$\mathbf{C}^{(}$	OLA") ON YOUR ASSIGNMENT. TIME: 1.5 hours.
	FIRST NAME:
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Exercise 1 [8 points]

- 1. Describe the general framework of binary classification.
- 2. Discuss the use of the logistic regression model for binary classification and describe how it can be trained using stochastic gradient descent.

[Solution: Exercise 1]

[Solution: Exercise 1]

Exercise 2 [8 points]

- 1. Introduce the concept of separating hyperplane and describe how it leads to the formulation of hard SVM.
- 2. In most practical situations data are not linearly separable. How can hard SVM be adapted to cope with this situation while still using a linear separation boundary? Formulate this adaptation in the form of an optimization problem, discussing the role and effect of the parameter λ that trades the two components of the cost function.

[Solution: Exercise 2]

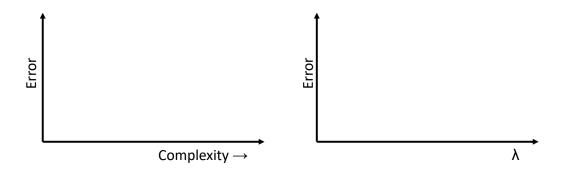
[Solution: Exercise 2]

[Solution: Exercise 2]

Exercise 3 [8 points]

With reference to the binary classification problem:

- 1. Describe how the true error $L_{\mathcal{D}}(h_s)$ of a predictor h_s can be decomposed into approximation ϵ_{app} and estimation ϵ_{est} error. Discuss how this decomposition is related to the complexity of the selected hypothesis class and draw a plot with the expected behaviour of the approximation, estimation, and true error, as functions of the complexity of the hypothesis class.
- 2. Formally introduce the Tikhonov regularization model writing down the function to be optimized. In relation with the previous answer, discuss how Tikhonov regularization can be used to control the fitting-stability trade-off. In particular discuss the behaviour of the approximation, estimation, and true error, as functions of the regularization parameter λ .



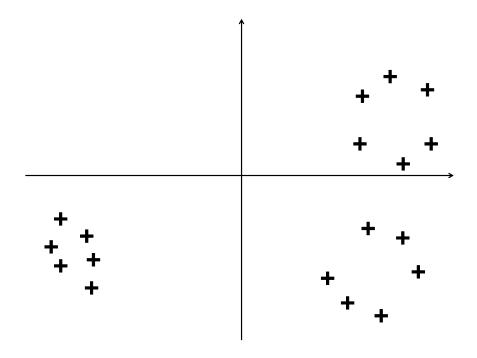
[Solution: Exercise 3]

[Solution: Exercise 3]

[Solution: Exercise 3]

Exercise 4 [8 points]

- 1. Introduce the k-means clustering problem and present the standard (i.e., Lloyd's) algorithm for its solution.
- 2. Assume that you need to cluster the points shown in the figure below into k=3 different clusters using k-means. The final solution depends on the initialization of the centroids: suggest two possible initializations, one leading to the optimal solution and one leading to a sub-optimal solution.



[Solution: Exercise 4]

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[Solution: Exercise 4]