System.Numerics.Multiprecision Library Reference

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Description

Multiprecision is a multiple precision arithmetic library. The library is implemented using GNU Multiple Precision Arithmetic Library (http://gmplib.org/).

Namespaces

Namespace	Description
System.Numerics.Multiprecision	Contains arbitrary precision integer type BigInt,
	arbitrary precision rational type BigRational and
	arbitrary precision floating point type BigFloat.

1 Usage

1.0.1 Referencing the System.Numerics.Multiprecision library

Right-click a project node in IDE | Project References... | Add System Extension Library Reference... | enable System.Numerics.Multiprecision check box

or add following line to your project's .cmp file:

reference <ext/System.Numerics.Multiprecision.cml>;

2 Installation

The System. Numerics.Multiprecision library uses the GNU MP library that is precompiled for the following platforms:

- 32-bit Windows (x86)
- 64-bit Windows (x64)
- 32-bit PC Linux (i686)
- 64-bit PC Linux (x86 64)

Current version of GNU MP library at the time of writing is 6.1.0.

If you want to install newer version of the GNU MP library or if you have different platform, you can compile the GNU MP library from sources by using the following instructions.

2.0.1 Compiling the GNU MP library from sources in Windows

• Install MinGW-w64 GCC to a path that does not contain spaces. I have mine installed in C:\mingw-w64.

Installer can be obtained from

 $\label{lem:mingwww64/files/Toolchains\%20targetting\%20Win32/Personal\%20Builds/mingw-builds/installer/mingw-w64-install.exe/download$

• Install MSYS2. Installation instructions can be found in http://sourceforge.net/p/msys2/wiki/MSYS2%20installation/

I have mine installed in C:\msys64.

- Start MSYS2 shell.
- In the MSYS2 shell obtain tar by executing

```
pacman -S tar
```

• Obtain make by executing

```
pacman -S make
```

• Mount your MinGW-directory (mine is in C:/mingw-w64) by executing

```
mkdir /mingw
mount C:/mingw-w64 /mingw
```

• Insert your MinGW bin-directory in front of the PATH by executing

export PATH=/mingw/mingw64/bin:\$PATH

• Now if you ask which GCC is used by executing

which gcc

you should get /mingw/mingw64/bin/gcc.

- Download the GNU MP library from http://gmplib.org/#DOWNLOAD in bz2 format and place it to your MSYS2 home directory (mine is in C:\msys64\home\Seppo).
- Extract the GNU MP library by executing

```
tar xjf gmp-6.1.0.tar.bz2
```

• Change to gmp-directory by executing

```
cd gmp-6.1.0
```

• Configure the library for 64-bit Windows by executing

```
./configure --enable-static --disable-shared --host=x86_64-w64-mingw32
```

For 32-bit Windows the command is

```
./configure --enable-static --disable-shared --host=i686-w64-mingw32
```

Shared libraries are not used in Cmajor so we are disabling them.

• Make the library by executing

make

• Install the library by executing

make install

• Optionally test the library by executing

make check

• Now the header file **gmp.h** should be in C:\msys64\usr\local\include directory and the library file **libgmp.a** should be in C:\msys64\usr\local\lib directory. Copy gmp.h and libgmp.a under the Cmajor System.Numerics.GmpIntf extension library to directory

for 64-bit Windows, or to

for 32-bit Windows.

• That's all.

2.0.2 Compiling the GNU MP library from sources in Linux

- Download the GNU MP library from http://gmplib.org/#DOWNLOAD in bz2 format and place it to your home directory.
- Extract the GNU MP library by executing

```
tar xjf gmp-6.1.0.tar.bz2
```

• Change to gmp-directory by executing

```
cd gmp-6.1.0
```

• Configure the library by executing

```
./configure --enable-static --disable-shared
```

Shared libraries are not used in Cmajor so we are disabling them.

• Make the library by executing

make

• Install the library by executing

```
make install
```

• Optionally test the library by executing

make check

• Now the header file **gmp.h** should be in /usr/local/include directory and the library file **libgmp.a** should be in /usr/local/lib directory. Copy gmp.h and libgmp.a under the Cmajor System.Numerics.GmpIntf extension library to

```
<your cmajor directory>/system/ext/System.Numerics.GmpIntf/gmp/linux/x86_64
directory for 64-bit Linux or to
```

<your cmajor directory>/system/ext/System.Numerics.GmpIntf/gmp/linux/i686
directory for 32-bit Linux.

• That's all.

3 System.Numerics.Multiprecision Namespace

Contains arbitrary precision integer type BigInt, arbitrary precision rational type BigRational and arbitrary precision floating point type BigFloat.

3.1 Classes

Class	Description
BigFloat	An arbitrary precision floating point type.
BigInt	An arbitrary precision signed integer type.
BigRational	An arbitrary precision rational number type.
Precision	Represents a precision of given number of digits.

3.1.1 BigFloat Class

An arbitrary precision floating point type.

Syntax

public class BigFloat;

3.1.1.1 Member Functions

Member Function	Description
BigFloat()	Default constructor. Creates an instance of arbitrary precision floating point type and initializes it to zero.
BigFloat(const System.Numerics.MultiprecisionBigFloat&)	Copy constructor.
operator=(const System.Numerics Multiprecision.BigFloat&)	Copy assignment.
BigFloat(System.Numerics.Multiprecision BigFloat&&)	Move constructor.
operator=(System.Numerics.Multiprecision BigFloat&&)	Move assignment.
$\begin{array}{c} \operatorname{BigFloat}(\operatorname{const}\ \operatorname{System.Numerics.Multiprecision.} \\ \operatorname{BigInt}\&) \end{array}$	Constructor. Creates an instance of arbitrary precision floating point type and initializes it from the given arbitrary precision integer type.
${\bf BigFloat(const~System.Numerics.MultiprecisionBigRational\&)}$	Constructor. Creates an instance of arbitrary precision floating point type and initializes it from the given arbitrary precision rational type.
${\bf BigFloat(const~System.Numerics.MultiprecisionPrecision\&)}$	Constructor. Constructs an arbitrary precision floating point value with given precision.
${\bf BigFloat(const~System.String < char} {\bf >} \&)$	Constructor. Constructs an arbitrary precision floating point value from given decimal digits.
BigFloat(const System.String <char>&, int)</char>	Constructor. Constructs an arbitrary precision floating point value from given digits that are in given base.
$\operatorname{BigFloat}(\operatorname{double})$	Constructor. Constructs an arbitrary precision floating point value from given double precision value.
$\operatorname{BigFloat}(\operatorname{int})$	Constructor. Constructs an arbitrary precision floating point value from given integer value.

 \sim BigFloat()

BigFloat(uint) Constructor. Constructs an arbitrary precision floating point value from given unsigned integer value. Handle() const Returns a handle to the GNU MP library arbitrary precision floating point number representation. ToDouble() const Converts the arbitrary precision floating point number to a double precision value by truncating it. ToString() const Returns the value of the **BigFloat** as a string. ToString(int) const Returns the value of the **BigFloat** as a string using given base. ToString(int, uint) const Returns the value of the **BigFloat** as a string using given base and given number of digits. operator=(const System.Numerics.-Assigns the value of the **BigFloat** from the given Multiprecision.BigInt&) arbitrary precision integer. operator=(const System.Numerics.-Assigns the value of the **BigFloat** from the given Multiprecision.BigRational&) arbitrary precision rational. operator=(double) Assigns the value of the **BigFloat** from the given double precision value. operator=(int) Assigns the value of the **BigFloat** from the given integer value. Assigns the value of the **BigFloat** from the given operator=(uint) unsigned integer value.

