

# Lecture 20

## Entity Authentication Protocols

Nicola Laurenti

December 4, 2020



Except where otherwise stated, this work is licensed under the Creative Commons Attribution-ShareAlike 4.0 International License.

G/K  
tUHC ✓  
✓ + +

# Lecture 20— Contents

General model

Weak authentication protocols

Strong authentication protocols

## General model for entity authentication

An entity A (called the **prover**) wants to prove his identity to another entity B (called the **verifier**), typically through an **interactive protocol**. At the end of the protocol, the entity B must decide whether he trusts A (**accept**) or not (**reject**)

### Attack scenario

**Masquerade** A malicious F wants to pose as A while interacting with B

### Requirements

**Correctness** If A is honest, B accepts him with high probability

**Security / robustness (to false provers)** If the prover is not honest (i.e., it is some F posing as A) it is hard for F to be accepted

**Non transferability (against malicious verifiers)** Even after the protocol has taken place between A and B it is hard for B to pose as A in an exchange with another entity C and be accepted

# Proofs of identity

Proof of identity in general can be based on:

- ▶ something that only A possesses: **token**, **smart card**
- ▶ something that only A is: **face**, **voice**, **biometrics**
- ▶ something that only A knows: **PIN**, **passwords**, **secret keys**

An entity authentication protocol is called **mutual** if it allows A and B to prove each one's identity to each other

We only consider protocols based on something that only A knows

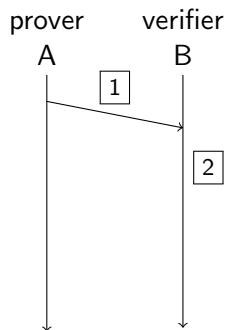
## Password based protocols

A password based entity protocol is called **strong** if

- ▶ passwords are changed frequently
- ▶ it is hard to break with sequential guessing (brute force)
- ▶ the password is never transmitted or stored in the clear

If any of the above is not met, the protocol is called **weak**

# Password authentication protocols



**entities** the prover A, the verifier B

**setup** A chooses a password  $w_A \in \mathcal{W}$  and securely delivers it to B  
 B stores a copy of  $(\text{id}_A, w_A)$  in a database  $\mathcal{D}$

**1**  $A \rightarrow B : u = (u_1, u_2) = (\text{id}_A, w_A)$

**2** B : checks if  $(u_1, u_2) \in \mathcal{D}$  and, if so, accepts A

## Weaknesses

- ▶ transferability, since B learns  $w_A$
- ▶  $w_A$  is transmitted in the clear
- ▶  $w_A$  is stored in the clear

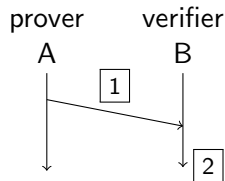
# Hashed password authentication protocols

**entities** the prover A, the verifier B

**tools** a hash function  $h : \mathcal{W} \mapsto \mathcal{T}$

**setup** A chooses a password  $w_A \in \mathcal{W}$  and securely delivers it to B

B computes  $t_A = h(w_A)$  and stores a copy of  $(\text{id}_A, t_A)$  in database  $\mathcal{D}$



1  $A \rightarrow B : u = (u_1, u_2) = (\text{id}_A, w_A)$

2 B : computes  $\tilde{t} = h(u_2)$  and checks if  $(u_1, t) \in \mathcal{D}$  and, if so, accepts A

## Improvement

- ▶  $w_A$  no longer stored in clear

## Weaknesses

- ▶ transferability, as B learns  $w_A$
- ▶  $w_A$  still transmitted in clear
- ▶ a forger could carry on a 2nd preimage

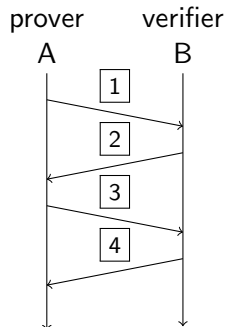
attack

# Challenge-handshake authentication protocols

**entities** the prover A, the verifier B

**tool** a hash function  $h : \mathcal{W} \times \mathcal{R} \mapsto \mathcal{X}$

**setup** A chooses a password  $w_A \in \mathcal{W}$  and securely delivers it to B



- 1  $A \rightarrow B : u_1 = [\text{id}_A]$
- 2  $B : \text{generates a challenge } r \sim \mathcal{U}(\mathcal{R})$   
 $B \rightarrow A : u_2 = [r]$
- 3  $A : \text{computes } x = h(w_A, r)$   
 $A \rightarrow B : u_3 = [x]$
- 4  $B : \text{retrieves } w_A \text{ from } \mathcal{D}$   
 $\text{computes } x = h(w_A, r)$   
 $\text{checks if } u_3 = x \text{ and, if so, accepts A}$

