

MECH6066 HW#5

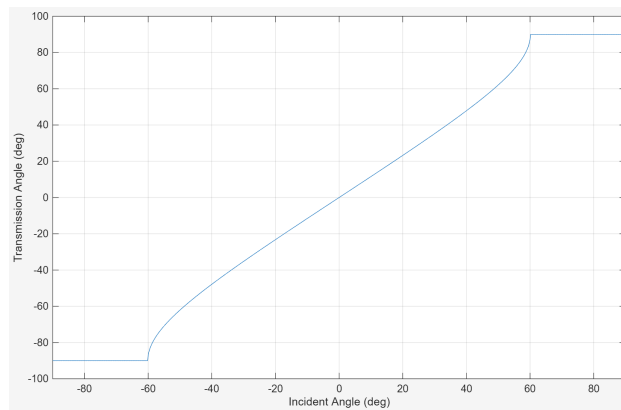
Slade Brooks

M13801712

11.17.25

Problem 1

(a)

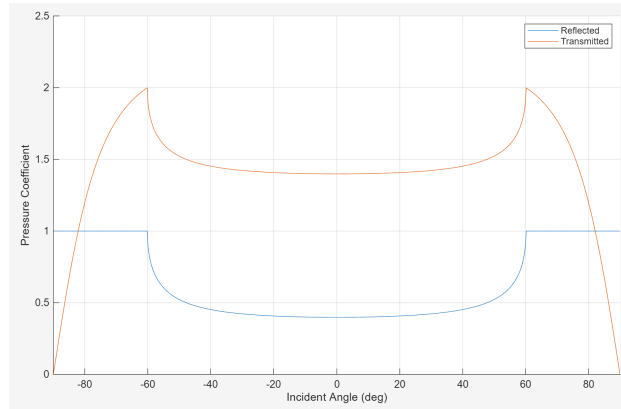


(b)

From the plot, it appears the critical angle is 60° . We can verify this analytically from: $\sin \theta_c = \frac{c_1}{c_2}$. We will do this in matlab to determine the critical angle and we get that

$$\boxed{\theta_c = 61.12^\circ}.$$

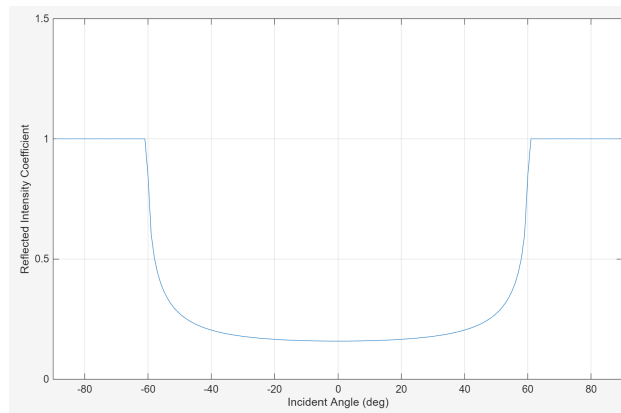
(c)



(d)

At normal incidence ($\theta_i = 0^\circ$), $\bar{R} = 0.398$ and $\bar{T} = 1.398$.

(e)



(f)

We can determine the Brewster angle based on the plot in part e. The brewster angle will be at 100% transmission, so our reflected intensity coefficient would be 0. We can see that since this does not happen, there is no brewster angle for this combination of materials.

Problem 2

(a)

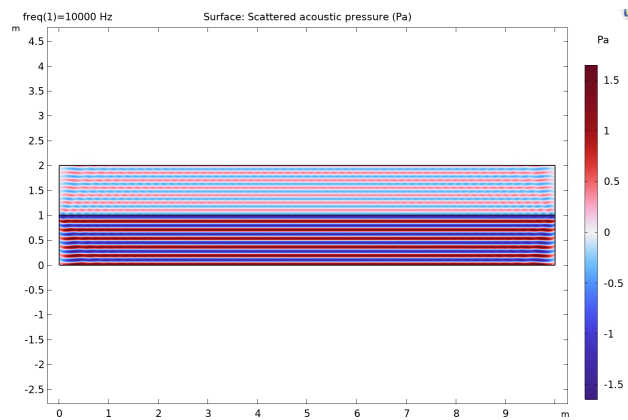
See attached model.

(b)

Yes, there are downwards moving waves and a standing wave in the water. The transmitted wave is roughly 1.4 Pa, so it matches very closely to previous calculations.

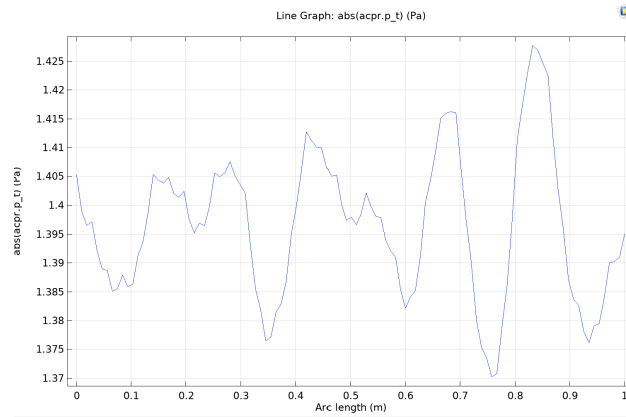
(c)

When plotting just ps, we can see that the reflected wave is roughly 0.4 Pa in amplitude which is exactly what we calculated previously.



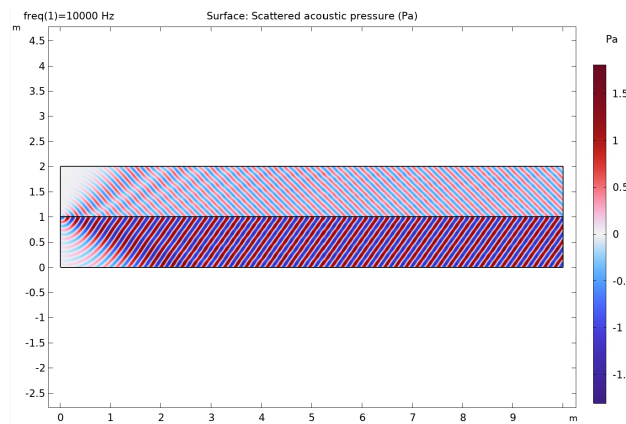
(d)

We can see that the amplitude does not vary since there is just a wave transmitted into the sand and no standing wave to change the amplitude.

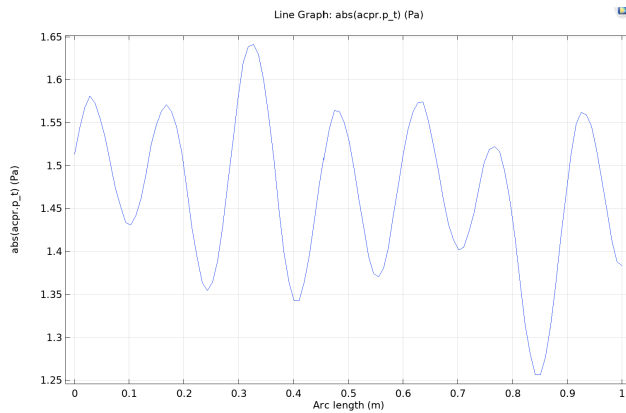


(e)

We can see that the reflected pressure does match what is expected (roughly 0.5 Pa).

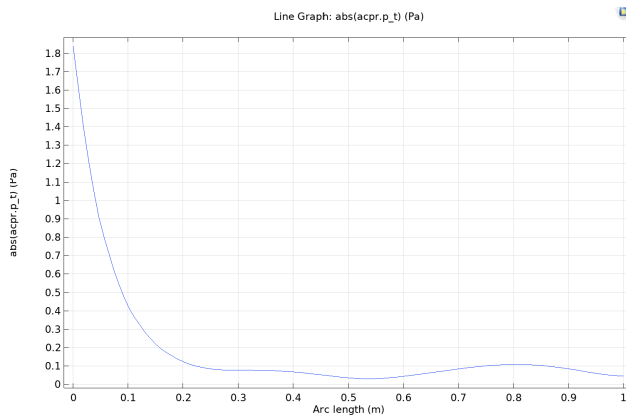


We can see that the amplitude still does not vary vertically, and shouldn't because it is still just transmitted pressure into the quartz sand not a standing wave.



(f)

The waves in the sand move only in the x direction. I believe these would be transverse waves. The amplitude does vary in the vertical direction but I believe this is due to artifacts in the simulation, not a physical phenomenon.



Problem 3

(a)

See attached model.

(b)

The generated waves can be approximated as spherical. The wavelength of the generated sound will be 0.343 meters and the largest dimension of the speaker geometry is only 0.02 meters, which should be small enough compared to the wavelength to approximate the generated wave as spherical.

(c)

Evaluating at the far right side of the domain gave an amplitude of 0.007 Pa at 1 m, which means $A = 0.007 \text{ Pa}\cdot\text{m}$

(d)

$$I = \text{re}\{0.5 \cdot p \cdot u^*\}$$

$$I = \text{re}\left\{\frac{p}{2} \left[\frac{1}{Z_0} \left(1 + \frac{1}{jkr} \right) p\hat{r} \right]^*\right\}$$

The exponential terms will now cancel out since one is a conjugate, and because we are taking only the real any remaining j terms disappear.

$$I = \frac{|A|}{2r} e^{j(\omega t - kr)} \frac{1}{Z_0} \frac{|A|}{r} e^{-j(\omega t - kr)} \hat{r}$$

$$I = \frac{|A|}{2r} \frac{1}{Z_0} \frac{|A|}{r} \hat{r}$$

$$I = \frac{|A|^2}{2Z_0 r^2} \hat{r}$$

We can see that the intensity goes down relative to the radius squared as we move farther away.

(e)

$$I = \frac{|A|^2}{2Z_0 r^2} = \frac{0.007^2}{2(343 \cdot 1.15)} = 6.2e-8 \text{ W/m}^2$$

$$SIL = 10 \log_{10} (I/I_{ref}) = 10 \log_{10} (6.2e-8/10^{-12}) = \boxed{SIL = 48 \text{ dB}}$$

I get an SPL of just under 48 dB from the comsol model, so the approximation is very accurate.

(f)

$$W = I4\pi a^2 = \frac{|A|^2}{2Z_0 r^2} 4\pi a^2 = \frac{2\pi|A|^2}{Z_0} = \boxed{7.8e-7W}$$

The power does not depend on the distance. The intensity depends on the distance, but the power equation simplifies to not have any radius term in it, so it depends only on the amplitude of the pressure and the impedance.

(g)

The comsol model reports a power of $8.3e-7$ W, whereas I calculated a power of $7.8e-7$ W. These values do differ slightly, but are fairly close. I believe the difference in value comes from the spherical assumption. The spherical assumption for the analytical value assumes a spherical source at 0, 0. Our comsol model is slightly offset from that and has a linear moving source instead of a single breathing point, so it makes sense that comsol would calculate a higher power. At some points, the sound generating surface is closer to the edge of the domain than it would be for the spherical approximation, and the pressure wave generated is larger since it has some length to it.

(h)

I would not assume the waves are spherical. The wavelength would go down to 0.03 m, which is only slightly bigger than the radius of the speaker, so it is probably not a large enough difference to be considered spherical.

Problem 4

My only change for this assignment would be less comsol work. I think this assignment is well-structured and helpful for understanding some of the concepts. However, I sometimes have issues where comsol is a little clunky or confusing and I waste time troubleshooting comsol instead of getting valuable insights.

