

- adaptr: an R package for simulating and comparing
- adaptive clinical trials
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Software

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Summary

The adaptr ${\bf R}$ package facilitates simulation and comparison of adaptive clinical trial designs using Bayesian statistical methods. The package supports a flexible number of arms, use of a common control arm, pre-specified and user-defined outcome- and posterior probability distribution-generating functions, fixed- and response-adaptive randomisation (RAR), various adaptation rules for arm dropping and stopping, calculation of trial design performance metrics, and visualisation of results. Simulations are relatively fast, can run in parallel, and can be reloaded from previous sessions.

Statement of need

Adaptive clinical trials are more flexible and can be more efficient than conventional randomised clinical trials (RCTs) with fixed sample sizes and allocation ratios (Pallmann et al., 2018). Because more efficient trials may be preferable for economic, logistic and ethical reasons, the interest in adaptive clinical trials is growing (Granholm et al., 2021). Planning adaptive trials and comparing adaptive trials designs is complex, however, and require statistical simulation because simple, closed-form sample size calculations are infeasible. Existing software is either closed source/commercial, has limited features or flexibility, or is based on graphical user interfaces that may hamper reproducibility (unlike scripting-based tools) (Meyer et al., 2021).

Overview and features

- The adaptr R package (R Core Team, 2021) focuses on multi-arm adaptive clinical trials using adaptive stopping, arm dropping and/or response-adaptive randomisation (Pallmann et al., 2018; Viele, Broglio, et al., 2020). Many realistic trial designs are supported by the built-in
- 29 functions and more advanced trial designs can be simulated with user-defined functions.
- $\textbf{Table 1} \ \ \text{gives an overview of the functionality of adaptr:}$

Table 1: Overview of functionality in the adaptr package.

Category	Description
General	Allows for two or more intervention arms and comparison of all arms or pairwise comparisons against a common control arms.
	Simulations use Bayesian statistics.



Category	Description
Outcomes and posteriors	Supports multiple outcome types specified by user-defined functions, with built-in convenience functions for easy use with binary, binomially distributed and continuous, normally distributed outcomes. For more flexibility, user-defined functions for generating outcomes and sampling from posterior distributions are supported; these may use more complex functions provided by other packages (e.g., Markov chain Monte Carlo or variational inference).
Random allocation	Supports fixed and response-adaptive randomisation, and combinations thereof, including special handling of control group allocation in trials with a common control (e.g., matching highest non-control group allocation ratio and square-root-ratio-based allocation (Park et al., 2020; Viele, Broglio, et al., 2020)). Supports minimum/maximum allocation limits and softening non-fixed allocation probabilities by raising them to a power (Ryan et al., 2020) (which may vary throughout the trial) and normalising probabilities to sum to 100%.
Adaptation rules Performance metrics	Supports probabilistic trial-stopping/arm-dropping rules for superiority, inferiority, and practical equivalence between all arms in trial designs without a common control. Supports probabilistic trial-stopping/arm-dropping rules for superiority, inferiority, practical equivalence, and futility compared to a common control in such designs. In trial designs with a common control, a superior arm becomes the new control. In these cases equivalence/futility testing may be continued (using the new control) or disabled. Supports the calculation of various trial design performance metrics (Viele, Broglio, et al., 2020; Viele, Saville, et al., 2020) according to
Visualisation	different arm selection strategies in trials not ending with superiority. Offers graphical summaries of the overall or arm-specific statuses over time across multiple simulations (such as still recruting or trial stopped/arm dropped for various reasons), and relevant arm-specific metrics (e.g., allocation probabilities) over time across single/multiple trial simulations.
Technical	Supports parallel execution on multiple cores using R 's built-in parallel package. Allows reproducible results with seeding. Supports saving/loading large trial objects and <i>growing</i> previous simulation objects. Uses base R with no required external dependencies; optional plotting functionality does, however, require the ggplot2-package (Wickham et al., 2019).

