

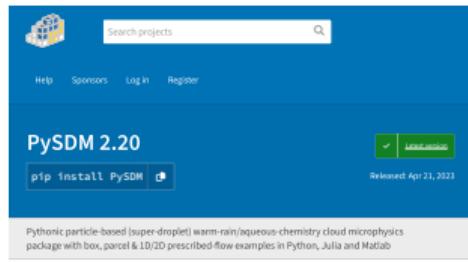
# **Modelling of water isotopic fractionation within and below clouds**

Sylwester Arabas

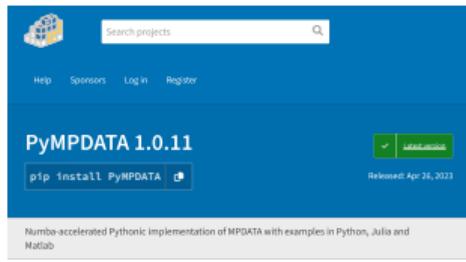


AGH University in Krakow

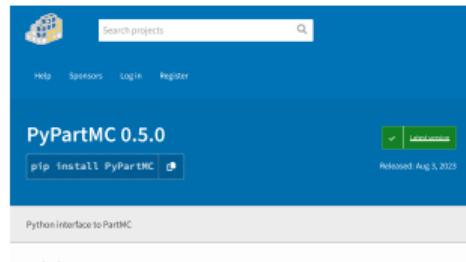
# github.com/open-atmos



The screenshot shows the GitHub project page for PySDM 2.20. At the top, there's a search bar and navigation links for Help, Sponsors, Log in, and Register. Below that is a large green header box with the title "PySDM 2.20" and a "New release" button. The release date is April 21, 2023. A "pip install PySDM" button is present. The main content area contains a brief description: "Pythonic particle-based (super-droplet) warm-rain/aqueous-chemistry cloud microphysics package with box, parcel & 1D/2D prescribed flow examples in Python, Julia and Matlab". Below this is a "Project description" section with tabs for "Project description" (selected), "Release history", "Download files", and "Project links". The "Project description" tab includes sections for "PySDM" (with a link to the code repository), "Statistics" (GitHub stats: 40 stars, 23 forks, 101 open issues, 13 open pull requests), and "PySDM" (with a detailed description of the package's purpose and features).



The screenshot shows the GitHub project page for PyMPDATA 1.0.11. It has a similar layout to the PySDM page, with a green header box for the release and a "Project description" section. The PyMPDATA section includes a "PyMPDATA" tab with a detailed description of the Numba-accelerated Pythonic implementation of MPDATA, and a "Statistics" section showing GitHub stats: 13 stars, 5 forks, 3 open issues, and 2 open pull requests.



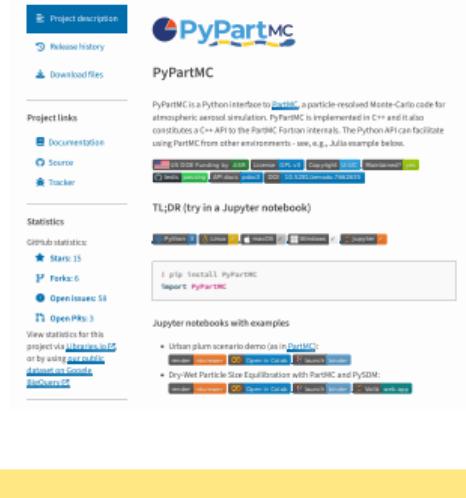
The screenshot shows the GitHub project page for PyPartMC 0.5.0. It follows the same structure, with a green header box for the release and a "Project description" section. The PyPartMC section includes a "PyPartMC" tab with a detailed description of the Python interface to PartMC, and a "Statistics" section showing GitHub stats: 15 stars, 6 forks, 5 open issues, and 3 open pull requests.



This screenshot shows the full GitHub project page for PySDM. It includes a "Navigation" bar with links for Help, Sponsors, Log in, Register, and a search bar. The main content area has a "Project description" section for PySDM, followed by "Statistics" (GitHub stats: 40 stars, 23 forks, 101 open issues, 13 open pull requests), and a "PySDM" section with a detailed description of the package's purpose and features.



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This screenshot shows the full GitHub project page for PyPartMC. It includes a "Navigation" bar, a "Project description" section for PyPartMC, a "Statistics" section (GitHub stats: 15 stars, 6 forks, 5 open issues, 3 open pull requests), and a "PyPartMC" section with a detailed description of the package's purpose and features.

Research Article

## The super-droplet method for the numerical simulation of clouds and precipitation: a particle-based and probabilistic microphysics model coupled with a non-hydrostatic model

S. Shima ✉, K. Kusano, A. Kawano, T. Sugiyama, S. Kawahara

First published: 19 June 2009 | <https://doi.org/10.1002/qj.441> | Citations: 150

### Abstract

A novel, particle-based, probabilistic approach for the simulation of cloud microphysics is proposed, which is named the super-droplet method (SDM). This method enables the accurate simulation of cloud microphysics with a less demanding cost in computation. SDM is applied to a warm-cloud system, which incorporates sedimentation, condensation/evaporation and stochastic coalescence. The methodology to couple super-droplets and a non-hydrostatic model is also developed. It is confirmed that the result of our Monte Carlo scheme for the stochastic coalescence of super-droplets agrees fairly well with the solutions of the stochastic coalescence equation. The behaviour of the model is evaluated using a simple test problem, that of a shallow maritime cumulus formation initiated by a warm bubble. Possible extensions of SDM are briefly discussed. A theoretical analysis suggests that the computational cost of SDM becomes lower than the spectral (bin) method when the number of attributes—the variables that identify the state of each super-droplet—becomes larger than some critical value, which we estimate to be in the range  $2 \sim 4$ .

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# PySDM: open-source particle-based cloud-microphysics package

The screenshot shows the GitHub repository page for PySDM. It includes sections for Python 3, LLVM, Numba, CUDA, ThrustRTC, Linux, macOS, Windows, Jupyter, maintenance status (yes), Open Hub, EU Funding by FNP, PL Funding by NCN, US DOE Funding by ASR, License (GPL v3), test status (tests+artifacts+pypi: passing, build: passing, codecov: 84%), pypi package (2.54), API docs (pdoc3), and GitHub statistics (stars: 51, watching: 5, forks: 28).

PySDM is a package for simulating the dynamics of population of particles. It is intended to serve as a building block for simulation systems modelling fluid flows involving a dispersed phase, with PySDM being responsible for representation of the dispersed phase. Currently, the development is focused on atmospheric cloud physics applications, in particular on modelling the dynamics of particles immersed in moist air using the particle-based (a.k.a. super-droplet) approach to represent aerosol/cloud/rain microphysics. The package features a Pythonic high-performance implementation of the Super-Droplet Method (SDM) Monte-Carlo algorithm for representing collisional growth ([Shima et al. 2009](#)), hence the name.

For an overview of PySDM features (and the preferred way to cite PySDM in papers), please refer to our JOSS papers:

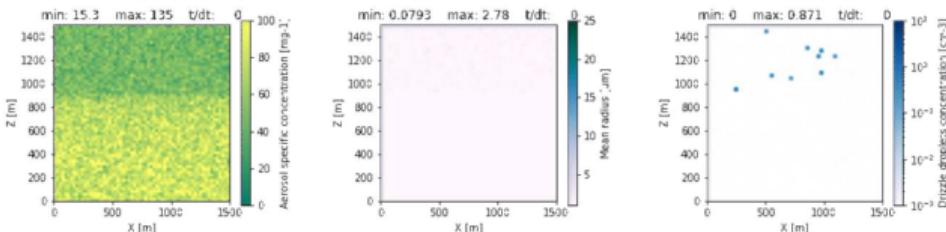
- [Bartman et al. 2022](#) (PySDM v1).
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PySDM includes an extension of the SDM scheme to represent collisional breakup described in [de Jong, Mackay et al. 2023](#).

For a list of talks and other materials on PySDM as well as a list of published papers featuring PySDM simulations, see the [project wiki](#).

## Example Jupyter notebooks (reproducing results from literature):

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GPL-3.0 license

51 stars

5 watching

28 forks

Report repository

## Releases 86

PySDM v2.56 Latest  
4 hours ago

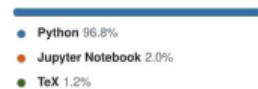
+ 85 releases

## Contributors 19



+ 5 contributors

## Languages



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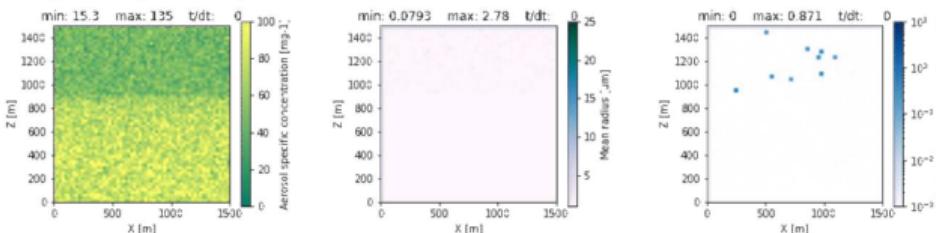
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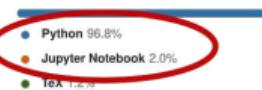
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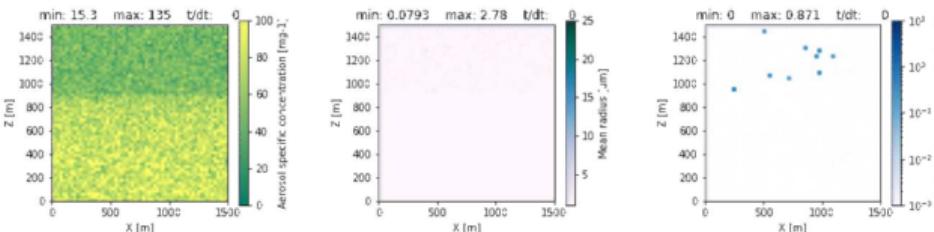
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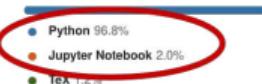
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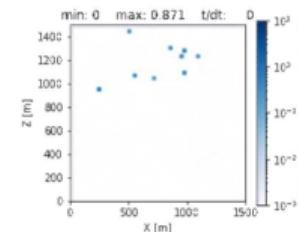
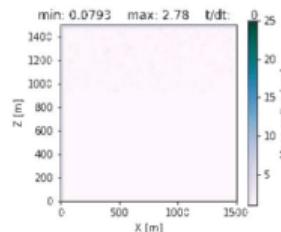
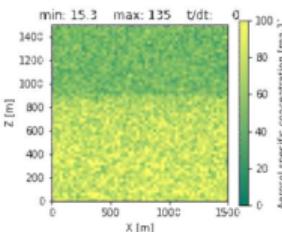
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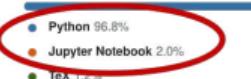
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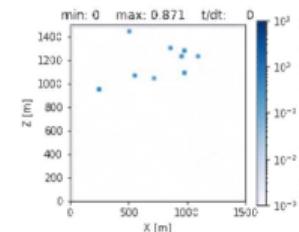
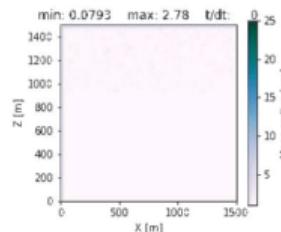
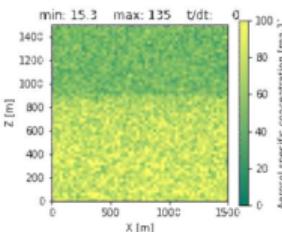
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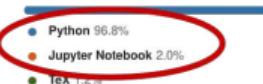
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Languages



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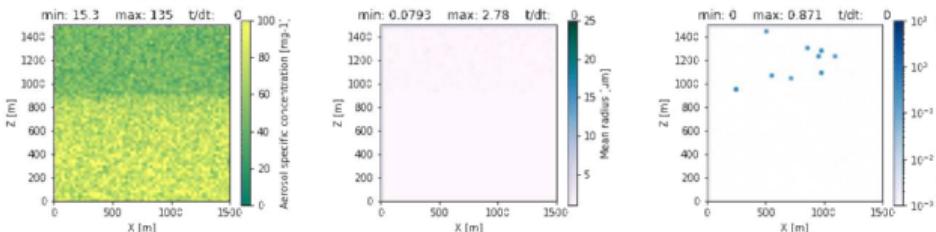
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Languages