Frees memory occupied by the **BigFloat** instance.

BigFloat() Member Function

Default constructor. Creates an instance of arbitrary precision floating point type and initializes it to zero.

Syntax

public BigFloat();

${\bf BigFloat(const~System.Numerics.Multiprecision.BigFloat\&)~Member~Function}$

Copy constructor.

Syntax

public BigFloat(const System.Numerics.Multiprecision.BigFloat& that);

Name	Type	Description
that	const System.Numerics.Multiprecision.BigFloat&	A BigFloat to copy from.

 $\label{eq:const_system} \mbox{operator=(const\ System.Numerics.Multiprecision.BigFloat\&)\ Member\ Function}$ Copy assignment.

Syntax

public void operator=(const System.Numerics.Multiprecision.BigFloat& that);

Name	Type	Description
that	$const\ System. Numerics. Multiprecision. BigFloat\&$	A BigFloat to assign from.

${\bf BigFloat(System.Numerics.Multiprecision.BigFloat\&\&)\ Member\ Function}$

Move constructor.

Syntax

public BigFloat(System.Numerics.Multiprecision.BigFloat&& that);

Name	Type	Description
that	System. Numerics. Multiprecision. BigFloat&&	A BigFloat to move from.

$\label{eq:operator} \mbox{operator=(System.Numerics.Multiprecision.BigFloat\&\&)\ Member\ Function}$ Move assignment.

Syntax

public void operator=(System.Numerics.Multiprecision.BigFloat&& __parameter0);

\mathbf{Name}	\mathbf{Type}	Description
parameter0	System. Numerics. Multiprecision. BigFloat&&	A BigFloat to assign from.

BigFloat(const System.Numerics.Multiprecision.BigInt&) Member Function

Constructor. Creates an instance of arbitrary precision floating point type and initializes it from the given arbitrary precision integer type.

Syntax

public BigFloat(const System.Numerics.Multiprecision.BigInt& that);

Name	Type	Description
that	$const\ System. Numerics. Multiprecision. BigInt \&$	An arbitrary precision integer
		type value to construct from.

BigFloat(const System.Numerics.Multiprecision.BigRational&) Member Function

Constructor. Creates an instance of arbitrary precision floating point type and initializes it from the given arbitrary precision rational type.

Syntax

public BigFloat(const System.Numerics.Multiprecision.BigRational& that);

Name	Type	Description	
that	$const\ System. Numerics. Multiprecision. BigRational \&$	An arbitrary precision rational	
		type value to construct from.	

BigFloat(const System.Numerics.Multiprecision.Precision&) Member Function

Constructor. Constructs an arbitrary precision floating point value with given precision.

Syntax

public BigFloat(const System.Numerics.Multiprecision.Precision& prec);

Name	Type	Description
prec	const System.Numerics.Multiprecision.Precision&	Precision.

BigFloat(const System.String<char>&) Member Function

Constructor. Constructs an arbitrary precision floating point value from given decimal digits.

Syntax

public BigFloat(const System.String<char>& str);

Name	Type	Description
str	const System.String <char>&</char>	Digit string.

BigFloat(const System.String<char>&, int) Member Function

Constructor. Constructs an arbitrary precision floating point value from given digits that are in given base.

Syntax

public BigFloat(const System.String<char>& str, int base_);

\mathbf{Name}	\mathbf{Type}	Description
str	const System.String <char>&</char>	Digit string.
$base_$	int	Base of digits.

${\bf BigFloat(double)\ Member\ Function}$

Constructor. Constructs an arbitrary precision floating point value from given double precision value.

Syntax

public BigFloat(double that);

Name	\mathbf{Type}	Description		
that	double	A double precision value to initialize from.		

BigFloat(int) Member Function

Constructor. Constructs an arbitrary precision floating point value from given integer value.

Syntax

public BigFloat(int that);

Name	\mathbf{Type}	Description	
that	int	An integer value to initialize from.	

BigFloat(uint) Member Function

Constructor. Constructs an arbitrary precision floating point value from given unsigned integer value.

Syntax

public BigFloat(uint that);

Name	\mathbf{Type}	Description		
that	uint	An unsigned integer value to initialize from.		

Handle() const Member Function

Returns a handle to the GNU MP library arbitrary precision floating point number representation.

Syntax

public void* Handle() const;

Returns

void*

Returns a handle to the GNU MP library arbitrary precision floating point number representation.

ToDouble() const Member Function

Converts the arbitrary precision floating point number to a double precision value by truncating it.

Syntax

public double ToDouble() const;

Returns

double

Returns the arbitrary precision floating point number converted to a double precision value by truncating it.

ToString() const Member Function

Returns the value of the BigFloat as a string.

Syntax

public System.String<char> ToString() const;

Returns

 ${\bf System.String}{<}{\bf char}{>}$

Returns the value of the BigFloat as a string.

ToString(int) const Member Function

Returns the value of the BigFloat as a string using given base.

Syntax

public System.String<char> ToString(int base_) const;

Parameters

Returns

 ${\bf System.String}{<}{\bf char}{>}$

Returns the value of the BigFloat as a string using given base.

ToString(int, uint) const Member Function

Returns the value of the BigFloat as a string using given base and given number of digits.

Syntax

public System.String<char> ToString(int base_, uint numDigits) const;

Parameters

\mathbf{Name}	\mathbf{Type}	Description
base_	int	Base.
numDigits	uint	Number of digits.

Returns

 ${\bf System.String}{<}{\bf char}{>}$

Returns the value of the BigFloat as a string using given base and given number of digits.

operator=(const System.Numerics.Multiprecision.BigInt&) Member Function

Assigns the value of the BigFloat from the given arbitrary precision integer.

Syntax

public void operator=(const System.Numerics.Multiprecision.BigInt& that);

\mathbf{Name}	Type	Description
that	$const\ System. Numerics. Multiprecision. BigInt \&$	An arbitrary precision integer to
		assign from.

$operator = (const\ System. Numerics. Multiprecision. BigRational \&)\ Member\ Function$

Assigns the value of the BigFloat from the given arbitrary precision rational.

Syntax

public void operator=(const System.Numerics.Multiprecision.BigRational& that);

Name	Type	Description
that	$const\ System. Numerics. Multiprecision. BigRational \&$	An arbitrary precision rational
		to assign from.

operator=(double) Member Function

Assigns the value of the BigFloat from the given double precision value.

Syntax

```
public void operator=(double that);
```

Name	\mathbf{Type}	Description		
that	double	A double precision value to assign from.		

operator=(int) Member Function

Assigns the value of the BigFloat from the given integer value.

Syntax

```
public void operator=(int that);
```

Name	Type	Description	
that	int	An integer value to assign from.	

operator=(uint) Member Function

Assigns the value of the BigFloat from the given unsigned integer value.

Syntax

```
public void operator=(uint that);
```

Name	Type	Description	
that	uint	An unsigned integer value to assign from.	

\sim BigFloat() Member Function

Frees memory occupied by the BigFloat instance.