Problem 1 Matlab

```
clear variables; close all;
```

```

% define properties from appendix
rhoSW = 1026;
cSW = 1500;
ZSW = 1.54e6;
rhoQS = 2070;
cQS = 1730;
ZQS = 3.58e6;

%% Part A
% set range of angles to check
thetai = -90:1:90;

% calculate xmission angle for each
thetat = asind(cQS/cSW.*sind(thetai));

% plot results
figure
plot(thetai, thetat)
xlim([thetai(1) thetai(end)]); xlabel("Incident Angle (deg)")
ylim([-100 100]); ylabel("Transmission Angle (deg)")
grid on

%% Part B
% calc critical angle
thetac = asind(cSW/cQS);

%% Part C
% calc reflection coef (magnitude)
Rbar = abs((ZQS./cosd(thetat) - ZSW./cosd(thetai))./(ZQS./cosd(thetat) + ZSW./cosd(thetai)));

% calc xmission coef (magnitude)
Tbar = abs(2*(ZQS./cosd(thetat))./(ZQS./cosd(thetat) + ZSW./cosd(thetai)));

% plot results
figure
hold on
plot(thetai, Rbar); plot(thetai, Tbar)
hold off

```



```

xlim([thetai(1) thetai(end)]); xlabel("Incident Angle (deg)")
ylim([0 2.5]); ylabel("Pressure Coefficient")
legend(["Reflected", "Transmitted"])
grid on

%% Part D
% calculate reflection intensity coeff
RI = Rbar.^2;

% plot
figure
plot(thetai, RI)
xlim([thetai(1) thetai(end)]); xlabel("Incident Angle (deg)")
ylim([0 1.5]); ylabel("Reflected Intensity Coefficient")
grid on

```

Hw5.2

| | |
|-------------|--------------------------|
| Report date | Nov 17, 2025, 8:58:57 PM |
|-------------|--------------------------|

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1 Global Definitions

| | |
|------|---------------------------|
| Date | Nov 16, 2025, 12:10:32 PM |
|------|---------------------------|

GLOBAL SETTINGS

| | |
|---------|--|
| Name | Hw5.2.mph |
| Path | \\clusterfsnew.ceas1.uc.edu\students\brooksl\desktop\hw5.2.mph |
| Version | COMSOL Multiphysics 6.3 (Build: 420) |

USED PRODUCTS

| |
|---------------------|
| Acoustics Module |
| COMSOL Multiphysics |

COMPUTER INFORMATION

| | |
|------------------|---|
| CPU | Intel64 Family 6 Model 198 Stepping 2, 28 cores, 63.46 GB RAM |
| Operating system | Windows 11 |

1.1 PARAMETERS

PARAMETERS 1

| Name | Expression | Value | Description |
|---------|--------------|------------------------|-------------|
| length | 10[m] | 10 m | |
| height | 1[m] | 1 m | |
| rho1 | 1026[kg/m^3] | 1026 kg/m ³ | |
| c1 | 1500[m/s] | 1500 m/s | |
| rho2 | 2070[kg/m^3] | 2070 kg/m ³ | |
| c2 | 1730[m/s] | 1730 m/s | |
| p_input | 1[Pa] | 1 Pa | |
| theta_i | 70[deg] | 1.2217 rad | |
| f_study | 10[kHz] | 10000 Hz | |

1.2 SHARED PROPERTIES

1.2.1 Default Model Inputs

| | |
|-----|--------|
| Tag | cminpt |
|-----|--------|

2 Component 1

SETTINGS

| Description | Value |
|-------------|----------------------------|
| Unit system | Same as global system (SI) |

2.1 DEFINITIONS

2.1.1 Coordinate Systems

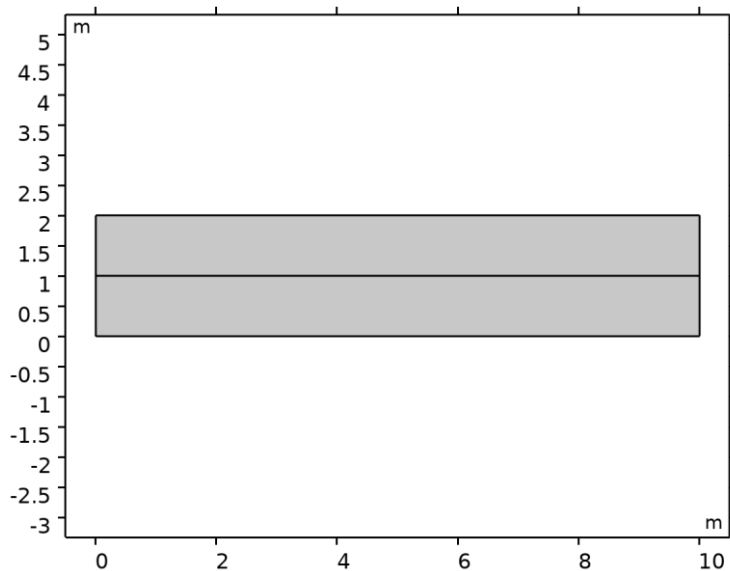
Boundary System 1

| | |
|------------------------|-----------------|
| Coordinate system type | Boundary system |
| Tag | sys1 |

COORDINATE NAMES

| First | Second | Third |
|-------|--------|-------|
| t1 | n | to |

2.2 GEOMETRY 1



Geometry 1

UNITS

| | |
|--------------|-----|
| Length unit | m |
| Angular unit | deg |

GEOMETRY STATISTICS

| Description | Value |
|-------------|-------|
|-------------|-------|

| Description | Value |
|----------------------|-------|
| Space dimension | 2 |
| Number of domains | 2 |
| Number of boundaries | 7 |
| Number of vertices | 6 |

2.2.1 Rectangle 1 (r1)

SIZE AND SHAPE

| Description | Value |
|-------------|--------|
| Width | length |
| Height | height |

POSITION

| Description | Value |
|-------------|--------|
| Position | {0, 0} |

2.2.2 Rectangle 2 (r2)

SIZE AND SHAPE

| Description | Value |
|-------------|--------|
| Width | length |
| Height | height |

POSITION

| Description | Value |
|-------------|-------------|
| Position | {0, height} |

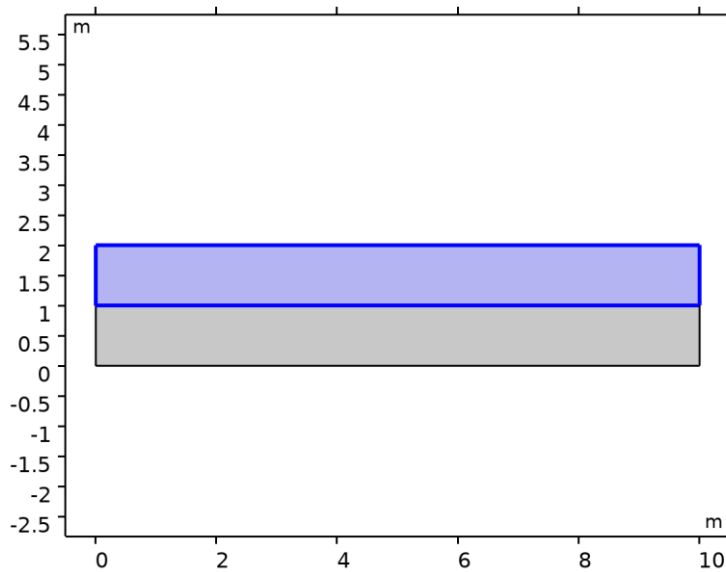
2.2.3 Form Union (fin)

INFORMATION

| Description | Value |
|---------------|---|
| Build message | Formed union of 2 solid objects. Union has 2 domains, 7 boundaries, and 6 vertices. |

2.3 MATERIALS

2.3.1 seawater



seawater

SELECTION

| | |
|------------------------|--|
| Geometric entity level | Domain |
| Selection | Geometry geom1: Dimension 2: All domains |

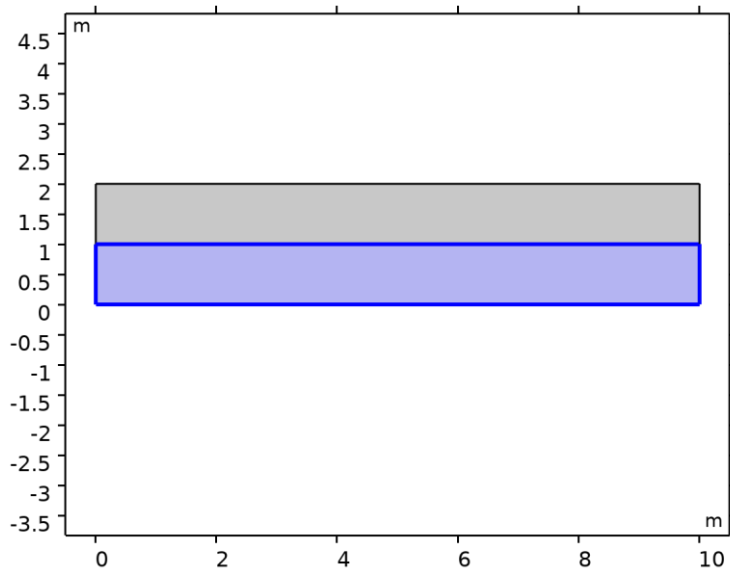
MATERIAL PARAMETERS

| Name | Value | Unit | Property group |
|----------------|-------|-------------------|----------------|
| Density | rho1 | kg/m ³ | Basic |
| Speed of sound | c1 | m/s | Basic |

BASIC

| Description | Value | Unit |
|----------------|-------|-------------------|
| Density | rho1 | kg/m ³ |
| Speed of sound | c1 | m/s |

2.3.2 quartz sand



quartz sand

SELECTION

| | |
|------------------------|---------------------------------------|
| Geometric entity level | Domain |
| Selection | Geometry geom1: Dimension 2: Domain 1 |

MATERIAL PARAMETERS

| Name | Value | Unit | Property group |
|----------------|-------|-------------------|----------------|
| Density | rho2 | kg/m ³ | Basic |
| Speed of sound | c2 | m/s | Basic |

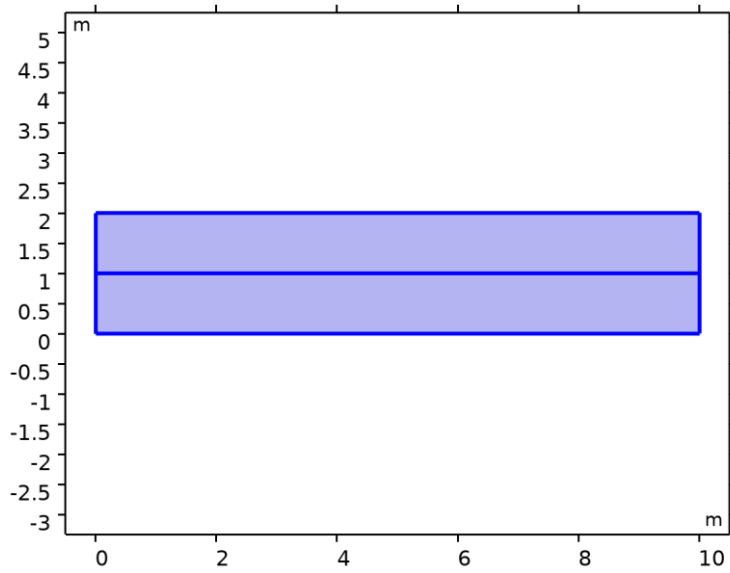
BASIC

| Description | Value | Unit |
|----------------|-------|-------------------|
| Density | rho2 | kg/m ³ |
| Speed of sound | c2 | m/s |

2.4 PRESSURE ACOUSTICS, FREQUENCY DOMAIN

USED PRODUCTS

| |
|---------------------|
| Acoustics Module |
| COMSOL Multiphysics |



Pressure Acoustics, Frequency Domain

SELECTION

| | |
|------------------------|--|
| Geometric entity level | Domain |
| Selection | Geometry geom1: Dimension 2: All domains |

EQUATIONS

$$\nabla \cdot \left(-\frac{1}{\rho_c} (\nabla p_t - \mathbf{q}_d) \right) - \frac{k_{eq}^2 p_t}{\rho_c} = Q_m$$

$$p_t = p + p_b$$

$$k_{eq}^2 = \left(\frac{\omega}{c_c} \right)^2 - k_z^2$$

2.4.1 Interface Settings

Physics Symbols

SETTINGS

| Description | Value |
|------------------------|-------|
| Enable physics symbols | On |

Discretization

SETTINGS

| Description | Value |
|---------------|--------------------|
| Element order | Quadratic Lagrange |

Physics-Controlled Mesh

SETTINGS

| Description | Value |
|---|------------|
| Maximum mesh element size control parameter | From study |
| Number of mesh elements per wavelength | Automatic |