Observe that the password  $w_A$  is no longer transmitted in the clear, but it is still stored in the clear in  $\mathcal{D}$

# One time password protocols [Lamport, '81]

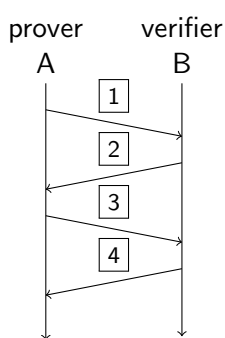
**entities** the prover A, the verifier B

**tool** two hash functions  $h : \mathcal{X} \mapsto \mathcal{X}$  and  $h' : \mathcal{W} \mapsto \mathcal{X}$

**setup** A chooses a password  $w_A \in \mathcal{W}$

A computes hash chain  $x_N = h'(w_A), x_{N-1} = h(x_N), \dots, x_0 = h(x_1)$

A securely delivers  $x_0$  to B



At the  $n$ -th protocol run,  $n = 1, \dots, N$

1 A  $\rightarrow$  B :  $u_1 = [\text{id}_A]$

2 B  $\rightarrow$  A :  $u_2 = [n]$

3 A  $\rightarrow$  B :  $u_3 = x_n$

4 B : computes  $\tilde{x}_{n-1} = h(x_n)$

checks if  $\tilde{x}_{n-1} = x_{n-1}$  and, if so, accepts A

Long-term  $w_A$  never stored or transmitted in clear

Temporary  $x_n$  transmitted in clear, but used only once

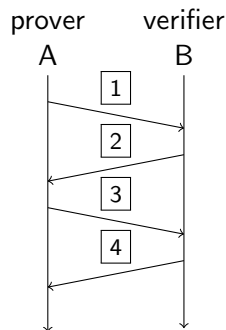
Vulnerable to **man-in-the-middle** attacks



# Challenge-response protocols with symmetric A+IP

**entities** the prover A, the verifier B

**tool** a symmetric message A+IP mechanism, of the tag appending type with key  $k_A$  and tag function  $T(\cdot, \cdot)$



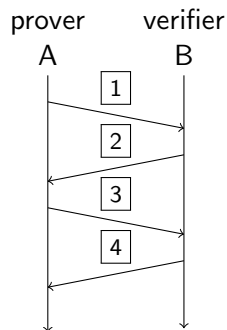
- 1  $A \rightarrow B : u_1 = \text{id}_A$
- 2  $B : \text{generates a random challenge } r \sim \mathcal{U}(\mathcal{R})$   
 $B \rightarrow A : u_2 = r$
- 3  $A : \text{builds } u_3 = \text{id}_A, r$   
 $\text{signs } t_3 = T(k_A, u_3)$   
 $A \rightarrow B : t_3$
- 4  $B : \text{verifies whether } V(k_A, u_3, t_3) = (r, \text{ok}) \text{ and, if so, accepts A}$

The challenge  $r$  must be changed at every run of the protocol, otherwise a dishonest prover F, pretending to be A, can replay 1 and 3 even without knowing  $k_A$ , and would be accepted

# Challenge-response protocols with asymmetric A+IP

**entities** the prover A, the verifier B

**tool** a digital signature mechanism, with keys  $k_A, k'_A$ ; a certificate  $c_A$  for  $k'_A$  and  $k'_B$



1  $A \rightarrow B : u_1 = \text{id}_A$

2 B : generates a random **challenge**  $r_B \sim \mathcal{U}(\mathcal{R})$

$B \rightarrow A : u_2 = r_B$

3 A : generates a random **challenge**  $r_A \sim \mathcal{U}(\mathcal{R})$

builds  $u_3 = [\text{id}_B, r_B, r_A]$  signs  $x_3 = S(k_A, u_3)$

$A \rightarrow B : x_3$

4 B : verifies whether  $V(k'_A, x_3) = ([\text{id}_B, r_B, r_A], \text{ok})$  and, if so, accepts A

The challenge  $r$  must be changed at every run of the protocol, otherwise an dishonest prover F, pretending to be A, can replay 1 and 3 even without knowing  $k_A$ , and would be accepted

# Zero-knowledge protocols [Goldwasser-Micali, '85]

A general formulation, due to [Maurer, '09]

**entities** the prover  $A$ , the verifier  $B$

**tools** two algebraic groups,  $(\mathbb{G}, \circ)$  and  $(\mathbb{H}, \star)$

the integer set  $C = \{1, |\mathbb{G}| - 1\} \subset \mathbb{N}$

a function  $f : \mathbb{G} \mapsto \mathbb{H}$  that is **one-way** and **homomorphic**, i.e.

