

Date) 28/02/23)

## { Data Structures }

Hashing :: It also a Searching technique.

What is Set?

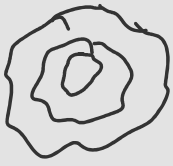
It is a Collection of objects themselves are Called Elements.

For Exe = A Set of Natural numbers  $M = \{1, 2, \dots, N\}$

$A = \{0, 2, 4, 6, 8\}$  Set of non-negative Even numbers less than 10.

↑  
Elements of Set.

$A = \{11, 12, 13, \dots\}$  Set of all numbers greater than 10.



Empty set

$$A = \{1, 2, 3, 4, 5, 6\}$$

$$B = \{2, 4, 6\}$$

$$A \cup B = \{1, 2, 3, 4, 5, 6\}$$

$$A \cap B = \{2, 4, 6\}$$

$$A - B = \{1, 3, 5\}$$

$$B - A = \{\emptyset\} \quad \{\} \quad \emptyset$$

The bit string of the sets  $\{1, 2, 3, 4, 5\}$  and  $\{1, 3, 5, 7, 9\}$  are  
1111100000 and 1010101010 respectively. We bit string  
find the union and intersection of sets.

$$A = \{1, 2, 3, 4, 5\} = 1111100000$$

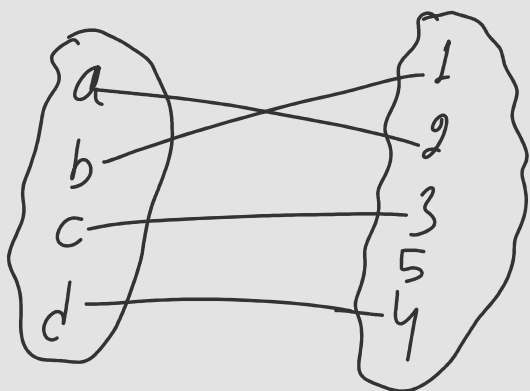
$$B = \{1, 3, 5, 7, 9\} = 1010101010$$

$$A \cap B = \{ \quad \quad \quad \} = 1010100000 \checkmark$$

$$A \cup B = \{ \quad \quad \quad \} = 1111101010 \checkmark$$

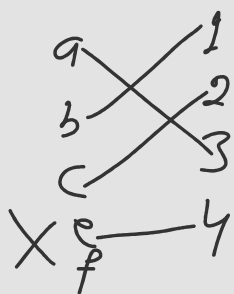
one-one & onto

$$f(x_1) = f(x_2) \text{ iff } x_1 = x_2$$

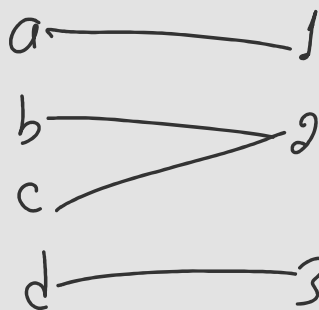


one-one

$f(x) = x^2$  is not one-one.



one-one.  
not onto



onto

$J = \mathbb{R}$

multisets:

$$A = \{1, 1, 1, 2, 2, 3\}$$

$$S = \{3 \cdot 1, 2 \cdot 2, 1 \cdot 3\}$$

$n_i$  = number of elements.  
element

$$S = \{n_1 \cdot a_1, n_2 \cdot a_2, n_3 \cdot a_3, \dots, n_i \cdot a_i\}$$

$$A = \{1, 1, 1, 2, 2, 3\}$$

$$B = \{1, 1, 4, 3\}$$

$$A \cup B = \{1, 1, 1, 2, 2, 3, 4\}$$

$$A \cap B = \{1, 1, 3\}$$

$$A + B = \{1, 1, 1, 1, 1, 2, 2, 3, 3, 4\}$$

$$A - B = \{1, 2, 2\}$$

$$A = \{3.a, 2.b, 1.c\}$$

$$B = \{2.a, 3.b, 4.d\}$$

$$A \cup B = \{3.a, 3.b, 1.c, 4.d\}$$

$$A \cap B = \{2.a, 2.b\}$$

$$A - B = \{1.c\}$$

$$B - A = \{4.d\}$$

Hashing technique: It is a searching method

Linear Search:

$$A = \begin{array}{|c|c|c|c|c|c|c|c|} \hline 8 & 3 & 5 & 7 & 2 & 4 & 6 & 1 \\ \hline 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ \hline \end{array}$$

