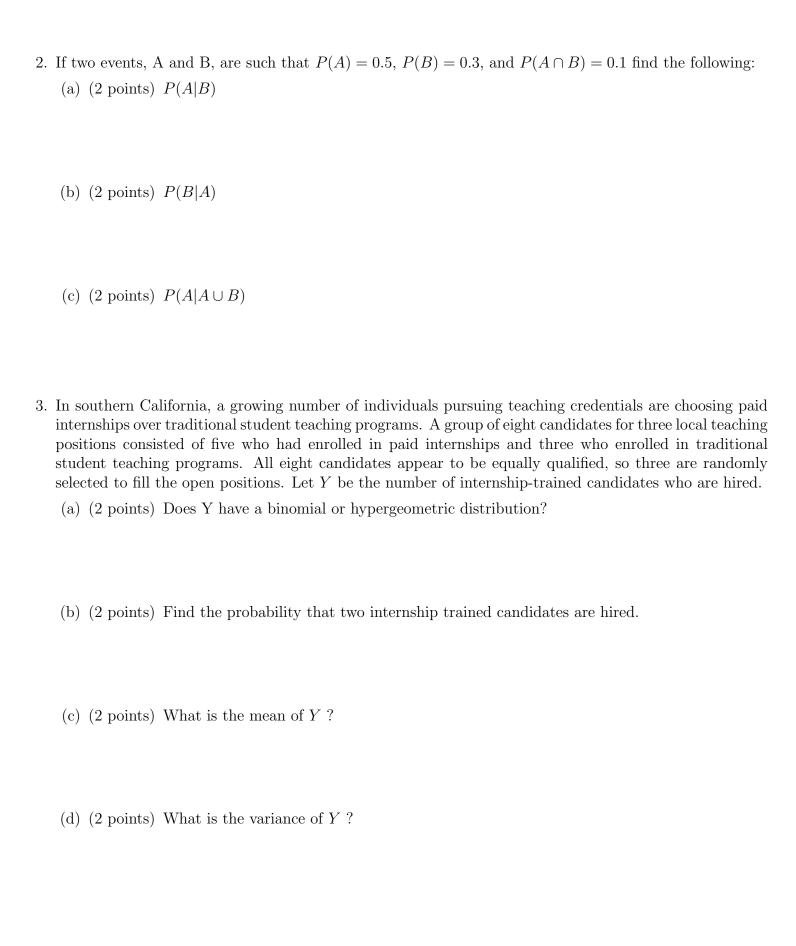
No books, no notes, only scientific (non-graphic) calculators. You must show work, unless the question is a true/false or fill-in-the-blank question.

Name:

Question	Points	Score
1	9	
2	6	
3	8	
4	6	
5	3	
6	3	
7	6	
8	6	
9	6	
10	7	
Total:	60	

1.	A friend who works in a big city owns two cars, one small and one large. Three-quarters of the time he drives the small car to work, and one-quarter of the time he drives the large car. If he takes the small car, he usually has little trouble parking, and so is at work on time with probability 0.9. If he takes the large car, he is at work on time with probability 0.6. Given that he was on time on a particular morning, what is the probability that he drove the small car?
	Solve this problem according to the following scheme. Make sure to give an appropriate answer for each part.
	(a) (3 points) Establish notation: name the relevant events.
	(b) (3 points) Write down the equation that lets you compute the answer, in the notation of part (a).
	(c) (3 points) Solve the problem, giving your answer as a percentage.



4.	For this question you may leave the answers in terms of binomial coefficients or factorials.
	A standard deck of cards has 52 cards, 4 of each type (Ace, King, Queen, Jack, 10,,2). From a well shuffled deck, you are dealt a hand of 5 cards (without replacement).
	(a) (3 points) What is the probability that you are dealt at least one face card (that is a king, queen or jack)?
	(b) (3 points) What is the probability that you are dealt both at least one ace and at least one face card?
5.	(3 points) Three cards are randomly selected, without replacement, from an ordinary deck of 52 playing cards. Compute the conditional probability that the first card selected is a spade, given that the second and third cards are spades.

6.	(3 points) If the number of phone calls to the fire department, Y, in a day has a Poisson distribution with mean 7.2, what is the most likely number of phone calls to the fire department on any day? Why?
7	The number of misprints on a page has a Poisson distribution with parameter $\lambda = 1$, and the numbers
١.	on different pages are independent.
	(a) (3 points) What is the probability that the second misprint will occur on page 1?
	(b) (3 points) What is the probability that the second misprint will occur on page 2?

8.	Sup	pose that there is a 1 in 50 chance of injury on a single skydiving attempt.
	(a)	(3 points) If we assume that the outcomes of different jumps are independent, what is the probability that a skydiver is injured if she jumps twice?
	(b)	(3 points) What is the probability of suffering at least one injury in 50 jumps.
9.		class of 20 students each student tosses a fair coin 4 times independently. (3 points) What is the probability that no student gets 4 heads.
	(b)	(3 points) What is the expected number of students who get 4 heads.

10.	A student is taking a multiple choice test with 10 questions for which she has mastered 60% of the material. Assume this means that she has a 0.6 chance of knowing the answer to a random test question and that if she does not know the answer to a question then she randomly selects among the four answer choices. Finally, assume that this holds for each question, independent of the others. (a) (2 points) What is the probability that the student correctly answers question 1?
	Let p be the probability of getting a random question correct. You likely found p in part (a), but in
	any case you should assume $0.7 .In parts (b) and (c) you can just use the letter p for this probability.$
	(b) (3 points) What is the probability that the student was certain of the answer to question 1 given that they got it correct. (Do not simplify the expression you get.)
	(c) (2 points) What is the probability that she will answer at least 9 questions correctly?