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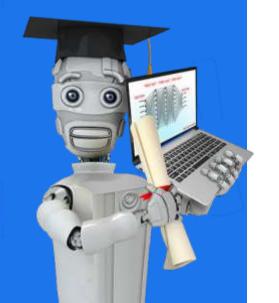
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Classification

Motivations

Classification

Question

Is this email spam?

Is the transaction fraudulent?

Is the tumor malignant?

Answer "y"

no yes

no yes

y can only be one of two values

"binary classification"

"negative class"

"bad"

absence

false

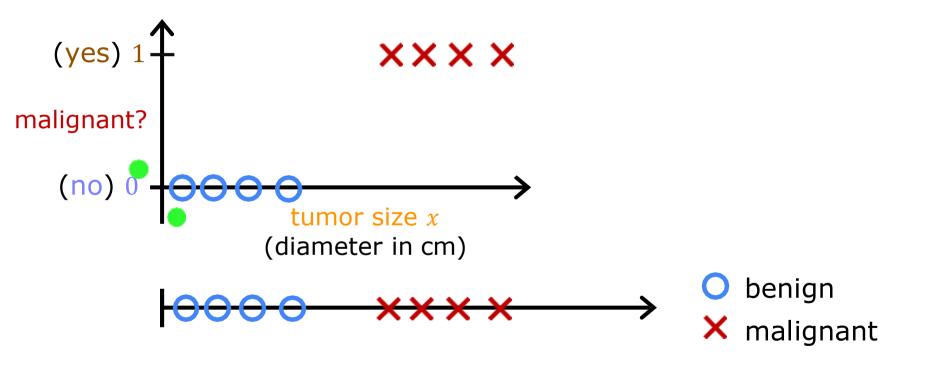
true

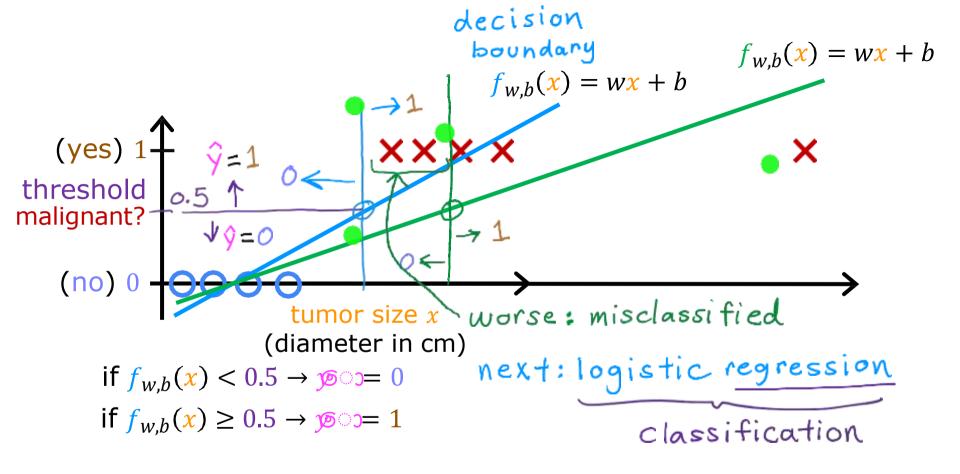
useful for classification

"positive class"

"good"

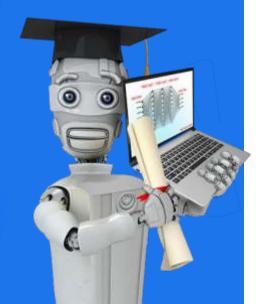
presence





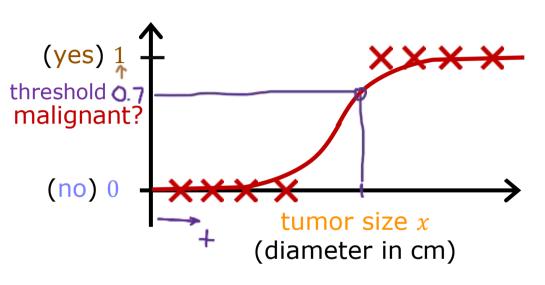


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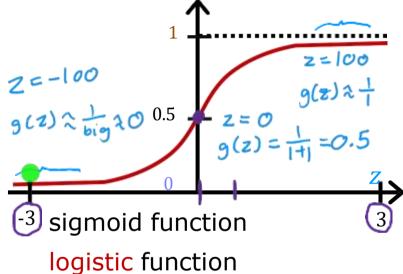