Pressure Acoustics Equation Settings

SETTINGS

| Description | Value | Unit |
|--------------------------|-------|-------|
| Out-of-plane wave number | 0 | rad/m |

Global Port Settings

SETTINGS

| Description | Value |
|--------------------------|-------------------------|
| Port sweep settings | No port sweep |
| Mode shape normalization | Amplitude normalization |

Sound Pressure Level Settings

SETTINGS

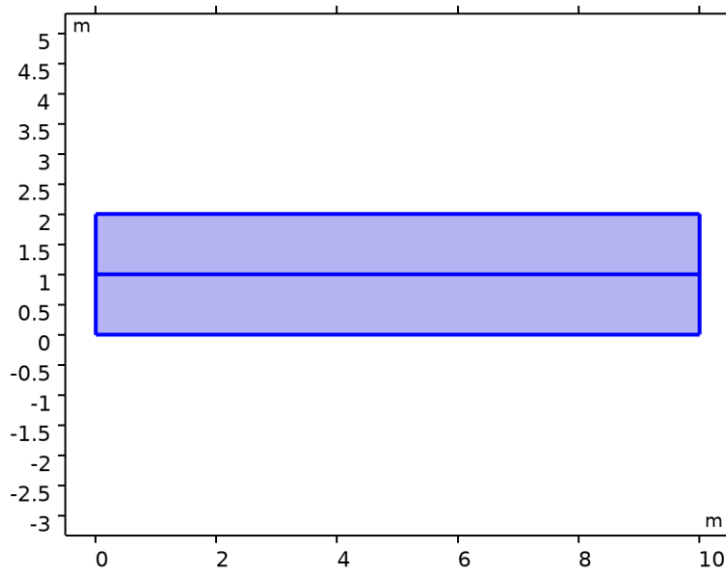
| Description | Value |
|---|--------------------------------|
| Reference pressure for the sound pressure level | Use reference pressure for air |

Typical Wave Speed for Perfectly Matched Layers

SETTINGS

| Description | Value | Unit |
|---|----------------|------|
| Typical wave speed for perfectly matched layers | real(acpr.c_c) | m/s |

2.4.2 Pressure Acoustics 1



Pressure Acoustics 1

SELECTION

| | |
|------------------------|--|
| Geometric entity level | Domain |
| Selection | Geometry geom1: Dimension 2: All domains |

EQUATIONS

$$\nabla \cdot \left(-\frac{1}{\rho_c} (\nabla p_t - \mathbf{q}_d) \right) - \frac{k_{eq}^2 p_t}{\rho_c} = Q_m$$

$$p_t = p + p_b$$

$$k_{eq}^2 = \left(\frac{\omega}{c_c} \right)^2 - k_z^2$$

$$c_c = c, \quad \rho_c = \rho$$

Pressure Acoustics Model

SETTINGS

| Description | Value |
|----------------|----------------------------|
| Fluid model | Linear elastic |
| Specify | Density and speed of sound |
| Speed of sound | From material |
| Density | From material |

Model Input

SETTINGS

| Description | Value |
|-------------------|--------------------|
| Temperature | Common model input |
| Absolute pressure | Common model input |

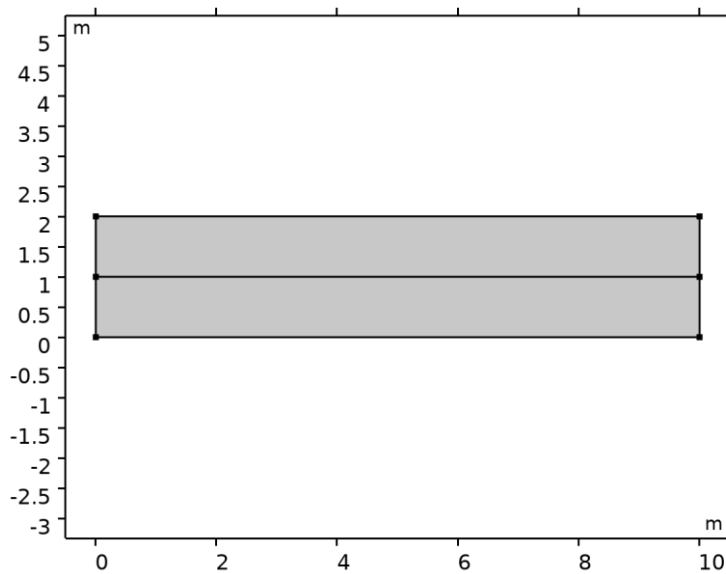
USED PRODUCTS

COMSOL Multiphysics

PROPERTIES FROM MATERIAL

| Property | Material | Property group |
|----------------|-------------|----------------|
| Density | seawater | Basic |
| Speed of sound | seawater | Basic |
| Density | quartz sand | Basic |
| Speed of sound | quartz sand | Basic |

2.4.3 Sound Hard Boundary (Wall) 1



Sound Hard Boundary (Wall) 1

SELECTION

| | |
|------------------------|---|
| Geometric entity level | Boundary |
| Selection | Geometry geom1: Dimension 1: All boundaries |

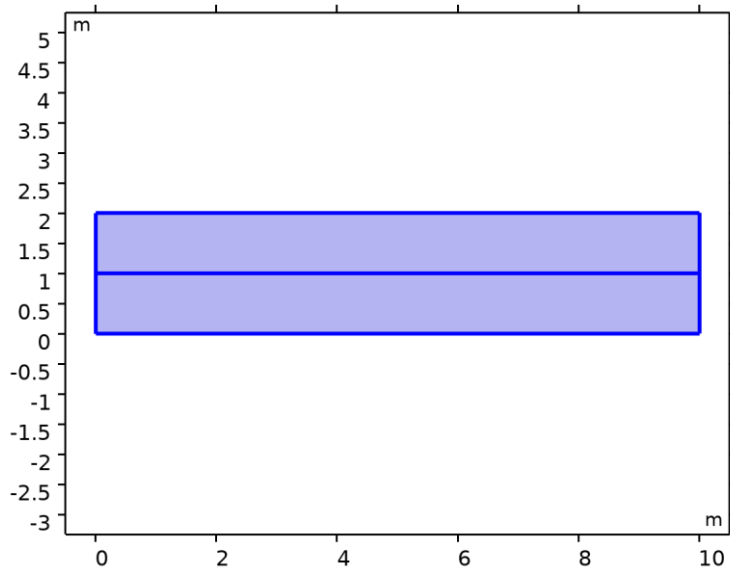
EQUATIONS

$$-\mathbf{n} \cdot \left(-\frac{1}{\rho_c} (\nabla p_t - \mathbf{q}_d) \right) = 0$$

USED PRODUCTS

COMSOL Multiphysics

2.4.4 Initial Values 1



Initial Values 1

SELECTION

| | |
|------------------------|--|
| Geometric entity level | Domain |
| Selection | Geometry geom1: Dimension 2: All domains |

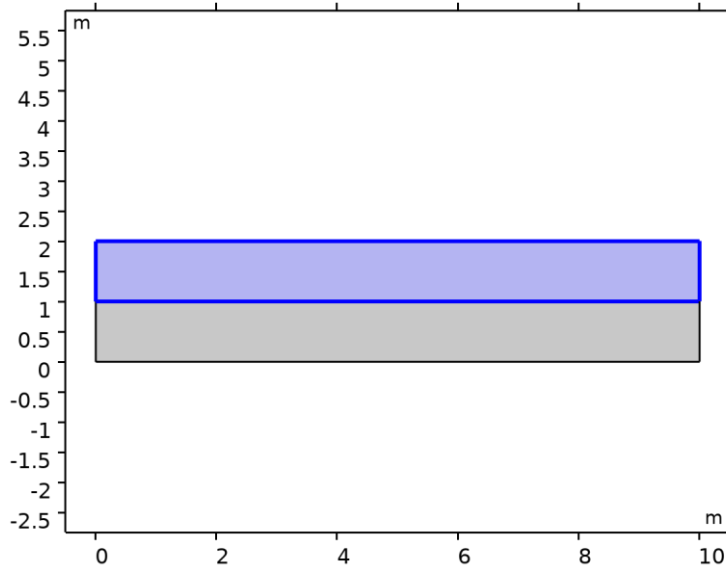
SETTINGS

| Description | Value | Unit |
|-------------------|-------|------|
| Acoustic pressure | 0 | Pa |

USED PRODUCTS

| |
|---------------------|
| COMSOL Multiphysics |
|---------------------|

2.4.5 Background Pressure Field 1



Background Pressure Field 1

SELECTION

| | |
|------------------------|---------------------------------------|
| Geometric entity level | Domain |
| Selection | Geometry geom1: Dimension 2: Domain 2 |

EQUATIONS

$$\nabla \cdot \left(-\frac{1}{\rho_c} (\nabla p_t - \mathbf{q}_d) \right) - \frac{k_{eq}^2 p_t}{\rho_c} = Q_m$$

$$p_t = p + p_b$$

$$k_{eq}^2 = \left(\frac{\omega}{c_c} \right)^2 - k_z^2$$

$$p_b = p_0 e^{i\phi} e^{-ik_s \frac{(\mathbf{x} \cdot \mathbf{e}_k)}{|\mathbf{e}_k|}}$$

$$k_s^2 = \left(\frac{\omega}{c} \right)^2 - k_z^2$$

$$\mathbf{v}_b = -\frac{\nabla p_b}{i\omega\rho}$$

Background Pressure Field

SETTINGS

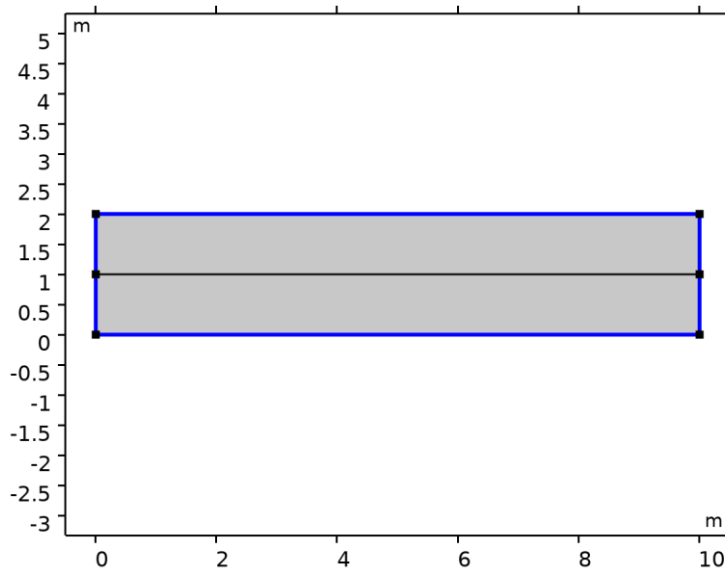
| Description | Value | Unit |
|---------------------|---------------|------|
| Pressure field type | Plane wave | |
| Pressure amplitude | p_input | Pa |
| Speed of sound | From material | |

| Description | Value | Unit |
|--|-----------------|------|
| Wave direction, x-component | sin(theta_i) | |
| Wave direction, y-component | -cos(theta_i) | |
| Wave direction, z-component | 0 | |
| Phase | 0 | rad |
| Calculate background and scattered field intensity | On | |
| Density | From material | |
| Material | Domain material | |

PROPERTIES FROM MATERIAL

| Property | Material | Property group |
|----------------|----------|----------------|
| Speed of sound | seawater | Basic |
| Density | seawater | Basic |

2.4.6 Plane Wave Radiation 1



Plane Wave Radiation 1

SELECTION

| | |
|------------------------|--|
| Geometric entity level | Boundary |
| Selection | Geometry geom1: Dimension 1: Boundaries 1–3, 5–7 |

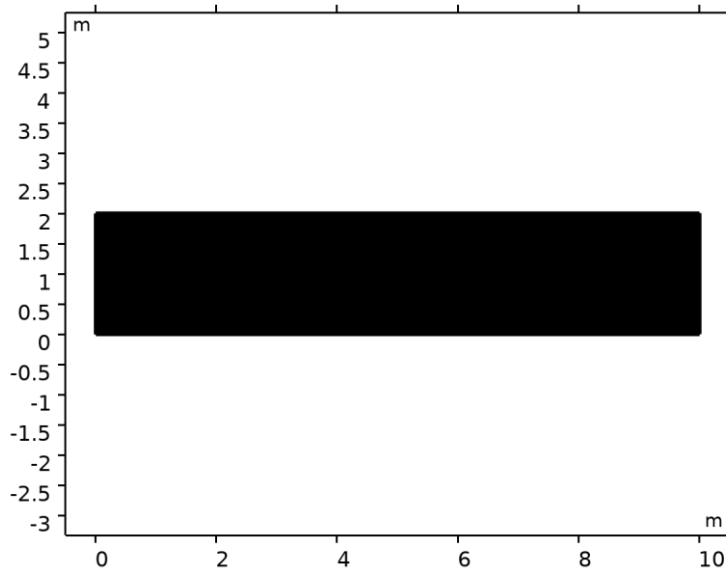
EQUATIONS

$$-\mathbf{n} \cdot \left(-\frac{1}{\rho_c} (\nabla p_t - \mathbf{q}_d) \right) + i \frac{k_{eq}}{\rho_c} p + \frac{i}{2k_{eq}\rho_c} \Delta_{||} p = Q_i$$

.....