- Adaptive analyses are conducted at specified recruitment numbers, after random allocation of
- simulated patients to currently active arms. Both fixed and response-adaptive randomisation
- (RAR) as well as combinations (including several restrictions of RAR) are supported (Pallmann
- et al., 2018; Park et al., 2020; Ryan et al., 2020; The Adaptive Platform Trials Coalition, 2019).
- Outcomes are then generated, followed by drawing samples from the posterior distributions;
- the packages comes with built-in functions for generating outcomes and posteriors using fast
- models with conjugate, flat priors (Ryan et al., 2019), but more advanced estimation are
- 38 allowed using user-defined functions.
- Posterior draws are used to calculate probabilities for (i) enforcing adaptive trial-stopping/arm-



- dropping rules with respect to superiority, inferiority, equivalence and/or futility, (ii) assessing
- the trial's final status (superiority, inferiority, equivalence, futility, or stopped at a maximum
- pre-specified sample size), and (iii) adjusting allocation probabilities if RAR is used. Single or
- 43 multiple trial simulations can be run, saved and grown, and summarised using multiple relevant
- performance metrics (Viele, Broglio, et al., 2020; Viele, Saville, et al., 2020). Performance
- 45 metrics can be calculated under different assumptions about the preferable intervention in
- clinical practice should the trials not end with superiority.

47 Functions and workflow

An overview of the principal functions in adaptr is given in **Table 2**:

Table 2: Overview of user-facing functions in adaptr.

Function name	Action
setup trial,	Defines the adaptive trial specification including arms, true
setup_trial_binom,	outcome rates, stopping rules, outcome/posterior generating
setup_trial_norm	functions, and summary settings.
	Full flexibility is provided by setup_trial ; the convenience
	<pre>functions setup_trial_binom and setup_trial_norm provide</pre>
	sensible defaults for binary, binomially distributed and
	continuous, normally distributed outcomes, respectively.
run_trial	Runs a single simulation using a trial specification defined with
	setup_trial.
run_trials	Runs multiple trial simulations using a trial specification
	defined with setup_trial. Can save simulation objects to
	external files and load/grow previous simulations.
extract_results	Extracts key results and (partial) performance metrics from
	multiple simulations conducted by run_trials according to a
	specified arm selection strategy for simulations not ending in
	superiority. Returns a tidy data.frame with one simulation per
	row (Wickham et al., 2019).
summary	Summarises, in a human-friendly way, key results and calculates
	overall performance metrics for multiple simulations according
	to a specified arm selection strategy for simulations not ending in superiority.
plot status	Plots the overall statuses or arm-specific statuses for multiple
ptot_status	simulations over the course of the simulated trials.
plot history	Plots the history of relevant metrics in each arm for one or
prot_incapor y	multiple simulations over the course of the simulated trial(s).
print	Print methods for printing the outputs of most of the included
F	functions in a human-friendly way.

- adaptr is available on CRAN and GitHub, where a stand-alone website with the package
- documentation is also available. adaptr can be installed using one of the following commands:

```
install.packages("adaptr") # CRAN

# install.packages("remotes")
remotes::install qithub("INCEPTdk/adaptr") # GitHub
```

Once installed, as any other R package, it is loaded with:

```
library(adaptr)
#> Loading adaptr package (version 1.0.0).
```



```
#> See 'help("adaptr")' or 'vignette("Overview", "adaptr")' for help.
#> Further information available on https://github.com/INCEPTdk/adaptr/.
```

