

Selection sort

Best $\rightarrow O(1)$

- ① take one element and compare it with every element

Bubble Sort

- ① make a bubble of 2 element and compare them
- ② from this max element is goes to ending index
- ③ then again we make a bubble of 2 element and compare them with $n-2-i$ index

Insertion sort

- ① ~~make~~ firstly make first element is sorted (Assume that is diff array)
- ② then go the next position and check above array for that position
- ③ every time we have a array for check that is already sorted

10 30 20 80 70 10 60 40 70

↓

10

↓

10 30

↓

10 20 30

↓

10 20 80

↓

10 20 30 70 80

↓

10 20 30 70 10 80

↓

10 20 20 30 70 80

↓

10 10 20 30 70 60 80

↓

10 10 20 30 60 70 80

↓

10 10 20 30 60 70 40 80

↓

10 10 20 30 40 60 70 80

↓

10 10 20 30 40 60 70 70 80

↓

10 10 20 30 40 60 70 70 80

$J = 0 \& \& A[J] > item$

- ① started \rightarrow comparison $\rightarrow n-1$
swap $\rightarrow 0 \quad O(n)$

- ② Input is sorted in reverse
comparison $= \frac{n(n-1)}{2}$
swap $= \frac{n(n-1)}{2} \quad O(n^2)$

- ③ Random $= A_{it} = \sum_{j=1}^n j \times P_j$
is is is
 $J = \text{key go to its location}$
 $P_j = \text{Probability of one element in array}$

10 20 30 10 70 80

10 20 10 30 70 80

$$\text{Avg comparison} \rightarrow A_{it+1} = \frac{1}{i+1} \times \frac{i(i+1)}{2} = \frac{i+2}{2}$$

$$= \frac{1}{i+1} \sum_{j=1}^{i+1} j$$

Total no of comparisons =

$$O(n) = \sum_{i=1}^{n-1} A_{it+1} = \frac{1+2}{2} \Rightarrow \sum_{i=0}^{n-1} \frac{1}{2} + \sum_{i=0}^{n-1} 1$$

$$= \frac{1}{2} \cdot \frac{n(n-1)}{2} + (n-1)$$

$$\text{movement} = M_i = i + (i-1) + (i-2) + \dots + 1 = \frac{i+1}{2}$$

$$\text{Total no of movement} = \sum_{i=1}^{n-1} M_i = \frac{1}{2} \cdot \frac{n(n-1)}{2} + \frac{(n-1)}{2} \Rightarrow \frac{(n-1)(n+2)}{4}$$

$$\text{Average case} = O(n^2)$$

for time complexity = comparison + movement

Selection sort:- Best case \rightarrow Sorted \rightarrow Comparison $\rightarrow C(n) = \sum_{i=1}^{n-1} (n-i)$

$$= \frac{n(n-1)}{2} \quad O(n^2)$$

$$\text{Movement} = 0$$

Reverse unsorted \rightarrow Comparison $= C(n) = \sum_{i=1}^{n-1} (n-i)$

$$= \frac{n(n-1)}{2} \quad O(n^2)$$

$$\text{Movement}(n) = \frac{3}{2}(n-1)$$

swapping $\left[\begin{array}{l} \text{temp} = a[i] \\ a[i] = a[j] \\ a[j] = \text{temp} \end{array} \right]$

Random order \rightarrow Comparison $= \frac{n(n-1)}{2}$

$$\text{Movement} = \text{Total no of swap operations} = (1-p_i) \times (n-1)$$

$$p_1 = p_2 = p_3 \dots p_n = \frac{1}{n}$$

$$M(n) = \left(1 - \frac{1}{n}\right) \times (n-1)$$

$$= \frac{(n-1)(2n-1)}{2}$$

Bubble Sort:- sorted order \rightarrow Best case $= C(n) = \sum_{i=1}^{n-1} (n-i)$

$$= \frac{n(n-1)}{2} \quad (O(n^2))$$

$OR (O(n))$

$$\text{movement} = 0$$

$$\text{Reverse order} = C(n) = \frac{n(n-1)}{2}$$

$$\text{movement} = \frac{n(n-1)}{2}$$

$$\text{Random order} = C(n) = \sum_{j=1}^{n-i+1} (n-i+1-j) \cdot p_j$$

$$1 \leq j \leq n-i+1$$

$$= \frac{1}{n-i+1} \sum_{j=1}^{n-i+1} (n-i+1-j) = \frac{1}{n-i+1} \sum_{j=1}^{n-i+1} j$$

$$= (n-i+1) \Rightarrow \frac{1}{n-i+1} \frac{(n-i+1)(n-i+2)}{2}$$

$$= \frac{2n-2i+2 - n-i+2}{2} = \frac{n-i}{2}$$

$$= \frac{n(n-1)}{4}$$

Quick Sort

$$\text{space of stack} = \log(n)$$

$$\text{ascending order} = \text{comparison} = C(n) = n-1 + (n-1) + \dots$$

$$(\text{worst case}) \quad C(n) = (n-1) + (n-2) + (n-3) + \dots + 1$$

$$C(n) = \frac{n(n-1)}{2}$$

$$O(n^2)$$

$$\text{Movement} = 0$$

$$\text{Reverse order} = \text{comparison} = C(n) = (n-1) + (n-2) + (n-3) + \dots + 1$$

$$= \frac{n(n-1)}{2}$$

$$\text{Movement} = \begin{cases} \frac{n-1}{2} & \text{if } n \text{ is odd} \\ \frac{n}{2} & \text{if } n \text{ is even} \end{cases}$$