Classification

Logistic Regression



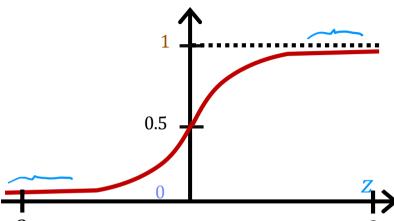
Want outputs between 0 and 1



outputs between 0 and 1

$$g(z) = \frac{1}{1+e^{-z}}$$
 $0 < g(z) < 1$

Want outputs between 0 and 1

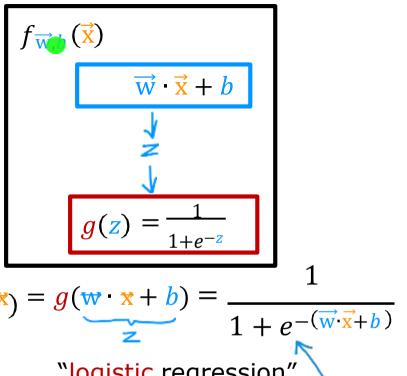


sigmoid function

logistic function

outputs between 0 and 1

$$g(z) = \frac{1}{1+e^{-z}}$$
 $0 < g(z) < 1$



"logistic regression"

Interpretation of logistic regression output

$$f_{\overrightarrow{\mathbf{w}},b}(\overset{\mathbf{x}}{)} = \frac{1}{1 + e^{-(\overrightarrow{\mathbf{w}}\cdot\overrightarrow{\mathbf{x}}+b)}}$$

"probability" that class is 1

Example:

x is "tumor size" y is 0 (not malignant) or 1 (malignant)

$$f_{\overrightarrow{\mathbf{w}},b}(\overrightarrow{\mathbf{x}}) = 0.7$$

70% chance that y is 1

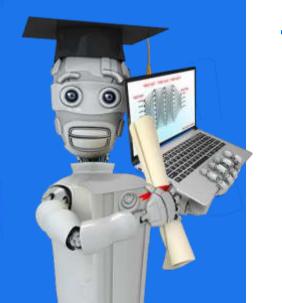
$$f_{\overrightarrow{\mathbf{w}},b}(\overrightarrow{\mathbf{x}}) = P(y = 1 | \overrightarrow{\mathbf{x}}; \overrightarrow{\mathbf{w}},b)$$

Probability that y is 1, given input \vec{x} , parameters \vec{w} , b

$$P(y = 0) + P(y = 1) = 1$$

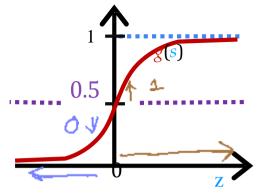


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Classification

Decision Boundary



$$f_{\overrightarrow{\mathbf{w}},b} (\overrightarrow{\mathbf{X}})$$

$$s = \overrightarrow{\mathbf{w}} \cdot \overrightarrow{\mathbf{x}} + b$$

$$y$$

$$\mathbf{z}$$

$$y$$

$$\mathbf{g}(s) = \frac{1}{1 + e^{-s}}$$

$$f_{\overrightarrow{w},b}(\overrightarrow{x}) = g(\overrightarrow{w} \bullet \overrightarrow{x} + \overline{b}) \frac{1}{1 + e^{-(\overrightarrow{w} \bullet \overrightarrow{x} + b)}}$$

$$= P(y = 1 | x; \overrightarrow{w},b) \quad 0.7 \quad 0.3$$

$$O \text{ or } 1? \quad \text{threshold}$$

$$\text{Is } f_{\overrightarrow{w},b}(\overrightarrow{x}) \geq 0.5?$$

$$\text{Yes: } \hat{y} = 1 \qquad \text{No: } \hat{y} = 0$$

$$\text{When is }$$

$$f_{\overrightarrow{w},b}(\overrightarrow{x}) \geq 0.5$$

$$s \geq 0 \qquad < 0$$

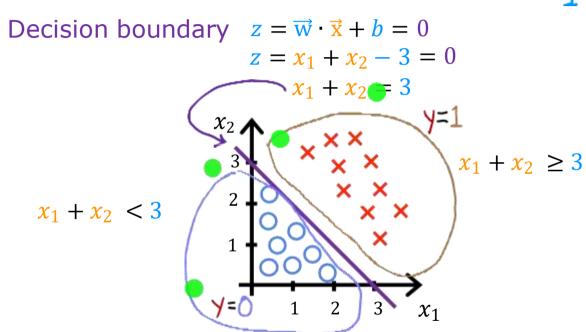
$$\overrightarrow{w} \bullet \overrightarrow{x} + b \geq 0 \qquad \overrightarrow{w} \bullet \overrightarrow{x} + b < 0$$