USED PRODUCTS

2.5 MESH 1



Mesh 1

2.5.1 Size (size)

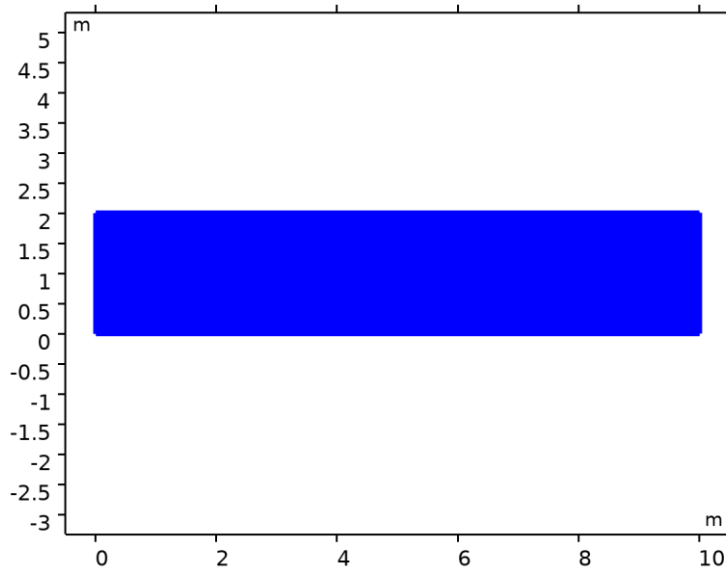
SETTINGS

| Description | Value |
|-----------------------------|------------|
| Maximum element size | 0.2 |
| Minimum element size | 1E-4 |
| Curvature factor | 0.25 |
| Maximum element growth rate | 1.2 |
| Predefined size | Extra fine |
| Custom element size | Custom |

2.5.2 Size Expression 1 (se1)

SELECTION

| | |
|------------------------|--|
| Geometric entity level | Domain |
| Selection | Geometry geom1: Dimension 2: Domains 1–2 |



Size Expression 1

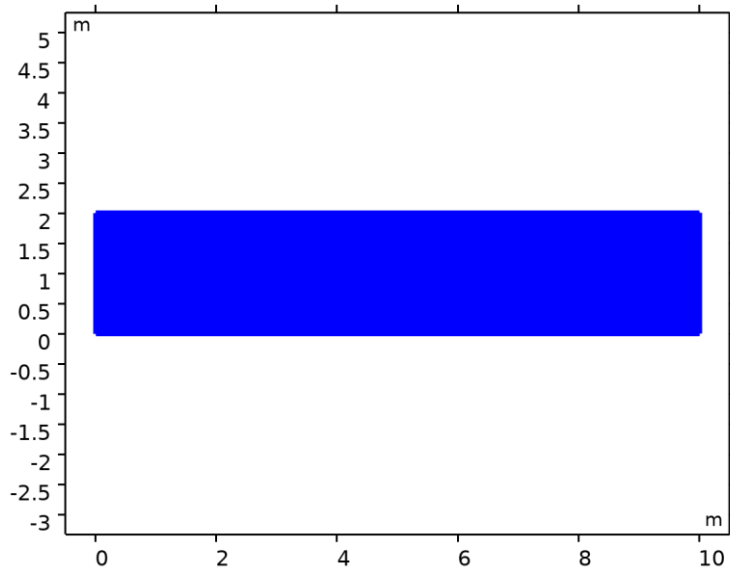
SETTINGS

| Description | Value |
|-------------------------------|--|
| Evaluate on | Initial expression |
| Study step | Study 1: Frequency Domain |
| Size expression | <code>subst(real(acpr.c_c), acpr.freq, freqmax)/freqmax/5</code> |
| Reevaluate with updated model | |

2.5.3 Free Triangular 1 (ftri1)

SELECTION

| | |
|------------------------|-----------|
| Geometric entity level | Domain |
| Selection | Remaining |



Free Triangular 1

SETTINGS

| Description | Value |
|----------------------------------|-------|
| Number of iterations | 4 |
| Maximum element depth to process | 4 |

INFORMATION

| Description | Value |
|-----------------|--|
| Last build time | < 1 second |
| Built with | COMSOL 6.3.0.420 (win64), Nov 17, 2025, 8:52:46 PM |

3 Study 1

COMPUTATION INFORMATION

| | |
|------------------|-----|
| Computation time | 1 s |
|------------------|-----|

3.1 FREQUENCY DOMAIN

Frequencies (Hz)

f_study

STUDY SETTINGS

| Description | Value |
|--------------------------------|-------|
| Include geometric nonlinearity | Off |

SETTINGS

| Description | Value |
|-------------|-------|
| Frequencies | 10000 |

PHYSICS AND VARIABLES SELECTION

| Key | Solve for |
|---|-----------|
| Pressure Acoustics, Frequency Domain (acpr) | On |

STORE IN OUTPUT

| Interface | Output | Selection |
|---|--------------------|-----------|
| Pressure Acoustics, Frequency Domain (acpr) | Physics controlled | |

MESH SELECTION

| Component | Mesh |
|-------------|--------|
| Component 1 | Mesh 1 |

3.2 SOLVER CONFIGURATIONS

3.2.1 Solution 1

Compile Equations: Frequency Domain (st1)

STUDY AND STEP

| Description | Value |
|----------------|-------------------------|
| Use study | Study 1 |
| Use study step | Frequency Domain |

Dependent Variables 1 (v1)

GENERAL

| Description | Value |
|-----------------------|--|
| Defined by study step | Step 1: Frequency Domain |

INITIAL VALUE CALCULATION CONSTANTS

| Constant name | Initial-value source |
|---------------|----------------------|
| freq | f_study |

Acoustic Pressure (comp1.p) (comp1_p)

GENERAL

| Description | Value |
|------------------|---------|
| Field components | comp1.p |

Stationary Solver 1 (s1)

GENERAL

| Description | Value |
|-----------------------|--|
| Defined by study step | Step 1: Frequency Domain |

RESULTS WHILE SOLVING

| Description | Value |
|-------------|-------|
| Probes | None |

Advanced (aDef)

ASSEMBLY SETTINGS

| Description | Value |
|--|-------|
| Reuse sparsity pattern | On |
| Allow complex-valued output from functions with real input | On |

Parametric 1 (p1)

GENERAL

| Description | Value |
|-----------------------|--|
| Defined by study step | Step 1: Frequency Domain |
| Run continuation for | No parameter |

PARAMETERS

| Parameter name | Parameter value list | Parameter unit |
|----------------|----------------------|----------------|
| freq | f_study | Hz |

Fully Coupled 1 (fc1)

GENERAL

| Description | Value |
|-------------|-------|
|-------------|-------|

| Description | Value |
|---------------|------------------------|
| Linear solver | Direct |

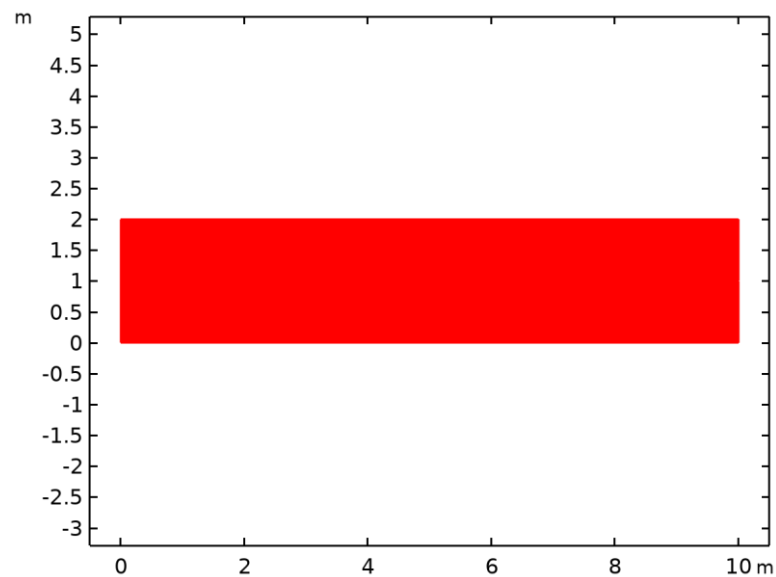
4 Results

4.1 DATASETS

4.1.1 Study 1/Solution 1

SOLUTION

| Description | Value |
|-------------|-----------------------------------|
| Solution | Solution 1 (sol1) |
| Component | Component 1 (comp1) |



Dataset: Study 1/Solution 1

4.1.2 Cut Line 2D 1

DATA

| Description | Value |
|-------------|---|
| Dataset | Study 1/Solution 1 (sol1) |

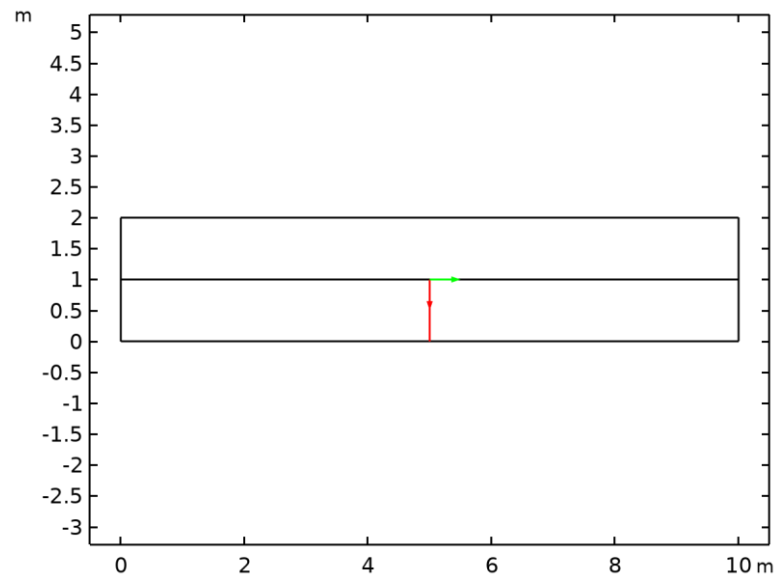
LINE DATA

| Description | Value |
|-------------------|-------------------------------------|
| Line entry method | Two points |
| Points | {{length/2, height}, {length/2, 0}} |

ADVANCED

| Description | Value |
|----------------|-------|
| Space variable | cln1x |

| Description | Value |
|-------------------|------------------|
| Normal variables | {cln1nx, cln1ny} |
| Tangent variables | {cln1tx, cln1ty} |