Python 96.8%  
Jupyter Notebook 2.0%  
TeX 1.2%

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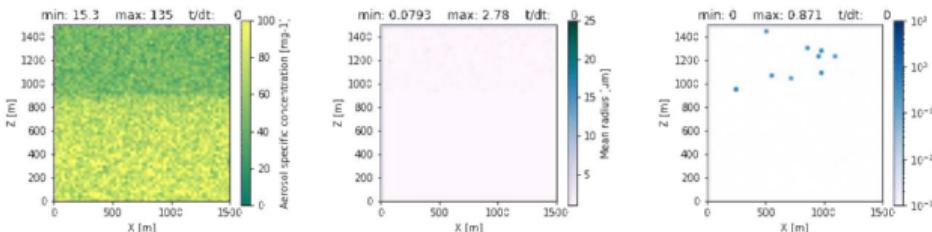
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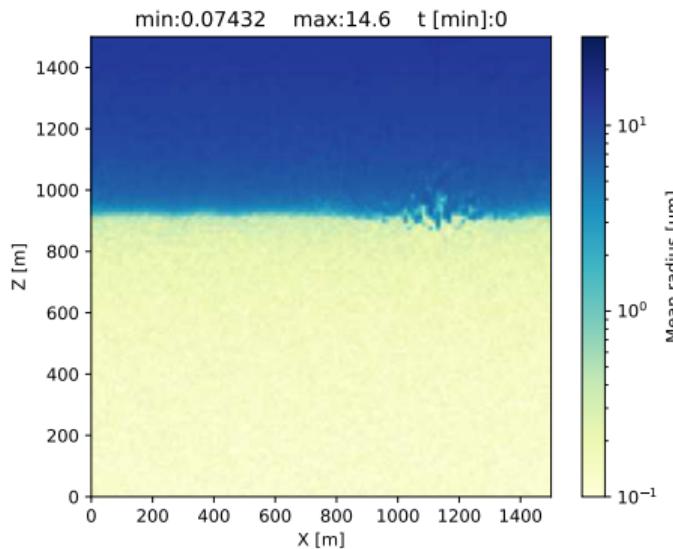
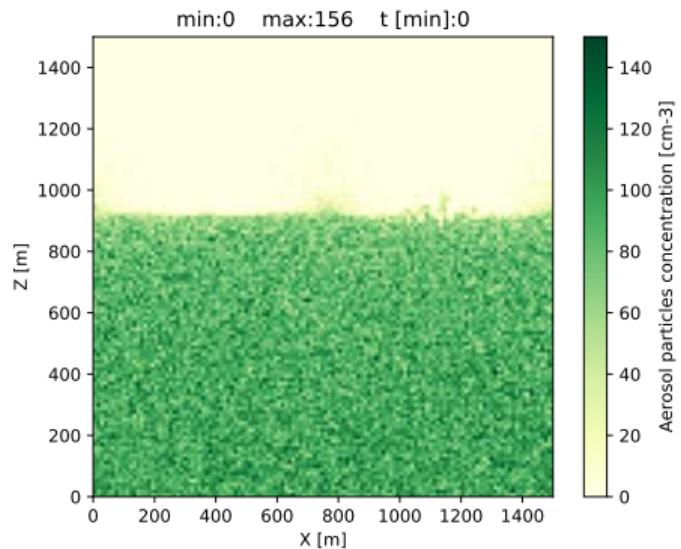


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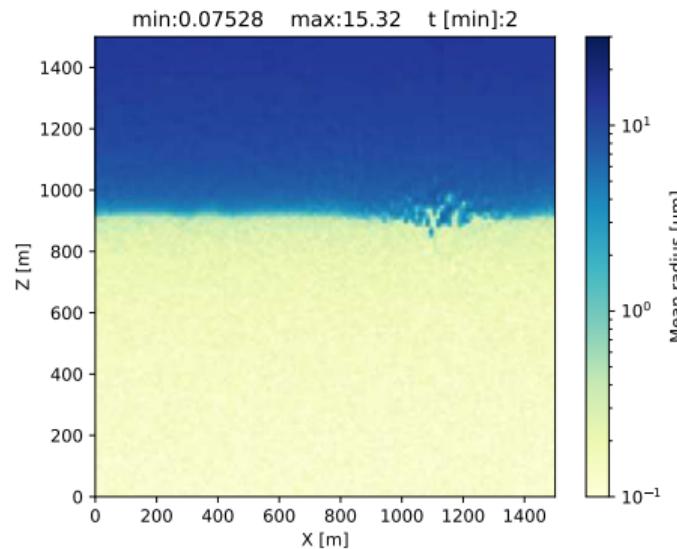
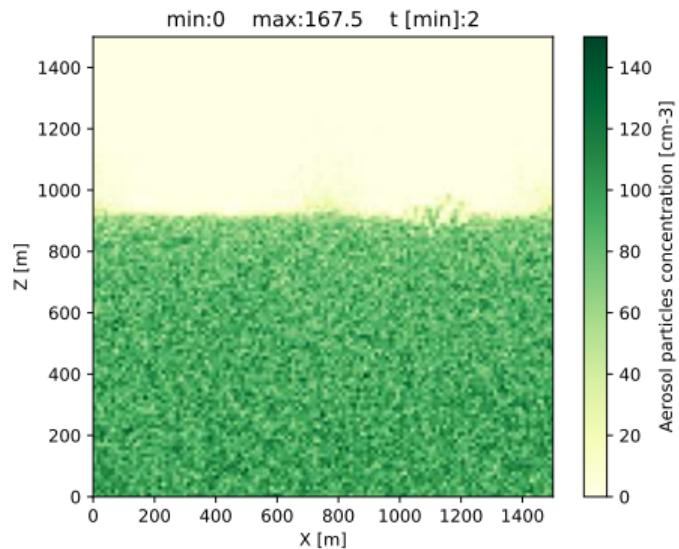
Python 96.8%  
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Eulerian solver (kinematic flow) grid:  $128 \times 128$   
Lagrangian super-particles population:  $2^{21}$



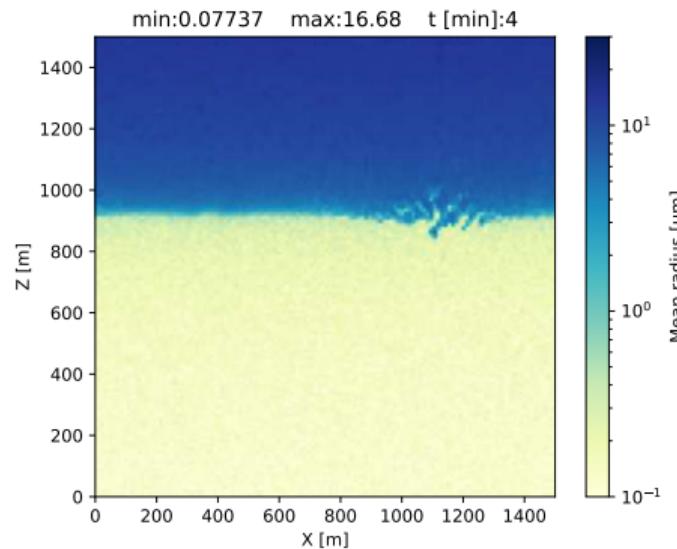
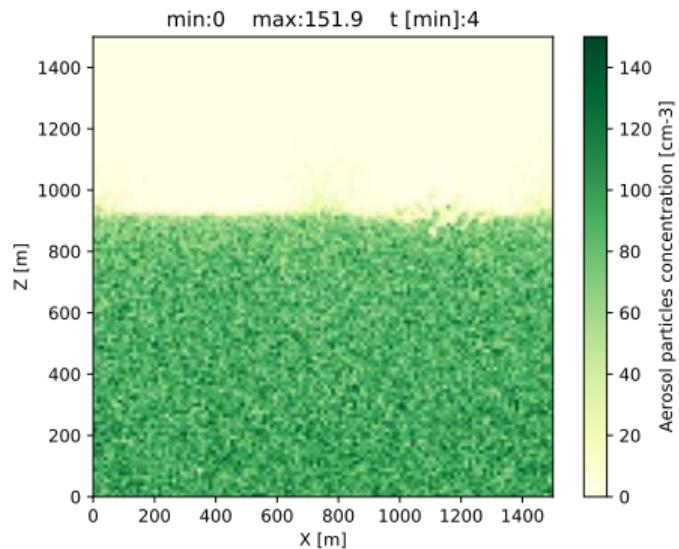
simulation & vis.: Piotr Bartman