Random order

Counting Sort

A

1	2	3	4	5	6	7	8
2	5	3	0	2	3	0	3

Start from last
and update c array every
time

C

0	1	2	3	4	5
2	0	2	3	0	1

 frequency

C

0	1	2	3	4	5
2	2	4	7	7	8

 cumulative sum

B

1	2	3	4	5	6	7	8
						3	

C

0	1	2	3	4	5
2	2	4	6	7	8

B

1	2	3	4	5	6	7	8
	0					3	

C

0	1	2	3	4	5
1	2	4	6	7	8

B

1	2	3	4	5	6	7	8
	0				3	3	

C

0	1	2	3	4	5
1	2	4	5	7	8

B

1	2	3	4	5	6	7	8
	0		2		3	3	

C

0	1	2	3	4	5
1	2	3	5	7	8

B

1	2	3	4	5	6	7	8
0	0		2		3	3	

C

0	1	2	3	4	5
0	2	3	5	7	8

B

1	2	3	4	5	6	7	8
0	0		2	3	3	3	

C

0	1	2	3	4	5
0	2	3	4	7	8

B

1	2	3	4	5	6	7	8
0	0		2	3	3	3	5

C

0	1	2	3	4	5
0	2	3	4	7	7

B

1	2	3	4	5	6	7	8
0	0	2	2	3	3	3	5

C

0	1	2	3	4	5
0	2	2	4	7	7

$O(n)$

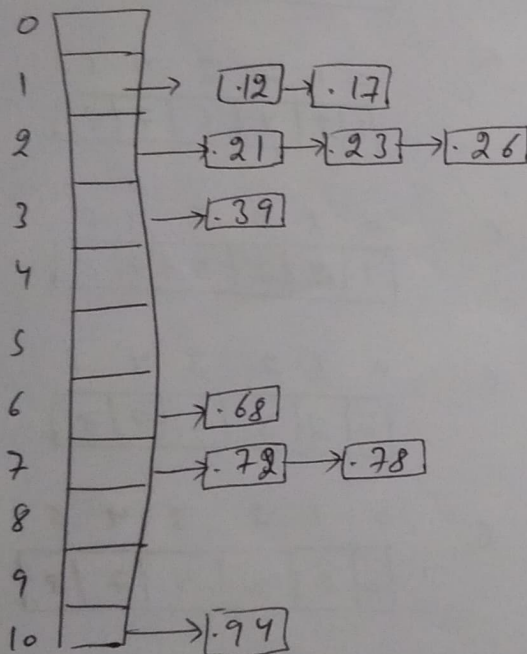
Bucket Sort

$\text{Floor}\left(\frac{n * (\text{element} - \text{min})}{1 + \text{max} - \text{min}}\right) \rightarrow$ if no's are not only in 0,1 range

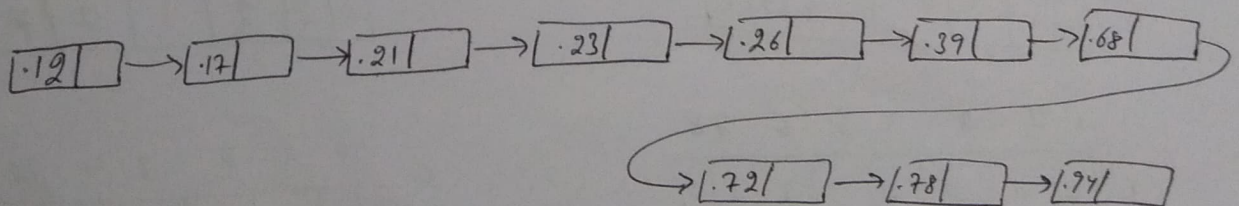
$\text{Floor}(n * A[i]) \rightarrow$ if no's are in range of 0,1

A

1	2	3	4	5	6	7	8	9	10
.78	.17	.39	.26	.72	.94	.21	.12	.23	.68



when no is placing in Bucket
also sort that list of Buckets
this time



Heap Sort

Heapify

Build Heap

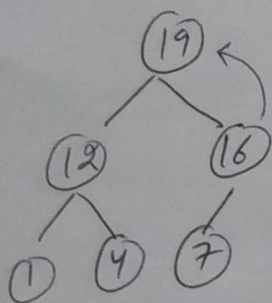
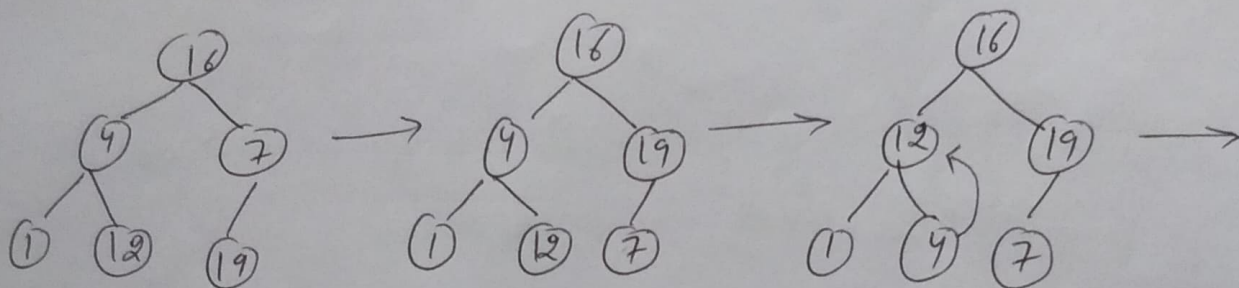
Heap Sort

$n \log n$

16	4	7	1	12	19
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for ~~max~~ increasing order \rightarrow make max heap

" decreasing order \rightarrow make min heap



here we make max heap now we delete element from root and replace it with lowest element (leaf node) element and delete that leaf element and again call heapify function

Simultaneously repeat this process