Dataset: Cut Line 2D 1

4.1.3 Cut Line 2D 2

DATA

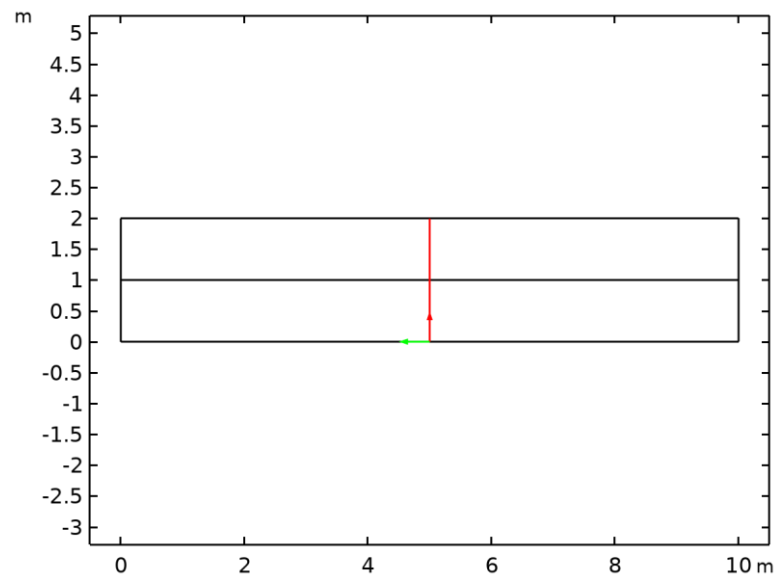
| Description | Value |
|-------------|---|
| Dataset | Study 1/Solution 1 (sol1) |

LINE DATA

| Description | Value |
|-------------------|------------------|
| Line entry method | Two points |
| Points | {{5, 0}, {5, 2}} |

ADVANCED

| Description | Value |
|-------------------|------------------|
| Space variable | cln2x |
| Normal variables | {cln2nx, cln2ny} |
| Tangent variables | {cln2tx, cln2ty} |



Dataset: Cut Line 2D 2

4.2 TABLES

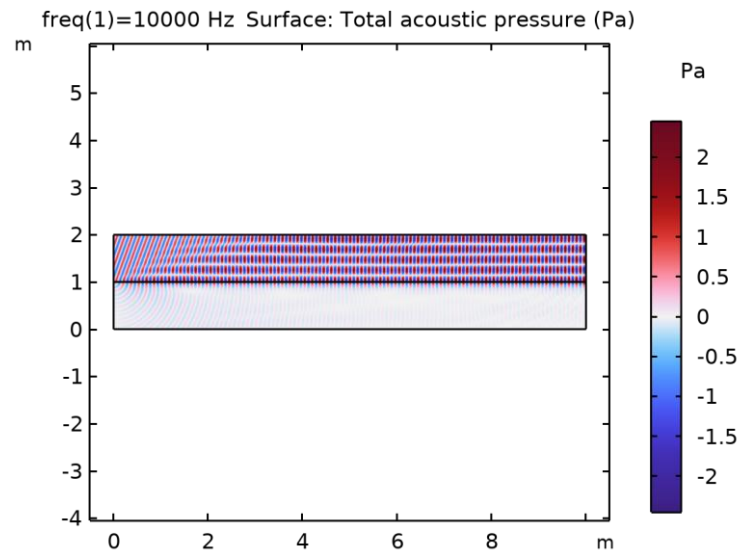
4.2.1 Evaluation 2D

Interactive 2D values

| x | y | Value |
|--------|---------|------------|
| 4.9514 | 0.19459 | -0.0025911 |
| 3.6091 | 0.26523 | 0.012694 |

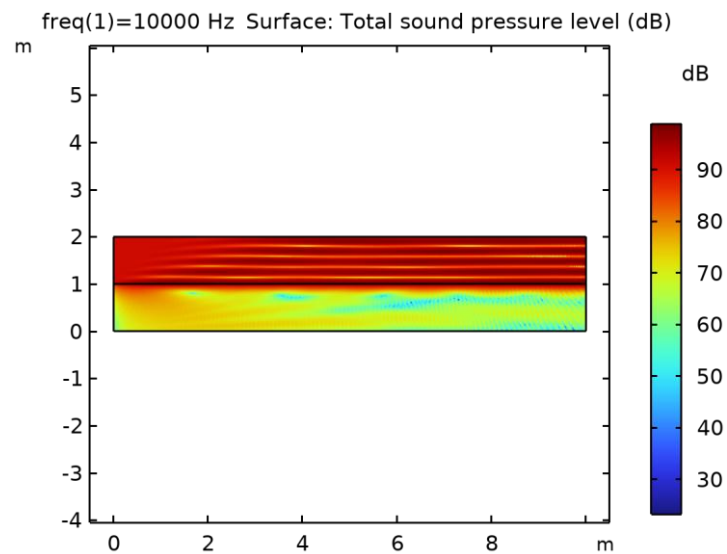
4.3 PLOT GROUPS

4.3.1 Acoustic Pressure (acpr)



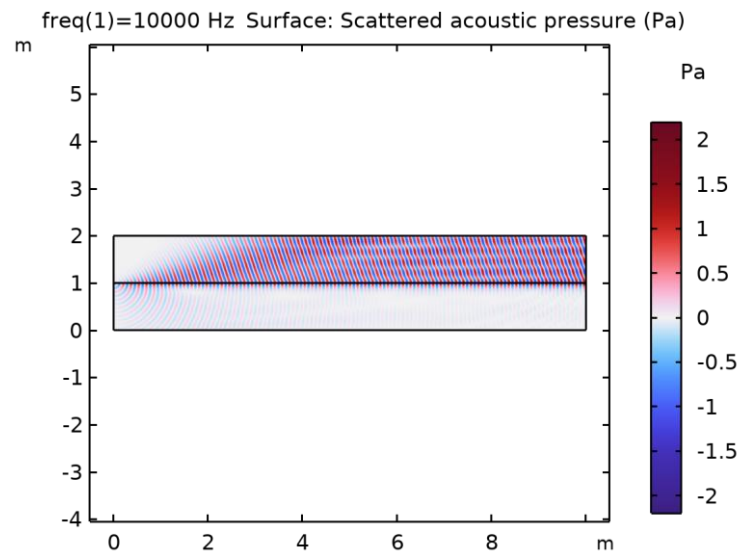
Surface: Total acoustic pressure (Pa)

4.3.2 Sound Pressure Level (acpr)



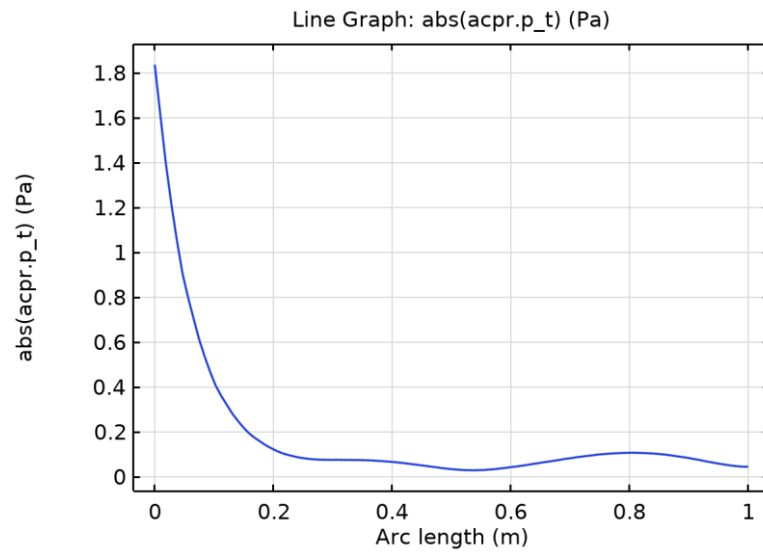
Surface: Total sound pressure level (dB)

4.3.3 Acoustic Pressure (acpr) 1



Surface: Scattered acoustic pressure (Pa)

4.3.4 1D Plot Group 4



Line Graph: abs(acpr.p_t) (Pa)

Hw5.3

| | |
|-------------|--------------------------|
| Report date | Nov 16, 2025, 1:21:15 PM |
|-------------|--------------------------|

Contents

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| 1. Global Definitions..... | 3 |
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1 Global Definitions

| | |
|------|--------------------------|
| Date | Nov 16, 2025, 1:20:39 PM |
|------|--------------------------|

GLOBAL SETTINGS

| | |
|---------|--|
| Name | Hw5.3.mph |
| Path | \\clusterfsnew.ceas1.uc.edu\students\brooksl\desktop\hw5.3.mph |
| Version | COMSOL Multiphysics 6.3 (Build: 420) |

USED PRODUCTS

| |
|---------------------|
| COMSOL Multiphysics |
| Acoustics Module |

COMPUTER INFORMATION

| | |
|------------------|---|
| CPU | Intel64 Family 6 Model 198 Stepping 2, 28 cores, 63.46 GB RAM |
| Operating system | Windows 11 |

1.1 PARAMETERS

PARAMETERS 1

| Name | Expression | Value | Description |
|--------|------------|--------|-------------|
| width | 2[cm] | 0.02 m | |
| height | 1[cm] | 0.01 m | |

2 Component 1

SETTINGS

| Description | Value |
|-------------|----------------------------|
| Unit system | Same as global system (SI) |

2.1 DEFINITIONS

2.1.1 Coordinate Systems

Boundary System 1

| | |
|------------------------|-----------------|
| Coordinate system type | Boundary system |
| Tag | sys1 |

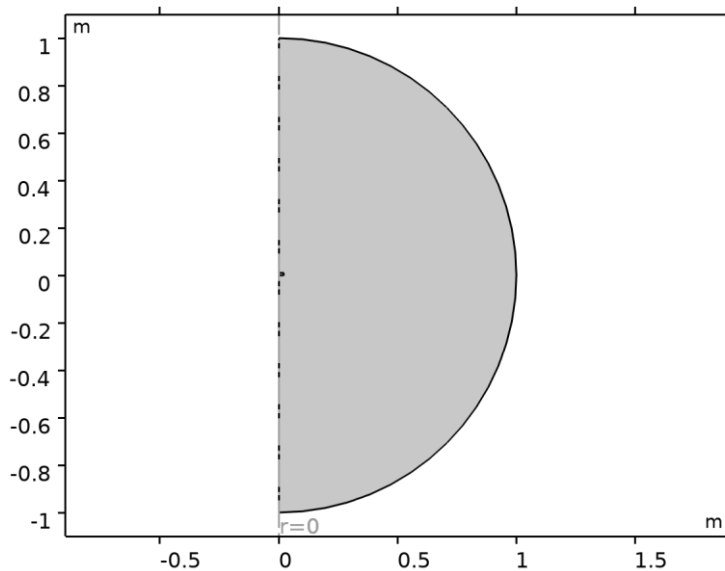
COORDINATE NAMES

| First | Second | Third |
|-------|--------|-------|
| t1 | to | n |

SETTINGS

| Description | Value |
|-------------|-------|
| Axis | phi |

2.2 GEOMETRY 1



Geometry 1

UNITS

| | |
|-------------|---|
| Length unit | m |
|-------------|---|

| | |
|--------------|-----|
| Angular unit | deg |
|--------------|-----|

GEOMETRY STATISTICS

| Description | Value |
|----------------------|-------|
| Space dimension | 2 |
| Number of domains | 1 |
| Number of boundaries | 7 |
| Number of vertices | 7 |

2.2.1 Rectangle 1 (r1)

SIZE AND SHAPE

| Description | Value |
|-------------|--------|
| Width | width |
| Height | height |

POSITION

| Description | Value |
|-------------|--------|
| Position | {0, 0} |

2.2.2 Circle 1 (c1)

SIZE AND SHAPE

| Description | Value |
|-------------|-------|
| Radius | 1 |

POSITION

| Description | Value |
|-------------|--------|
| Position | {0, 0} |

2.2.3 Difference 1 (dif1)

INPUT OBJECTS

| Description | Value |
|---------------------|-----------------------------------|
| Objects to add | geom1, Geometry geom1: Object: c1 |
| Objects to subtract | geom1, Geometry geom1: Object: r1 |

