

# Markle Root Tree

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# Introduction

- ❑ **Markle tree is introduced by the Ralph Markle in 1979**
- ❖ As **classic** cryptographic construction
- ❖ **It involves combination of hash functions in binary tree structure**
- ❑ **It is an efficient Data Structure for many applications**

# Markle Tree Data Structure

- Binary tree nodes are assigned (160 Bits) values
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← Interior Nodes  $v = \text{Hash}(V_{\text{left}} || V_{\text{right}})$

← Leaves  $V_i = \text{Hash}(s_i)$

← Secret  $S_i$

# Computing Tree and Root Hash

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# Complexity Analysis

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# Authenticating A Secret

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# Merkle Hash Function

- Ensures Authenticity of the document as well as the schema
- Associate a hash value with each node in the graph representation
- The hash value of a node is obtained by applying a hash function over the concatenation of its children
- The hash values are computed using the Merkle Hash Function



# Merkle Hash Function

# Example : Alice and Bob

- Bob stores a set of items for Alice
- Alice keeps a single value
- Alice can validate the Items returned to her

# First Solution

- Alice keeps the hash of the entire set

$H(\text{---}, \text{---}, \text{---})$

# Validation Of An Item



Bob sends all of the items to Alice



Alice computes the  
hash of the items

Alice compares the result to  
the value she has saved.



$H( \quad , \quad )$



# Problems With First Solution

- Bob must send Alice the entire set for validation

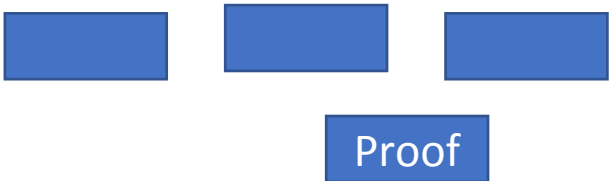
OK

# Problems With First Solution

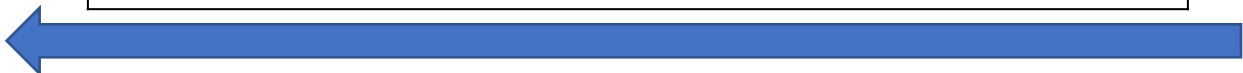
OK

- Bob must send Alice the entire set for validation
- Denote  $m$  to be the size of the set
- We have  $O(m)$  network traffic for validating a single item.
- Can we do better?

