

Tutorial 6

Example 1

It is NOT possible to prove

Pre: $l = \langle a_1, a_2, \dots, a_n \rangle$ s.t. $\text{VALUE_TYPE} = \text{int}$

$x := \text{sum}(l)$

$y := \text{sum}(l)$

Post: $x + y = 2 \cdot \sum_{i=1..n} a_i.\text{value}$

because it is not in general guaranteed that the list l is not modified after the execution of $x := \text{sum}(l)$. However, by changing the specification for the `sum` function as follows

Pre: $l = \langle a_1, a_2, \dots, a_n \rangle$ s.t. $\text{VALUE_TYPE} = \text{int}$

$x := \text{sum}(l)$

Post: $x = \sum_{i=1..n} a_i.\text{value}$ and $\underline{l'} = \underline{l}$

we can now prove the original claim:

Pre: $l = \langle a_1, a_2, \dots, a_n \rangle$ s.t. $\text{VALUE_TYPE} = \text{int}$

$\{l = \langle a_1, a_2, \dots, a_n \rangle \text{ and } \text{VALUE_TYPE} = \text{int} \}$

$x := \text{sum}(l)$

$\{x = \sum_{i=1..n} a_i.\text{value} \text{ and } l = \langle a_1, a_2, \dots, a_n \rangle \text{ and } \text{VALUE_TYPE} = \text{int} \}$

$y := \text{sum}(l)$

$\{y = x = \sum_{i=1..n} a_i.\text{value} \}$

Post: $x + y = 2 \cdot \sum_{i=1..n} a_i.\text{value}$

Example 2

- **find**(i, l) =
 $j := 1$
 $x := l.\text{first}$
while (NOT $l.\text{nil_entry}(x)$) and $j < i$ **do**
 $x := l.\text{next}(x)$
 $j := j + 1$
end while
return x
- $O(|l|)$

Example 3**Pre:** $l = \langle a_1, a_2, \dots, a_n \rangle$ $res := l.first$ **Post:** $res = a_1$ if $l \neq \langle \rangle$ and $res = \text{NIL}$ otherwise ($l = \langle \rangle$), and $l' = l$ **Pre:** $l = \langle a_1, a_2, \dots, x, \dots, a_n \rangle$ $res := l.next(x)$ **Post:** $res = a_i$ if $l = \langle a_1, a_2, \dots, x, a_i, \dots, a_n \rangle$ (i.e. x is not the last entry) and $res = \text{NIL}$ if $x = a_n$ (i.e. x is the last entry), and $l' = l$