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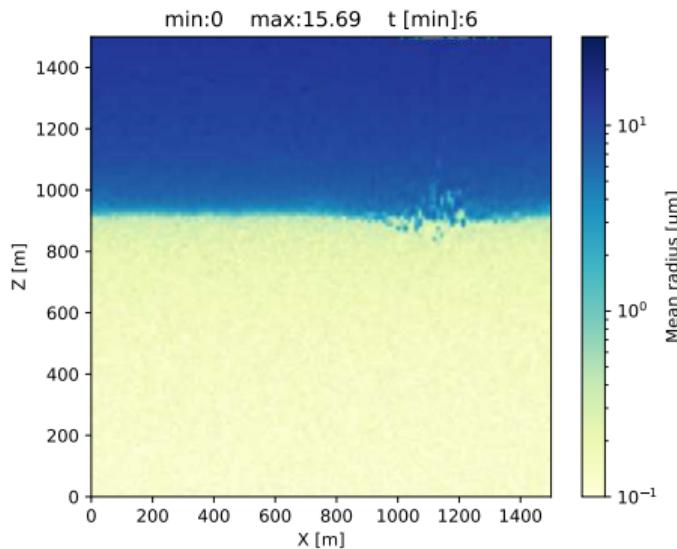
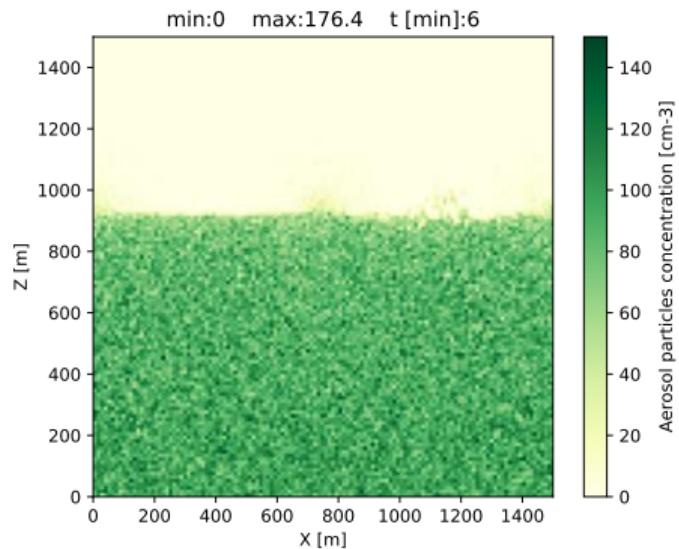
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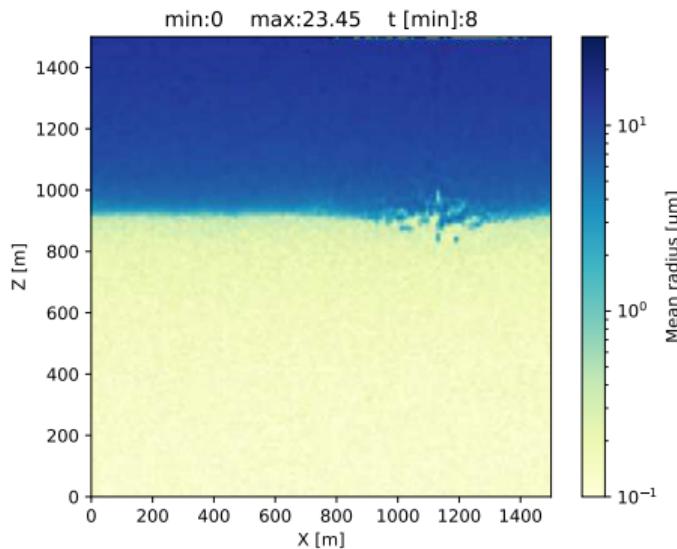
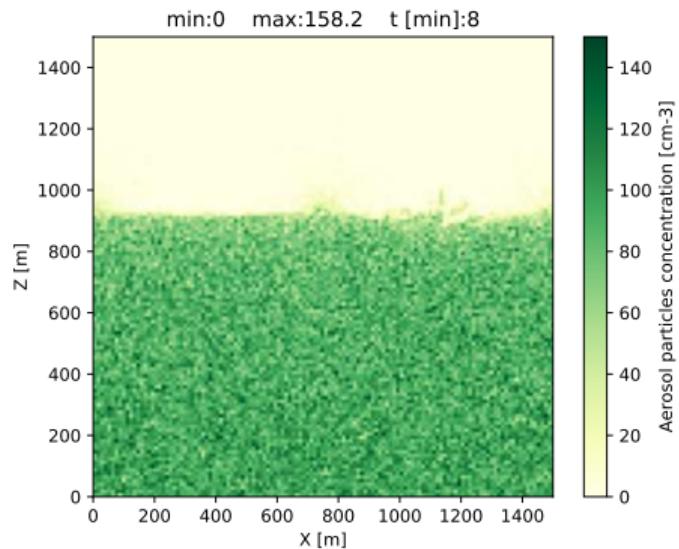
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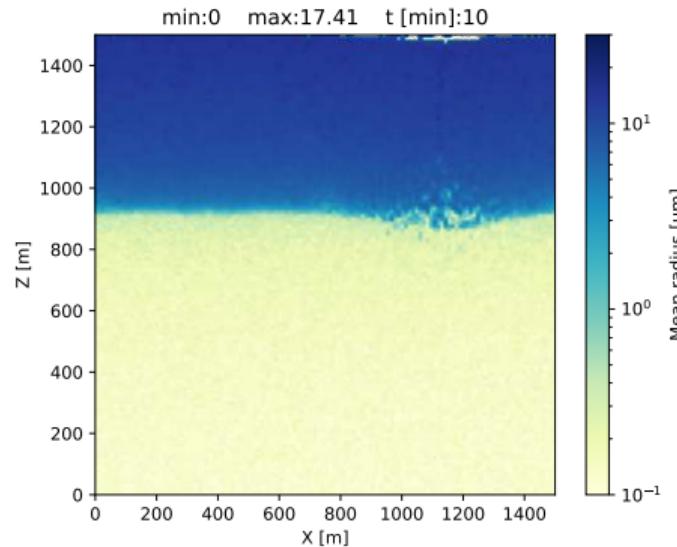
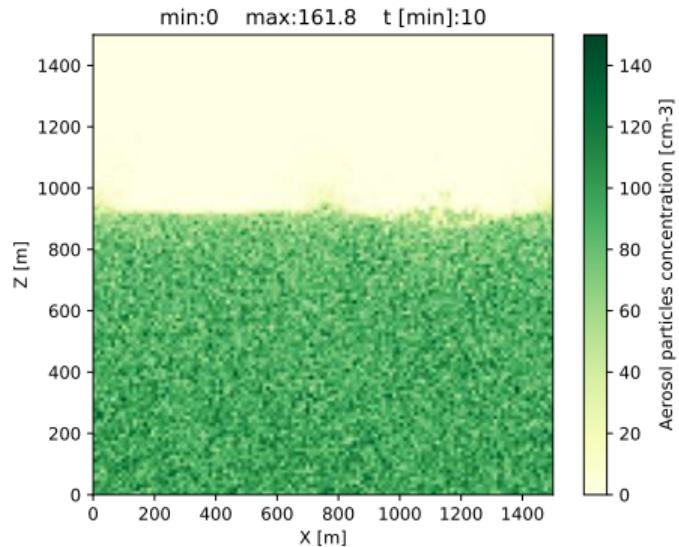
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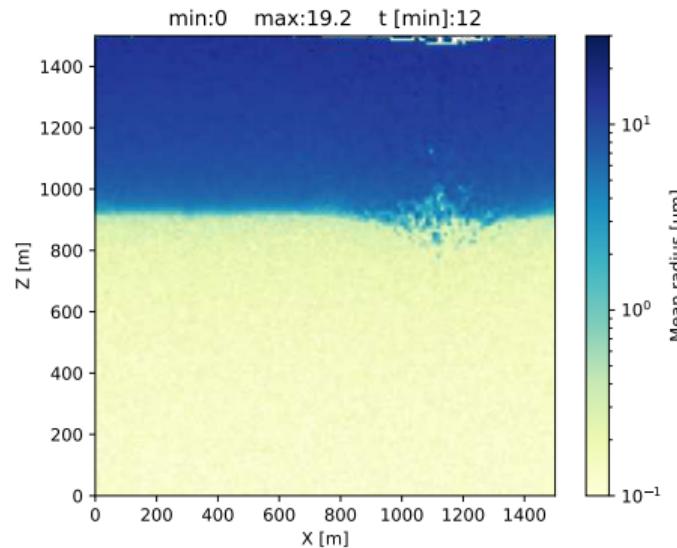
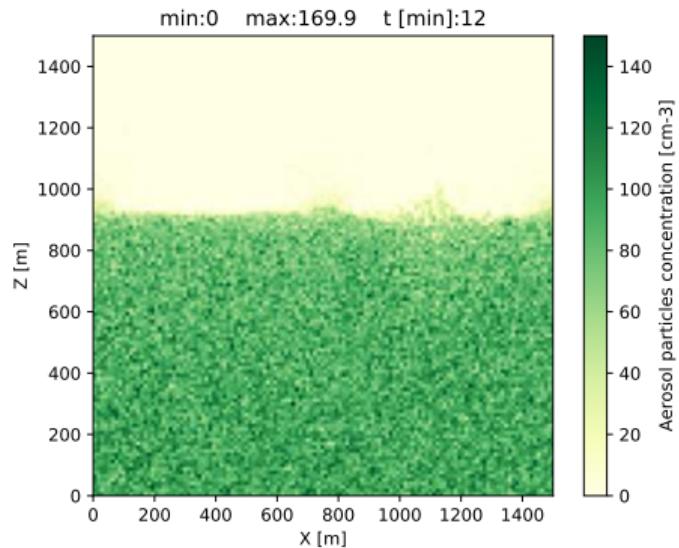
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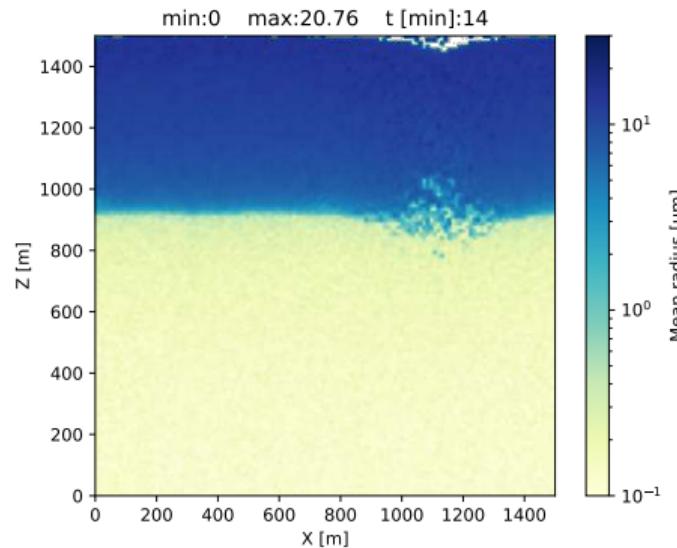
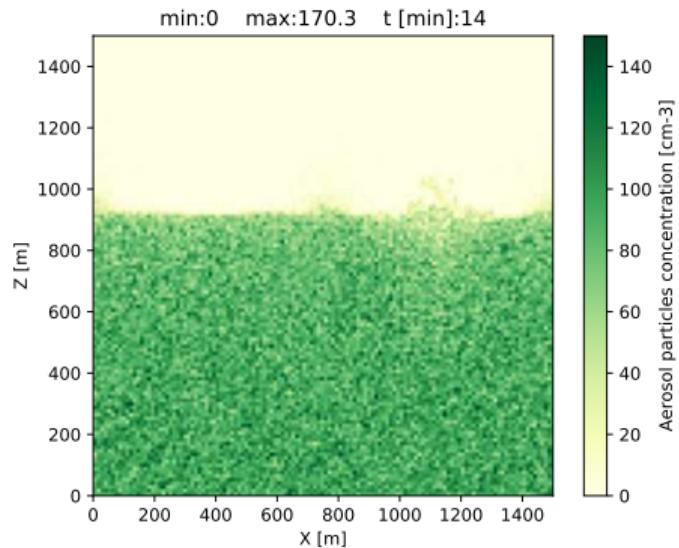
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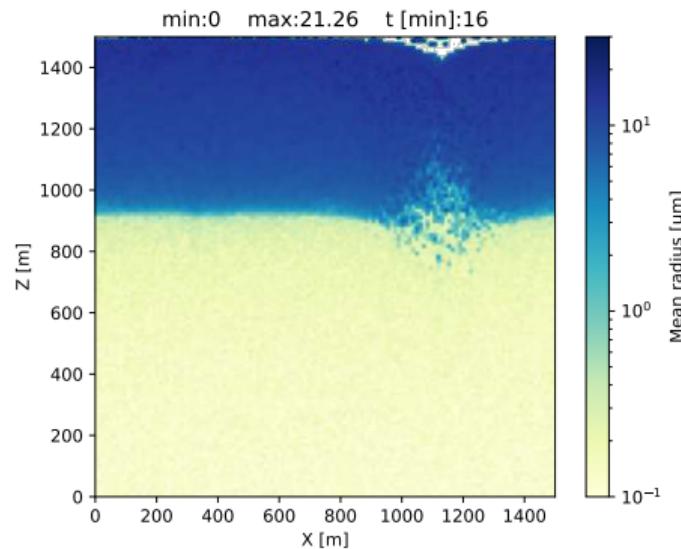
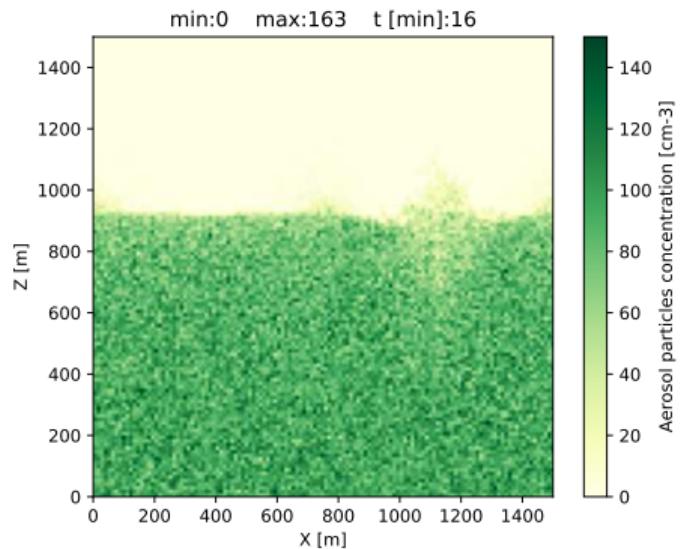
simulation & vis.: Piotr Bartman

Eulerian solver (kinematic flow) grid:  $128 \times 128$   
Lagrangian super-particles population:  $2^{21}$



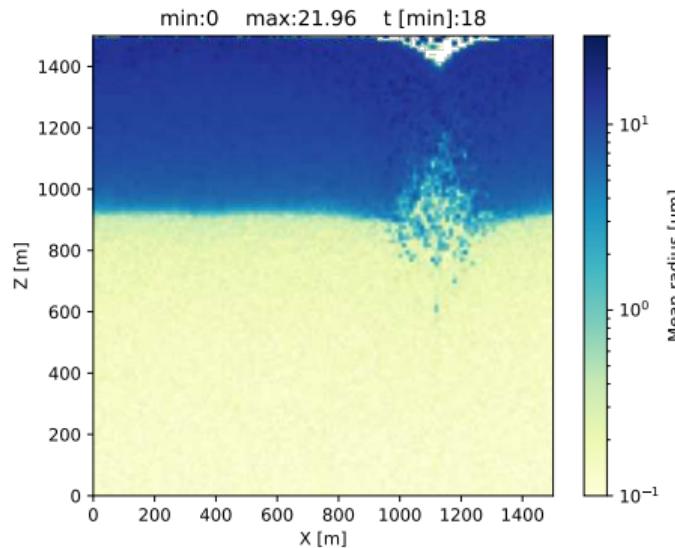
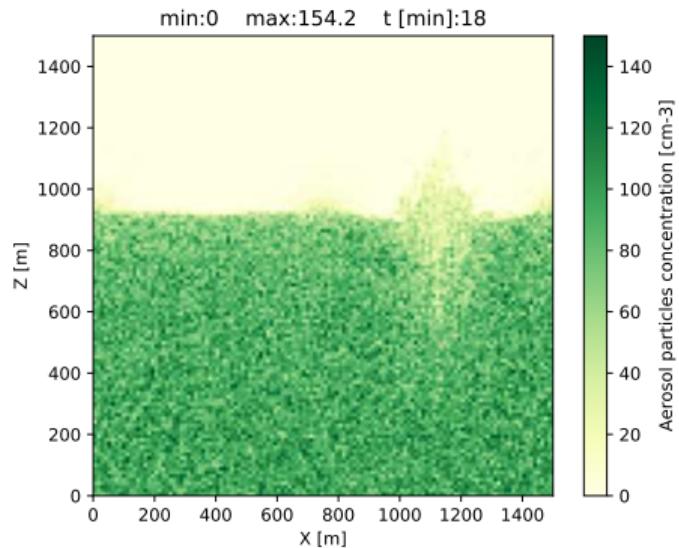
simulation & vis.: Piotr Bartman

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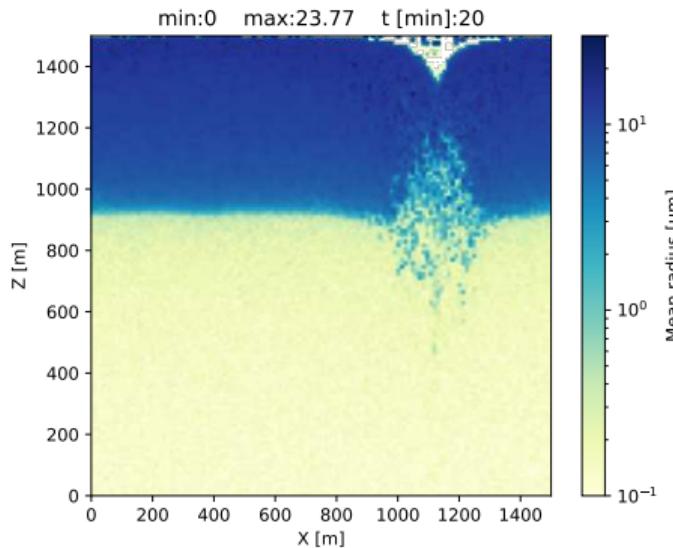
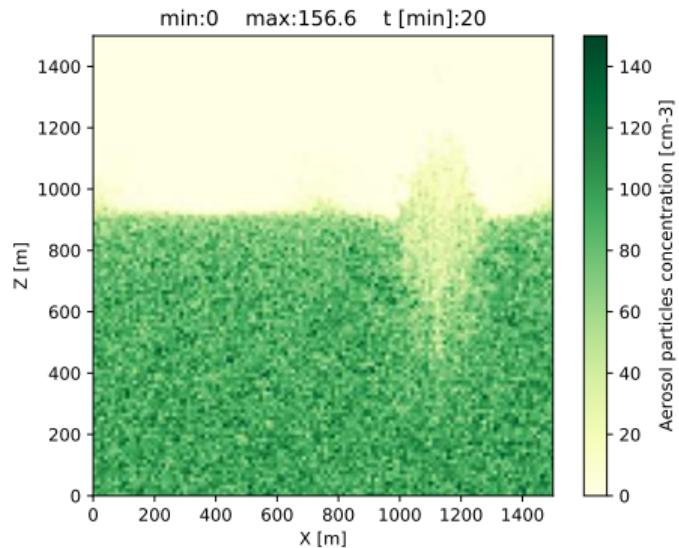
simulation & vis.: Piotr Bartman