Syntax

public ~BigFloat();

3.1.1.2 Nonmember Functions

Function			Description
Abs(const BigFloat&)	System.Numerics.Multiprecision		Returns the absolute value of the given BigFloat value.
Ceil(const BigFloat&)	· · · · · · · · · · · · · · · · · · ·		Returns the BigFloat rounded up to the next arbitrary precision integer value.
Floor(const BigFloat&)	System.Num	erics.Multiprecision	Returns the BigFloat rounded down to the previous arbitrary precision integer value.
$\begin{array}{c} \operatorname{Sqrt}(\operatorname{const} \\ \operatorname{BigFloat}\&) \end{array}$			Returns the square root of the given BigFloat number.
Trunc(const BigFloat&)	System.Num	erics.Multiprecision	Returns the ${\bf BigFloat}$ truncated towards zero.
operator*(cons Multiprecision		System.Numerics const System Float&)	Returns the product of given BigFloat value multiplied by another.
operator+(con Multiprecision	nst	System.Numerics const System	Returns the sum of given BigFloat value added to another.
operator-(cons Multiprecision	st	System.Numerics	Returns the negation of ${\bf BigFloat}$.
operator-(cons Multiprecision	st	System.Numerics const System Float&)	Returns the difference of given BigFloat value subtracted from another.
operator/(cons Multiprecision	st	System.Numerics const System	Returns the quotient when given BigFloat is divided by another.
operator<(cor Multiprecision	nst	System.Numerics const System	Returns true if the first ${\bf BigFloat}$ is less than the second ${\bf BigFloat}$, false otherwise.
operator==(conditional Multiprecision	onst	System.Numerics const System	Returns true if the first ${\bf BigFloat}$ is equal to the second ${\bf BigFloat}$, false otherwise.

$Abs (const\ System. Numerics. Multiprecision. BigFloat\&)\ Function$

Returns the absolute value of the given BigFloat value.

Syntax

public System.Numerics.Multiprecision.BigFloat Abs(const System.Numerics.Multiprecision.BigFloat&x);

Parameters

\mathbf{Name}	Type	Description
X	$const\ System. Numerics. Multiprecision. BigFloat\&$	Arbitrary precision floating
		point number.

Returns

 ${\bf System. Numerics. Multiprecision. BigFloat}$

Returns the absolute value of the given BigFloat value.

$\label{lem:const_system} \textbf{Ceil} (\textbf{const System.Numerics.Multiprecision.BigFloat} \&) \ \textbf{Function}$

Returns the BigFloat rounded up to the next arbitrary precision integer value.

Syntax

public System.Numerics.Multiprecision.BigFloat Ceil(const System.Numerics.Multiprecision.BigFloat
x);

Parameters

Name	Type	Description
X	const System.Numerics.Multiprecision.BigFloat&	BigFloat.

Returns

 ${\bf System. Numerics. Multiprecision. BigFloat}$

BigFloat

$Floor(const\ System. Numerics. Multiprecision. BigFloat\&)\ Function$

Returns the BigFloat rounded down to the previous arbitrary precision integer value.

Syntax

public System.Numerics.Multiprecision.BigFloat Floor(const System.Numerics.Multiprecision.BigFloat x);

Parameters

Name	Type	Description
X	const System.Numerics.Multiprecision.BigFloat&	BigFloat.

Returns

 ${\bf System. Numerics. Multiprecision. BigFloat}$

Returns the BigFloat rounded down to the previous arbitrary precision integer value.

$Sqrt(const\ System. Numerics. Multiprecision. BigFloat\&)\ Function$

Returns the square root of the given BigFloat number.

Syntax

public System.Numerics.Multiprecision.BigFloat Sqrt(const System.Numerics.Multiprecision.BigFloat
x);

Parameters

\mathbf{Name}	Type	Description
X	$const\ System. Numerics. Multiprecision. BigFloat \&$	BigFloat.

Returns

 ${\bf System. Numerics. Multiprecision. BigFloat}$

Returns the square root of the given BigFloat number.

Trunc (const~System. Numerics. Multiprecision. BigFloat &)~Function

Returns the BigFloat truncated towards zero.

Syntax

public System.Numerics.Multiprecision.BigFloat Trunc(const System.Numerics.Multiprecision.BigFloat x);

Parameters

Name	Type	Description
X	const System.Numerics.Multiprecision.BigFloat&	BigFloat.

Returns

 ${\bf System. Numerics. Multiprecision. BigFloat}$

Returns the BigFloat truncated towards zero.

$operator*(const\ System. Numerics. Multiprecision. BigFloat\&,\ const\ System. BigFloat\&,\ const\ System$

Returns the product of given BigFloat value multiplied by another.

Syntax

public System.Numerics.Multiprecision.BigFloat operator*(const System.Numerics.Multiprecision.BigFloat& right);

Parameters

Name	Type	Description
left	const~System. Numerics. Multiprecision. BigFloat &	Left operand.
right	const System.Numerics.Multiprecision.BigFloat&	Right operand.

Returns

System. Numerics. Multiprecision. BigFloat

Returns the product of given BigFloat value multiplied by another.

$operator + (const\ System. Numerics. Multiprecision. BigFloat\&,\ const\ System. System. BigFloat\&,\ const\ System. BigF$

Returns the sum of given BigFloat value added to another.

Syntax

public System.Numerics.Multiprecision.BigFloat operator+(const System.Numerics.Multiprecision.BigFloat& right);

Parameters

Name	Type	Description
left	$const\ System. Numerics. Multiprecision. BigFloat \&$	Left operand.
right	const System.Numerics.Multiprecision.BigFloat&	Right operand.

Returns

 ${\bf System. Numerics. Multiprecision. BigFloat}$

Returns the sum of given BigFloat value added to another.

operator-(const System. Numerics.
Multiprecision. BigFloat&)
 Function

Returns the negation of BigFloat.

Syntax

public System.Numerics.Multiprecision.BigFloat operator-(const System.Numerics.Multiprecision.Big
x);

Parameters

Name	Type	Description
X	const System.Numerics.Multiprecision.BigFloat&	A value.

Returns

 ${\bf System. Numerics. Multiprecision. BigFloat}$

Returns the negation of BigFloat.

$operator-(const\ System. Numerics. Multiprecision. BigFloat\&,\ const\ System. BigFloat\&,\ const\ System.$

Returns the difference of given BigFloat value subtracted from another.

Syntax

public System.Numerics.Multiprecision.BigFloat operator-(const System.Numerics.Multiprecision.BigFloat& right);

Parameters

Name	Type	Description
left	const~System. Numerics. Multiprecision. BigFloat &	Left operand.
right	const System.Numerics.Multiprecision.BigFloat&	Right operand.

Returns

System. Numerics. Multiprecision. BigFloat

Returns the difference of given ${\bf BigFloat}$ value subtracted from another.

$operator/(const\ System. Numerics. Multiprecision. BigFloat\&,\ const\ System. BigFloat\&,\ const\ Syst$

Returns the quotient when given BigFloat is divided by another.

Syntax

public System.Numerics.Multiprecision.BigFloat operator/(const System.Numerics.Multiprecision.BigFloat& right);

Parameters

Name	Type	Description
left	$const\ System. Numerics. Multiprecision. BigFloat \&$	Left operand.
right	const System.Numerics.Multiprecision.BigFloat&	Right operand.

