Task 1. A subspace W should statisfy 3 definitions

(1) 0 EW

(2) X+y EW whenever XEW and yEW

(3) CX = W whenever CEF and X = W so we will use the definitions to check whether the following set is a subspace.

WI. (1) (X, Y, Z)=(0,0,0) X=0=24 (V)

(3) UEW, V=(X, Y, Z), CV=c(X, Y, Z)=(cX, CY, CZ) CX=1(cy)=c(24)(V) WI is a subspace

W2.(11(X,y,z)=(0,0,0), y=0 (V)

(2) U, VEW, U=(U, U2, U3), V=(V, V2, V3) U+V=(U,+V, U2+V2, U3+V3) W2+V2=0+0=0=(W2+V2) (V)

(3) UEW, V=(X, Y, Z), EV=c(X, Y, Z)=(cX, CY, CZ) C·Y=CY=O(V) W= is a subspace

W3(1)(x,y,z)=(0,0,0), Z=0 \$2(x) W3 is not a subspace

W4(1)(X,Y,Z)=(0,0,0) X=0=y²(V) (2)U,VEW, U=(1,1,0),V=(4,2,0), V+V=(5,3,0) U,+V=5 \(\lambda\)=3²=9 (X) W4 is not a subspace

Task 2. Symmetric motrix is a square matrix which Aij = Aj; (A+A+)ij = A; j+(A+); j = A; j+Aj; = (A+A+)j; co A+A+ is symmetric for any square motix A

Task3, if x=a(y)+b(z), x is the linear combination of y and z (1) -2x+3 = a(x+3x)+b(2x+4x-1) =(a+2b)x²+(3a+4b)x+(-b) -b=3 >b=-3, a+2b=-2=a-6>a=4, 3a+4b=0=3.4+4(-3) a=4,b=-3=) Trace

(2) x2+2x-3=a(-3x2+2x+1)+b(2x2-x-1)=(-3x+2b)x2+(2a-b)x+(a-b) -3a+2b=1,2a-b=2,a-b=-3 => (2a-b)-(a-b)=a=2-(-3)=5,a-b=-3=>b=8 -3a+2b=-3:5+2:8=-1+1 count combine to x2+1x-3. False

(3) $3x^{2}+4x+1=\alpha(x^{2}-2x+1)+b(-2x^{2}-x+1)=(\alpha-2b)x^{2}+(-2\alpha-b)x+(a+b)$ $\alpha-2b=3,-2\alpha-b=4, a+b=1=(\alpha-2b)-(a+b)=-3b=3-1=2=3b=-\frac{2}{5}, a+b=1=3a=\frac{2}{5}$ $\alpha-2b=\frac{2}{5}-4-\frac{2}{5})=\frac{2}{5}+\frac{4}{5}=\frac{2}{5}=3$ $\alpha=\frac{2}{5},b=-\frac{2}{5}>\text{True}$ Task 4, if vector V in the Span(s) means V is the linear combination of S

- (i) check (2,-1,1) = a(1,0,2) +b(-1,1,1) a-b=2, b=-1,2a+b=1=>(2a+b)+(a-b)=3a=3=a=1,b=-1 a-b=1-(-1)=2,2a+b=2+(-1)=1 (2,-1,1) is in the Span(s)
- (2) check (-1,2,1) = a(1,0,2)+b(-1,1,1) a-b=-1, b=2, 2a+b=1=>(a-b)+(2a+b)=3a=0=a=0, b=2 A-b=0-2=-2+-1 carlt combine to (-1,2,1), inft in the Span(s)
- (3) check (-1,1,2)=a(1,0,1,-1)+b(0,1,1,1) a=-1,b=1, a+b=1,2a+b=2=) a+b=(-1)+1=0+1 court combine to (-1,1,1,2), isn't in the Span(s)

Task S. We attempt Martix A is the linear combination of Mi, M2, M3, A = [A11 A22] = a [69] + b [09] + c [96] the equation can be express below:

 $0+0+0=A_{11}$ $0=A_{11}$ $0=A_{12}$ $0=A_{12}$ and because A_{12} and A_{21} always be the same $0+0+0=A_{21}$ $0+b+0=A_{22}$ $0+b+0=A_{22}$

which means span (M, M2, M3) is the set of all symmetic matrix