 $\hat{v} = 1$

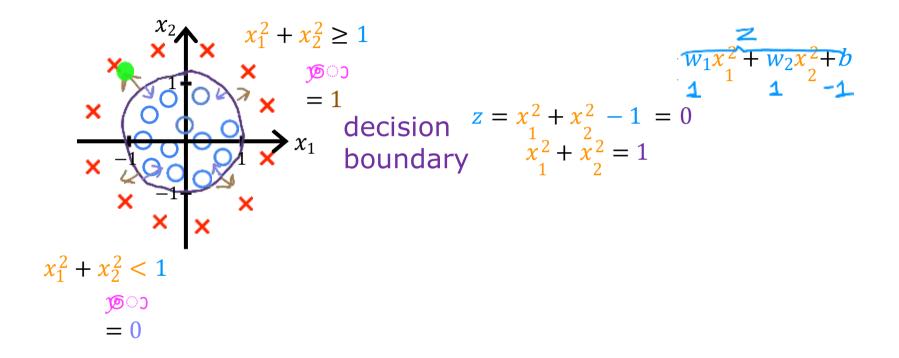
 $\hat{v} = 0$

Decision boundary

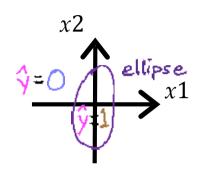
$$f_{\vec{w},b}(\vec{x}) = g(z) = g(w_1x_1 + w_2x_2 + b)$$

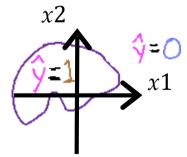


Non-linear decision boundaries



Non-linear decision boundaries

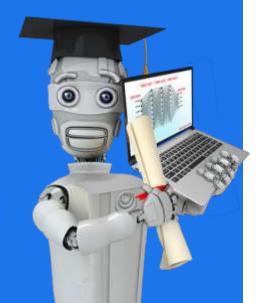




$$f_{\vec{w},b}(\vec{x}) = g(s) = g(r_1x_1 + r_2x_2 + r_3x_1^2 + r_4x_1x_2 + r_5x_2^2 + r_6x_1^3 + \dots + b)$$

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Cost Function

Cost Function for Logistic Regression

Training set

| | tumor size (cm) | patient's age | malignant? | i=1,,m training examples |
|-----|-----------------|-------------------|------------|---|
| | X <u>1</u> | Χn | У | j=1,,n features |
| i=1 | 10 | 52 | 1 | target y is 0 or 1 |
| : | 2 | 73 | 0 | target y 15 0 01 1 |
| • | 5 | 55 | 0 | $f_{\overrightarrow{x}} \cdot (\overrightarrow{y}) = \frac{1}{1}$ |
| | 12 | 49 | 1 | $f_{\overrightarrow{\mathbf{w}},b}(\overrightarrow{\mathbf{x}}) = \frac{1}{1 + e^{-(\overrightarrow{\mathbf{w}} \cdot \overrightarrow{\mathbf{x}} + b)}}$ |
| i=m | | | | |

How to choose $\vec{w} = [w_1 \ w_2 \ \cdots \ w_n]$ and b?

Squared error cost

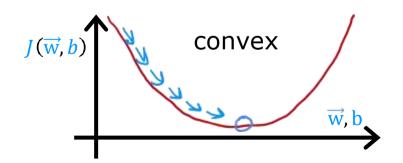
$$J(\overrightarrow{\mathbf{w}}, b) = \frac{1}{m} \sum_{i=1}^{m} \frac{1}{2} (f_{\overrightarrow{\mathbf{w}}, b}(\overrightarrow{\mathbf{x}}^{(i)}) - y^{(i)})^{2}$$

$$L(f_{\overrightarrow{\mathbf{w}}, b}(\overrightarrow{\mathbf{x}}^{(i)}), y^{(i)})$$

average of training set

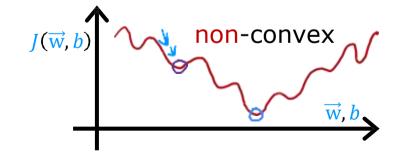
linear regression

$$f_{\overrightarrow{\mathbf{w}},b}(\overrightarrow{\mathbf{x}}) = \overrightarrow{\mathbf{w}} \cdot \overrightarrow{\mathbf{x}} + b$$

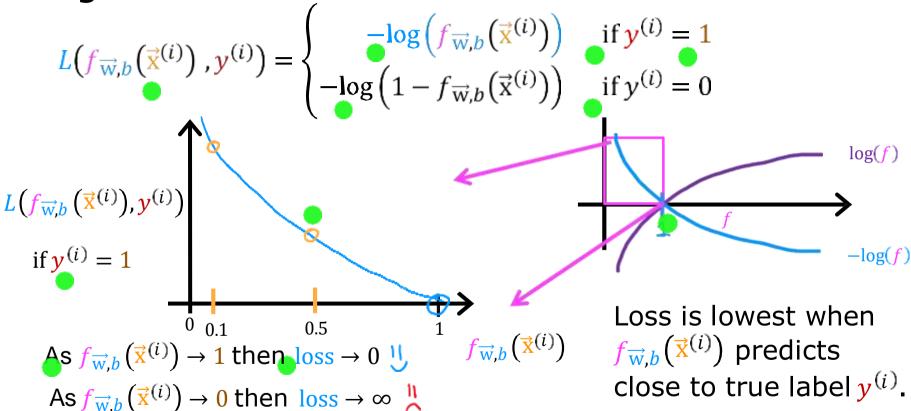


logistic regression

$$f_{\overrightarrow{\mathbf{w}},b}(\overrightarrow{\mathbf{x}}) = \frac{1}{1 + e^{-(\overrightarrow{\mathbf{w}} \cdot \overrightarrow{\mathbf{x}} + b)}}$$



