

Lab Assignment 9, 05/18/2017, 1800 -- 2000

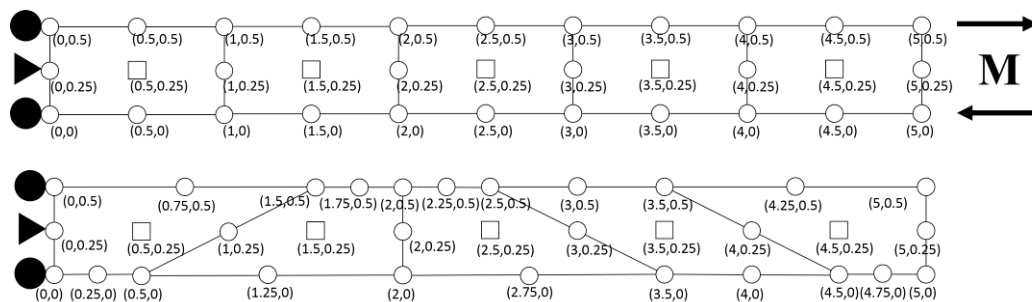
Due 2000

Lab Grading Policy: Attendance 20%, Score 80%, Bonus 40%

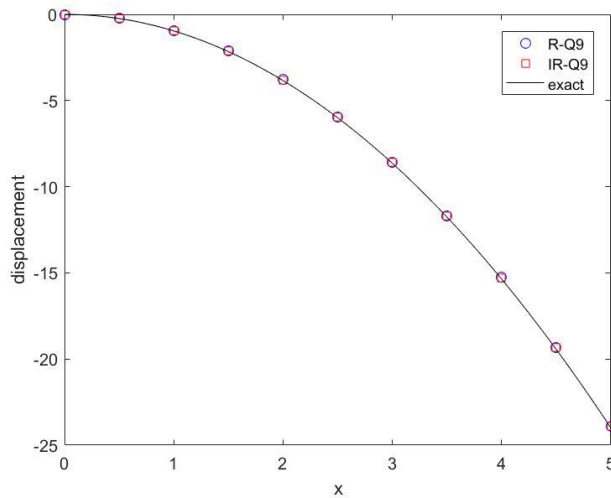
In case you have difficulty in finishing the exercises on time, you should upload them before **2100 on Saturday** and a penalty of 20% discount will be applied on your score. No late submission after 2100 on Saturday is permitted. We will in general post the reference solutions **by Sunday**.

Download Q9Simple.zip from the course website and unzip it. You will find a folder containing Q9Simple.m script file with six functions, formStiffnessRec.m guass2d.m outputDisplacements.m shapeFunctionQ9.m solution.m.

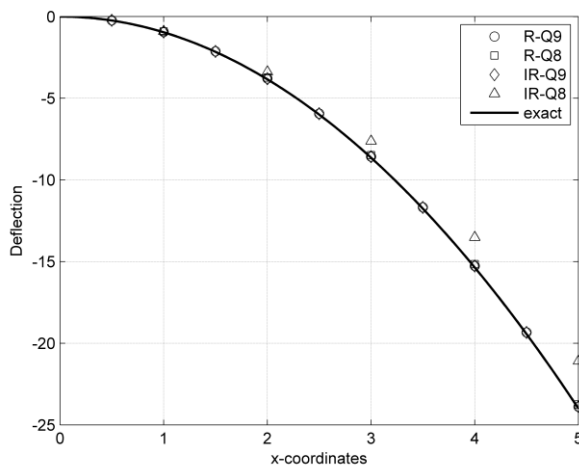
- (40%)** Consider a pure bending problem with two meshes shown below and model the problem with Q9 elements using 3x3 Gauss integration.



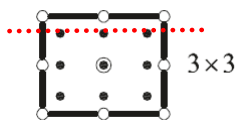
The properties are taken as $E = 30,000$, $\nu = 0.3$, thickness = 1, and $M = 600$ which gives a vertical tip displacement of -24 units. Report the displacement along the centerline and compare your Q9 results with the exact solution from the beam theory $\frac{Mx^2}{2EI}$. Below is a sample plot:



2. (40%) Extend your implementation in Problem 1 to include the eight-noded quadrilateral element with 3x3 full integration and consider the same pure bending problem again. Report the displacement along the centerline and compare your Q8 and Q9 (from Problem 1) results with the exact solution from the beam theory $\frac{Mx^2}{2EI}$. Below is a sample plot:



3. (Bonus 40%) Extend your implementation to compute the stresses at Gauss points and report the axial stress σ_{xx} along the upper line of quadrature points (靠近上邊界的高斯點) for the same pure bending problem.



Compare your Q8 and Q9 results with the exact solution from the elementary beam theory. Below is the sample plot:

