

Feedforward Neural Network with tanh Activation – Version 3

Python Code Example

```
import numpy as np

# ----- tanh Activation Function -----
def tanh(x):
    return np.tanh(x)

# Input values
X = np.array([[0.05], [0.10]])

# Biases
bias1 = 0.5
bias2 = 0.7

# Random Weights initialization in range [-0.5, 0.5]
np.random.seed(100)
W_input_to_hidden = np.random.uniform(-0.5, 0.5, (2, 2))
W_hidden_to_output = np.random.uniform(-0.5, 0.5, (2, 2))

# ----- Forward Pass -----

# Hidden layer computation
hidden_input = np.dot(W_input_to_hidden, X) + bias1
hidden_output = tanh(hidden_input)

# Output layer computation
final_input = np.dot(W_hidden_to_output, hidden_output) + bias2
final_output = tanh(final_input)

print("Hidden Layer Output:\n", hidden_output)
print("Final Network Output:\n", final_output)
```

Feedforward Steps

1 . Hidden Layer Input:

$$Z_h = W_{\text{input_to_hidden}} * X + \text{bias } 1$$

1 . Hidden Layer Activation:

$$H = \tanh(Z_h)$$

1 . Output Layer Input:

$$Z_o = W_{\text{hidden_to_output}} * H + \text{bias}_2$$

1 . Output Activation:

$$\text{Output} = \tanh(Z_o)$$

Sample Output (Random Weights – Values May Vary)

Hidden Layer Output: $\begin{bmatrix} 0.4 & 0.2 \end{bmatrix} \begin{bmatrix} 0.2 & 9.8 \end{bmatrix}$

Final Network Output: $\begin{bmatrix} 0.6 & 1.5 \end{bmatrix} \begin{bmatrix} 0.5 & 7.4 \end{bmatrix}$

Backpropagation Overview

1 Compute Error:

$$\text{Error} = \text{Target} - \text{Output}$$

2 Output Layer Delta:

$$\text{delta}_o = \text{Error} * \tanh'(Z_o)$$

3 Hidden Layer Delta:

$$\text{delta}_h = (W_{\text{hidden_to_output}}^T * \text{delta}_o) * \tanh'(Z_h)$$

4 Weight Update:

$$W_{\text{new}} = W_{\text{old}} + \text{learning_rate} * \text{delta} * \text{input}$$