Eulerian solver (kinematic flow) grid:  $128 \times 128$   
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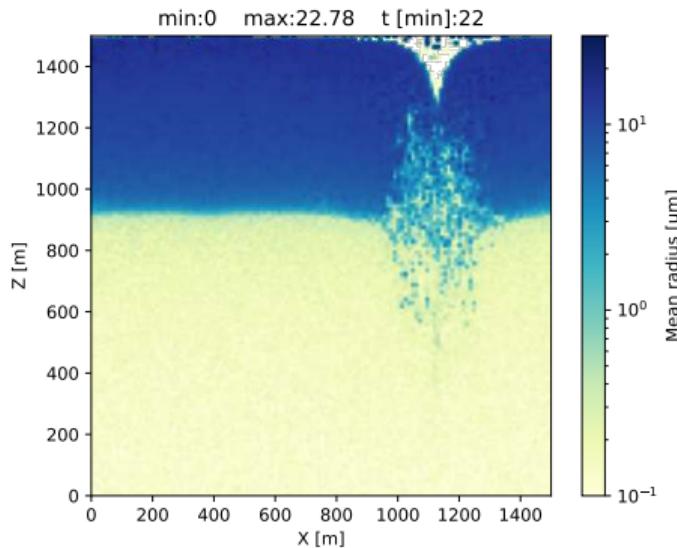
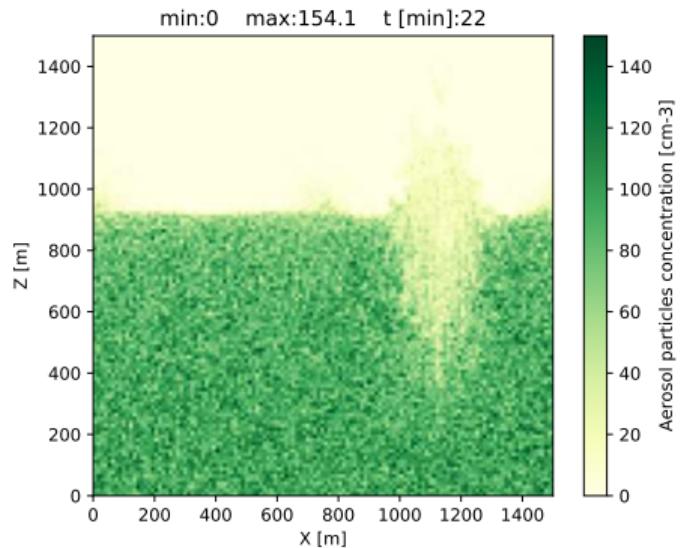
simulation & vis.: Piotr Bartman

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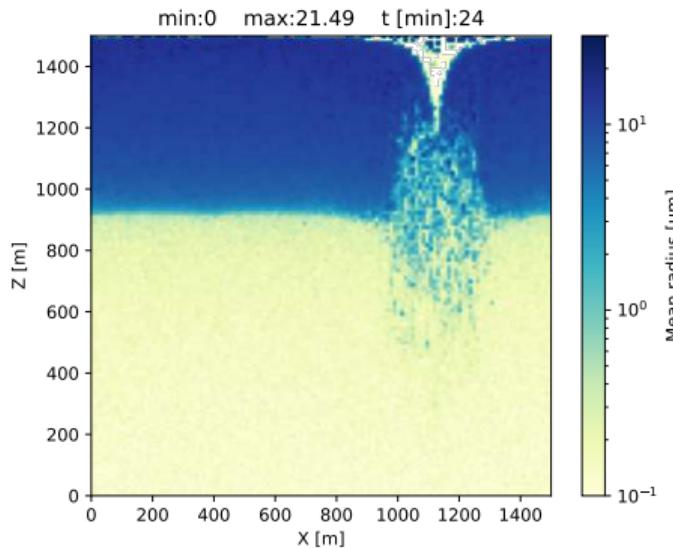
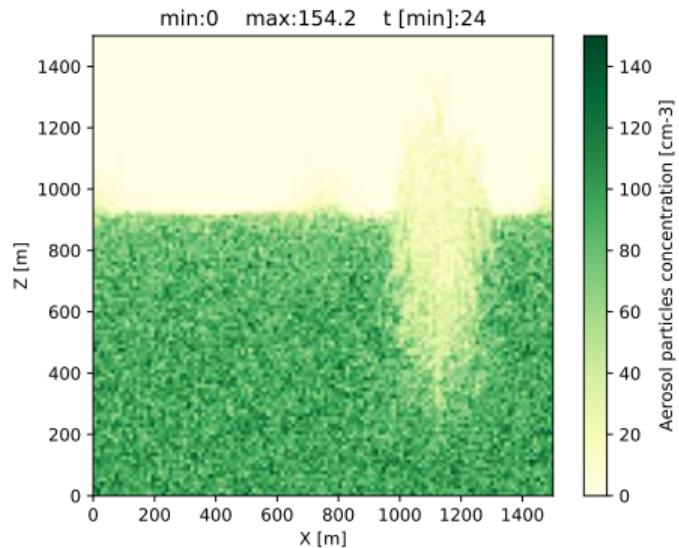
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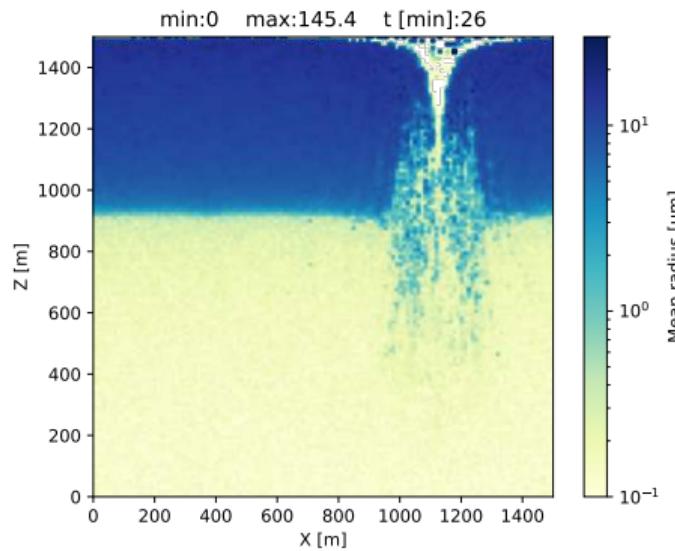
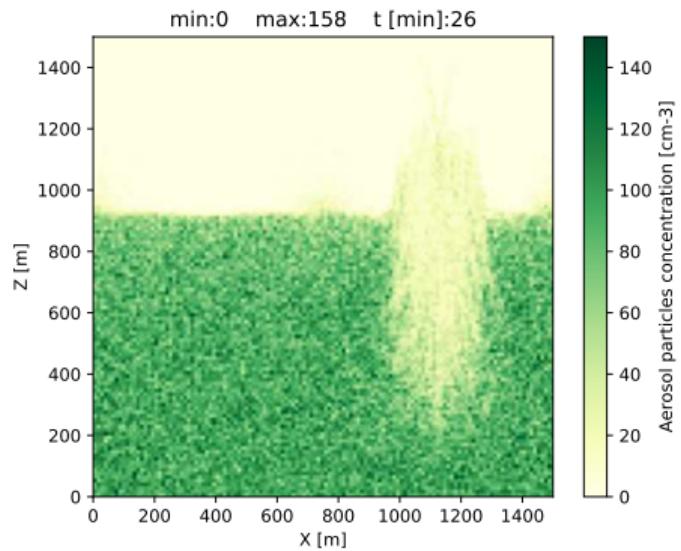
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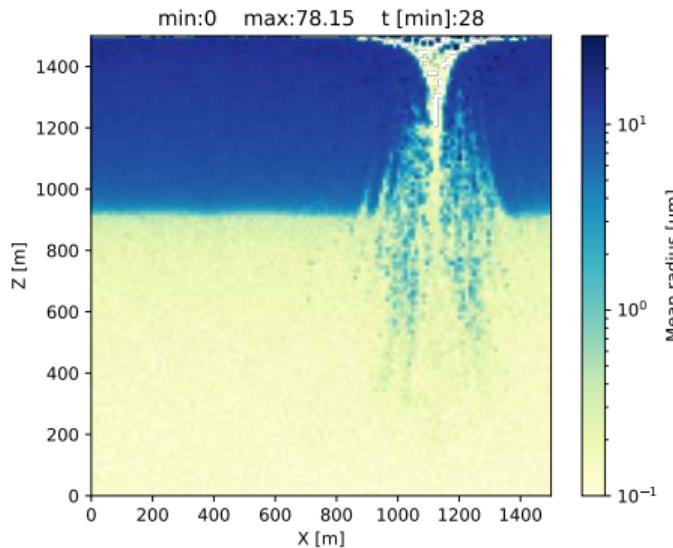
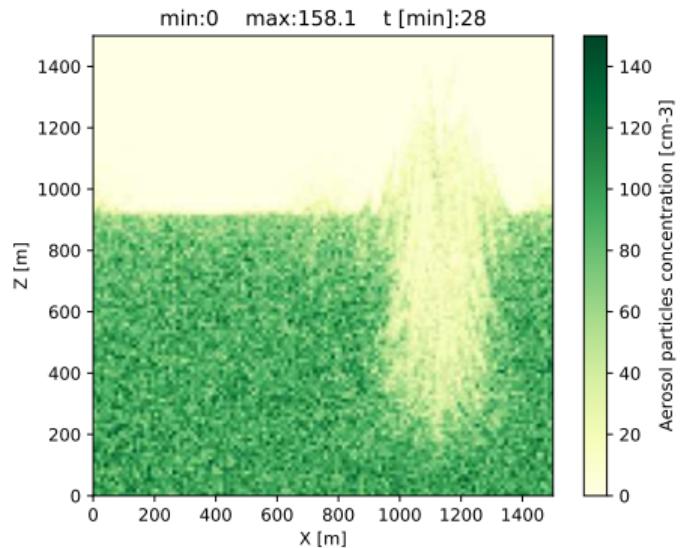
simulation & vis.: Piotr Bartman

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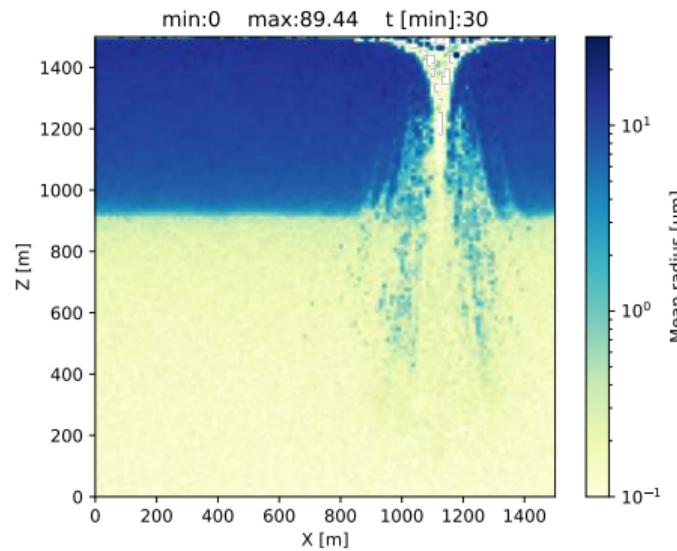
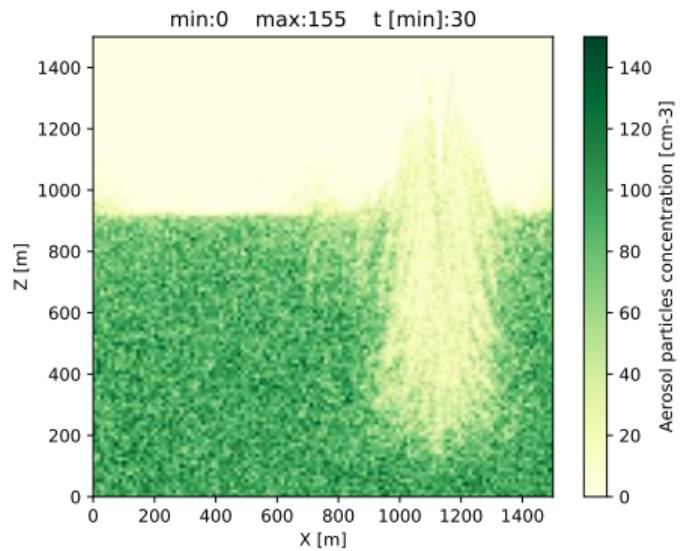
simulation & vis.: Piotr Bartman