$O(n)$

Binary Search

key = 22  
key = 9

$O(1)$ ,  $O(1)$

Best Case Worst Case

$$B = \begin{array}{|c|c|c|c|c|c|c|c|} \hline 9 & 4 & 6 & 7 & 9 & 12 & 15 & 20 \\ \hline 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ \hline \end{array}$$

key = 12

~~9~~

12 > 9

$$T(n) = T(n/2) + O(1)$$

0, 1, 2, 3, 4, 5, 6, 7, 8

$$O(1) \text{ mid} = \frac{8+0}{2} = 4$$

if (key == A[mid])  
return mid.  $O(1)$

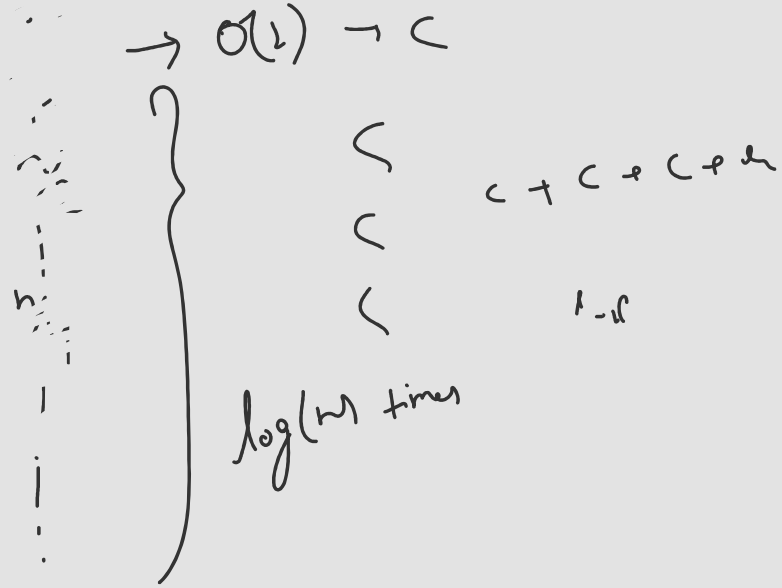
$$T(n) = T(n/2) + 1$$

$$O(\lg n)$$

$$T(n) = T(n/2) + 1$$

$$T(n/2) = T(n/4) + 1$$

$$T(n/4) = T(n/8) + 1$$





$$\frac{n}{2^k} = 1$$

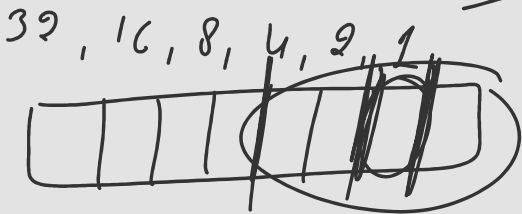
$$n = 2^k$$

$$k = \log_2 n$$

$$T(n) = 1 + K$$

$$= 1 + (\log_2 n)$$

$$T(n) = O(\log_2 n)$$



$$T(n) = T(n/2) + 1 \Rightarrow T(n) = T(n/8) + 3$$

$$T(n/2) = T(n/4) + 1 \Rightarrow T(n/2) = T(n/8) + 2$$

$$T(n/4) = T(n/8) + 1$$

After 3<sup>rd</sup> iteration

