkl : $h+k+l=2n$
			(5) $\bar{x},\bar{y},\bar{z}$	(6) $x+\frac{1}{2},y,\bar{z}+\frac{1}{2}$	(7) $y+\frac{1}{4},\bar{x}+\frac{3}{4},\bar{z}+\frac{3}{4}$	(8) $\bar{y}+\frac{1}{4},x+\frac{1}{4},\bar{z}+\frac{1}{4}$	$hk0$: $h,k=2n$
							$0kl$: $k+l=2n$
							hhl : $l=2n$
							$00l$: $l=4n$
							$h00$: $h=2n$
							$h\bar{h}0$: $h=2n$
							Special: as above, plus
8	e	$2\,.\,.$	$0,\frac{1}{4},z$	$\frac{1}{2},\frac{1}{4},z+\frac{1}{4}$	$0,\frac{3}{4},\bar{z}$	$\frac{1}{2},\frac{3}{4},\bar{z}+\frac{3}{4}$	hkl : $l=2n+1$ or $2h+l=4n$
8	d	$\bar{1}$	$0,0,\frac{1}{2}$	$\frac{1}{2},0,0$	$\frac{3}{4},\frac{1}{4},\frac{3}{4}$	$\frac{3}{4},\frac{3}{4},\frac{1}{4}$	hkl : $l=2n+1$ or $h,k=2n$, $h+k+l=4n$
8	c	$\bar{1}$	$0,0,0$	$\frac{1}{2},0,\frac{1}{2}$	$\frac{3}{4},\frac{1}{4},\frac{1}{4}$	$\frac{3}{4},\frac{3}{4},\frac{3}{4}$	
4	b	$\bar{4}\,.\,.$	$0,\frac{1}{4},\frac{5}{8}$	$\frac{1}{2},\frac{1}{4},\frac{7}{8}$			hkl : $l=2n+1$ or $2h+l=4n$
4	a	$\bar{4}\,.\,.$	$0,\frac{1}{4},\frac{1}{8}$	$\frac{1}{2},\frac{1}{4},\frac{3}{8}$			

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Origin at $\frac{1}{4},0,z$

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$\mathbf{a}'=\mathbf{b}$ $\mathbf{b}'=\mathbf{c}$
Origin at $x,\frac{1}{4},\frac{1}{4}$

Along [110] $p2mg$
$\mathbf{a}'=\frac{1}{2}(-\mathbf{a}+\mathbf{b})$ $\mathbf{b}'=\frac{1}{2}\mathbf{c}$
Origin at $x,x,0$

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