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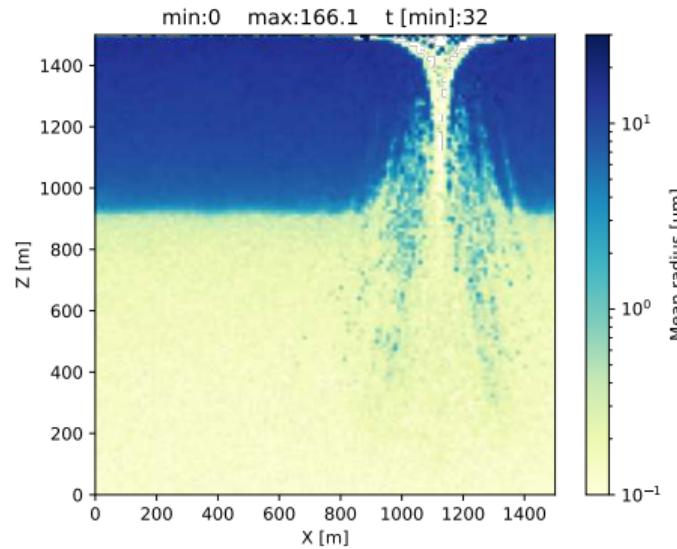
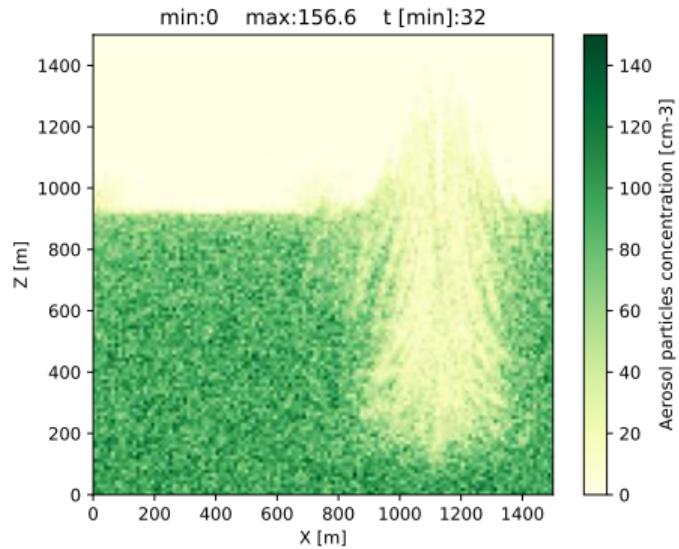
simulation & vis.: Piotr Bartman

Eulerian solver (kinematic flow) grid:  $128 \times 128$   
Lagrangian super-particles population:  $2^{21}$



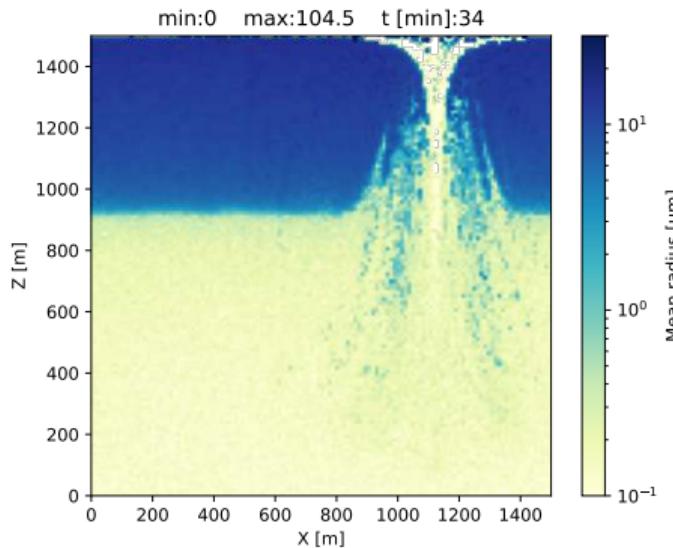
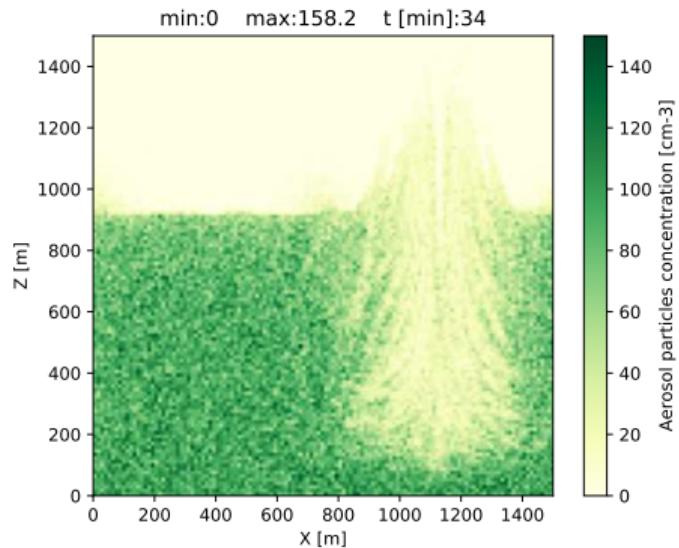
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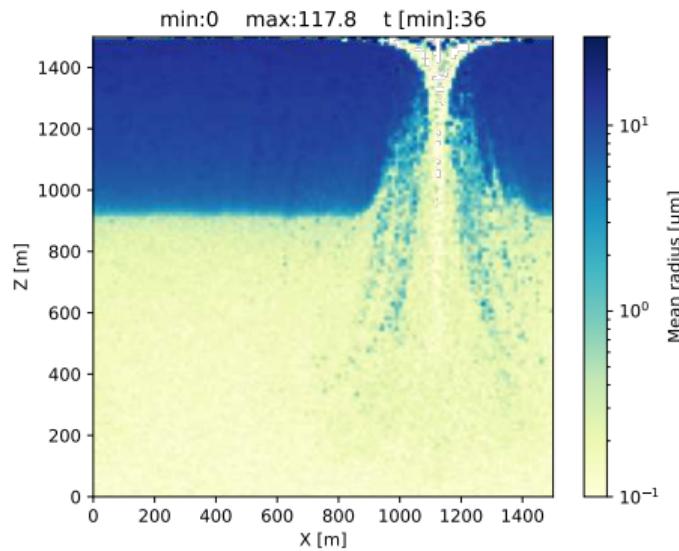
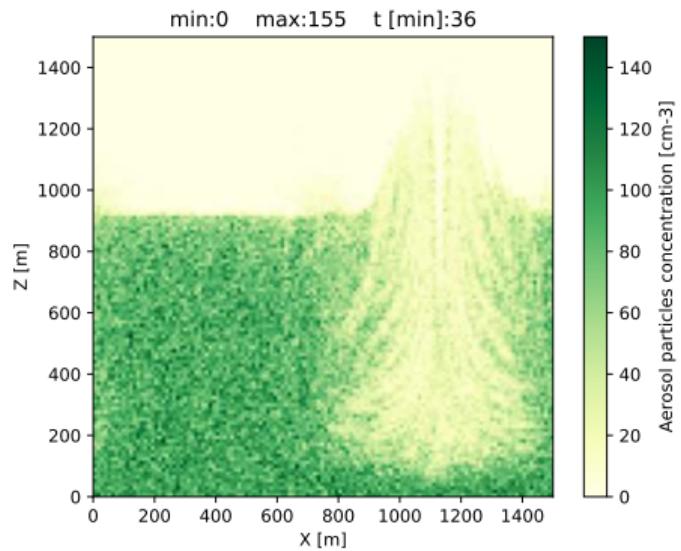
simulation & vis.: Piotr Bartman

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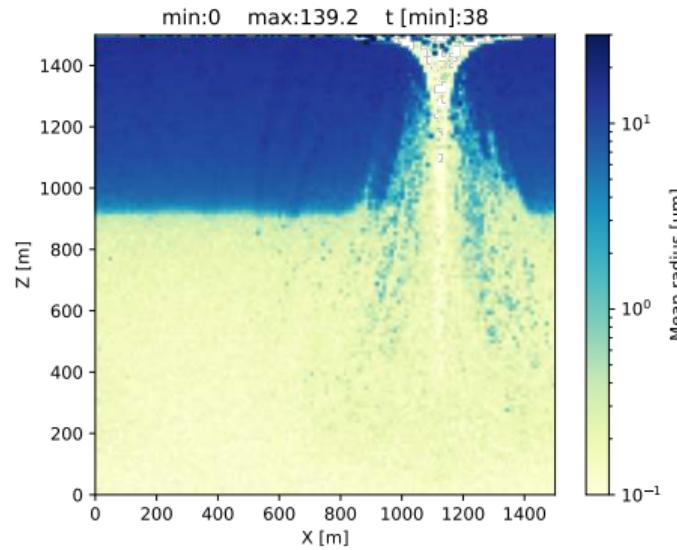
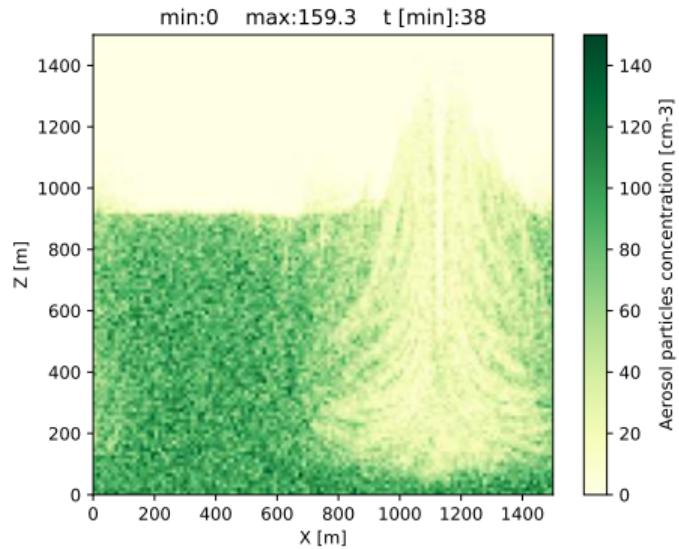
simulation & vis.: Piotr Bartman

Eulerian solver (kinematic flow) grid:  $128 \times 128$   
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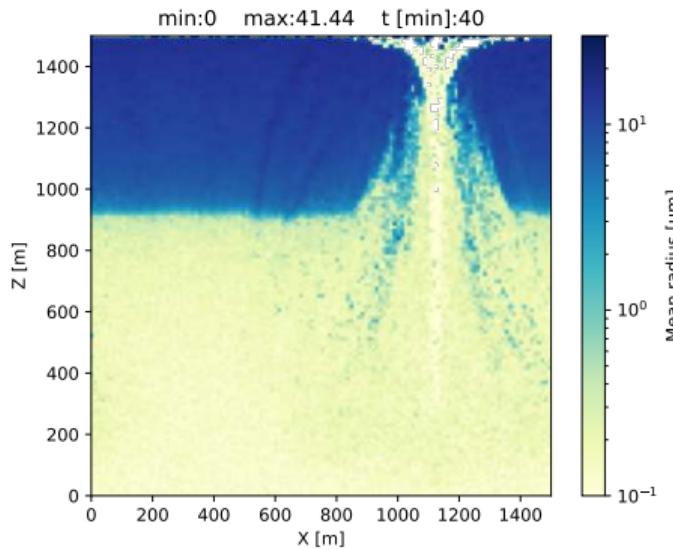
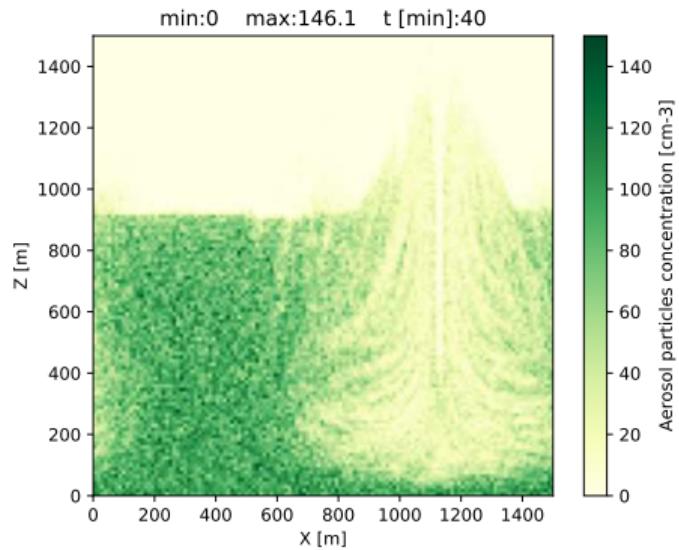
simulation & vis.: Piotr Bartman