$$T(n) = T(n/8) + 3$$

$$T(n) = T(n/2^3) + 3$$

After  $k^{th}$  iteration

$$T(n) = T(n/2^k) + k$$

$$T(n) = T(1) + k$$

$$n = 2^{10} \text{ power}$$

$$n = n/2^6$$

$$n/2 = n/2^1$$

$$n/4 = n/2^2$$

$$n/2^k = 1$$

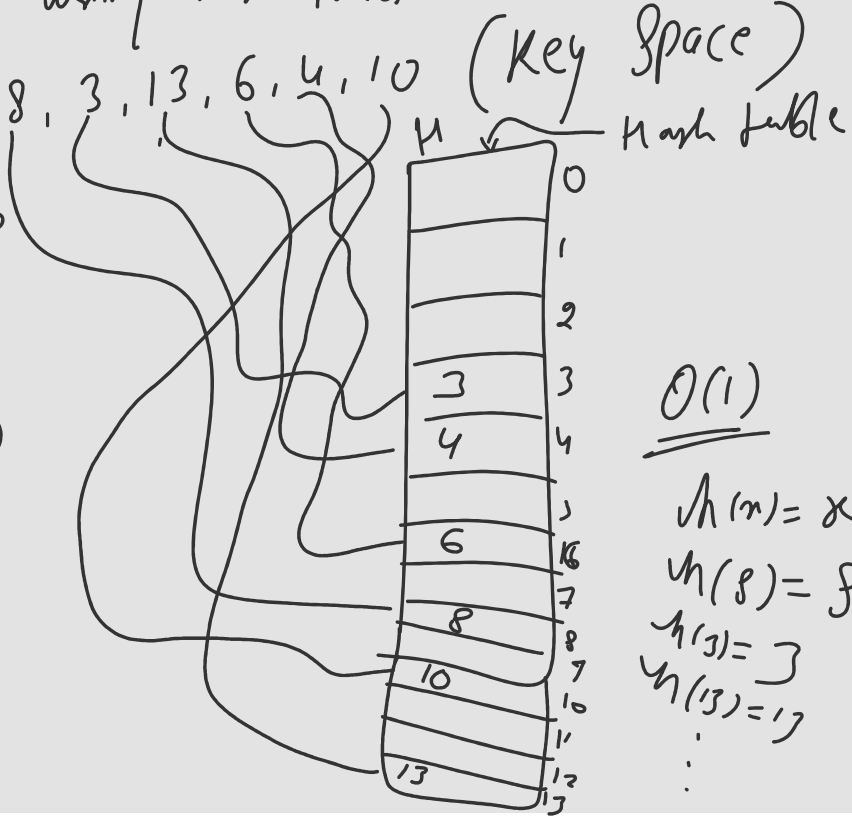
Hashing: Hashing is a technique or process of mapping keys and values into hash table using hash function.

Given Key: 8, 3, 13, 6, 4, 10 (Key space)

8, 3, 13, 6, 4, 10, 1000

	0
	1
3	2
4	3
	4
6	5
	6
8	7
10	8
	9
	10
	11
13	12
	13
...	...
1000	1000

$O(1)$



$O(1)$

$$h(n) = x$$

$$h(8) = 7$$

$$h(3) = 2$$

$$h(13) = 12$$

...

$O(n)$

$O(n)$

$E(n)$

-18

Modified hash function:

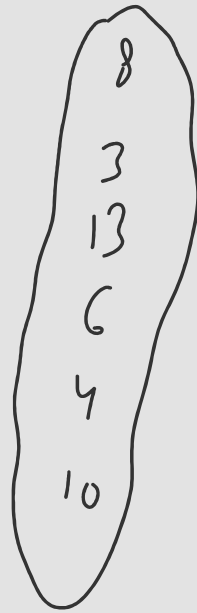
$$h(x) = x \% \text{size}$$

$$h(8) = 8 \% 10 = 8$$

$$h(3) = 3 \% 10 = 3$$

$$h(13) = 13 \% 10 = 3$$

$$h(6) = 6 \% 6 = 6$$



hash table:

10	0
	1
	2
3, 13	3
4	4
	5
6	6
	7
8	8
	9

Collision

Collision resolution methods.