# Validating An Item



Bob sends Alice an item  $d$  and a logarithmic size proof

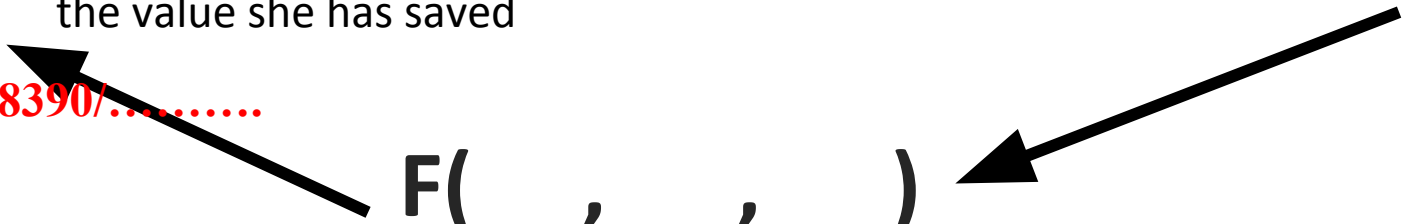


Alice computes a function of the item and proof

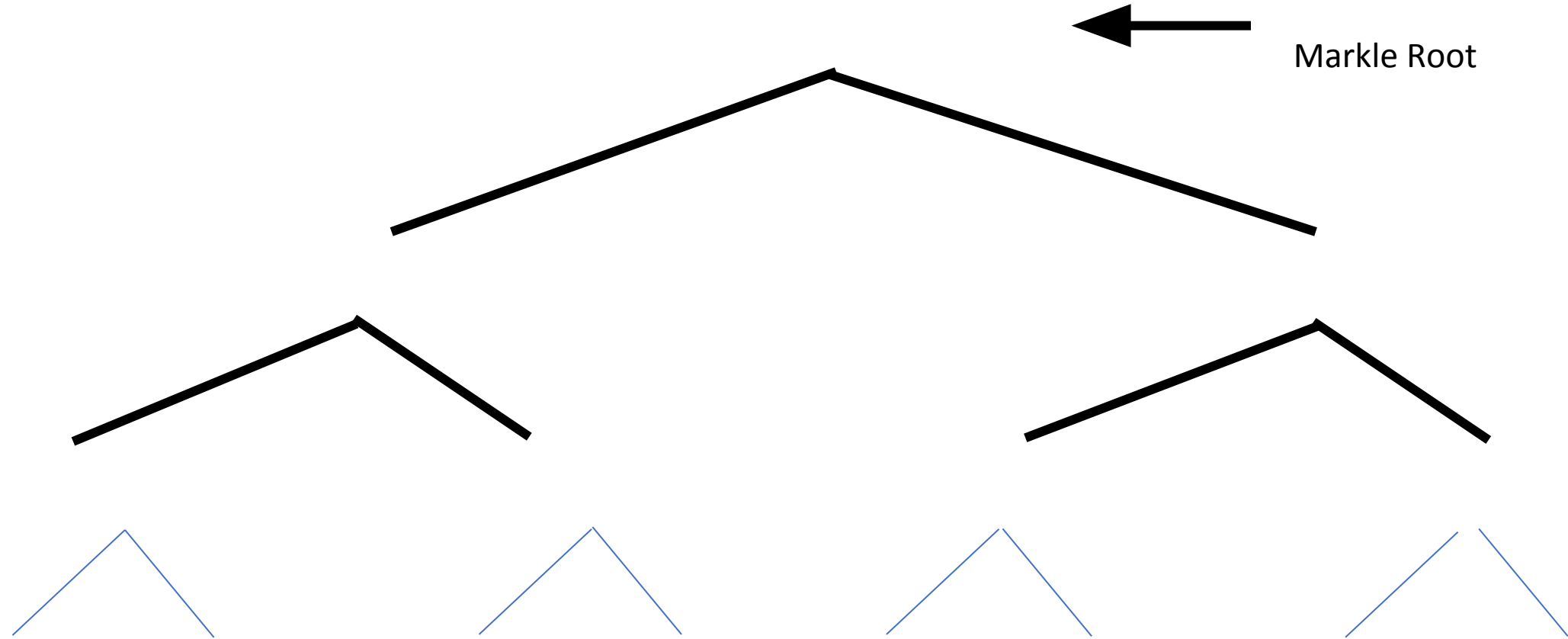
Alice compares the result to the value she has saved

Cfcdhgasv57654738390/.....