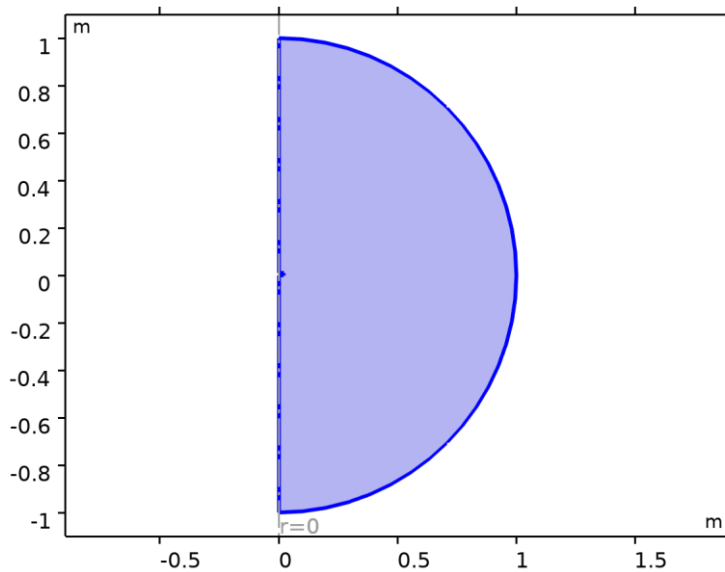
2.2.4 Form Union (fin)

INFORMATION

| Description | Value |
|---------------|---|
| Build message | Formed union of 1 solid object. Union has 1 domain, 7 boundaries, and 7 vertices. |

2.3 MATERIALS

2.3.1 air



air

SELECTION

| | |
|------------------------|--|
| Geometric entity level | Domain |
| Selection | Geometry geom1: Dimension 2: All domains |

MATERIAL PARAMETERS

| Name | Value | Unit | Property group |
|----------------|-------|-------------------|----------------|
| Density | 1.15 | kg/m ³ | Basic |
| Speed of sound | 343 | m/s | Basic |

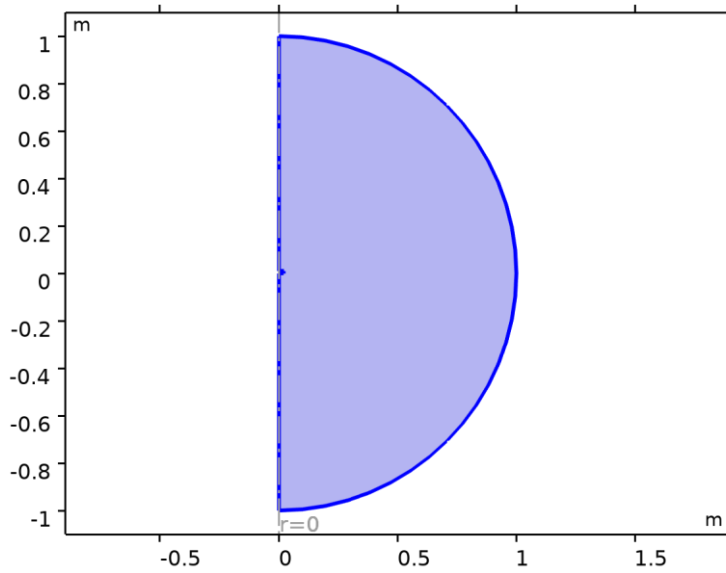
BASIC

| Description | Value | Unit |
|----------------|-------|-------------------|
| Density | 1.15 | kg/m ³ |
| Speed of sound | 343 | m/s |

2.4 PRESSURE ACOUSTICS, FREQUENCY DOMAIN

USED PRODUCTS

| |
|---------------------|
| COMSOL Multiphysics |
| Acoustics Module |



Pressure Acoustics, Frequency Domain

SELECTION

| | |
|------------------------|--|
| Geometric entity level | Domain |
| Selection | Geometry geom1: Dimension 2: All domains |

EQUATIONS

$$\nabla \cdot \left(-\frac{1}{\rho_c} (\nabla p_t - \mathbf{q}_d) \right) - \frac{k_{eq}^2 p_t}{\rho_c} = Q_m$$

$$p_t = p + p_b$$

$$k_{eq}^2 = \left(\frac{\omega}{c_c} \right)^2 - k_m^2$$

2.4.1 Interface Settings

Physics Symbols

SETTINGS

| Description | Value |
|------------------------|-------|
| Enable physics symbols | On |

Discretization

SETTINGS

| Description | Value |
|---------------|--------------------|
| Element order | Quadratic Lagrange |

Physics-Controlled Mesh

SETTINGS

| Description | Value |
|---|------------|
| Maximum mesh element size control parameter | From study |
| Number of mesh elements per wavelength | Automatic |

Pressure Acoustics Equation Settings

SETTINGS

| Description | Value |
|-----------------------|-------|
| Azimuthal mode number | 0 |

Global Port Settings

SETTINGS

| Description | Value |
|--------------------------|-------------------------|
| Port sweep settings | No port sweep |
| Mode shape normalization | Amplitude normalization |

Sound Pressure Level Settings

SETTINGS

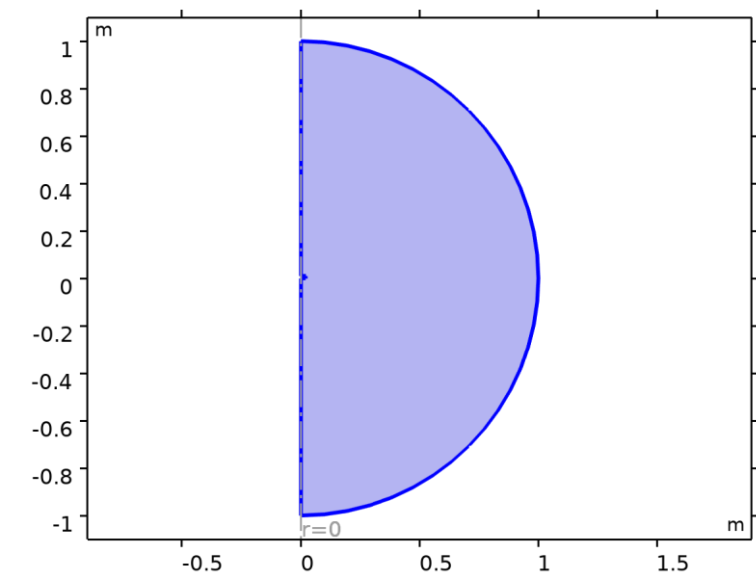
| Description | Value |
|---|--------------------------------|
| Reference pressure for the sound pressure level | Use reference pressure for air |

Typical Wave Speed for Perfectly Matched Layers

SETTINGS

| Description | Value | Unit |
|---|----------------|------|
| Typical wave speed for perfectly matched layers | real(acpr.c_c) | m/s |

2.4.2 Pressure Acoustics 1



Pressure Acoustics 1

SELECTION

| | |
|------------------------|--|
| Geometric entity level | Domain |
| Selection | Geometry geom1: Dimension 2: All domains |

EQUATIONS

$$\nabla \cdot \left(-\frac{1}{\rho_c} (\nabla p_t - \mathbf{q}_d) \right) - \frac{k_{eq}^2 p_t}{\rho_c} = Q_m$$

.....

$$p_t = p + p_b$$
$$k_{eq}^2 = \left(\frac{\omega}{c_c} \right)^2 - k_m^2$$
$$c_c = c, \quad \rho_c = \rho$$

Pressure Acoustics Model

SETTINGS

| Description | Value |
|----------------|----------------------------|
| Fluid model | Linear elastic |
| Specify | Density and speed of sound |
| Speed of sound | From material |
| Density | From material |

Model Input

SETTINGS

| Description | Value | Unit |
|-------------------|--------------|------|
| Temperature | User defined | |
| Temperature | 293.15 | K |
| Absolute pressure | User defined | |
| Absolute pressure | 1.0133E5 | Pa |

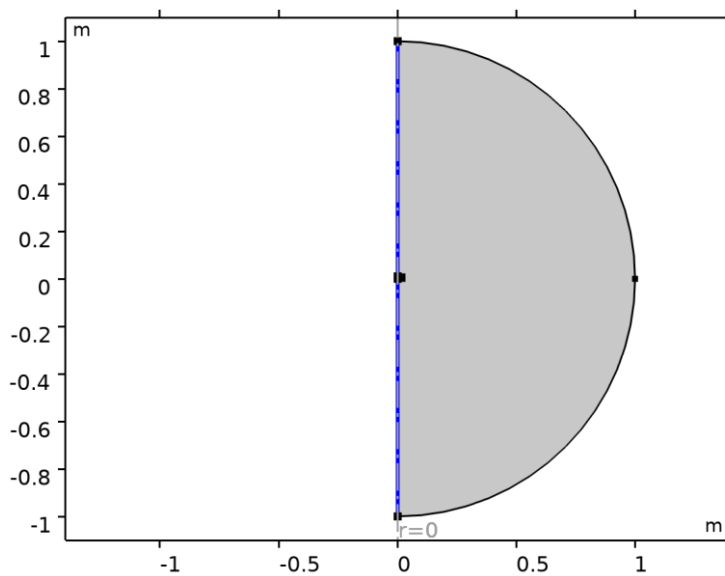
USED PRODUCTS

COMSOL Multiphysics

PROPERTIES FROM MATERIAL

| Property | Material | Property group |
|----------------|----------|----------------|
| Density | air | Basic |
| Speed of sound | air | Basic |

2.4.3 Axial Symmetry 1



Axial Symmetry 1

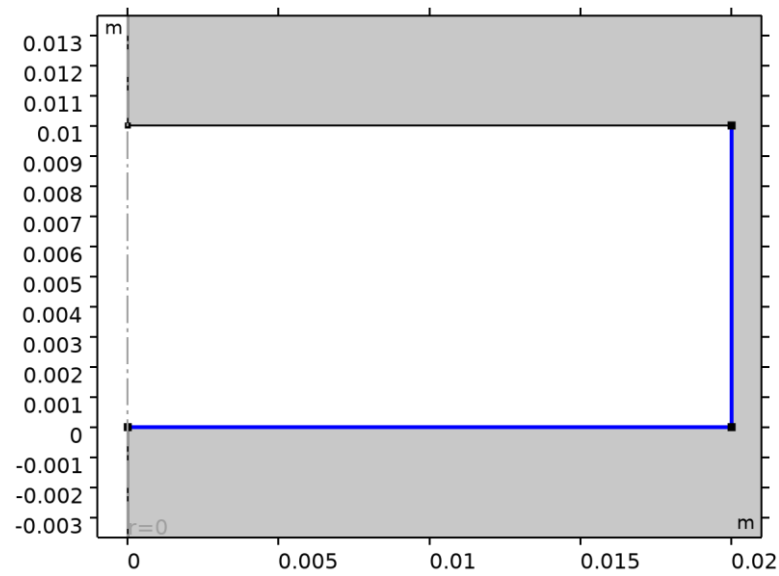
SELECTION

| | |
|------------------------|---|
| Geometric entity level | Boundary |
| Selection | Geometry geom1: Dimension 1: All boundaries |

USED PRODUCTS

COMSOL Multiphysics

2.4.4 Sound Hard Boundary (Wall) 1



Sound Hard Boundary (Wall) 1

SELECTION

| | |
|------------------------|---|
| Geometric entity level | Boundary |
| Selection | Geometry geom1: Dimension 1: All boundaries |

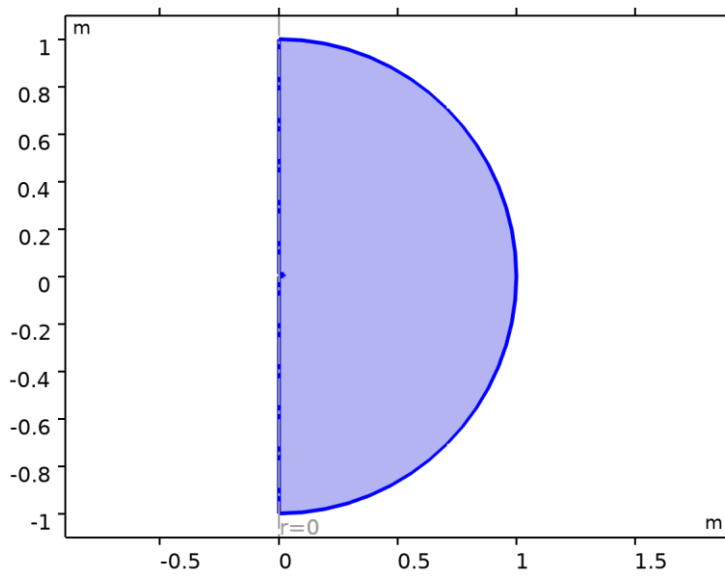
EQUATIONS

$$-\mathbf{n} \cdot \left(-\frac{1}{\rho_c} (\nabla p_t - \mathbf{q}_d) \right) = 0$$