Logistic loss function



Logistic loss function

$$L(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}),y^{(i)}) = \begin{cases} -\log\left(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)})\right) & \text{if } y^{(i)} = 1\\ -\log\left(1-f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)})\right) & \text{if } y^{(i)} = 0 \end{cases}$$

$$As \ f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}) \rightarrow 0 \text{ then } loss \rightarrow 0 \text{ l.}$$

$$L(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}),y^{(i)}) \\ \text{if } y^{(i)} = 0 \\ \text{not malignate} \end{cases}$$

$$The further prediction f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}) \text{ is from target } y^{(i)}, \text{ the higher the loss.}$$

Cost

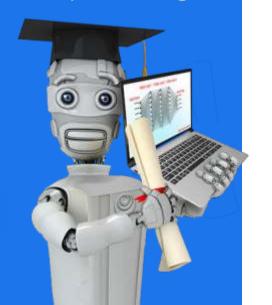
$$J(\vec{w},b) = \frac{1}{m} \sum_{i=1}^{m} L(f_{\vec{w},b}(\vec{x}^{(i)}), y^{(i)})$$

$$= \begin{cases} \bullet & -\log(f_{\vec{w},b}(\vec{x}^{(i)})) & \text{if } y^{(i)} = 1 \\ -\log(1 - f_{\vec{w},b}(\vec{x}^{(i)})) & \text{if } y^{(i)} = 0 \end{cases} \text{ global minimum}$$

$$find w, b \text{ that minimize cost } J$$

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Cost Function

Simplified Cost Function for Logistic Regression

Simplified loss function

$$L(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}), y^{(i)}) = \begin{cases} -\log(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)})) & \text{if } y^{(i)} = 1\\ -\log(1 - f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)})) & \text{if } y^{(i)} = 0 \end{cases}$$

$$L(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}), y^{(i)}) = -y^{(i)}\log(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)})) - (1 - y^{(i)})\log(1 - f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}))$$

$$\text{if } y^{(i)} = 1:$$

$$L(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}), y^{(i)}) = -1\log(f(\overrightarrow{x}))$$

Simplified loss function

$$L(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}), y^{(i)}) = \begin{cases} -\log(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)})) & \text{if } y^{(i)} = 1\\ -\log(1 - f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)})) & \text{if } y^{(i)} = 0 \end{cases}$$

$$L(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}), y^{(i)}) = -y^{(i)}\log(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)})) - (1 - y^{(i)})\log(1 - f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}))$$

$$\text{if } y^{(i)} = 1:$$

$$L(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}), y^{(i)}) = -1\log(f(\overrightarrow{x}))$$

$$\text{if } y^{(i)} = 0:$$

$$L(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}), y^{(i)}) = -1\log(f(\overrightarrow{x}))$$

Simplified cost function

$$L(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}), y^{(i)}) = \frac{1}{m} \sum_{i=1}^{m} \left[L(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}), y^{(i)}) \right]$$

$$= \frac{1}{m} \sum_{i=1}^{m} \left[L(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}), y^{(i)}) \right]$$

$$= \frac{1}{m} \sum_{i=1}^{m} \left[y^{(i)} \log \left(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}) \right) + (1 - y^{(i)}) \log \left(1 - f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}) \right) \right]$$

$$= \frac{1}{m} \sum_{i=1}^{m} \left[y^{(i)} \log \left(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}) \right) + (1 - y^{(i)}) \log \left(1 - f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}) \right) \right]$$

$$= \frac{1}{m} \sum_{i=1}^{m} \left[y^{(i)} \log \left(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}) \right) + (1 - y^{(i)}) \log \left(1 - f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}) \right) \right]$$

$$= \frac{1}{m} \sum_{i=1}^{m} \left[y^{(i)} \log \left(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}) \right) + (1 - y^{(i)}) \log \left(1 - f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}) \right) \right]$$

$$= \frac{1}{m} \sum_{i=1}^{m} \left[y^{(i)} \log \left(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}) \right) + (1 - y^{(i)}) \log \left(1 - f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}) \right) \right]$$