Returns

System. Numerics. Multiprecision. BigFloat

Returns the quotient when given BigFloat is divided by another.

$operator < (const\ System. Numerics. Multiprecision. BigFloat\&,\ const\ System. System. BigFloat\&,\ const\ System. System. BigFloat\&,\ const\ Syst$

Returns true if the first BigFloat is less than the second BigFloat, false otherwise.

Syntax

public bool operator<(const System.Numerics.Multiprecision.BigFloat& left, const System.Numerics right);

Parameters

\mathbf{Name}	\mathbf{Type}	Description
left	$const\ System. Numerics. Multiprecision. BigFloat\&$	Left operand.
right	const~System. Numerics. Multiprecision. BigFloat&	Right operand.

Returns

bool

Returns true if the first BigFloat is less than the second BigFloat, false otherwise.

$operator == (const\ System. Numerics. Multiprecision. BigFloat\&, const\ System. BigFloat\&, const\ System. BigFloat\&, const\ System. BigFloat\&, const \ System. BigFloat\&, const\ System. BigFloat\&, co$

Returns true if the first BigFloat is equal to the second BigFloat, false otherwise.

Syntax

public bool operator==(const System.Numerics.Multiprecision.BigFloat& left, const System.Numerics.Multiprecision.BigFloat& right);

Parameters

\mathbf{Name}	\mathbf{Type}	Description
left	$const\ System. Numerics. Multiprecision. BigFloat\&$	Left operand.
right	const~System. Numerics. Multiprecision. BigFloat &	Right operand.

Returns

bool

Returns true if the first BigFloat is equal to the second BigFloat, false otherwise.

3.1.2 BigInt Class

An arbitrary precision signed integer type.

Syntax

public class BigInt;

3.1.2.1 Member Functions

Member Function	Description
BigInt()	Default constructor. Creates an instance of arbitrary precision signed integer and initializes it to zero.
BigInt(const System.Numerics.MultiprecisionBigInt&)	Copy constructor.
operator=(const System.Numerics Multiprecision.BigInt&)	Copy assignment.
BigInt(System.Numerics.Multiprecision.BigInt&-&)	Move constructor.
operator=(System.Numerics.Multiprecision BigInt&&)	Move assignment.
BigInt(const System.String <char>&)</char>	Constructor. Constructs an arbitrary precision floating point value from given decimal digits.
BigInt(const System.String <char>&, int)</char>	Constructor. Constructs an arbitrary precision floating point value from given digits of given base.
$\operatorname{BigInt}(\operatorname{int})$	Creates an instance of arbitrary precision signed integer and initializes it to given signed integer value.
$\operatorname{BigInt}(\operatorname{uint})$	Creates an instance of arbitrary precision signed integer and initializes it to given unsigned integer value.
Handle() const	Returns a handle to the GNU MP library arbitrary precision integer representation.
ToString() const	Returns the value of the BigInt as a string of decimal digits prefixed by minus sign if the value is negative.
ToString(int) const	Returns the value of the BigInt as a string of digits in given base prefixed by minus sign if the value is negative.

Frees memory occupied by the ${\bf BigInt}$ instance.

operator=(int) Assigns the value of the ${\bf BigInt}$ to given signed integer value. operator=(uint) Assigns the value of the ${\bf BigInt}$ to given unsigned integer value. \sim BigInt()

BigInt() Member Function

Default constructor. Creates an instance of arbitrary precision signed integer and initializes it to zero.

Syntax

public BigInt();

${\bf BigInt (const~System. Numerics. Multiprecision. BigInt \&)~Member~Function}$

Copy constructor.

Syntax

public BigInt(const System.Numerics.Multiprecision.BigInt& that);

Name	Type	Description
that	$const\ System. Numerics. Multiprecision. BigInt \&$	A BigInt to copy from.

 $\label{eq:const_system} \begin{tabular}{ll} \textbf{operator=} (\textbf{const System.Numerics.Multiprecision.BigInt\&) Member Function} \\ \textbf{Copy assignment.} \end{tabular}$

Syntax

public void operator=(const System.Numerics.Multiprecision.BigInt& that);

Name	Type	Description
that	$const\ System. Numerics. Multiprecision. BigInt \&$	A BigInt to assign.

${\bf BigInt(System.Numerics.Multiprecision.BigInt\&\&)\ Member\ Function}$

Move constructor.

Syntax

public BigInt(System.Numerics.Multiprecision.BigInt&& that);

Name	Type	Description
that	System. Numerics. Multiprecision. BigInt&&	A BigInt to move from.

$operator = (System. Numerics. Multiprecision. BigInt\&\&) \ Member \ Function$

Move assignment.

Syntax

public void operator=(System.Numerics.Multiprecision.BigInt&& that);

Name	Type	Description
that	System. Numerics. Multiprecision. BigInt&&	A BigInt to assign.

$BigInt(const\ System.String{<}char{>}\&)\ Member\ Function$

Constructor. Constructs an arbitrary precision floating point value from given decimal digits.

Syntax

public BigInt(const System.String<char>& str);

Name	Type	Description
str	const System.String <char>&</char>	Decimal digit string.

$BigInt(const\ System.String{<}char{>}\&,\ int)\ Member\ Function$

Constructor. Constructs an arbitrary precision floating point value from given digits of given base.

Syntax

public BigInt(const System.String<char>& str, int base_);

Name	\mathbf{Type}	Description
str	const System.String <char>&</char>	Digit string.
$base_$	int	Base of digits.

BigInt(int) Member Function

Creates an instance of arbitrary precision signed integer and initializes it to given signed integer value.

Syntax

public BigInt(int that);

Name	\mathbf{Type}	Description
that	$_{ m int}$	A signed integer value.

BigInt(uint) Member Function

Creates an instance of arbitrary precision signed integer and initializes it to given unsigned integer value.

Syntax

public BigInt(uint that);

Name	\mathbf{Type}	Description
that	uint	An unsigned integer value.

Handle() const Member Function

Returns a handle to the GNU MP library arbitrary precision integer representation.

Syntax

public void* Handle() const;

Returns

void*

Returns a handle to the GNU MP library arbitrary precision integer representation.

ToString() const Member Function

Returns the value of the $\frac{\text{BigInt}}{\text{BigInt}}$ as a string of decimal digits prefixed by minus sign if the value is negative.

Syntax

public System.String<char> ToString() const;

Returns

 ${\bf System.String}{<}{\bf char}{>}$

Returns the value of the $\frac{\text{BigInt}}{\text{BigInt}}$ as a string of decimal digits prefixed by minus sign if the value is negative.

ToString(int) const Member Function

Returns the value of the BigInt as a string of digits in given base prefixed by minus sign if the value is negative.

Syntax

public System.String<char> ToString(int base_) const;

Parameters

Name	\mathbf{Type}	Description
base_	int	Base of digits. Base may vary from 2 to 62.

Returns

System. String < char >

Returns the value of the BigInt as a string of digits in given base prefixed by minus sign if the value is negative.

operator=(int) Member Function

Assigns the value of the BigInt to given signed integer value.

Syntax

public void operator=(int that);

\mathbf{Name}	\mathbf{Type}	Description
that	int	A signed integer value.

operator=(uint) Member Function

Assigns the value of the BigInt to given unsigned integer value.

Syntax

```
public void operator=(uint that);
```

Name	Type	Description
that	uint	An unsigned integer value.

