uhuge.cm

```
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    */
// Copyright (c) 1994
// Hewlett-Packard Company
// Copyright (c) 1996
// Silicon Graphics Computer Systems, Inc.
// Copyright (c) 2009 Alexander Stepanov and Paul McJones
// 128-bit unsigned integer arithmetics...
using System. Collections;
namespace System
    public class uhuge
        public nothrow uhuge(): h(0u), l(0u)
        public nothrow uhuge(ulong l_): h(0u), l(l_)
        public nothrow uhuge(ulong h_, ulong l_): h(h_), l(l_)
        public nothrow uhuge& operator++()
            ++1;
            if (1 == 0u)
                ++h;
            return *this;
        public nothrow uhuge& operator--()
            if (1 == 0xFFFFFFFFFFFFF)
                —h;
```

```
return *this;
    public ulong h;
    public ulong 1;
public nothrow inline uhuge operator+(uhuge left , uhuge right)
    uhuge result;
    result.h = left.h + right.h;
    result.l = left.l + right.l;
    if (result.1 < left.1)
        result.h = result.h + 1u;
    return result;
}
public nothrow inline uhuge operator-(uhuge left , uhuge right)
    uhuge result;
    result.h = left.h - right.h;
    result.l = left.l - right.l;
    if (result.l > left.l)
        result.h = result.h - 1u;
    return result;
}
public nothrow uhuge operator<<(uhuge left , uhuge right)</pre>
    uhuge zero = 0u;
    uhuge sixtyfour = 64u;
    while (right >= sixtyfour)
        left.h = left.l;
        left.l = 0u;
        right = right - sixtyfour;
    if (right > zero)
        \mathbf{ulong} \ \mathbf{s} = \mathbf{right.l};
        ulong lefthl = left.h << s;
        ulong leftlh = left.l \gg (64u - s);
        left.h = lefthl + leftlh;
        left.l = left.l \ll s;
    return left;
}
public nothrow uhuge operator>>(uhuge left , uhuge right)
```

```
{
     uhuge zero = 0u;
     uhuge sixtyfour = 64u;
     while (right >= sixtyfour)
          left.l = left.h;
          left.h = 0u;
          right = right - sixtyfour;
     if (right > zero)
          ulong s = right.l;
          ulong lefthl = left.h \ll (64u - s);
          ulong leftlh = left.l >> s;
          \mbox{left.h} \; = \; \mbox{left.h} \; >> \; \mbox{s} \; ;
          left.l = lefthl + leftlh;
     return left;
public nothrow inline uhuge operator&(uhuge left , uhuge right)
     uhuge result;
     result.h = left.h & right.h;
     result.l = left.l & right.l;
     return result;
}
public nothrow inline uhuge operator | (uhuge left , uhuge right)
     uhuge result;
     result.h = left.h | right.h;
     result.l = left.l | right.l;
     return result;
}
public nothrow inline uhuge operator (uhuge left , uhuge right)
     uhuge result;
     result.h = left.h ^ right.h;
result.l = left.l ^ right.l;
     return result;
public nothrow inline uhuge operator (uhuge x)
     uhuge result;
     \begin{array}{lll} r\,e\,s\,u\,l\,t\,\,.\,h &=& \tilde{\phantom{a}}\,x\,.\,h\,;\\ r\,e\,s\,u\,l\,t\,\,.\,l &=& \tilde{\phantom{a}}\,x\,.\,l\,; \end{array}
     return result;
}
```

```
The Art of Computer Programming, Volume 2, 4.3.1, Algorithm M (
multiplication of nonnegative integers), p. 268
public Pair<uhuge, uhuge> mul(uhuge left, uhuge right)
    ulong [4] u;
    u[3] = left.h >> 32u;
    u[2] = left.h & 0xFFFFFFFF;
    u[1] = left.l >> 32u;
    u[0] = left.l & 0xFFFFFFFF;
    \mathbf{ulong}[4] \ \mathbf{v};
    v[3] = right.h >> 32u;
    v[2] = right.h \& 0xFFFFFFFF;
    v[1] = right.1 >> 32u;
    v[0] = right.l \& 0xFFFFFFFF;
    ulong [8] w;
    for (int j = 0; j < 4; ++j)
        if (v[j] != 0u)
             uint k = 0u;
             for (int i = 0; i < 4; ++i)
                 ulong t = u[i] * v[j] + w[i + j] + k;
                 w[i + j] = t \& 0xFFFFFFFF;
                 k = cast < uint > (t >> 32u);
            w[j + 4] = k;
        }
    uhuge h((w[7] \ll 32u) + w[6], (w[5] \ll 32u) + w[4]);
    uhuge l((w[3] \ll 32u) + w[2], (w[1] \ll 32u) + w[0]);
    return MakePair(h, l);
public uhuge operator*(uhuge left , uhuge right)
    Pair < uhuge, uhuge > hl = mul(left, right);
    return hl.second;
The Art of Computer Programming, Volume 2, 4.3.1 exercise 16 (short
division), p. 625...