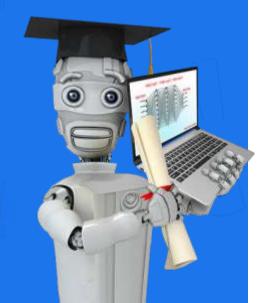
$$= \frac{1}{m} \sum_{i=1}^{m} \left[y^{(i)} \log \left(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}) \right) + (1 - y^{(i)}) \log \left(1 - f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}) \right) \right]$$

$$= \frac{1}{m} \sum_{i=1}^{m} \left[y^{(i)} \log \left(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}) \right) + (1 - y^{(i)}) \log \left(1 - f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}) \right) \right]$$

$$= \frac{1}{m} \sum_{i=1}^{m} \left[y^{(i)} \log \left(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}) \right) + (1 - y^{(i)}) \log \left(1 - f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}) \right) \right]$$

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Gradient Descent

Gradient Descent Implementation

Training logistic regression

Find $\vec{\mathbf{w}}$, b

Given new
$$\vec{x}$$
, output $f_{\vec{w},b}(\vec{x}) = \frac{1}{1+e^{-(\vec{w}\cdot\vec{x}+b)}}$
$$P(y=1|\vec{x};\vec{w},b)$$

Gradient descent

$$J(\overrightarrow{w},b) = -\frac{1}{m} \sum_{i=1}^{m} \left[y^{(i)} \log \left(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}) \right) + \left(1 - y^{(i)} \right) \log \left(1 - f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}) \right) \right]$$
repeat {
$$\frac{\partial}{\partial w_j} (\overrightarrow{w},b) = \frac{1}{m} \underbrace{ \begin{bmatrix} w \\ \overrightarrow{w},b(\overrightarrow{x}^{(i)}) - y^{(i)} \end{bmatrix} x_j^{(i)}}_{\overrightarrow{w},b}$$

$$b = b - \alpha \frac{\partial}{\partial b} J(\overrightarrow{w},b)$$

$$\frac{\partial}{\partial b} J(\overrightarrow{w},b) = \frac{1}{m} \underbrace{ \begin{bmatrix} w \\ \overrightarrow{w},b(\overrightarrow{x}^{(i)}) - y^{(i)} \end{bmatrix} x_j^{(i)}}_{(f_{w,bi=1})}$$
} simultaneous updates

Gradient descent for logistic regression

} simultaneous updates

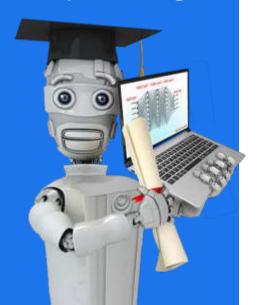
Linear regression
$$f_{\overrightarrow{w},b}(\overrightarrow{x}) = \overrightarrow{w} \cdot \overrightarrow{x} + b$$

Logistic regression
$$f_{\vec{w},b}(\vec{x}) = \frac{1}{1 + e^{(-\vec{w} \cdot \vec{x} + b)}}$$

- (learning curve)
- Vectorized implementation
- Feature scaling

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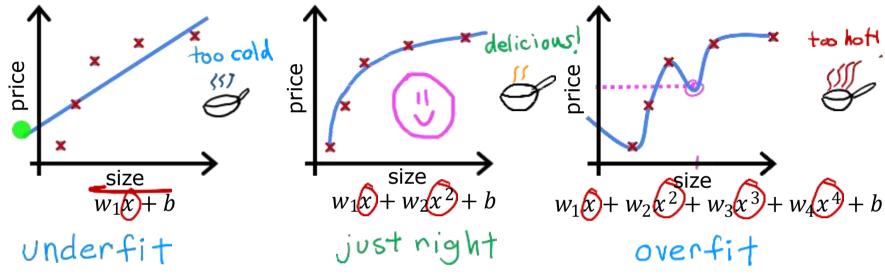
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Regularization to Reduce Overfitting