\sim BigInt() Member Function

Frees memory occupied by the BigInt instance.

Syntax

public ~BigInt();

3.1.2.2 Nonmember Functions

Function	Description
Abs(const System.Numerics.Multiprecision	Returns absolute value of given BigInt .
$\operatorname{BigInt} \&)$	
ClearBit(System.Numerics.Multiprecision	Clear given bit of given \mathbf{BigInt} .
BigInt&, uint)	
SetBit(System.Numerics.Multiprecision.BigInt&	s, Set given bit of given BigInt .
uint)	
TestBit(System.Numerics.Multiprecision	Returns true if given bit of given BigInt is set,
BigInt&, uint)	false otherwise.
ToggleBit(System.Numerics.Multiprecision	Toggle given bit of given \mathbf{BigInt} .
BigInt&, uint)	GC 0 0 0
operator%(const System.Numerics	8 Returns the remainder when given BigInt is di-
Multiprecision.BigInt&, const System.Numerics	
Multiprecision.BigInt&)	·
operator&(const System.Numerics	8 Returns bitwise AND of two BigInt values.
Multiprecision.BigInt&, const System.Numerics	5. -
Multiprecision.BigInt&)	
operator*(const System.Numerics	Returns the product of given BigInt value multi-
Multiprecision.BigInt&, const System.Numerics	s plied by another.
Multiprecision.BigInt&)	
operator+(const System.Numerics	Returns the sum of given BigInt value added to
Multiprecision.BigInt&, const System.Numerics	s another.
Multiprecision.BigInt&)	
operator-(const System.Numerics	Returns the negation of BigInt .
Multiprecision.BigInt&)	
operator-(const System.Numerics	
Multiprecision.BigInt&, const System.Numerics	s tracted from another.
Multiprecision.BigInt&)	
operator/(const System.Numerics	-
Multiprecision.BigInt&, const System.Numerics	s vided by another.
Multiprecision.BigInt&)	
operator<(const System.Numerics	
Multiprecision.BigInt&, const System.Numerics	s second BigInt , false otherwise.
Multiprecision.BigInt&)	
operator << (System.IO.OutputStream&, con	Ŭ Ŭ
System.Numerics.Multiprecision.BigInt&)	output stream as string of decimal digits prefixed
	by minus sign if the value is negative.

Returns true if the first BigInt is equal to the operator == (constSystem.Numerics.-Multiprecision.BigInt&, const System.Numerics.second \mathbf{BigInt} , false otherwise. Multiprecision.BigInt&) operator^(const System.Numerics.-Returns bitwise XOR of two **BigInt** values. Multiprecision.BigInt&, const System.Numerics.-Multiprecision.BigInt&) operator—(const System.Numerics.-Returns bitwise inclusive OR of two \mathbf{BigInt} val-Multiprecision.BigInt&, const System.Numerics.-Multiprecision.BigInt&) $operator \sim (const$ System.Numerics.-Returns bitwise complement of **BigInt** value. Multiprecision.BigInt&)

$Abs (const\ System. Numerics. Multiprecision. BigInt \&)\ Function$

Returns absolute value of given BigInt.

Syntax

public System.Numerics.Multiprecision.BigInt Abs(const System.Numerics.Multiprecision.BigInt&
x);

Parameters

\mathbf{Name}	Type	Description
X	$const\ System. Numerics. Multiprecision. BigInt \&$	A BigInt.

Returns

 ${\bf System. Numerics. Multiprecision. BigInt}$

Returns absolute value of given ${\color{red} {
m BigInt.}}$

${\bf Clear Bit (System. Numerics. Multiprecision. Big Int \&, \ uint) \ \ Function}$

Clear given bit of given BigInt.

Syntax

public void ClearBit(System.Numerics.Multiprecision.BigInt& x, uint bitIndex);

Name	Type	Description
X	System. Numerics. Multiprecision. BigInt &	A reference to a BigInt.
bitIndex	uint	Index of bit to clear.

${\bf SetBit (System. Numerics. Multiprecision. BigInt \&, \ uint) \ Function}$

Set given bit of given BigInt.

Syntax

public void SetBit(System.Numerics.Multiprecision.BigInt& x, uint bitIndex);

Name	Type	Description
X	System. Numerics. Multiprecision. BigInt &	A reference to a BigInt.
bitIndex	uint	Index of bit to set.

$TestBit(System.Numerics.Multiprecision.BigInt\&,\ uint)\ Function$

Returns true if given bit of given BigInt is set, false otherwise.

Syntax

public bool TestBit(System.Numerics.Multiprecision.BigInt& x, uint bitIndex);

Parameters

Name	Type	Description
X	System. Numerics. Multiprecision. BigInt &	A reference to a BigInt.
bitIndex	uint	Index of bit to test.

Returns

bool

Returns true if given bit of given BigInt is set, false otherwise.

$ToggleBit (System. Numerics. Multiprecision. BigInt \&, \ uint) \ \ Function$

Toggle given bit of given BigInt.

Syntax

public void ToggleBit(System.Numerics.Multiprecision.BigInt& x, uint bitIndex);

Name	Type	Description
X	System. Numerics. Multiprecision. BigInt &	A reference to a BigInt.
bitIndex	uint	Index of bit to toggle.

operator% (const~System. Numerics. Multiprecision. BigInt&,~const~System. BigInt&

Returns the remainder when given BigInt is divided by another.

Syntax

public System.Numerics.Multiprecision.BigInt operator%(const System.Numerics.Multiprecision.BigInt
left, const System.Numerics.Multiprecision.BigInt& right);

Parameters

\mathbf{Name}	Type	Description
left	const System.Numerics.Multiprecision.BigInt&	Divisor.
right	const System.Numerics.Multiprecision.BigInt&	Dividend.

Returns

 ${\bf System. Numerics. Multiprecision. BigInt}$

Returns the remainder when left is divided by right.

operator & (const~System. Numerics. Multiprecision. BigInt &, const~System. BigInt &, co

Returns bitwise AND of two BigInt values.

Syntax

public System.Numerics.Multiprecision.BigInt operator&(const System.Numerics.Multiprecision.BigInt
left, const System.Numerics.Multiprecision.BigInt& right);

Parameters

Name	\mathbf{Type}	Description
left	$const\ System. Numerics. Multiprecision. BigInt \&$	Left operand.
right	const System.Numerics.Multiprecision.BigInt&	Right operand.

Returns

 ${\bf System. Numerics. Multiprecision. BigInt}$

Returns bitwise AND of given BigInt values.

$operator*(const\ System. Numerics. Multiprecision. BigInt\&,\ const\ System. BigInt\&,\ const\ System. BigIn$

Returns the product of given BigInt value multiplied by another.

Syntax

public System.Numerics.Multiprecision.BigInt operator*(const System.Numerics.Multiprecision.BigInt
left, const System.Numerics.Multiprecision.BigInt& right);

Parameters

Name	\mathbf{Type}	Description
left	$const\ System. Numerics. Multiprecision. BigInt \&$	Left operand.
right	const System.Numerics.Multiprecision.BigInt&	Right operand.

Returns

System. Numerics. Multiprecision. BigInt

Returns the product of given BigInt value multiplied by another.

$operator + (const\ System. Numerics. Multiprecision. BigInt\&, const\ System. BigInt\&, const\ System. BigInt\&, const\ System. BigInt\&, const System. BigInt$

Returns the sum of given BigInt value added to another.