$F( \quad , \quad , \quad )$



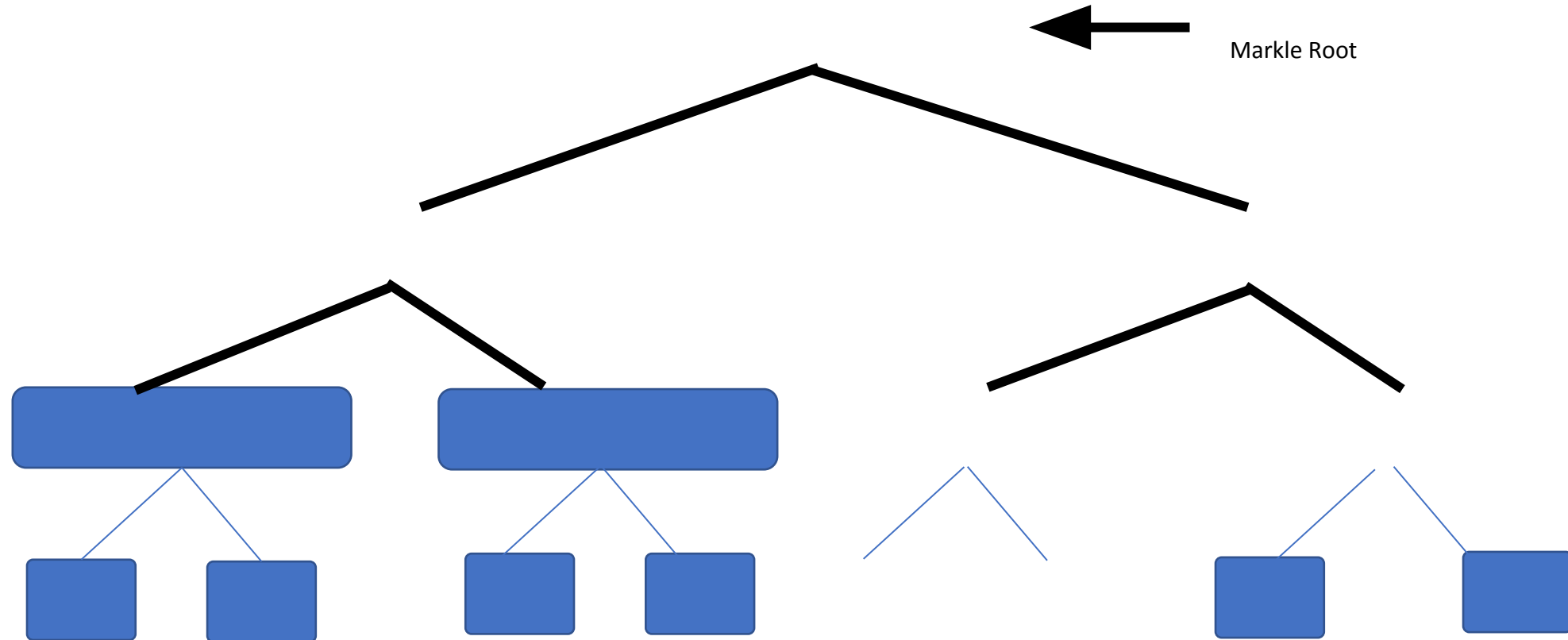
# Markle Tree





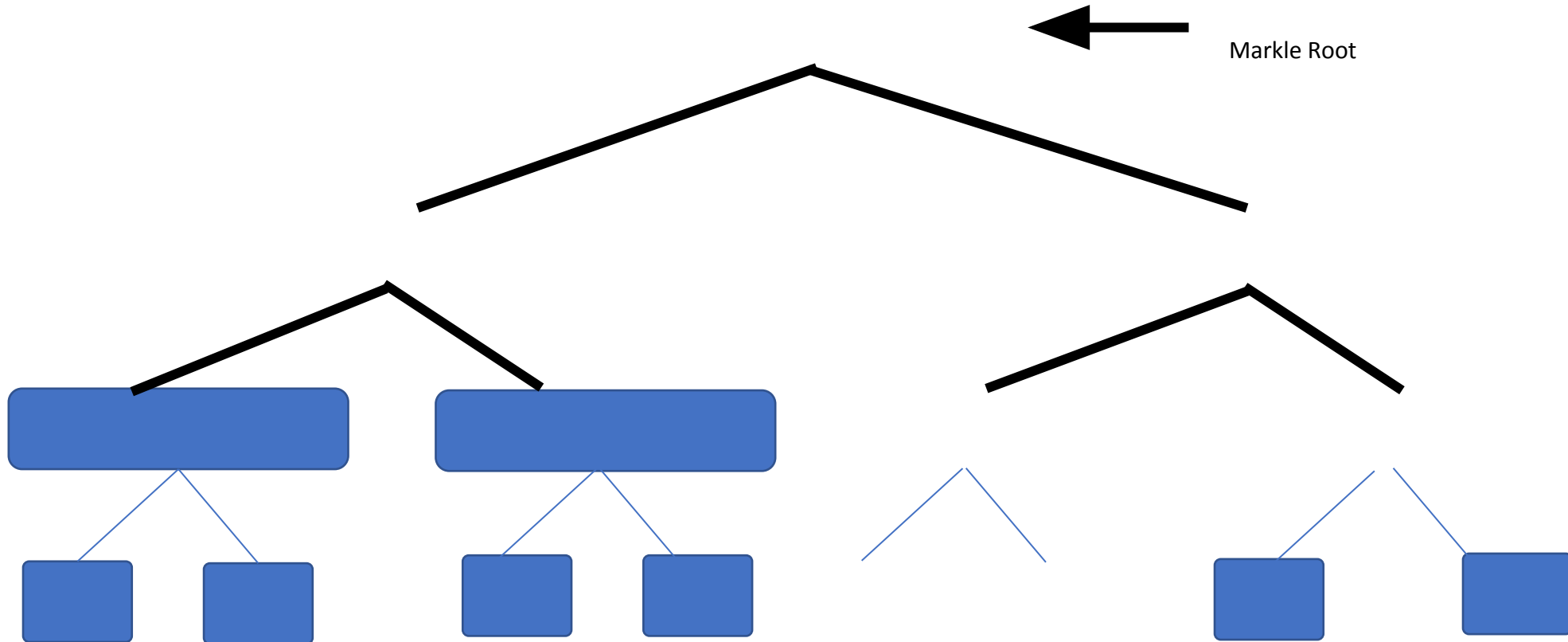
# Alice Computes The Root

Given an item  $d$  and  $H1, H2, H3$  hash values

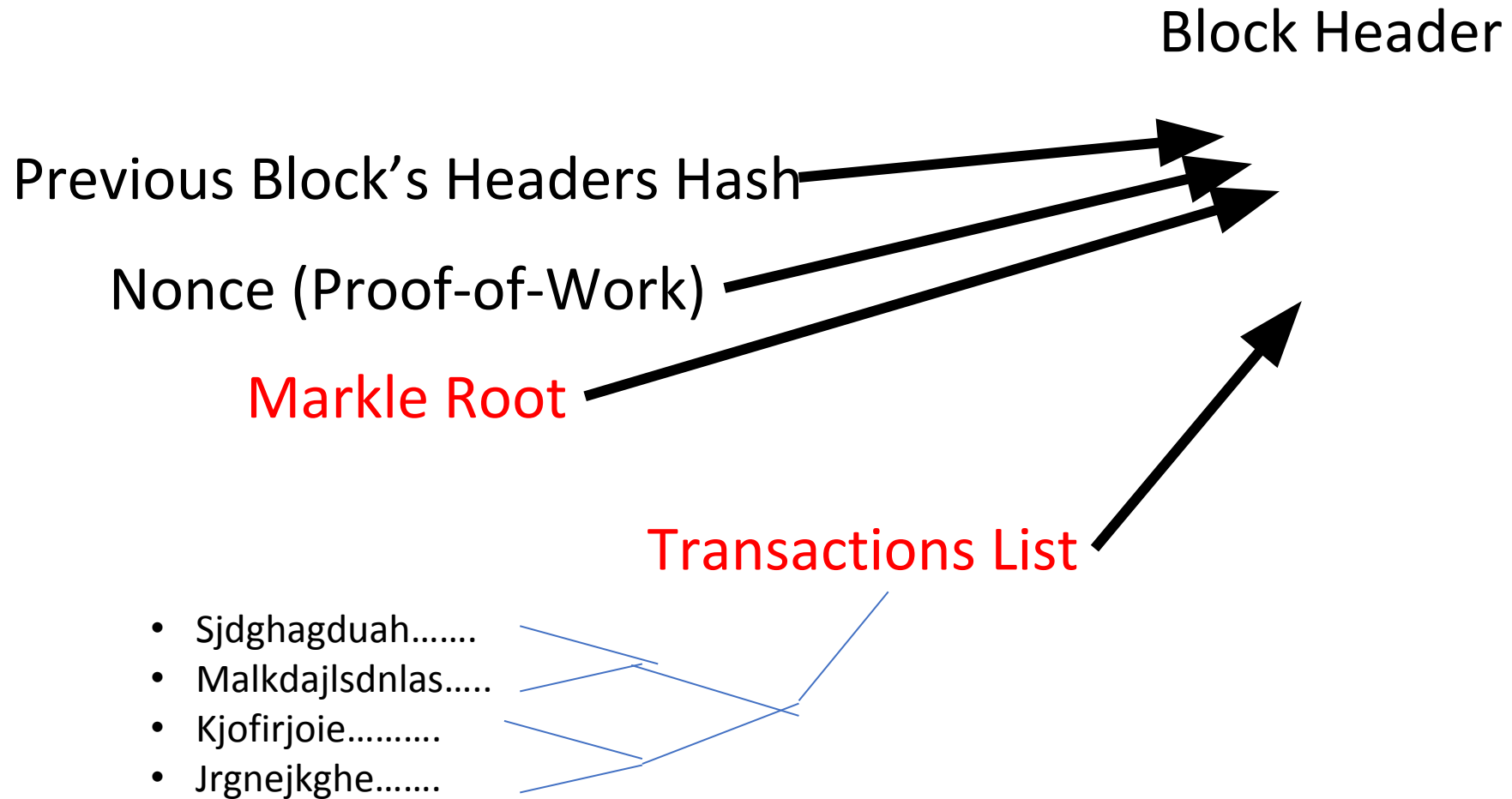


# What if d is not valid

Given an item d and H1,H2,H3 hash values



# Merkle Root In Header



# Advantages of Markle Root in Blockchain

- Merkle trees are a smart way to hash.
- They allow for easier storage of Blockchains, allowing headers to represent the entire block in a concise way.
- They even allows us to forget the transaction IDs of spent transactions.

# Questions