The Problem of Overfitting

Regression example



 Does not fit the training set well

high bias

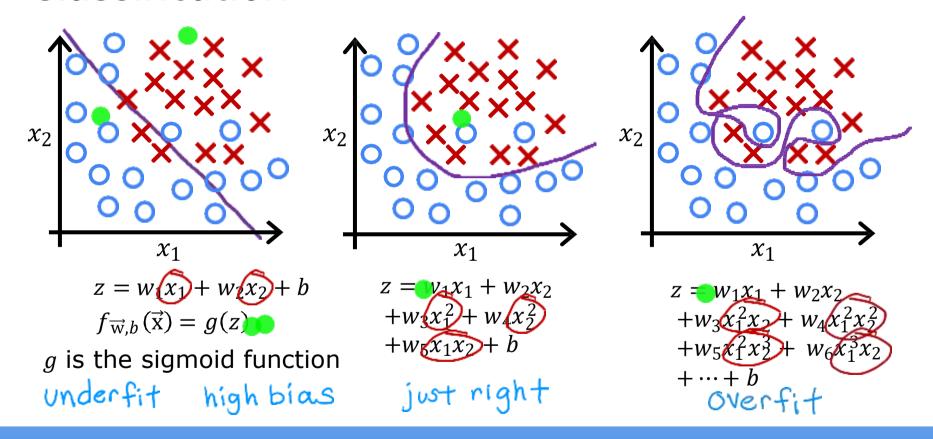
 Fits training set pretty well

generalization

 Fits the training set extremely well

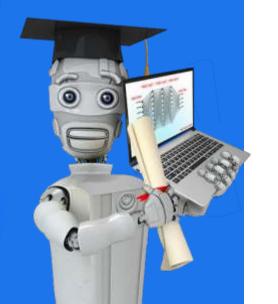
high variance

Classification





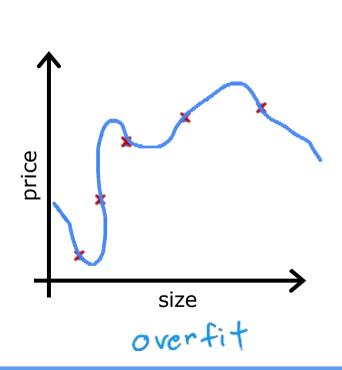
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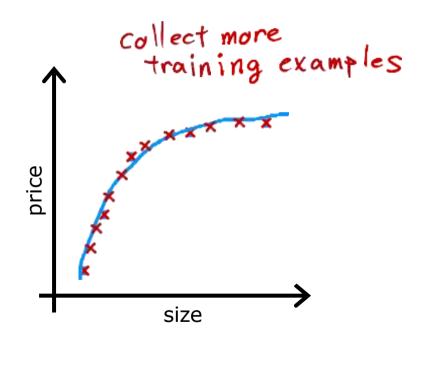


Regularization to Reduce Overfitting

Addressing Overfitting

Collect more training examples



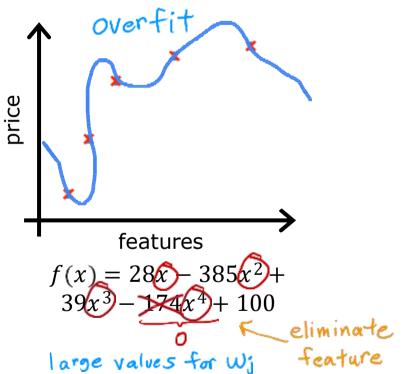


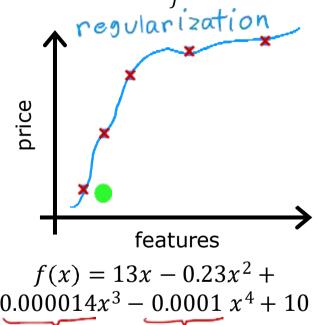
Select features to include/exclude

| size | bedrooms X2 | floors X ₃ | age | avg income | | distance to coffee shop | price Y | _ |
|------|-------------------------------------|--------------------------|-----|---------------|---|-------------------------|--------------|---------------------------------------|
| | all feature insufficient over fit | | | | size edroum age ust ri featur | | uset coul | dvantage ful features d be lost |

Regularization

Reduce the size of parameters w_j





$$f(x) = 13x - 0.23x^{2} + 0.000014x^{3} - 0.00011x^{4} + 10$$
Small values for Wij

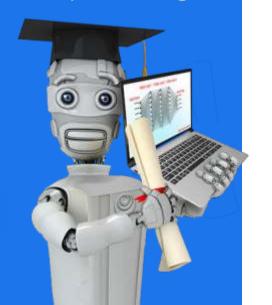
Addressing overfitting

Options

- 1. Collect more data
- 2. Select features
 - Feature selection in course 2
- 3. Reduce size of parameters
 - "Regularization" next videos!

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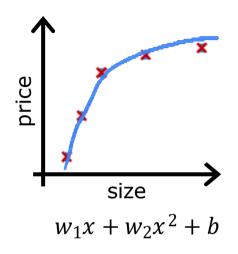
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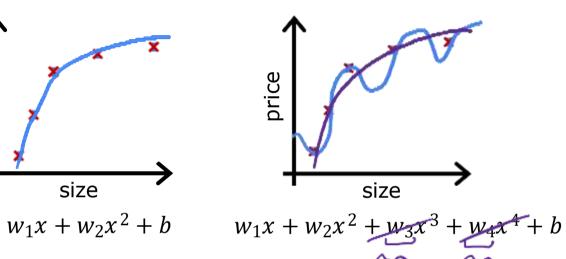