- $_{52}$ An adaptive trial design is specified with the generic setup_trial function (requires user-defined
- functions to generate/compare outcomes), or one of the helper functions setup_trial_binom
- or setup_trial_norm (wrappers around setup_trial with appropriate functions for generating
- outcomes and sampling from posterior distributions). For example, a simple four-arm trial with
- a binary, binomially distributed outcome can be specified with:

```
binom_trial <- setup_trial_binom(</pre>
   # Treatment arms
   arms = c("Control", "Experimental A", "Experimental B", "Experimental C"),
   # True event rates
   true ys = c(0.25, 0.30, 0.22, 0.19),
   # Time of adaptive analyses
   # - first analysis when 400 patients are included, then after every 100
   data_looks = seq(from = 400, to = 2000, by = 100),
   # Name of the common control leave undefined if no common control is desired)
   control = "Control",
   # Use square-root-ratio-based allocation (sqrt(number of non-control arms):1
   # for each non-control arm), with fixed control group allocation and RAR in
   # the non-control arms
   control_prob_fixed = "sqrt-based",
   # Define stopping rules
   superiority = 0.99, # Superiority probability threshold
   inferiority = 0.01, # Inferiority probability threshold
   equivalence_prob = 0.85, # Equivalence probability threshold
   equivalence_diff = 0.05, # Equivalence difference
   equivalence only first = TRUE, # Only assess equivalence for first control
   # Restrict non-fixed allocation ratios (limit extreme RAR)
   soften power = 0.5
print(binom_trial)
#> Trial specification: generic binomially distributed outcome trial
#> * Undesirable outcome
#> * Common control arm: Control
#> * Control arm probability fixed at 0.366 (for 4 arms), 0.414 (for 3 arms),
#> 0.5 (for 2 arms)
#> * Best arm: Experimental C
#>
#> Arms, true outcomes, starting allocation probabilities
#> and allocation probability limits:
#>
             arms true_ys start_probs fixed_probs min_probs max_probs
                                0.366 0.366
#>
          Control 0.25
                                                        NA
                                                                    NA
#> Experimental A
                     0.30
                                0.211
                                              NA
                                                         NA
                                                                    NA
#> Experimental B
                   0.22
                                0.211
                                               NA
                                                         NA
                                                                    NA
#> Experimental C 0.19
                                0.211
                                               NA
                                                                    NA
                                                          NA
#>
#> Maximum sample size: 2000
```



```
#> Maximum number of data looks: 17
   #> Planned data looks after: 400, 500, 600, 700, 800, 900, 1000, 1100,
   #> 1200, 1300, 1400, 1500, 1600, 1700, 1800, 1900, 2000 patients
   #>
   #> Superiority threshold: 0.99
   #> Inferiority threshold: 0.01
   #> Equivalence threshold: 0.85 (only checked for first control)
   #> Absolute equivalence difference: 0.05
   #> No futility threshold
   #> Soften power for all analyses: 0.5
57 Once specified, simulating a single trial is easy:
   run trial(binom trial, seed = 202203) # Fixed random seed
   #> Single simulation result: generic binomially distributed outcome trial
   #> * Undesirable outcome
   #> * Initial/final common control arms: Control/Experimental C
   #>
   #> Final status: inconclusive, stopped at maximum sample size
   #> Final/maximum allowed sample sizes: 2000/2000 (100.0%)
   #> Final trial results:
   #>
                 arms true_ys sum_ys ns raw_ests post_ests post_errs lo_cri hi_cri
                                    42 145
                                              0.290
                                                         0.293
                                                                  0.0375 0.223 0.366
   #>
              Control
                          0.25
                                   27 87
       Experimental A
                          0.30
                                              0.310
                                                         0.314
                                                                  0.0492
                                                                          0.223 0.415
       Experimental B
                          0.22
                                  192 888
                                              0.216
                                                         0.217
                                                                  0.0138 0.190 0.245
                                                         0.188
                          0.19
                                   165 880
                                              0.188
                                                                  0.0133 0.163 0.215
   #>
       Experimental C
       final_status_status_look status_probs final_alloc
   #>
           inferior
                             400
                                       0.0032
                                                     0.366
   #>
   #>
            inferior
                                        0.0036
                                                     0.211
   #>
             active
                              NA
                                            NA
                                                     0.500
                                                     0.500
   #>
            control
                              NA
                                            NA
   #> Simulation details:
   #> * Random seed: 202203
   #> * Credible interval width: 95%
   #> * Number of posterior draws: 5000
   #> * Posterior estimation method: medians with MAD-SDs
  —so is running multiple trials, for example 1000. If cores > 1, simulations are runs in parallel
   on the number of cores specified. Setting sparse = FALSE keeps all intermediate simulation
   results; this is required for plot_history (see below) but makes the object a lot larger (in this
   case, by a factor 15).
   sims <- run_trials(trial_spec = binom_trial, n_rep = 1000, cores = 4,</pre>
                       base seed = 202204, sparse = FALSE)
   Numerical results
   We summarise the results, assuming the control arm would be used in clinical practice in case
   of inconclusive trials (unless dropped early):
   summary(sims, select strategy = "control")
   #> Multiple simulation results: generic binomially distributed outcome trial
   #> * Undesirable outcome
   #> * Number of simulations: 1000
```