public Pair < uhuge , uint > divmod(uhuge left , uint right)
    uhuge digitBits = 32u;
    ulong b = 0x100000000u;
    uint r = 0u;
    uhuge q = 0u;
    int j = 3;
    while (j >= 0)
    {
```

```
uhuge shift = uhuge(cast<uint>(j) * 32u);
             uhuge m = left \gg shift;
             uint u = cast < uint > (m. 1);
             \mathbf{ulong} \ d = r * b + u;
             \mathbf{uint} \ \mathbf{w} = \mathbf{cast} < \mathbf{uint} > (\mathbf{d} \ / \ \mathrm{right});
             q = (q \ll digitBits) \mid uhuge(w);
             r = cast < uint > (d \% right);
             —j;
         }
         return MakePair(q, r);
    The Art of Computer Programming, Volume 2, 4.3.1, Algorithm D (
    division of nonnegative integers), p. 272
    public Pair<uhuge, uhuge> divmod(uhuge left, uhuge right)
         ulong b = 0x100000000u;
         if (right < b) // see, if we manage using short division
             algorithm...
             Pair<uhuge, uint> p = divmod(left, cast<uint>(right.l));
             return MakePair(p.first , uhuge(p.second));
         ulong m = 0xFFFFFFFF;
         ulong[8] u;
         u[3] = left.h >> 32u;
         u[2] = left.h \& m;
         u[1] = left.l >> 32u;
         u[0] = left.1 \& m;
         \mathbf{ulong}[4] \quad v;
         v[3] = right.h >> 32u;
         v[2] = right.h \& m;
         v[1] = right.l >> 32u;
         v[0] = right.l \& m;
         \mathbf{ulong}[4] \neq ;
//
         D1. [Normalize.]
         int n = 4;
         while (v[n-1] == 0u)
         {
             --n;
         ulong vh = v[n - 1];
         int d = 0;
         while (vh < 0x80000000u)
             ++d;
             vh = vh \ll 1u;
         ulong t = 0u;
         ulong k = 0u;
         for (int j = 0; j < n + 4; ++j)
```

```
t = (u[j] \ll cast < uint > (d)) + k;
    u[j] = t \& m;
    k = t >> 32u;
k = 0u;
for (int j = 0; j < 4; ++j)
    t = (v[j] \ll cast < uint > (d)) + k;
    v[j] = t \& m;
    k = t >> 32u;
vh = v[n - 1];
ulong vmh = 0u;
if (n > 1)
    vmh = v[n - 2];
D2. [Initialize j.]
for (int j = 3; j >= 0; ---j)
D3. [Calculate qhat.]
    t = (u[j + n] \ll 32u) + u[j + n - 1];
    \mathbf{ulong} \ \mathrm{qhat} = \mathrm{t} \ / \ \mathrm{vh};
    \mathbf{ulong} \ \mathrm{rhat} = \mathrm{t} - \mathrm{vh} * \mathrm{qhat};
    if (n > 1)
         while (qhat == b \mid \mid qhat * vmh > (rhat << 32u) + u[j + n]
             -2])
         {
             --qhat;
             rhat = rhat + vh;
              if (rhat >= b) break;
D4. [Multiply and subtract.]
    k = 0u;
    for (int i = 0; i < n; ++i)
         int ipj = i + j;
         uhuge tc = u[ipj] + uhuge(0xFFFFFFF00000000u) - k - qhat
             * v[i];
         t = tc.1;
         u[ipj] = t \& m;
         k = m - (t >> 32u);
D5. | Test remainder. |
    if (u[j + n] != k)
D6. [Add back.]
         --qhat;
         k = 0u;
         for (int i = 0; i < n; ++i)
         {
```

```
int ipj = i + j;
                   t = u[ipj] + v[i] + k;
                   u[ipj] = t \& m;
                   k = t >> 32u;
         q[j] = qhat;
    D7. [Loop on j.]
    D8. [Unnormalize.]
    \mathbf{ulong} \; \mathrm{mask} = (\mathbf{ulong}(1\mathbf{u}) << \mathbf{cast} < \mathbf{ulong} > (\mathbf{d})) - \mathbf{ulong}(1\mathbf{u});
    int j = 3;
    while (j >= n)
         \mathbf{u}[\mathbf{j}] = 0\mathbf{u};
         —j;
    k = 0u;
    while (j >= 0)
         t = (k \ll 32u) + u[j];
         u[j] = t \gg cast < uint > (d);
         k = t \& mask;
         —j;
    uhuge \ quotient ((q[3] << 32u) + q[2], \ (q[1] << 32u) + q[0]);
    uhuge remainder ((u[3] \ll 32u) + u[2], (u[1] \ll 32u) + u[0]);
    return MakePair(quotient, remainder);
}
public uhuge operator/(uhuge left , uhuge right)
    Pair < uhuge, uhuge > qr = divmod(left, right);
    return qr.first;
public uhuge operator%(uhuge left , uhuge right)
    Pair < uhuge, uhuge > qr = divmod(left, right);
    return qr.second;
public nothrow inline bool operator==(uhuge left, uhuge right)
    return left.h == right.h && left.l == right.l;
public nothrow inline bool operator<(uhuge left , uhuge right)</pre>
    if (left.h < right.h)</pre>
    {
         return true;
    }
```

```
else if (left.h > right.h)
{
     return false;
}
else
{
     return left.l < right.l;
}
}</pre>
```