Regularization to Reduce Overfitting

Cost Function with Regularization

Intuition





make w_3 , w_4 really small (≈ 0)

$$\min_{\overrightarrow{w},b} \frac{1}{2n_{t}} \stackrel{m}{\text{?}} \left(\overrightarrow{w}_{,b} (\overrightarrow{x}^{(i)}) - y^{(i)} \right)^{2} + 1000 \stackrel{3}{\text{0.002}} + 1000 \stackrel{3}{\text{0.002}}$$

Regularization

small values w_1, w_2, \dots, w_n, b

simpler model $W_3 \stackrel{>}{\sim} O$ less likely to overfit $W_4 \stackrel{>}{\sim} O$

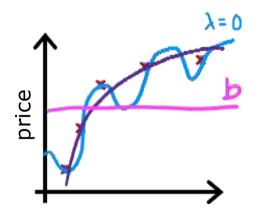
| size X ₁ | bedrooms X ₂ | floors X ₃ | age ४ _५ | avg income ^X 5 | | distance to coffee shop | price Y |
|------------------------|----------------------------|--------------------------|-----------------------|---------------------------------|---------|-------------------------|------------|
| | W1.W1.W | o <i>W</i> 10 | n featur | es | v = 100 | | |

Regularization

regularization mean squarederror

$$\min_{\vec{w},b} J(\vec{w},b) = \min_{\vec{w},b} \left[\frac{1}{2m} \sum_{i=1}^{m} (f_{\vec{w},b}(\vec{x}^{(i)}) - y^{(i)})^2 + \frac{\lambda}{2m} \sum_{i=1}^{n} w_i^2 \right]$$
fit data

**Keep w; small*



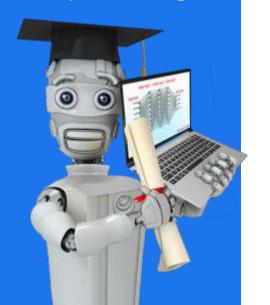
halances both goals

choose
$$\lambda = 10^{10}$$
 $f_{\overrightarrow{w},b}(\overrightarrow{x}) = \underbrace{w_1x + w_2x^2 + w_3x^3 + w_4x^4 + b}_{\approx 0}$
 $f(x) = b$

term

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Regularization to Reduce Overfitting

Regularized Linear Regression

Regularized linear regression

$$\min_{\vec{w},b} J(\vec{w},b) = \min_{\vec{w},b} \left[\frac{1}{2m} \sum_{i=1}^{m} (f_{\vec{w},b}(\vec{x}^{(i)}) - y^{(i)})^2 + \frac{\lambda}{2m} \sum_{j=1}^{n} w_j^2 \right]$$

Gradient descent

repeat {
$$w_{j} = w_{j} - \alpha \frac{\partial}{\partial w_{j}} J(\overrightarrow{w}, b)$$

$$= \frac{1}{m} \sum_{i=1}^{m} (f_{\overrightarrow{w}, b}(\overrightarrow{x}^{(i)}) - y^{(i)}) x_{j}^{(i)} + \frac{\lambda}{m} w_{j}^{(i)}$$

$$b = b - \alpha \frac{\partial}{\partial b} J(\overrightarrow{w}, b)$$

$$= \frac{1}{m} \sum_{i=1}^{m} (f_{\overrightarrow{w}, b}(\overrightarrow{x}^{(i)}) - y^{(i)})$$
don't have to regularize b

Implementing gradient descent

repeat {
$$w_{j} = w_{j} - \alpha \left[\frac{1}{m} \sum_{i=1}^{m} \left[\left(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}) - y^{(i)} \right) x_{j}^{(i)} \right] + \frac{\lambda}{m} w_{j} \right]$$

$$b = b - \alpha \frac{1}{m} \sum_{i=1}^{m} \left(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}) - y^{(i)} \right)$$
} simultaneous update $j = land$

Implementing gradient descent

repeat {
$$w_{j} = w_{j} - \alpha \left[\frac{1}{m} \sum_{i=1}^{m} \left[\left(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}) - y^{(i)} \right) x_{j}^{(i)} \right] + \frac{\lambda}{m} w_{j} \right]$$

$$b = b - \alpha \frac{1}{m} \sum_{i=1}^{m} \left(f_{\overrightarrow{w},b}(\overrightarrow{x}^{(i)}) - y^{(i)} \right)$$
} simultaneous update $j = loon$

$$w_{j} = 1 w_{j} - \alpha \frac{\lambda}{m} w_{j} - \alpha \frac{1}{m} \sum_{i=1}^{m} \left(f_{w,b}(\overrightarrow{X}^{(i)}) - y^{(i)} \right) \chi_{j}^{(i)}$$

$$w_{j} \left(1 - \alpha \frac{\lambda}{m} \right) \quad \text{usual update}$$

$$w_{j} \left(1 - \alpha \frac{\lambda}{m} \right) \quad \text{usual update}$$

$$w_{j} \left(1 - \alpha \frac{\lambda}{m} \right) \quad \text{usual update}$$

How we get the derivative term (optional)

$$\frac{\partial}{\partial w_{j}}J(\vec{w},b) = \frac{\partial}{\partial w_{j}} \left(\frac{1}{2m} \sum_{i=1}^{m} \left(f(\vec{x}^{(i)}) - y^{(i)}\right)^{2} + \frac{\lambda}{2m} \sum_{j=1}^{n} w_{j}^{2}\right)$$