#> * Number of simulations summarised: 1000 (all trials)



```
#> * Common control arm: Control
#> * Selection strategy: first control if available (otherwise no selection)
#> * Treatment effect compared to: no comparison
#> Performance metrics (using posterior estimates):
#> * Sample sizes: mean 1708.3 (SD: 438.0) | median 2000.0 (IQR: 1500.0 to
#> 2000.0)
#> * Total summarised outcomes: mean 382.5 (SD: 96.4) | median 422.0 (IQR:
#> 338.8 to 449.0)
#> * Total summarised outcome rates: mean 0.225 (SD: 0.014) | median 0.225
#> (IQR: 0.216 to 0.234)
#> * Conclusive: 45.2%
#> * Superiority: 39.0%
#> * Equivalence: 6.2%
#> * Futility: 0.0% [not assessed]
#> * Inconclusive at max sample size: 54.8%
#> * Selection probabilities: Control 24.0% | Experimental A: 0.0% |
#> Experimental B: 1.3% | Experimental C: 33.1% | None: 41.6%
#> * RMSE: 0.02742
#> * RMSE treatment effect: 0.04741
#> * Ideal design percentage: 77.0%
#> Simulation details:
#> * Simulation time: 19.9 secs
#> * Base random seed: 202204
#> * Credible interval width: 95%
#> * Number of posterior draws: 5000
#> * Estimation method: posterior medians with MAD-SDs
Alternatively, we can get tidy results (Wickham et al., 2019) for each simulation using the
same selection strategy as above:
extr_res <- extract_results(sims, select_strategy = "control")</pre>
head(extr_res) # Print results for first six simulations
      sim final_n sum_ys ratio_ys final_status
                                                   superior arm
                                                                   selected arm
             2000
                     436 0.2180000
                                                           < NA >
                                                                           < NA >
                                             max
#> 2
             2000
                     452 0.2260000
                                                           < NA >
                                                                           < NA >
                                             max
#> 3
                     389 0.2161111
                                    superiority Experimental C Experimental C
             1800
#> 4
             2000
                     440 0.2200000
                                             max
                                                           <NA>
 #> 5
              500
                     118 0.2360000 superiority Experimental B Experimental B
#> 6
              900
                     182 0.2022222 superiority Experimental C Experimental C
            sq_err
                     sq_err_te
                NA
                            NA
#>
                NA
                            NA
#> 3 0.0004297484 0.004184831
                NA
#> 5 0.0078199784 0.015558136
#> 6 0.0019097953 0.001558565
```

Visual summaries

We can plot the overall trial statuses at each adaptive analysis using:

plot_status(sims)



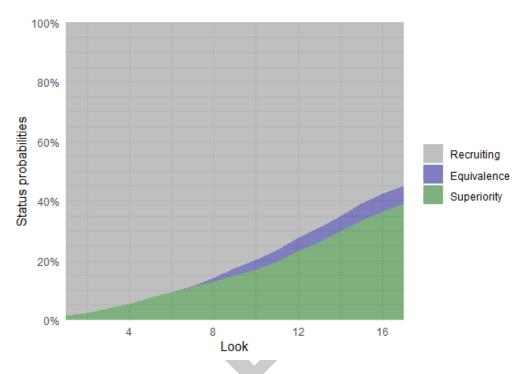


Figure 1: Status plot

The overall allocation probabilities in each arm (y axis) against the total number of patients included in the trial (x axis) are plotted using:

```
# Requires sparse = FALSE in run_trials
plot_history(sims, x_value = "total n", y_value = "prob")
    100%
     80%
 Allocation probability
     60%
                                                                               Control
                                                                               Experimental A
                                                                               Experimental B
     40%
                                                                               Experimental C
     20%
      0%
                                      1000
                                                     1500
                                                                    2000
```

Figure 2: Allocation probabilities history plot

Total no. of patients randomised



Arm-specific statuses and additional metrics over time may be plotted as well.

Discussion

- We have developed a flexible, extensible and comprehensive **R** package that allows relatively easy and efficient simulation of adaptive clinical trials using various features with few, well-documented user-facing functions.
- The package facilitates planning of adaptive clinical trials and comparison of trial designs using combinations of the most important and common adaptive features. In addition to the efficient convenience functions provided for common outcome types, more complex models are supported but may increase simulation time substantially and require (highly) parallel execution on multiple cores locally and/or remotely using cloud computing.
- Compared to other open-source solutions (Meyer et al., 2021), adaptr comprises a completely 81 functional and well-documented R package with support for multiple complex randomisation 82 strategies, different stopping rules with detailed control, full support for user-defined outcomeposterior-generating functions, parallel computation, easy calculation of various trial design performance metrics according to different arm selection strategies for trials not ending in superiority, and visualisation of relevant metrics across single or multiple simulations. While relatively feature-rich, the package currently has some limitations. These primarily include the lack of a 'flooring' option (stopping allocation to arms when their probabilities of being the best fall below a certain threshold, possibly with subsequent resumption of allocation (Viele, Broglio, et al., 2020)), inability to add arms during the conduct (as done in adaptive platform trials (The Adaptive Platform Trials Coalition, 2019); this is complex and not supported in most 91 other software (Meyer et al., 2021)) and the lack of separate stopping rules/allocation ratios in subgroups or enrichment (which is similarly complex (The Adaptive Platform Trials Coalition, 2019)). Finally, the package uses Bayesian statistical methods as these are well-suited for adaptive trials and easily extended; frequentist statistical methods are not supported. 95
- In conclusion, the adaptr **R** package provides a feature-rich and extensible open-source, scripting-based solution for planning, simulating and comparing adaptive clinical trials.