Eulerian solver (kinematic flow) grid:  $128 \times 128$   
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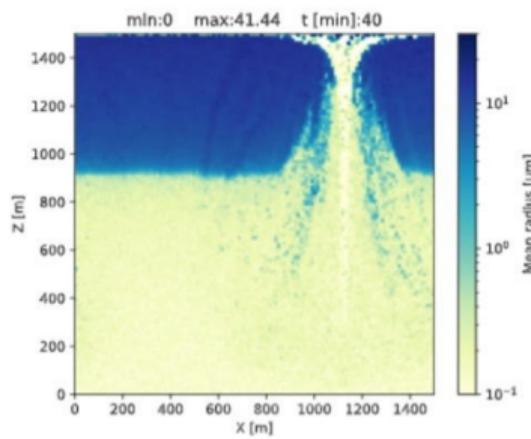
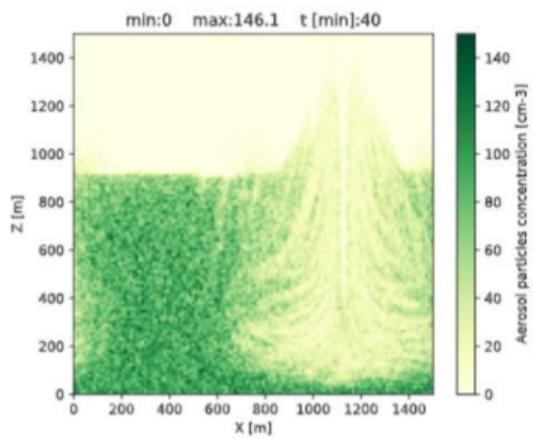


simulation & vis.: Piotr Bartman

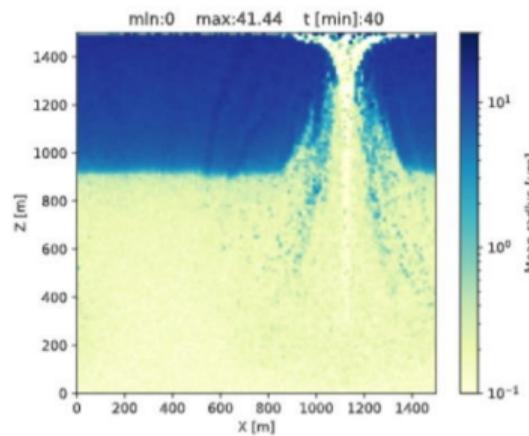
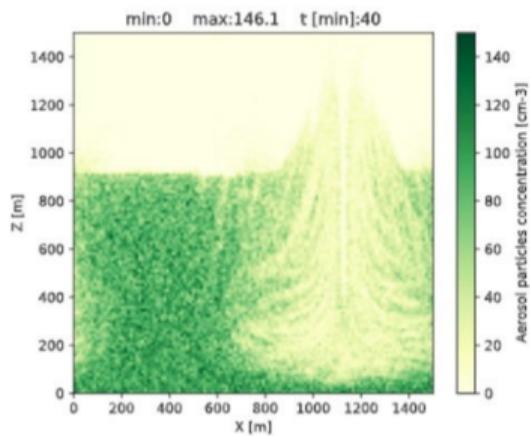
Eulerian solver (kinematic flow) grid:  $128 \times 128$   
Lagrangian super-particles population:  $2^{21}$

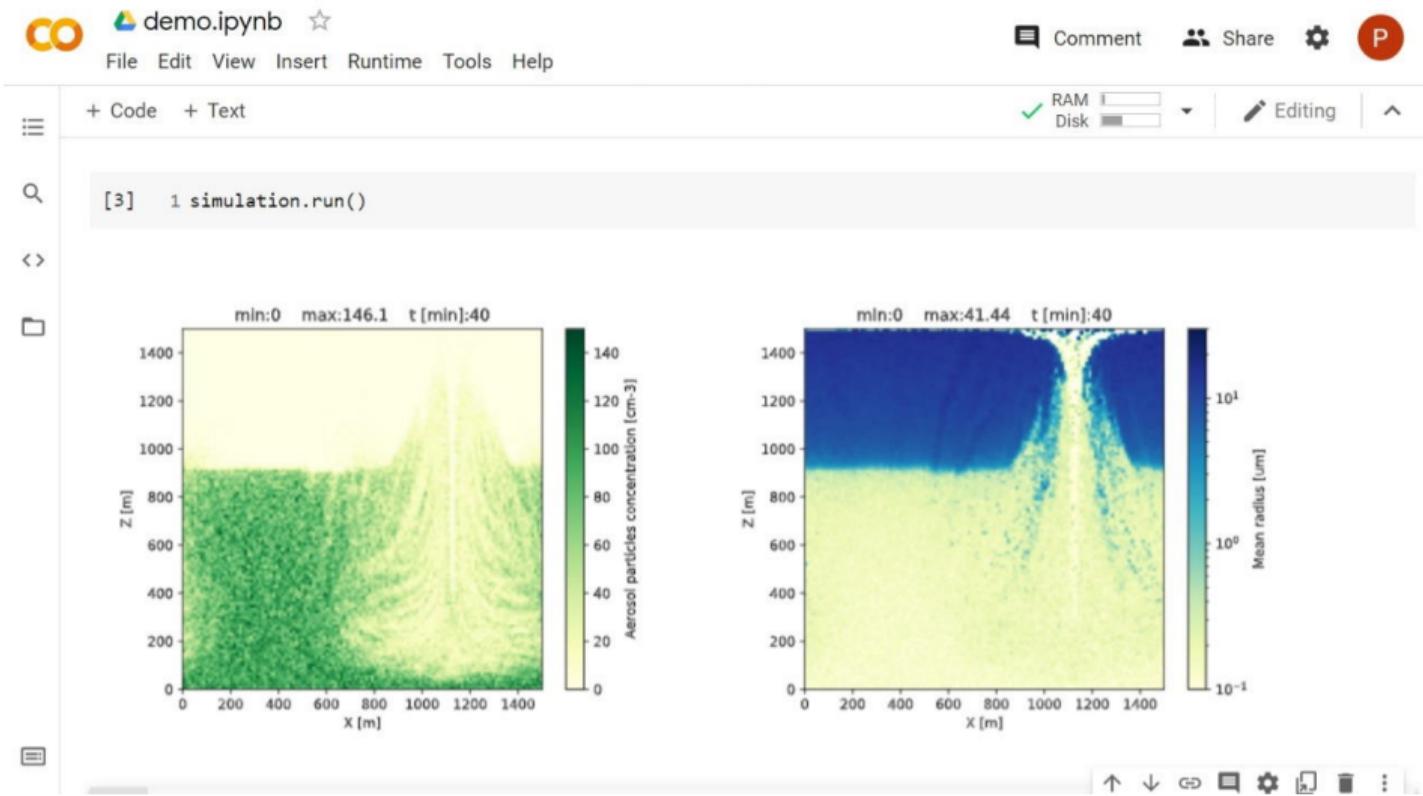


simulation & vis.: Piotr Bartman



```
[3] 1 simulation.run()
```





demo.ipynb

File Edit View Insert Runtime Tools Help All changes saved

Comment Share P

+ Code + Text

RAM Disk Editing

[3] 1 simulation.run()

Q

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□

min:0 max:146.1 t [min]

Z [m]

X [m]

Aerosol

44 t [min]:40

10<sup>1</sup>

10<sup>0</sup>

10<sup>-1</sup>

Mean radius [μm]

Notebook settings

Hardware accelerator

GPU

To get the most out of Colab, avoid using a GPU unless you need one. [Learn more](#)

Omit code cell output when saving this notebook

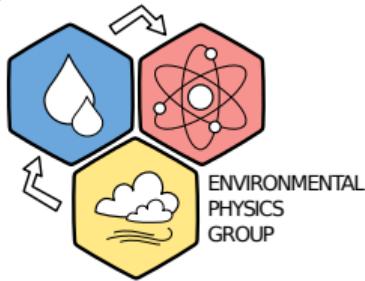
CANCEL SAVE

9/26

# PySDM: Jupyter notebooks reproducing results from literature

pypi.org/p/PySDM-examples

literature reference	cond/evap	coalescence	isotopes	breakup	transport	chemistry	freezing	keywords
<b>formulae-only</b>								
Gedzelman & Arnold 1994			x					#dynamics
Pierchala et al. 2022			x					#lab-experiment
...								
<b>OD box environment</b>								
Berry 1967		x						#kernels
Shima et al. 2009		x						#analytic-solution
Alpert & Knopf 2016						x		#ABIFM
de Jong et al. 2023		x		x				#analytic-solution
...								
<b>OD parcel environment</b>								
Rozanski & Sonntag 1982	x		x					#iterative-parcel
Abdul-Razzak & Ghan 2000	x							#pysdm-vs-gcm-param
Kreidenweis et al. 2003	x				x			#Hoppel-gap
Arabas and Shima 2017	x							#dynamics
Jensen and Nugent 2017	x							#giant-CCN
Yang et al. 2018	x							#ripening
Lowe et al. 2019	x							#surfactants
Grabowski and Pawlowska 2023	x							#ripening
...								
<b>1D single-column kinematic env. (advection: PyMPDATA)</b>								
Shipway & Hill 2012	x	x			x			#KiD
deJong et al. 2023 (figures 6-8)	x	x		x	x			#KiD
...								
<b>2D prescribed-flow environment (advection: PyMPDATA)</b>								
Arabas et al. 2015	x	x			x			#GUI
Arabas et al. 2023 (figure 11)	x	x			x	x		#Paraview





■ IAEA/GNIP site in Kraków

The Global Network of Isotopes in Precipitation (GNIP) is a worldwide isotope monitoring network of hydrogen and oxygen isotopes in precipitation, initiated in 1960 by the International Atomic Energy Agency (IAEA) and the World Meteorological Organization (WMO), and operates in cooperation with numerous partner institutions in Member States.

Press centre Employment Contact



- ❑ IAEA/GNIP site in Kraków
- ❑ 50-year precip isotopic data record

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- ▶ IAEA/GNIP site in Kraków
- ▶ 50-year precip isotopic data record
- ▶ high-altitude lab (clouds in-situ)  
@Kasprowy Wierch (1987 m AMSL)

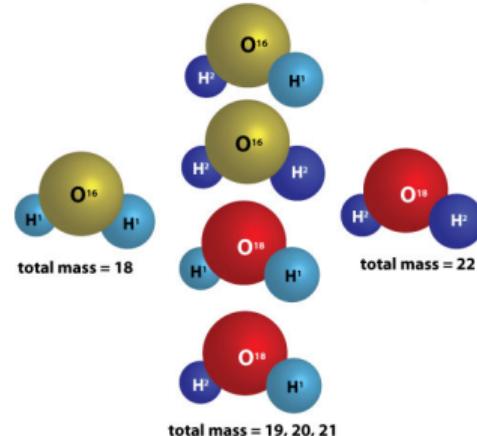


photo: naukaoklimacie.pl

# clouds from a water isotopic point of view

- water isotopologues (stable):  $\text{H}_2\text{O}$  (99.7%),  
 $\text{H}_2^{18}\text{O}$  (0.2%),  $\text{HDO}$  (0.03%),  $\text{H}_2^{17}\text{O}$  (0.04%), ...

Oxygen and hydrogen isotopes in water  
Light  $\xrightarrow{\hspace{1cm}}$  Heavy

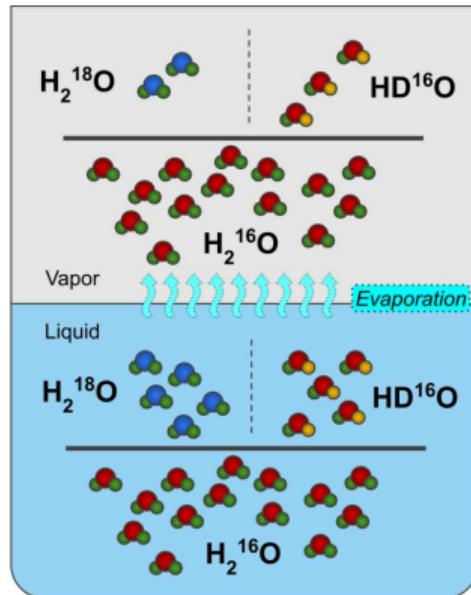


graphic: usgs.gov

$$M_v \approx 18.015 \text{ g/mol}$$

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- condensation “favors” heavy over light isotopologues (evaporation vice versa)
  - equilibrium fractionation
  - more pronounced in colder temperatures
  - larger ( $\times 8$ ) effect for H than O



graphic: scisnack.com

$$\alpha_{\text{eq}}^{\text{HDO}}(20^\circ\text{C}) = e_s^{\text{light}} / e_s^{\text{heavy}} \approx 1.08$$

$$\alpha_{\text{eq}}^{\text{H}_2^{18}\text{O}}(20^\circ\text{C}) \approx 1.01$$

# clouds from a water isotopic point of view

- water isotopologues (stable):  $\text{H}_2\text{O}$  (99.7%),  $\text{H}_2^{18}\text{O}$  (0.2%), HDO (0.03%),  $\text{H}_2^{17}\text{O}$  (0.04%), ...
- condensation “favors” heavy over light isotopologues (evaporation vice versa)
  - equilibrium fractionation
  - more pronounced in colder temperatures
  - larger ( $\times 8$ ) effect for H than O
- differences in diffusivity in air
  - non-equilibrium (kinetic) fractionation
  - applies to sub- and super-saturated conditions
  - more pronounced for O than H

$$\frac{\alpha_{\text{eff}}}{\alpha_{\text{eq}}} - 1 \approx n \cdot \left(1 - \frac{D^{\text{heavy}}}{D^{\text{light}}}\right) \cdot (1 - RH)$$

$\alpha_{\text{eff}}$  effective fractionation coeff.