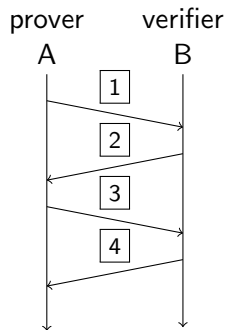
$$f(x \circ y) = f(x) \star f(y) \quad , \quad \forall x, y \in \mathbb{G}$$

**setup**  $A$  generates a random  $s_A \sim \mathcal{U}(\mathbb{G})$

computes  $t_A = f(s_A) \in \mathbb{H}$  and

securely delivers  $t_A$  to  $B$

# Zero-knowledge protocols



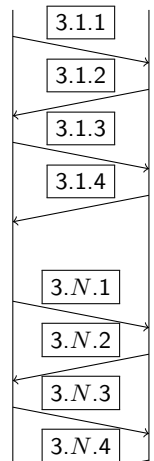
- 1  $A \rightarrow B : u_1 = [\text{id}_A]$
- 2  $B \rightarrow A : u_2 = \text{start}$
- 3  $A \leftrightarrow B : \text{perform } N \text{ iterations of the single check protocol}$
- 4  $B : \text{if all checks up to } n = N \text{ are correct, B accepts A}$

$$f(x \circ y) = f(x) \star f(y)$$

## Zero-knowledge protocols, single check

prover      verifier

A                  B



3.n.1 A : generates a random  $r_n \sim \mathcal{U}(\mathbb{G})$

computes  $v_n = f(r_n)$

$A \rightarrow B : u_{n,1} = [v_n]$

3.n.2 B : generates a random challenge  $c_n \sim \mathcal{U}(C)$

$B \rightarrow A : u_{n,2} = [c_n]$

3.n.3 A : computes  $z_n = r_n \circ \begin{pmatrix} s & c_n \\ & 0 \end{pmatrix}$

$A \rightarrow B : u_{n,3} = [z_n]$

3.n.4 B : computes  $y_n = f(z_n)$

checks whether  $y_n = v_n \star \begin{pmatrix} c_n \\ t \star \end{pmatrix}$ , and if not, rejects A

A:  $r_n$   
 $f(r_n)$

# Summary

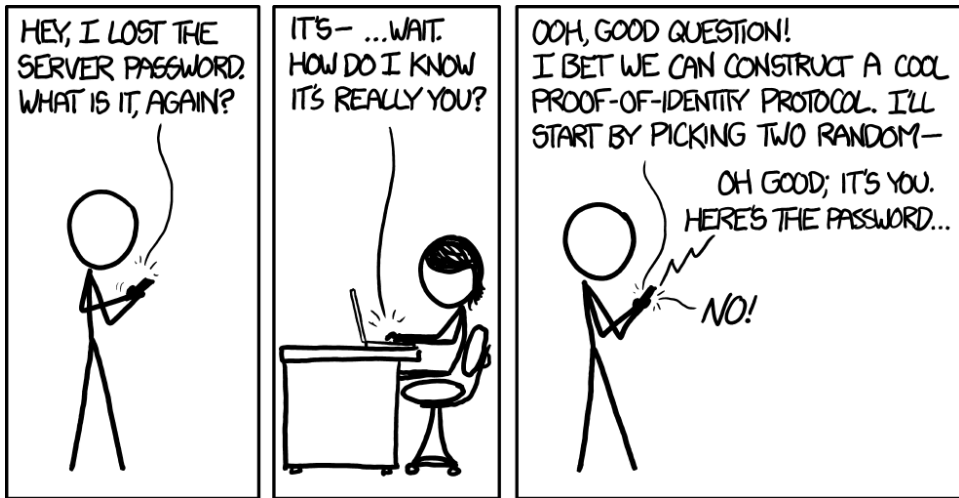
In this lecture we have:

- ▶ presented a general model for **entity authentication** and described the target requirements
- ▶ introduced examples of weak password-based entity authentication protocols
- ▶ introduced examples of strong challenge-response entity authentication protocols

## Assignment

- ▶ **class notes**
- ▶ **textbook**, §10.1 – §10.3

## End of lecture



Identity, reproduced from [xkcd](https://xkcd.com/1121) URL: [xkcd.com/1121](https://xkcd.com/1121)