1) open hashing ✓  
 . chaining ✓

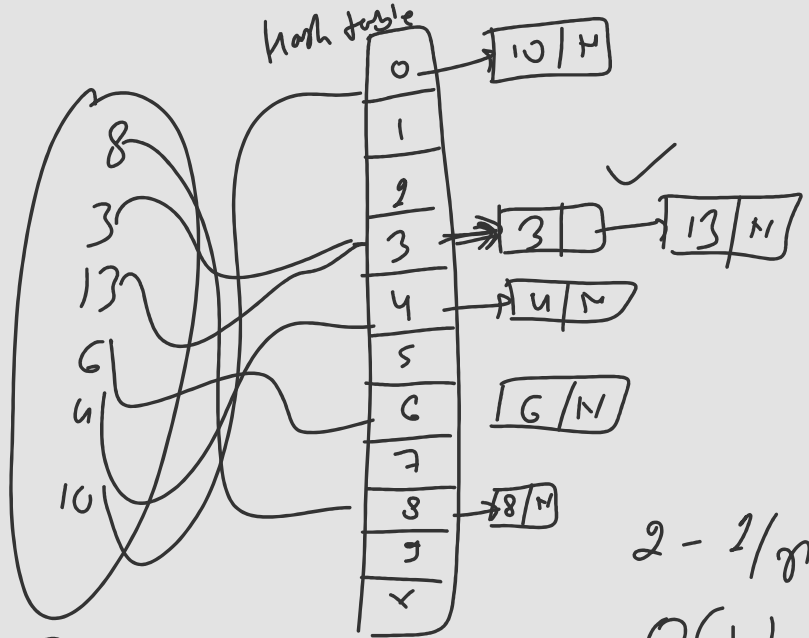
2) closed hashing

i) Linear Probing  
 ii) Quadratic Probing

key = 13



7, 72, 77, 74, 71, 72, 73, ...



$$2 - 1/n$$

$$O(1)$$

Worst Case =  $O(n)$

Closed hashing

- 1) Linear probing
- 1b) Quadratic probing

1) Linear probing:  $h(n) = x \% \text{size}$  ✓ <sup>10</sup>

$$h'(n) = [h(n) + f(i)] \% \text{size}$$

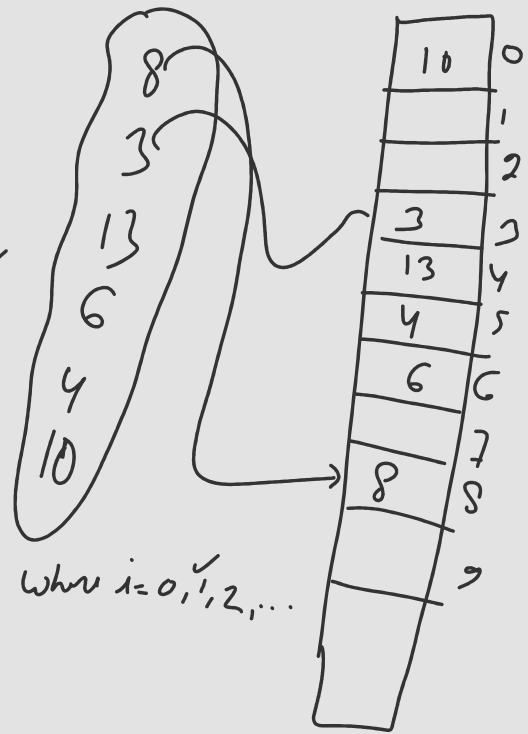
$$h'(8) = [8 \% 10 + 0] \% 10 = 8$$

linear function

$$h'(3) = [3 \% 10 + 0] \% 10 = 3 \quad h'(4) = 4$$

$$h'(13) = [13 \% 10 + 0] \% 10 = 3$$

$$h'(13) = [13 \% 10 + 1] \% 10 = 4$$



§ Quadratic probing:

$$h'(n) = [h(n) + f(i)] \% \text{size}$$

$$h'(8) = [8 \% 10 + 0] \% 10 = 8 \quad f(i) = i^2$$

$$h'(3) = [3 \% 10 + 0] \% 10 = 3$$

$$h'(13) = [13 \% 10 + 0] \% 10 = 3$$

$$h'(13) = [13 \% 10 + 1] \% 10 = 4 \quad f(i) = i^2$$

$$h'(23) = [23 \% 10 + 0] \% 10 = 3$$

$$h'(23) = [23 \% 10 + 1] \% 10 = 4$$

$$h'(23) = [23 \% 10 + 4] \% 10 = 7$$

$$h'(43) = [43 \% 10 + 9] \% 10 = 2$$