$n$  turbulence parameter

$D$  diffusion coeffs:

$$\text{HDO: } (1 - D^{\text{heavy}} / D^{\text{light}}) \Big|_{T=20^\circ\text{C}} \approx 2.5\%$$

$$\text{H}_2^{18}\text{O: } (1 - D^{\text{heavy}} / D^{\text{light}}) \Big|_{T=20^\circ\text{C}} \approx 2.9\%$$

$RH$  rel. humidity

## precipitating cloud as an isotopic distillation column



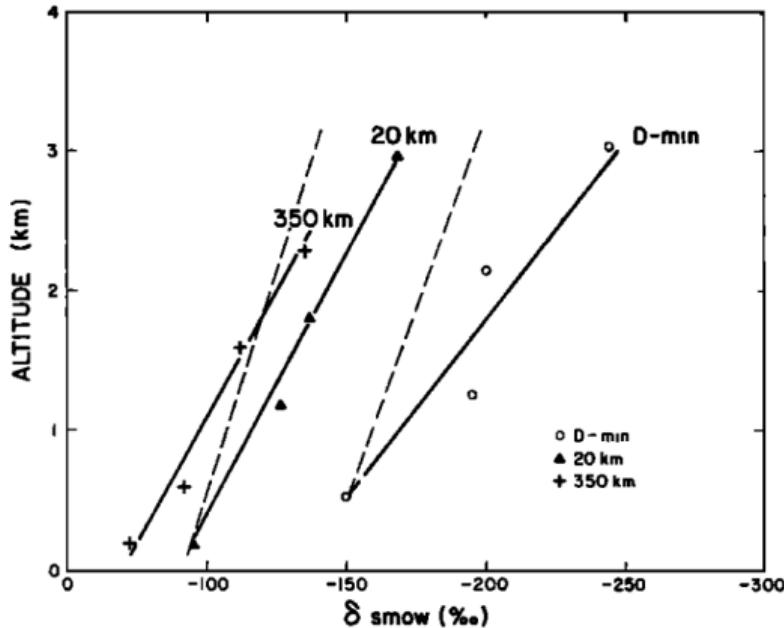
(photo: Yevgen Timashov / National Geographic; Ai-Petri, Crimea, Ukraine)

# clouds from a water isotopic point of view

literature reference	cond/evap	coalescence	isotopes	breakup	transport	chemistry	freezing	keywords
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Arabas et al. 2023 (figure 11)	x	x			x	x		#Paraview

# Rozanski & Sonntag '82 – iterative parcel PySDM setup

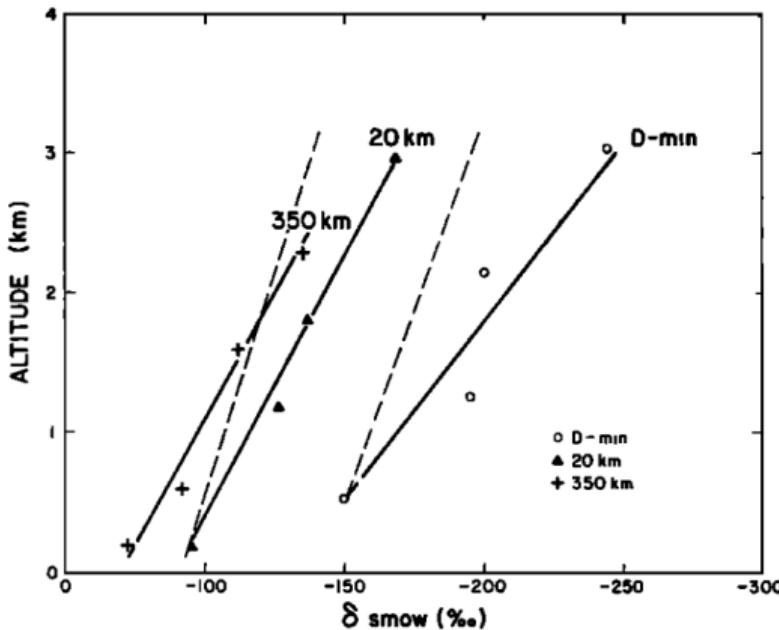
Ehhalt & Östlund 1970



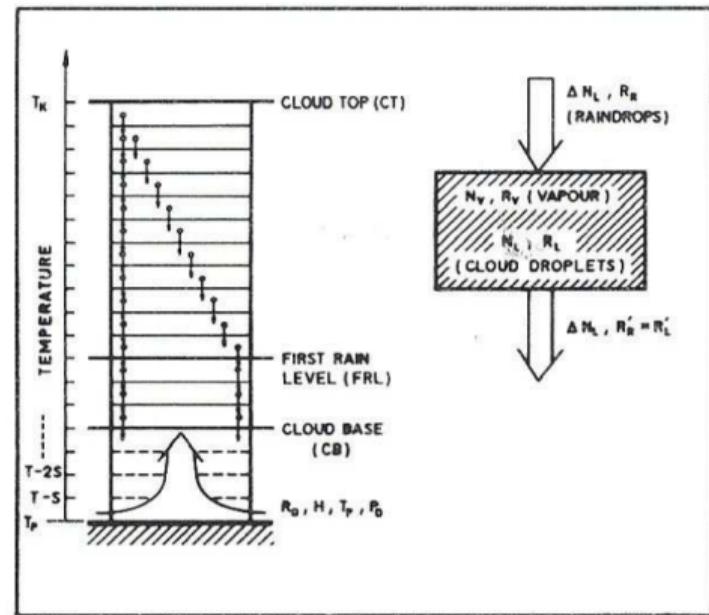
$$\delta_{\text{SMOW}} = \frac{[\text{heavy}]/[\text{light}]|_{\text{sample}}}{[\text{heavy}]/[\text{light}]|_{\text{standard}}} - 1$$

# Rozanski & Sonntag '82 – iterative parcel PySDM setup

Ehhalt & Östlund 1970



Rozanski & Sonntag 1982



# Rozanski & Sonntag '82 – iterative parcel PySDM setup<sup>a</sup>

<sup>a</sup>launch-in-the-cloud URL: [https://mybinder.org/v2/gh/slayoo/PySDM.git/isotopes\\_rozanski\\_and\\_sonntag\\_example?urlpath=lab/tree/examples/PySDM\\_examples](https://mybinder.org/v2/gh/slayoo/PySDM.git/isotopes_rozanski_and_sonntag_example?urlpath=lab/tree/examples/PySDM_examples)

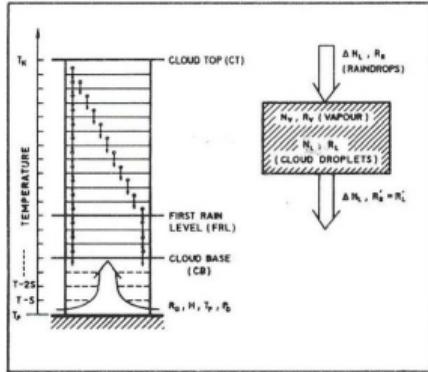


Fig. 3. Schematic diagram of the multibox cloud model.  
Input data: initial temperature,  $T_p$ ; final temperature,  $T_k$ ;  
initial pressure,  $P_0$ ; relative humidity,  $H$ ; initial isotopic  
composition of water vapour,  $R_0$ ; cloud water mixing ratio,  
 $N_L$ ; temperature step,  $S$ ; isotope exchange factor,  
 $K$ .

Tellus 34 (1982), 2

# Rozanski & Sonntag '82 – iterative parcel PySDM setup<sup>a</sup>

<sup>a</sup>launch-in-the-cloud URL: [https://mybinder.org/v2/gh/slayoo/PySDM.git/isotopes\\_rozanski\\_and\\_sonntag\\_example?urlpath=lab/tree/examples/PySDM\\_examples](https://mybinder.org/v2/gh/slayoo/PySDM.git/isotopes_rozanski_and_sonntag_example?urlpath=lab/tree/examples/PySDM_examples)

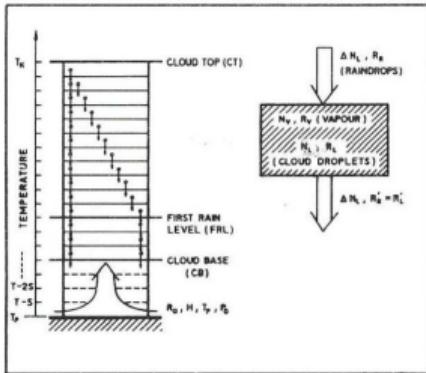


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Tellus 34 (1982), 2

hydrostatic/adiabatic rainshaft with precip removal

# Rozanski & Sonntag '82 – iterative parcel PySDM setup<sup>a</sup>

<sup>a</sup>launch-in-the-cloud URL: [https://mybinder.org/v2/gh/slayoo/PySDM.git/isotopes\\_rozanski\\_and\\_sonntag\\_example?urlpath=lab/tree/examples/PySDM\\_examples](https://mybinder.org/v2/gh/slayoo/PySDM.git/isotopes_rozanski_and_sonntag_example?urlpath=lab/tree/examples/PySDM_examples)

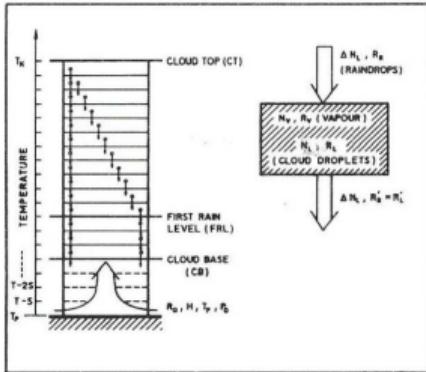


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- hydrostatic/adiabatic rainshaft with precip removal
- condensation: saturation adjustment

# Rozanski & Sonntag '82 – iterative parcel PySDM setup<sup>a</sup>

<sup>a</sup>launch-in-the-cloud URL: [https://mybinder.org/v2/gh/slayoo/PySDM.git/isotopes\\_rozanski\\_and\\_sonntag\\_example?urlpath=lab/tree/examples/PySDM\\_examples](https://mybinder.org/v2/gh/slayoo/PySDM.git/isotopes_rozanski_and_sonntag_example?urlpath=lab/tree/examples/PySDM_examples)

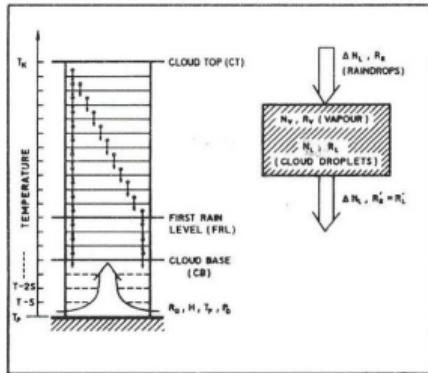


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Tellus 34 (1982), 2

- ▶ hydrostatic/adiabatic rainshaft with precip removal
- ▶ condensation: saturation adjustment
- ▶ rain formation: liquid water content threshold

# Rozanski & Sonntag '82 – iterative parcel PySDM setup<sup>a</sup>

<sup>a</sup>launch-in-the-cloud URL: [https://mybinder.org/v2/gh/slayoo/PySDM.git/isotopes\\_rozanski\\_and\\_sonntag\\_example?urlpath=lab/tree/examples/PySDM\\_examples](https://mybinder.org/v2/gh/slayoo/PySDM.git/isotopes_rozanski_and_sonntag_example?urlpath=lab/tree/examples/PySDM_examples)

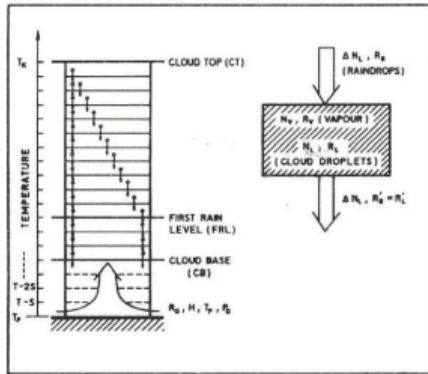


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- hydrostatic/adiabatic rainshaft with precip removal
- condensation: saturation adjustment
- rain formation: liquid water content threshold
- parcel-model iterations towards stationary state  
(no explicit role of time)

# Rozanski & Sonntag '82 – iterative parcel PySDM setup<sup>a</sup>

<sup>a</sup>launch-in-the-cloud URL: [https://mybinder.org/v2/gh/slayoo/PySDM.git/isotopes\\_rozanski\\_and\\_sonntag\\_example?urlpath=lab/tree/examples/PySDM\\_examples](https://mybinder.org/v2/gh/slayoo/PySDM.git/isotopes_rozanski_and_sonntag_example?urlpath=lab/tree/examples/PySDM_examples)

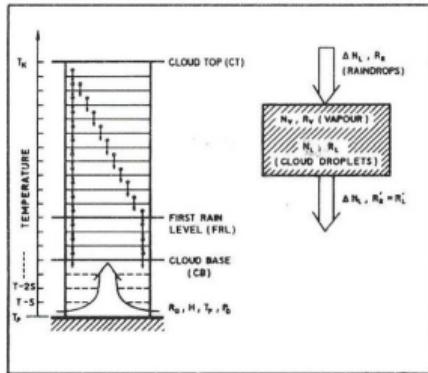


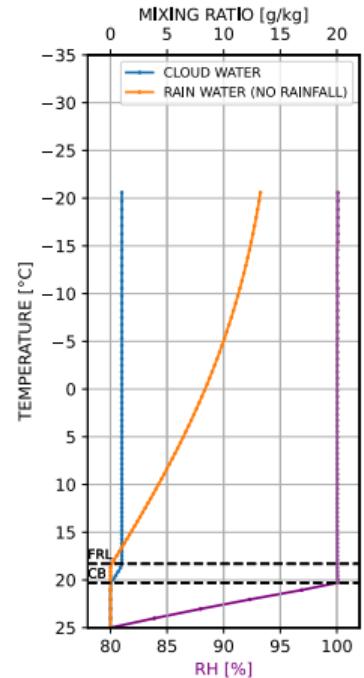
Fig. 3. Schematic diagram of the multibox cloud model. Input data: initial temperature,  $T_p$ ; final temperature,  $T_k$ ; initial pressure,  $P_0$ ; relative humidity,  $H$ ; initial isotopic composition of water vapour,  $R_0$ ; cloud water mixing ratio,  $N_L$ ; temperature step,  $S$ ; isotope exchange factor,  $K$ .