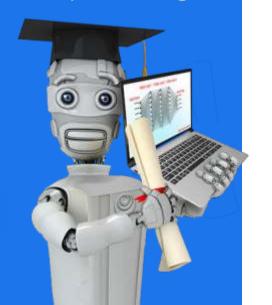
$$= \frac{1}{2m} \sum_{i=1}^{m} \left(\vec{w} \cdot \vec{x}^{(i)} + b - y^{(i)}\right) \chi_{j}^{(i)} + \frac{\lambda}{2m} \chi_{j}^{2}$$

$$= \frac{1}{m} \sum_{i=1}^{m} \left(\vec{w} \cdot \vec{x}^{(i)} + b - y^{(i)}\right) \chi_{j}^{(i)} + \frac{\lambda}{m} w_{j}$$

$$= \frac{1}{m} \sum_{i=1}^{m} \left[\left(f_{\vec{w},b}(\vec{x}^{(i)}) - y^{(i)}\right) \chi_{j}^{(i)}\right] + \frac{\lambda}{m} w_{j}$$

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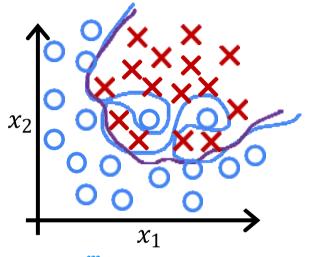
DeepLearning.AI



Regularization to Reduce Overfitting

Regularized Logistic Regression

Regularized logistic regression



$$z = w_1 x_1 + w_2 x_2
+ w_3 x_1^2 x_2 + w_4 x_1^2 x_2^2
+ w_5 x_1^2 x_2^3 + \dots + b$$

$$f_{\vec{w},b}(\vec{x}) = \frac{1}{1 + e^{-z}}$$

Cost function

$$J(\overrightarrow{\mathbf{w}},b) = -\frac{1}{m} \left[\sum_{i=1}^{m} \left[y^{(i)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) + (1 - y^{(i)}) \log \left(1 - f_{\overrightarrow{\mathbf{w}},b} \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=1}^{m} \left[y^{(j)} \log \left(\overrightarrow{\mathbf{x}}^{(i)} \right) \right] + \sum_{j=$$

Regularized logistic regression

$$J(\overrightarrow{\mathbf{w}},b) = -\frac{1}{m} \left[y \log \left(f_{\overrightarrow{\mathbf{w}},b}(\overrightarrow{\mathbf{x}}^{(i)}) \right) + \left(1 - y^{(i)} \right) \log \left(1 - f_{\overrightarrow{\mathbf{w}},b}(\overrightarrow{\mathbf{x}}^{(i)}) \right) \right] + \frac{\lambda}{2m} \left[y^2 \log \left(f_{\overrightarrow{\mathbf{w}},b}(\overrightarrow{\mathbf{x}}^{(i)}) \right) \right] + \frac{\lambda}{2m} \left[y^2 \log \left(f_{\overrightarrow{\mathbf{w}},b}(\overrightarrow{\mathbf{x}}^{(i)}) \right) \right] + \frac{\lambda}{2m} \left[y^2 \log \left(f_{\overrightarrow{\mathbf{w}},b}(\overrightarrow{\mathbf{x}}^{(i)}) \right) \right] + \frac{\lambda}{2m} \left[y^2 \log \left(f_{\overrightarrow{\mathbf{w}},b}(\overrightarrow{\mathbf{x}}^{(i)}) \right) \right] + \frac{\lambda}{2m} \left[y^2 \log \left(f_{\overrightarrow{\mathbf{w}},b}(\overrightarrow{\mathbf{x}}^{(i)}) \right) \right] + \frac{\lambda}{2m} \left[g_{\overrightarrow{\mathbf{w}},b}(\overrightarrow{\mathbf{x}}^{(i)}) \right] + \frac{\lambda}{2m} \left[g_{\overrightarrow{\mathbf{w},b}}(\overrightarrow{\mathbf{x}}^{(i)}) \right] + \frac{\lambda}{2m} \left[g_{\overrightarrow{\mathbf{w},b}}(\overrightarrow{\mathbf{x}}^{(i)}) \right] + \frac{\lambda}{2m} \left[g_{\overrightarrow{\mathbf{w},b}}(\overrightarrow{\mathbf{x}}^{(i)}) \right] + \frac{\lambda}{2m} \left[$$