Syntax

public System.Numerics.Multiprecision.BigInt operator+(const System.Numerics.Multiprecision.BigInt
left, const System.Numerics.Multiprecision.BigInt& right);

Parameters

\mathbf{Name}	\mathbf{Type}	Description
left	const System. Numerics. Multiprecision. BigInt &	Left operand.
right	$const\ System. Numerics. Multiprecision. BigInt \&$	Right operand.

Returns

 ${\bf System. Numerics. Multiprecision. BigInt}$

Returns the sum of given BigInt value added to another.

operator-(const System. Numerics.
Multiprecision. BigInt&) Function

Returns the negation of BigInt.

Syntax

public System.Numerics.Multiprecision.BigInt operator-(const System.Numerics.Multiprecision.BigInt x);

Parameters

\mathbf{Name}	Type	Description
X	const System. Numerics. Multiprecision. BigInt&	A value.

Returns

 ${\bf System. Numerics. Multiprecision. BigInt}$

Returns the negation of BigInt.

$operator-(const\ System. Numerics. Multiprecision. BigInt\&,\ const\ System. BigInt\&$

Returns the difference of given BigInt value subtracted from another.

Syntax

public System.Numerics.Multiprecision.BigInt operator-(const System.Numerics.Multiprecision.BigInt
left, const System.Numerics.Multiprecision.BigInt& right);

Parameters

Name	Type	Description
left	$const\ System. Numerics. Multiprecision. BigInt \&$	Left operand.
right	const System.Numerics.Multiprecision.BigInt&	Right operand.

Returns

System. Numerics. Multiprecision. BigInt

Returns the difference of given ${\color{blue} {\bf BigInt}}$ value subtracted from another.

 $operator/(const\ System. Numerics. Multiprecision. BigInt\&,\ const\ System. BigInt\&,\ const\ System. BigIn$

Returns the quotient when given BigInt is divided by another.

Syntax

public System.Numerics.Multiprecision.BigInt operator/(const System.Numerics.Multiprecision.BigInt
left, const System.Numerics.Multiprecision.BigInt& right);

Parameters

\mathbf{Name}	Type	Description	
left	const System. Numerics. Multiprecision. BigInt &	Divisor.	
right	const System.Numerics.Multiprecision.BigInt&	Dividend.	

Returns

System. Numerics. Multiprecision. BigInt

Returns the quotient when given BigInt is divided by another.

Remarks

Quotient is rounded towards zero.

$operator < (const\ System. Numerics. Multiprecision. BigInt\&, const\ System. System. BigInt\&, const System. System. BigInt\&, const System. BigInt\&, con$

Returns true if the first BigInt is less than the second BigInt, false otherwise.

Syntax

public bool operator<(const System.Numerics.Multiprecision.BigInt& left, const System.BigInt& left, con

Parameters

Name	\mathbf{Type}	Description
left	$const\ System. Numerics. Multiprecision. BigInt \&$	Left operand.
right	const System.Numerics.Multiprecision.BigInt&	Right operand.

Returns

bool

Returns true if the first BigInt is less than the second BigInt, false otherwise.

operator<<<(System.IO.OutputStream&, const System.Numerics.Multiprecision.BigInt&) Function

Puts the value of the given BigInt to the given output stream as string of decimal digits prefixed by minus sign if the value is negative.

Syntax

public System.IO.OutputStream& operator<<(System.IO.OutputStream& s, const System.Numerics.Multi
x);</pre>

Parameters

\mathbf{Name}	\mathbf{Type}	Description
S	System.IO.OutputStream&	An output stream.
X	const System.Numerics.Multiprecision.BigInt&	A BigInt value.

Returns

System. IO. Output Stream &

Returns a reference to the output stream.

 $operator == (const\ System. Numerics. Multiprecision. BigInt\&,\ const\ System. Numerics. Multiprecision. BigInt\&,\ const System. BigInt\&,\ con$

Returns true if the first BigInt is equal to the second BigInt, false otherwise.

Syntax

public bool operator==(const System.Numerics.Multiprecision.BigInt& left, const System.BigInt& left, co

Parameters

Name	Type	Description
left	const System.Numerics.Multiprecision.BigInt&	Left operand.
right	const System.Numerics.Multiprecision.BigInt&	Right operand.

Returns

bool

Returns true if the first BigInt is equal to the second BigInt, false otherwise.

 $operator \^{}(const\ System. Numerics. Multiprecision. BigInt\&,\ const\ System. Multiprecision. BigInt\&,\ const\ System. BigInt\&,\ const\ System. BigInt\&,\ const\ System. BigInt\&,\ const\ System. BigInt\&,\ con$

Returns bitwise XOR of two BigInt values.

Syntax

public System.Numerics.Multiprecision.BigInt operator^(const System.Numerics.Multiprecision.BigInt
left, const System.Numerics.Multiprecision.BigInt& right);

Parameters

Name	\mathbf{Type}	Description
left	$const\ System. Numerics. Multiprecision. BigInt \&$	Left operand.
right	const System.Numerics.Multiprecision.BigInt&	Right operand.

Returns

 ${\bf System. Numerics. Multiprecision. BigInt}$

Returns bitwise XOR of two BigInt values.

$operator | (const\ System. Numerics. Multiprecision. BigInt\&, const\ System. Numerics. Multiprecision. BigInt\&, const System. Numerics. Multiprecision. BigInt\&, const System. BigInt\&, const System.$

Returns bitwise inclusive OR of two BigInt values.

Syntax

public System.Numerics.Multiprecision.BigInt operator|(const System.Numerics.Multiprecision.BigInt
left, const System.Numerics.Multiprecision.BigInt& right);

Parameters

Name	Type	Description
left	$const\ System. Numerics. Multiprecision. BigInt \&$	Left operand.
right	const System.Numerics.Multiprecision.BigInt&	Right operand.

Returns

 ${\bf System. Numerics. Multiprecision. BigInt}$

Returns bitwise inclusive OR of two ${\bf BigInt}$ values.

$operator{\sim}(const~System.Numerics.Multiprecision.BigInt\&)~Function$

Returns bitwise complement of BigInt value.

Syntax

 $\verb|public System.Numerics.Multiprecision.BigInt operator \sim (\verb|const System.Numerics.Multiprecision.BigIx|); \\$

Parameters

\mathbf{Name}	Type	Description
X	$const\ System. Numerics. Multiprecision. BigInt \&$	Operand.

Returns

 ${\bf System. Numerics. Multiprecision. BigInt}$

Returns bitwise complement of ${\bf BigInt}$ value.

3.1.3 BigRational Class

An arbitrary precision rational number type.