USED PRODUCTS

COMSOL Multiphysics

2.4.5 Initial Values 1



Initial Values 1

SELECTION

| | |
|------------------------|--|
| Geometric entity level | Domain |
| Selection | Geometry geom1: Dimension 2: All domains |

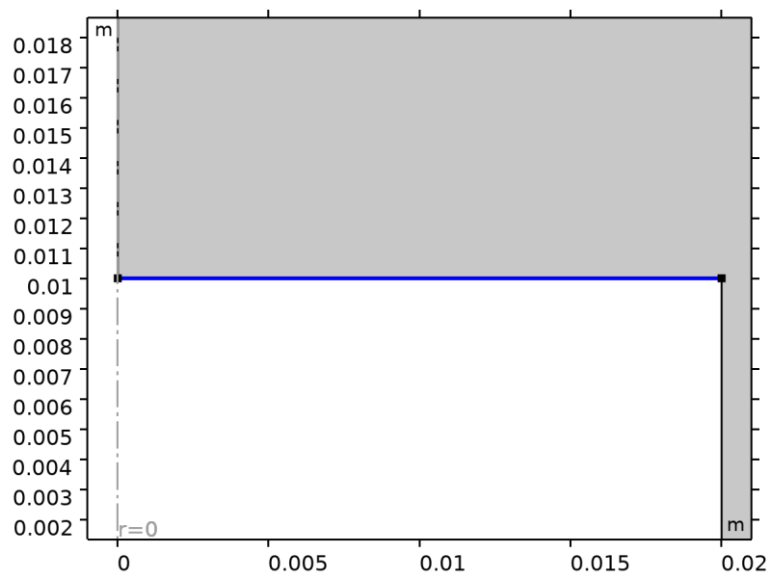
SETTINGS

| Description | Value | Unit |
|-------------------|-------|------|
| Acoustic pressure | 0 | Pa |

USED PRODUCTS

| |
|---------------------|
| COMSOL Multiphysics |
|---------------------|

2.4.6 Normal Velocity 1



Normal Velocity 1

SELECTION

| | |
|------------------------|---|
| Geometric entity level | Boundary |
| Selection | Geometry geom1: Dimension 1: Boundary 4 |

EQUATIONS

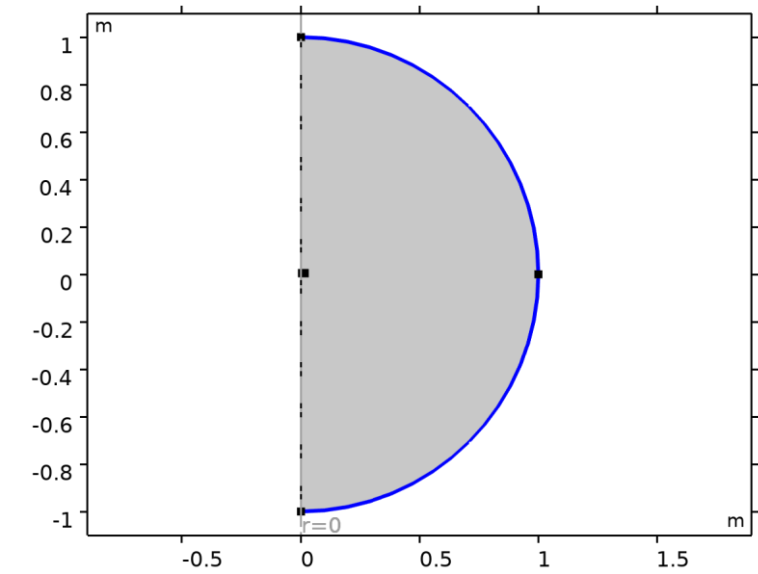
$$-\mathbf{n} \cdot \left(-\frac{1}{\rho_c} (\nabla p_t - \mathbf{q}_d) \right) = i \omega \mathcal{V}_n$$

Normal Velocity

SETTINGS

| Description | Value | Unit |
|-----------------|-----------------|------|
| Type | Inward velocity | |
| Inward velocity | 0.01 | m/s |

2.4.7 Spherical Wave Radiation 1



Spherical Wave Radiation 1

SELECTION

| | |
|------------------------|---|
| Geometric entity level | Boundary |
| Selection | Geometry geom1: Dimension 1: Boundaries 6–7 |

EQUATIONS

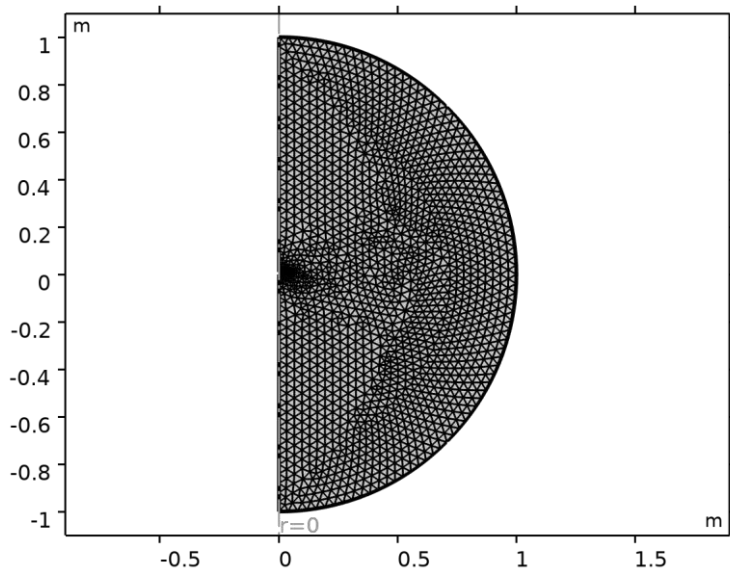
$$-\mathbf{n}\cdot\left(-\frac{1}{\rho_c}(\nabla p_t-\mathbf{q}_d)\right)+\underbrace{\left(ik_{eq}+\frac{1}{r_{rf}}\right)\frac{p}{\rho_c}}_{\text{}}-\frac{r_{rf}\Delta_{||}p}{2\rho_c(1+ik_{eq}r_{rf})}=Q_i$$

$$r_{rf}=|\mathbf{x}-\mathbf{r}_0|$$

USED PRODUCTS

| |
|---------------------|
| COMSOL Multiphysics |
|---------------------|

2.5 MESH 1



Mesh 1

2.5.1 Size (size)

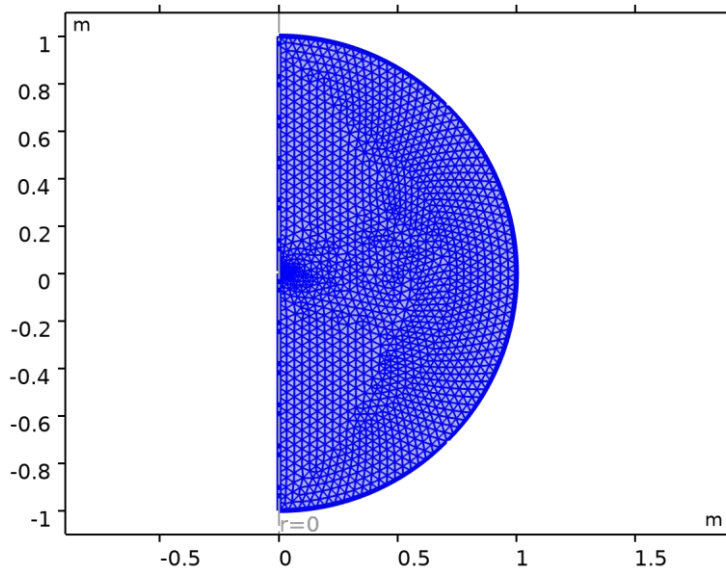
SETTINGS

| Description | Value |
|-----------------------------|------------|
| Maximum element size | 0.04 |
| Minimum element size | 2E-5 |
| Curvature factor | 0.25 |
| Maximum element growth rate | 1.2 |
| Predefined size | Extra fine |
| Custom element size | Custom |

2.5.2 Size Expression 1 (se1)

SELECTION

| | |
|------------------------|---------------------------------------|
| Geometric entity level | Domain |
| Selection | Geometry geom1: Dimension 2: Domain 1 |



Size Expression 1

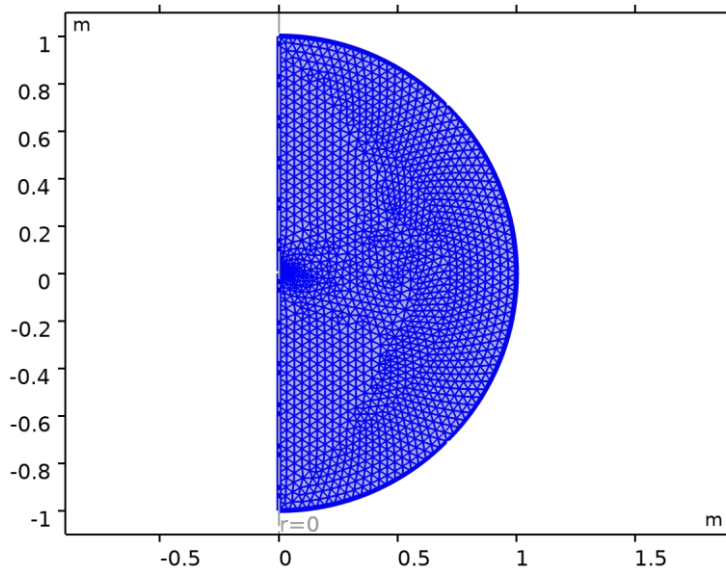
SETTINGS

| Description | Value |
|-------------------------------|--|
| Evaluate on | Initial expression |
| Study step | Study 1: Frequency Domain |
| Size expression | <code>subst(real(acpr.c_c), acpr.freq, freqmax)/freqmax/5</code> |
| Reevaluate with updated model | |

2.5.3 Free Triangular 1 (ftri1)

SELECTION

| | |
|------------------------|-----------|
| Geometric entity level | Domain |
| Selection | Remaining |



Free Triangular 1

SETTINGS

| Description | Value |
|----------------------------------|-------|
| Number of iterations | 4 |
| Maximum element depth to process | 4 |

INFORMATION

| Description | Value |
|-----------------|---|
| Last build time | < 1 second |
| Built with | COMSOL 6.3.0.420 (win64), Nov 16, 2025, 12:16:42 PM |

3 Study 1

COMPUTATION INFORMATION

| | |
|------------------|-----|
| Computation time | 1 s |
|------------------|-----|

3.1 FREQUENCY DOMAIN

| Frequencies (Hz) |
|------------------|
| 1000 |

STUDY SETTINGS

| Description | Value |
|--------------------------------|-------|
| Include geometric nonlinearity | Off |

SETTINGS

| Description | Value |
|-------------|-------|
| Frequencies | 1000 |

PHYSICS AND VARIABLES SELECTION

| Key | Solve for |
|---|-----------|
| Pressure Acoustics, Frequency Domain (acpr) | On |

STORE IN OUTPUT

| Interface | Output | Selection |
|---|--------------------|-----------|
| Pressure Acoustics, Frequency Domain (acpr) | Physics controlled | |

MESH SELECTION

| Component | Mesh |
|-------------|--------|
| Component 1 | Mesh 1 |

3.2 SOLVER CONFIGURATIONS

3.2.1 Solution 1

Compile Equations: Frequency Domain (st1)

STUDY AND STEP

| Description | Value |
|----------------|-------------------------|
| Use study | Study 1 |
| Use study step | Frequency Domain |

Dependent Variables 1 (v1)

GENERAL

| Description | Value |
|-----------------------|--|
| Defined by study step | Step 1: Frequency Domain |

INITIAL VALUE CALCULATION CONSTANTS

| Constant name | Initial-value source |
|---------------|----------------------|
| freq | 1000[Hz] |