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References

- Granholm, A., Alhazzani, W., Derde, L., Angus, D., Zampieri, F., Hammond, N., Sweeney, R., Myatra, S., Azoulay, E., Rowan, K., Young, P., Perner, A., & Møller, M. (2021).
 Randomised clinical trials in critical care: Past, present and future. *Intensive Care Medicine*. https://doi.org/10.1007/s00134-021-06587-9
- Meyer, E., Mesenbrink, P., Mielke, T., Parke, T., Evans, D., König, F., & on behalf of EU-PEARL (EU Patient-cEntric clinicAl tRial pLatforms) Consortium. (2021). Systematic review of available software for multi-arm multi-stage and platform clinical trial design.
 Trials, 22, 183. https://doi.org/10.1186/s13063-021-05130-x
- Pallmann, P., Bedding, A., Choodari-Oskooei, B., Dimairo, M., Flight, L., Hampson, L., Holmes, J., Mander, A., Odondi, L., Sydes, M., Villar, S., Wason, J., Weir, C., Wheeler, G., Yap, C., & Jaki, T. (2018). Adaptive designs in clinical trials: Why use them, and how to run and report them. *BMC Medicine*, 16, 29. https://doi.org/10.1186/s12916-018-1017-7



- Park, J., Harari, O., Dron, L., Lester, R., Thorlund, K., & Mills, E. (2020). An overview of platform trials with a checklist for clinical readers. *Journal of Clinical Epidemiology*, 125, 1–8. https://doi.org/10.1016/j.jclinepi.2020.04.025
- R Core Team. (2021). *R: A language and environment for statistical computing*. R Foundation for Statistical Computing. https://www.R-project.org/
- Ryan, E., Harrison, E., Pearse, R., & Gates, S. (2019). Perioperative haemodynamic therapy for major gastrointestinal surgery: The effect of a bayesian approach to interpreting the findings of a randomised controlled trial. *BMJ Open*, *9*, e024256. https://doi.org/10.1136/bmjopen-2018-024256
- Ryan, E., Lamb, S., Williamson, E., & Gates, S. (2020). Bayesian adaptive designs for multi-arm trials: An orthopaedic case study. *Trials*, 21, 83. https://doi.org/10.1186/s13063-019-4021-0
- The Adaptive Platform Trials Coalition. (2019). Adaptive platform trials: Definition, design, conduct and reporting considerations. *Nature Reviews Drug Discovery*, *18*, 797–807. https://doi.org/10.1038/s41573-019-0034-3
- Viele, K., Broglio, K., McGlothlin, A., & Saville, B. (2020). Comparison of methods for control allocation in multiple arm studies using response adaptive randomization. *Clinical Trials*, 17, 52–60. https://doi.org/10.1177/1740774519877836
- Viele, K., Saville, B., McGlothlin, A., & Broglio, K. (2020). Comparison of response adaptive randomization features in multiarm clinical trials with control. *Pharmaceutical Statistics*, 19, 602–612. https://doi.org/10.1002/pst.2015
- Wickham, H., Averick, M., Bryan, J., Chang, W., D'Agostino, L., Francois, R., Grolemund,
 G., Hayes, A., Henry, L., Hester, J., Kuhn, M., Pedersen, T., Miller, E., Bache, S., Müller,
 K., Ooms, J., Robinson, D., Seidel, D., Spinu, V., ... Yutani, H. (2019). Welcome to the
 tidyverse. Journal of Open Source Software, 4, 1686. https://doi.org/10.21105/joss.01686