Syntax

public class BigRational;

3.1.3.1 Member Functions

Member Function	Description
BigRational()	Default constructor. Creates an instance of arbitrary precision rational number and initializes it to zero.
BigRational(const System.NumericsMultiprecision.BigRational&)	Copy constructor.
operator=(const System.Numerics Multiprecision.BigRational&)	Copy assignment.
BigRational(System.Numerics.MultiprecisionBigRational&&)	Move constructor.
operator=(System.Numerics.Multiprecision BigRational&&)	Move assignment.
BigRational(const System.NumericsMultiprecision.BigInt&)	Constructor. Creates an instance of arbitrary precision rational type and initializes it from the given arbitrary precision integer type.
BigRational(const System.String <char>&)</char>	Constructor. Creates an instance of arbitrary precision rational type and initializes it from the given string.
BigRational(const System.String <char>&, int)</char>	Constructor. Creates an instance of arbitrary precision rational type and initializes it from the given string of given base.
BigRational(int)	Constructor. Creates an instance of arbitrary precision rational type and initializes it from the given integer value.
BigRational(uint)	Constructor. Creates an instance of arbitrary precision rational type and initializes it from the given unsigned integer value.
Denominator() const	Returns the denominator of the arbitrary precision ration number.
Handle() const	Returns a handle to the GNU MP library arbitrary precision rational representation.

Numerator() const Returns the numerator of the arbitrary precision

ration number.

ToString() const Returns the value of the **BigRational** as a string.

ToString(int) const Returns the value of the **BigRational** as a string

of given base.

 \sim BigRational() Frees memory occupied by the **BigRational** in-

stance.

BigRational() Member Function

Default constructor. Creates an instance of arbitrary precision rational number and initializes it to zero.

Syntax

public BigRational();

 ${\bf BigRational (const~System. Numerics. Multiprecision. BigRational \&)~Member~Function} \\ {\bf Copy~constructor.}$

Syntax

public BigRational(const System.Numerics.Multiprecision.BigRational& that);

Name	Type	Description
that	const System.Numerics.Multiprecision.BigRational&	A BigRational to copy from.

 $\label{eq:const_system} \mbox{operator=(const\ System.Numerics.Multiprecision.BigRational\&)\ Member\ Function}$ Copy assignment.

Syntax

public void operator=(const System.Numerics.Multiprecision.BigRational& that);

\mathbf{Name}	Type	Description
that	$const\ System. Numerics. Multiprecision. BigRational \&$	A BigRational to assign from.

$BigRational (System. Numerics. Multiprecision. BigRational \&\&) \ Member \ Function$

Move constructor.

Syntax

public BigRational(System.Numerics.Multiprecision.BigRational&& that);

Name	Type	Description
that	System.Numerics.Multiprecision.BigRational&&	A BigRational to move from.

 $\label{eq:operator} \mbox{operator=(System.Numerics.Multiprecision.BigRational\&\&)\ Member\ Function}$ Move assignment.

Syntax

public void operator=(System.Numerics.Multiprecision.BigRational&& that);

Name	Type	Description
that	System.Numerics.Multiprecision.BigRational&&	A BigRational to assign from.

BigRational(const System.Numerics.Multiprecision.BigInt&) Member Function

Constructor. Creates an instance of arbitrary precision rational type and initializes it from the given arbitrary precision integer type.

Syntax

public BigRational(const System.Numerics.Multiprecision.BigInt& that);

\mathbf{Name}	Type	Description
that	const~System. Numerics. Multiprecision. BigInt &	An arbitrary precision integer
		type value to initialize from.

BigRational(const System.String<char>&) Member Function

Constructor. Creates an instance of arbitrary precision rational type and initializes it from the given string.

Syntax

public BigRational(const System.String<char>& str);

Name	Type	Description
str	const System.String <char>&</char>	A string to initialize from.

BigRational(const System.String<char>&, int) Member Function

Constructor. Creates an instance of arbitrary precision rational type and initializes it from the given string of given base.

Syntax

public BigRational(const System.String<char>& str, int base_);

Name	\mathbf{Type}	Description
str	const System.String <char>&</char>	A string to initialize from.
$base_$	int	Base of string.

BigRational(int) Member Function

Constructor. Creates an instance of arbitrary precision rational type and initializes it from the given integer value.

Syntax

public BigRational(int that);

Name	Type	Description
that	$_{ m int}$	An integer value to initalize from.

BigRational(uint) Member Function

Constructor. Creates an instance of arbitrary precision rational type and initializes it from the given unsigned integer value.

Syntax

public BigRational(uint that);

Name	\mathbf{Type}	Description
that	uint	An unsigned integer value to initalize from.

Denominator() const Member Function

Returns the denominator of the arbitrary precision ration number.

Syntax

public System.Numerics.Multiprecision.BigInt Denominator() const;

Returns

 ${\bf System. Numerics. Multiprecision. BigInt}$

Returns the denominator of the arbitrary precision ration number.

Handle() const Member Function

Returns a handle to the GNU MP library arbitrary precision rational representation.

Syntax

public void* Handle() const;

Returns

void*

Returns a handle to the GNU MP library arbitrary precision rational representation.

Numerator() const Member Function

Returns the numerator of the arbitrary precision ration number.

Syntax

public System.Numerics.Multiprecision.BigInt Numerator() const;

Returns

 ${\bf System. Numerics. Multiprecision. BigInt}$

Returns the numerator of the arbitrary precision ration number.

ToString() const Member Function

Returns the value of the BigRational as a string.

Syntax

public System.String<char> ToString() const;

Returns

 ${\bf System.String}{<}{\bf char}{>}$

Returns the value of the BigRational as a string.

ToString(int) const Member Function

Returns the value of the BigRational as a string of given base.

Syntax

public System.String<char> ToString(int base_) const;

Parameters

Returns

 ${\bf System.String}{<}{\bf char}{>}$

Returns the value of the BigRational as a string of given base.

\sim BigRational() Member Function

Frees memory occupied by the BigRational instance.

Syntax

public ~BigRational();

3.1.3.2 Nonmember Functions

Function	Description
Abs(const System.Numerics.Multiprecision	Returns the absolute value of the given BigRa-
BigRational&)	tional value.
operator*(const System.Numerics	Returns the product of given BigRational value
Multiprecision.BigRational&, const System	multiplied by another.
Numerics.Multiprecision.BigRational&)	
operator+(const System.Numerics	Returns the sum of given BigRational value
Multiprecision.BigRational&, const System	added to another.
Numerics. Multiprecision. BigRational &)	
operator-(const System.Numerics	Returns the negation of BigRational .
Multiprecision.BigRational&)	
operator-(const System.Numerics	Returns the difference of given BigRational
Multiprecision.BigRational&, const System	value subtracted from another.
Numerics. Multiprecision. BigRational &)	
operator/(const System.Numerics	Returns the quotient when given BigRational is
Multiprecision.BigRational&, const System	divided by another.
Numerics. Multiprecision. BigRational &)	
operator<(const System.Numerics	Returns true if the first BigRational is less than
Multiprecision.BigRational&, const System	the second $\mathbf{BigRational}$, false otherwise.
Numerics. Multiprecision. BigRational &)	
operator << (System. IO. Output Stream &, const	Puts the value of the given BigRational to the
System.Numerics.Multiprecision.BigRational&)	given output stream as string.
operator==(const System.Numerics	Returns true if the first BigRational is equal to
Multiprecision.BigRational&, const System	the second $\mathbf{BigRational}$, false otherwise.
Numerics. Multiprecision. BigRational &)	

$Abs (const\ System. Numerics. Multiprecision. BigRational \&)\ Function$

Returns the absolute value of the given BigRational value.

Syntax

public System.Numerics.Multiprecision.BigRational Abs(const System.Numerics.Multiprecision.BigRat x);

Parameters

Name	Type	Description	
X	const System.Numerics.Multiprecision.BigRational&	BigRational.	