Acoustic Pressure (comp1.p) (comp1_p)

GENERAL

| Description | Value |
|------------------|---------|
| Field components | comp1.p |

Stationary Solver 1 (s1)

GENERAL

| Description | Value |
|-----------------------|--|
| Defined by study step | Step 1: Frequency Domain |

RESULTS WHILE SOLVING

| Description | Value |
|-------------|-------|
| Probes | None |

Advanced (aDef)

ASSEMBLY SETTINGS

| Description | Value |
|--|-------|
| Reuse sparsity pattern | On |
| Allow complex-valued output from functions with real input | On |

Parametric 1 (p1)

GENERAL

| Description | Value |
|-----------------------|--|
| Defined by study step | Step 1: Frequency Domain |
| Run continuation for | No parameter |

PARAMETERS

| Parameter name | Parameter value list | Parameter unit |
|----------------|----------------------|----------------|
| freq | 1000 | Hz |

Fully Coupled 1 (fc1)

GENERAL

| Description | Value |
|-------------|-------|
|-------------|-------|

| Description | Value |
|---------------|------------------------|
| Linear solver | Direct |

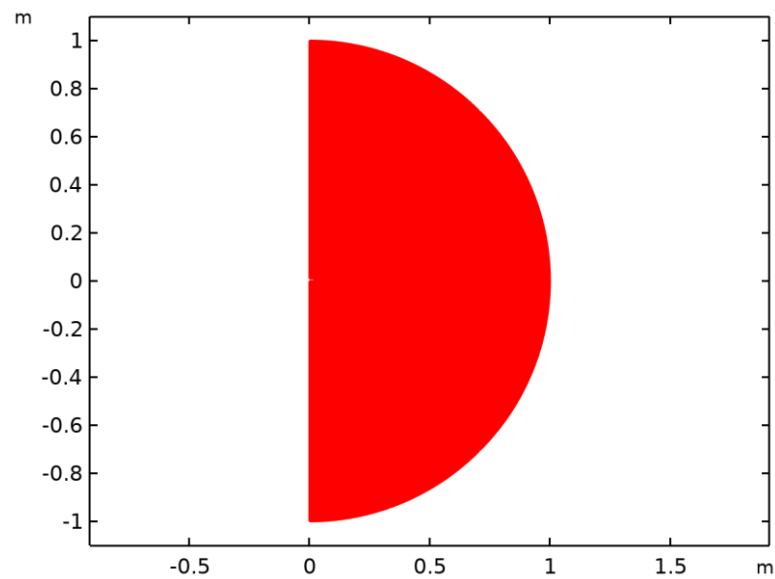
4 Results

4.1 DATASETS

4.1.1 Study 1/Solution 1

SOLUTION

| Description | Value |
|-------------|-----------------------------------|
| Solution | Solution 1 (sol1) |
| Component | Component 1 (comp1) |



Dataset: Study 1/Solution 1

4.1.2 Revolution 2D 1

DATA

| Description | Value |
|-------------|---|
| Dataset | Study 1/Solution 1 (sol1) |

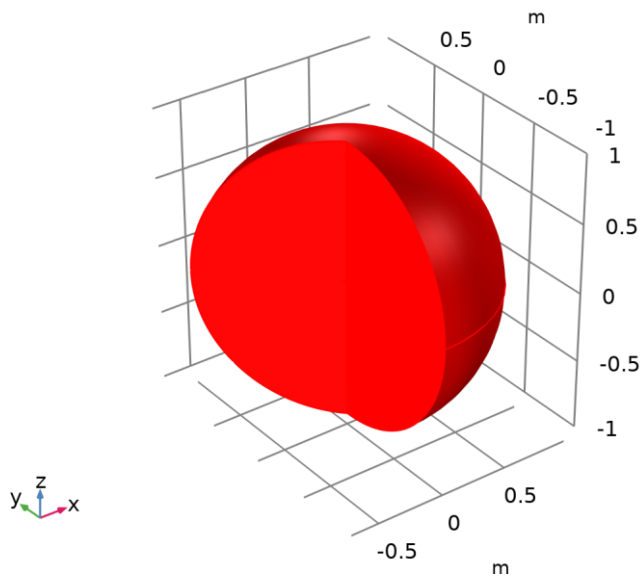
AXIS DATA

| Description | Value |
|-------------------|------------------|
| Axis entry method | Two points |
| Points | {{0, 0}, {0, 1}} |

REVOLUTION LAYERS

| Description | Value |
|-------------|-------|
| Start angle | -90 |

| Description | Value |
|------------------|-------|
| Revolution angle | 225 |



Dataset: Revolution 2D 1

4.2 DERIVED VALUES

4.2.1 Line Integration 1

OUTPUT

Evaluated in [Table 1](#)

DATA

| Description | Value |
|-------------|---|
| Dataset | Study 1/Solution 1 (sol1) |

EXPRESSIONS

| Expression | Unit | Description |
|------------|------|---------------------|
| acpr.l_mag | W | Intensity magnitude |

INTEGRATION SETTINGS

| Description | Value |
|--------------------------|-------|
| Integration order | 4 |
| Compute surface integral | On |

4.3 TABLES

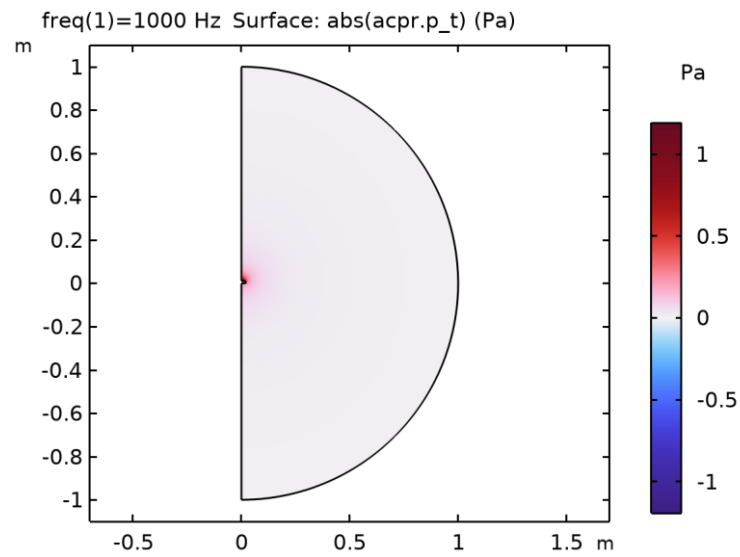
4.3.1 Table 1

Line Integration 1

| freq (Hz) | Intensity magnitude (W) |
|-----------|-------------------------|
| 1000 | 8.2901E-7 |

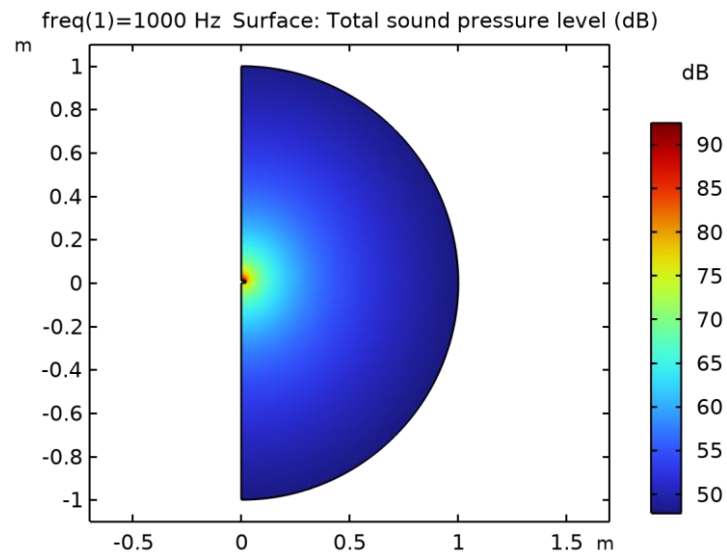
4.4 PLOT GROUPS

4.4.1 Acoustic Pressure (acpr)



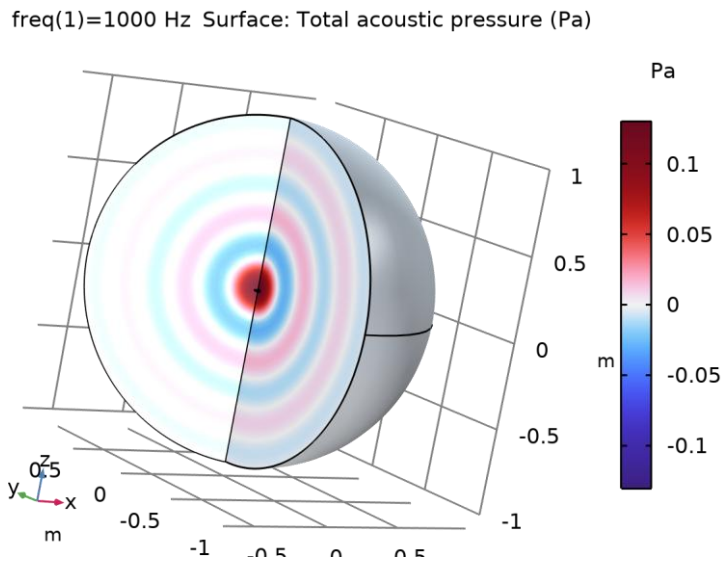
Surface: abs(acpr.p_t) (Pa)

4.4.2 Sound Pressure Level (acpr)



Surface: Total sound pressure level (dB)

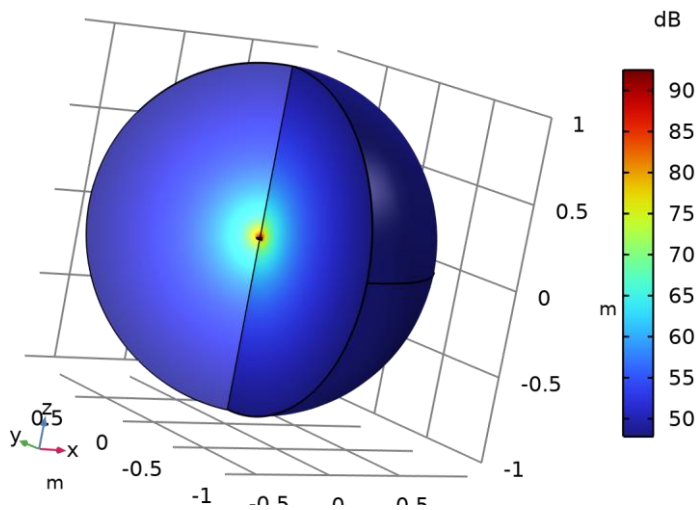
4.4.3 Acoustic Pressure, 3D (acpr)



Surface: Total acoustic pressure (Pa)

4.4.4 Sound Pressure Level, 3D (acpr)

freq(1)=1000 Hz Surface: Total sound pressure level (dB)



Surface: Total sound pressure level (dB)

4.5 EVALUATION GROUPS

4.5.1 Evaluation Group 1

DATA

| Description | Value |
|-------------|---|
| Dataset | Study 1/Solution 1 (sol1) |

FEATURES

| |
|------------------------------------|
| Point Evaluation 1 |
|------------------------------------|

RESULTS

| freq (Hz) | abs(acpr .p_t) (Pa), Point: 1 | abs(acpr .p_t) (Pa), Point: 3 | abs(acpr .p_t) (Pa), Point: 4 | abs(acpr .p_t) (Pa), Point: 7 | Total sound pressure level (dB), Point: 1 | Total sound pressure level (dB), Point: 3 | Total sound pressure level (dB), Point: 4 | Total sound pressure level (dB), Point: 7 |
|-----------|-------------------------------|-------------------------------|-------------------------------|-------------------------------|---|---|---|---|
| 1000 | 0.0071401 | 1.1931 | 0.0074765 | 0.0070062 | 48.043 | 92.502 | 48.443 | 47.879 |

Point Evaluation 1

EXPRESSIONS

| Expression | Unit | Description |
|---------------|------|-------------|
| abs(acpr.p_t) | Pa | |

| Expression | Unit | Description |
|------------|------|----------------------------|
| acpr.Lp_t | dB | Total sound pressure level |