Returns

 ${\bf System. Numerics. Multiprecision. BigRational}$

Returns the absolute value of the given ${\bf BigRational}$ value.

 $operator*(const\ System. Numerics. Multiprecision. BigRational\&, const\ System. System. BigRational\&, const\ System. Big$

Returns the product of given BigRational value multiplied by another.

Syntax

public System.Numerics.Multiprecision.BigRational operator*(const System.Numerics.Multiprecision.
left, const System.Numerics.Multiprecision.BigRational& right);

Parameters

Name	\mathbf{Type}	Description
left	$const\ System. Numerics. Multiprecision. BigRational \&$	Left operand.
right	const System.Numerics.Multiprecision.BigRational&	Right operand.

Returns

System. Numerics. Multiprecision. BigRational

Returns the product of given BigRational value multiplied by another.

$operator + (const\ System. Numerics. Multiprecision. BigRational\&,\ const\ System. BigRational\&,\ const\ S$

Returns the sum of given BigRational value added to another.

Syntax

public System.Numerics.Multiprecision.BigRational operator+(const System.Numerics.Multiprecision.BigRational& right);

Parameters

Name	Type	Description
left	$const\ System. Numerics. Multiprecision. BigRational \&$	Left operand.
right	const System.Numerics.Multiprecision.BigRational&	Right operand.

Returns

System. Numerics. Multiprecision. BigRational

Returns the sum of given ${\color{blue} {\rm BigRational}}$ value added to another.

$operator-(const\ System. Numerics. Multiprecision. BigRational \&)\ Function$

Returns the negation of BigRational.

Syntax

public System.Numerics.Multiprecision.BigRational operator-(const System.Numerics.Multiprecision.x);

Parameters

Name	Type	Description
X	const System.Numerics.Multiprecision.BigRational&	BigRational.

Returns

 ${\bf System. Numerics. Multiprecision. BigRational}$

Returns the negation of BigRational.

$operator-(const\ System. Numerics. Multiprecision. BigRational\&,\ const\ System. Numerics. Multiprecision. Function$

Returns the difference of given BigRational value subtracted from another.

Syntax

public System.Numerics.Multiprecision.BigRational operator-(const System.Numerics.Multiprecision.BigRational& right);

Parameters

Name	\mathbf{Type}	Description
left	$const\ System. Numerics. Multiprecision. BigRational \&$	Left operand.
right	const System.Numerics.Multiprecision.BigRational&	Right operand.

Returns

System. Numerics. Multiprecision. BigRational

Returns the difference of given BigRational value subtracted from another.

$operator/(const\ System. Numerics. Multiprecision. BigRational\&, const\ System. System. BigRational\&, const\ System. Big$

Returns the quotient when given BigRational is divided by another.

Syntax

public System.Numerics.Multiprecision.BigRational operator/(const System.Numerics.Multiprecision.BigRational& right);

Parameters

Name	Type	Description
left	$const\ System. Numerics. Multiprecision. BigRational \&$	Divisor.
right	const System.Numerics.Multiprecision.BigRational&	Dividend.

Returns

System. Numerics. Multiprecision. BigRational

Returns the quotient when given BigRational is divided by another.

$operator < (const\ System. Numerics. Multiprecision. BigRational\&,\ const\ System. BigRational\&,\ const\ S$

Returns true if the first BigRational is less than the second BigRational, false otherwise.

Syntax

public bool operator<(const System.Numerics.Multiprecision.BigRational& left, const System.Numerics.Multiprecision.BigRational& right);

Parameters

Name	Type	Description
left	$const\ System. Numerics. Multiprecision. BigRational \&$	Left operand.
right	const System.Numerics.Multiprecision.BigRational&	Right operand.

Returns

bool

Returns true if the first BigRational is less than the second BigRational, false otherwise.

operator << (System. IO. Output Stream &, const~System. Numerics. Multiprecision. BigRational &)~Function

Puts the value of the given BigRational to the given output stream as string.

Syntax

public System.IO.OutputStream& operator<<(System.IO.OutputStream& s, const System.Numerics.Multi
x):</pre>

Parameters

\mathbf{Name}	Type	Description
s	System.IO.OutputStream&	An output stream.
X	const System.Numerics.Multiprecision.BigRational&	A BigRational value.

Returns

System. IO. Output Stream &

Returns a reference to the output stream.

$operator == (const\ System. Numerics. Multiprecision. BigRational\&,\ const\ System. BigRational\&,\ const\$

Returns true if the first BigRational is equal to the second BigRational, false otherwise.

Syntax

public bool operator==(const System.Numerics.Multiprecision.BigRational& left, const System.Numerics.Multiprecision.BigRational& right);

Parameters

Name	Type	Description
left	$const\ System. Numerics. Multiprecision. BigRational \&$	Left operand.
right	const System.Numerics.Multiprecision.BigRational&	Right operand.

Returns

bool

Returns true if the first BigRational is equal to the second BigRational, false otherwise.

3.1.4 Precision Class

Represents a precision of given number of digits.

Syntax

public class Precision;

3.1.4.1 Member Functions

Member Function	Description
Precision()	Default constructor. Initializes the precision with zero digits.
Precision(const System.Numerics.MultiprecisionPrecision&)	Copy constructor.
operator=(const System.Numerics Multiprecision.Precision&)	Copy assignment.
Precision(System.Numerics.Multiprecision Precision&&)	Move constructor.
operator=(System.Numerics.Multiprecision Precision&&)	Move assignment.
Precision(uint)	Constructor. Initializes the precision with given number of digits.
operator_uint() const	Returns the number of digits of this precision.

Precision() Member Function

Default constructor. Initializes the precision with zero digits.

Syntax

public Precision();

 $\label{lem:precision} \mbox{Precision(const System.Numerics.Multiprecision.Precision\&) Member Function} \\ \mbox{Copy constructor.}$

Syntax

public Precision(const System.Numerics.Multiprecision.Precision& that);

Name	Type	Description
that	const System.Numerics.Multiprecision.Precision&	Argument to copy.

 $\label{eq:const_system} \mbox{operator=(const System.Numerics.Multiprecision.Precision\&) Member Function} \\ \mbox{Copy assignment.}$

Syntax

public void operator=(const System.Numerics.Multiprecision.Precision& that);

Name	Type	Description
that	const System.Numerics.Multiprecision.Precision&	Argument to assign.

${\bf Precision(System.Numerics.Multiprecision.Precision\&\&)~Member~Function}$

Move constructor.

Syntax

public Precision(System.Numerics.Multiprecision.Precision&& that);

Name	Type	Description
that	System.Numerics.Multiprecision.Precision&&	Argument to move from.

 $\label{eq:operator} \mbox{operator=(System.Numerics.Multiprecision.Precision\&\&)\ Member\ Function}$ Move assignment.

Syntax

public void operator=(System.Numerics.Multiprecision.Precision&& that);

Name	\mathbf{Type}	Description
that	System.Numerics.Multiprecision.Precision&&	Argument to assign from.

Precision(uint) Member Function

Constructor. Initializes the precision with given number of digits.

Syntax

public Precision(uint prec_);

Name	\mathbf{Type}	Description
prec	uint	Number of digits.

operator_uint() const Member Function

Returns the number of digits of this precision.

Syntax

public uint operator_uint() const;

Returns

uint

Returns the number of digits of this precision.

3.2 Functions

Function Description