Tellus 34 (1982), 2

- hydrostatic/adiabatic rainshaft with precip removal
- condensation: saturation adjustment
- rain formation: liquid water content threshold
- parcel-model iterations towards stationary state (no explicit role of time)
- minimal model for capturing isotope exchange between precip, ambient vapor and cloud water (↔ hypothesis explaining observed steep  $\delta^2\text{H}$  profile gradients beyond condensation-only effects)

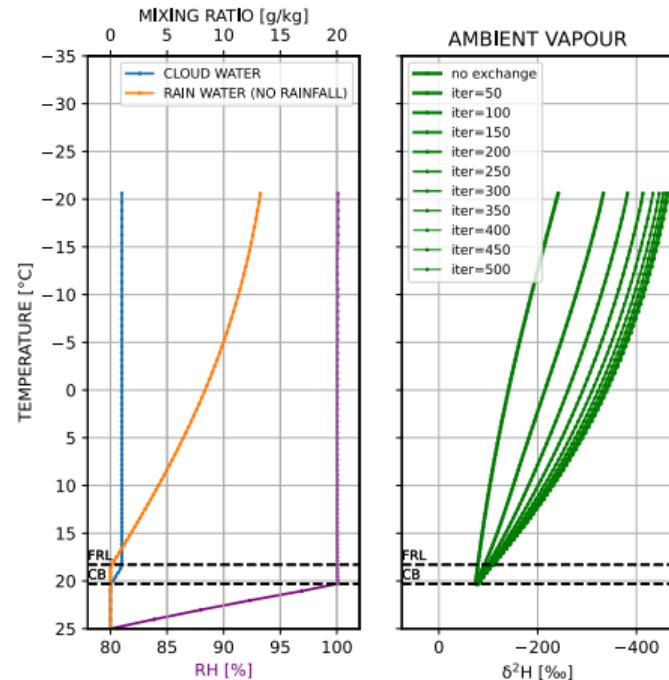
# Rozanski & Sonntag '82 – iterative parcel PySDM setup<sup>a</sup>

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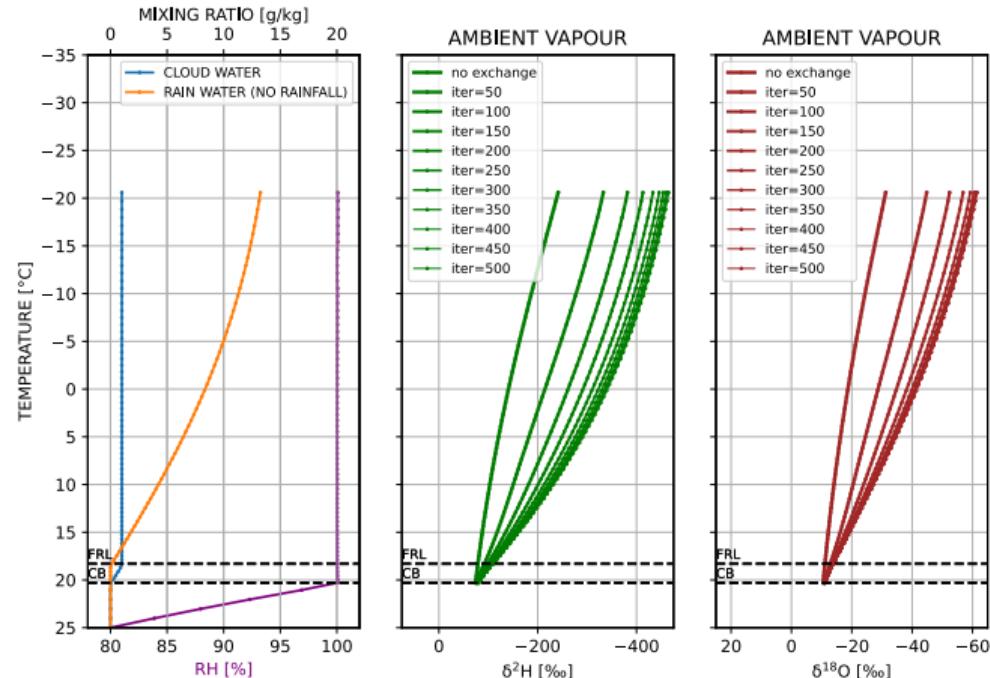
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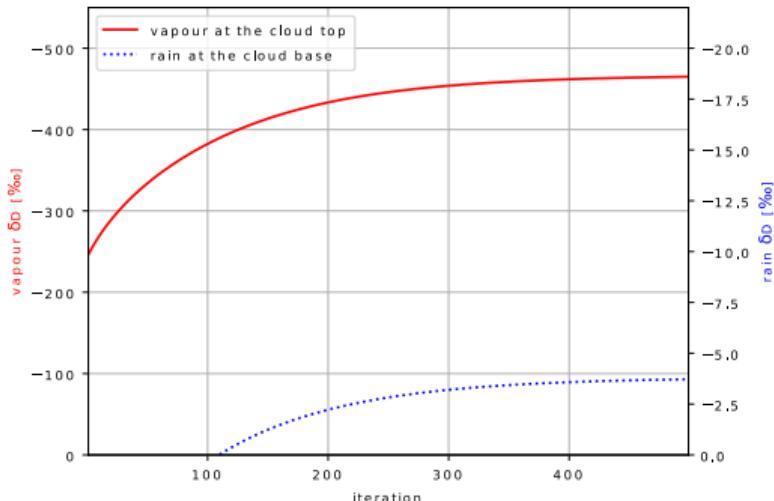
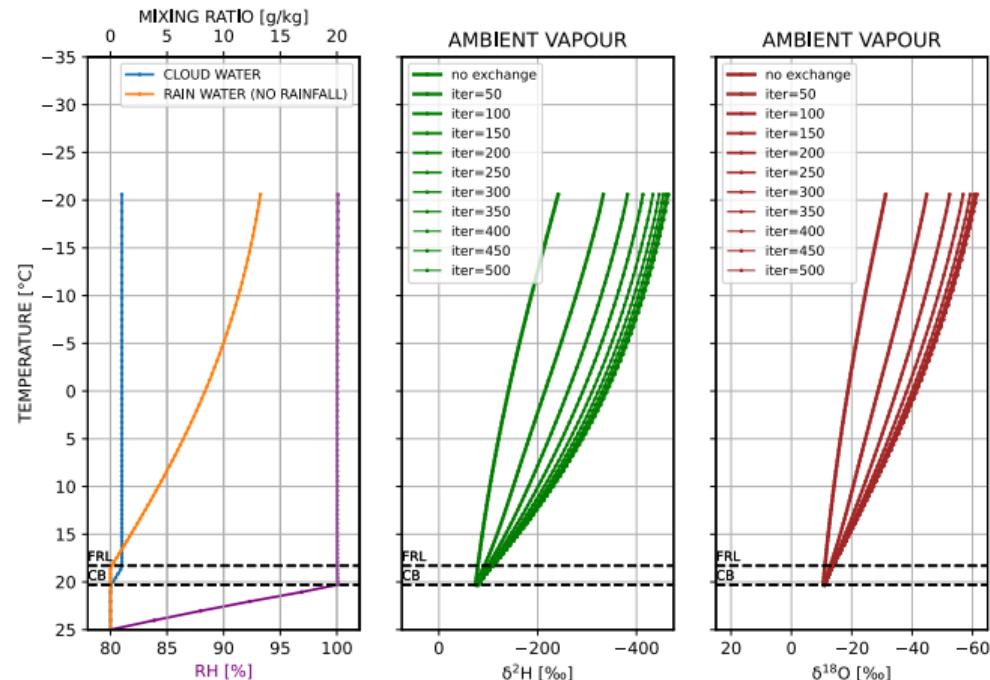
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# Rozanski & Sonntag '82 – iterative parcel PySDM setup

literature reference	cond/evap	coalescence	isotopes	breakup	transport	chemistry	freezing	keywords
<b>formulae-only</b>								
Gedzelman & Arnold 1994			x					#dynamics
Pierchala et al. 2022			x					#lab-experiment
...								
<b>OD box environment</b>								
Berry 1967		x						#kernels
Shima et al. 2009		x						#analytic-solution
Alpert & Knopf 2016						x		#ABIFM
de Jong et al. 2023		x		x				#analytic-solution
...								
<b>OD parcel environment</b>								
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Abdul-Razzak & Ghan 2000	x							#pysdm-vs-gcm-param
Kreidenweis et al. 2003	x				x			#Hoppel-gap
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Jensen and Nugent 2017	x							#giant-CCN
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...								
<b>1D single-column kinematic env. (advection: PyMPDATA)</b>								
Shipway & Hill 2012	x	x			x			#KiD
deJong et al. 2023 (figures 6-8)	x	x		x	x			#KiD
...								
<b>2D prescribed-flow environment (advection: PyMPDATA)</b>								
Arabas et al. 2015	x	x			x			#GUI
Arabas et al. 2023 (figure 11)	x	x			x	x		#Paraview

<sup>a</sup>launch-in-the-cloud URL: [https://mybinder.org/v2/gh/open-atmos/PySDM.git/main?urlpath=lab/tree/examples/PySDM\\_examples/Pierchala\\_et\\_al\\_2022](https://mybinder.org/v2/gh/open-atmos/PySDM.git/main?urlpath=lab/tree/examples/PySDM_examples/Pierchala_et_al_2022)

doi:10.1016/j.gca.2022.01.020

Geochimica et Cosmochimica Acta 322 (2022) 244–259

[www.elsevier.com/locate/gca](http://www.elsevier.com/locate/gca)

## Quantification the diffusion-induced fractionation of $^1\text{H}_2^{17}\text{O}$ isotopologue in air accompanying the process of water evaporation

Anna Pierchala <sup>\*</sup>, Kazimierz Rozanski, Marek Dulinski, Zbigniew Gorczyca

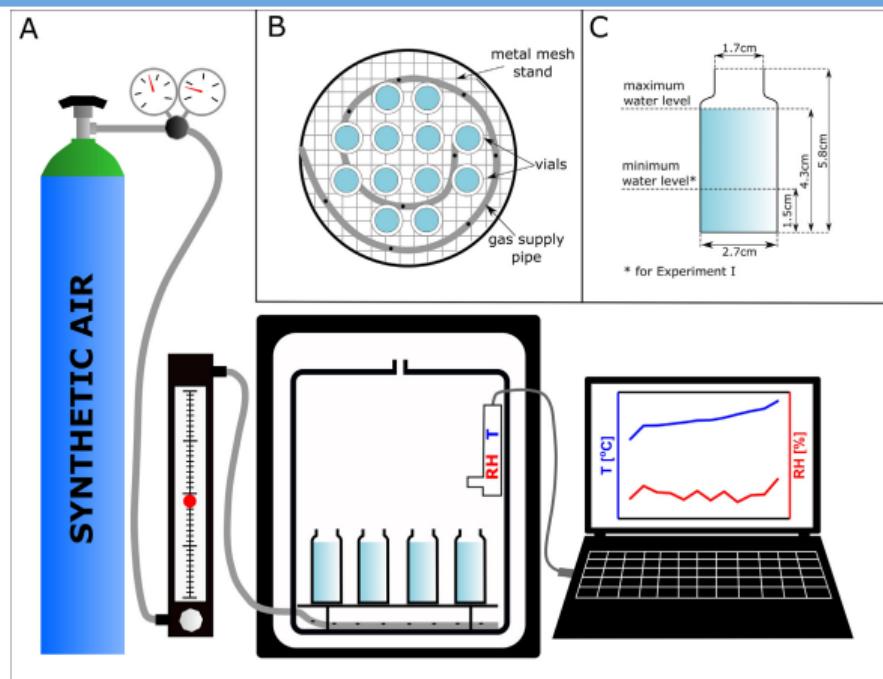
AGH University of Science and Technology, Faculty of Physics and Applied Computer Science, al. Mickiewicza 30, 30-059 Krakow, Poland

Received 25 February 2021; accepted in revised form 15 January 2022; Available online 24 January 2022

# Pierchala et al. '22 – triple isotope / kinetic fract. PySDM setup<sup>a</sup>

<sup>a</sup>launch-in-the-cloud URL: [https://mybinder.org/v2/gh/open-atmos/PySDM.git/main?urlpath=lab/tree/examples/PySDM\\_examples/Pierchala\\_et\\_al\\_2022](https://mybinder.org/v2/gh/open-atmos/PySDM.git/main?urlpath=lab/tree/examples/PySDM_examples/Pierchala_et_al_2022)

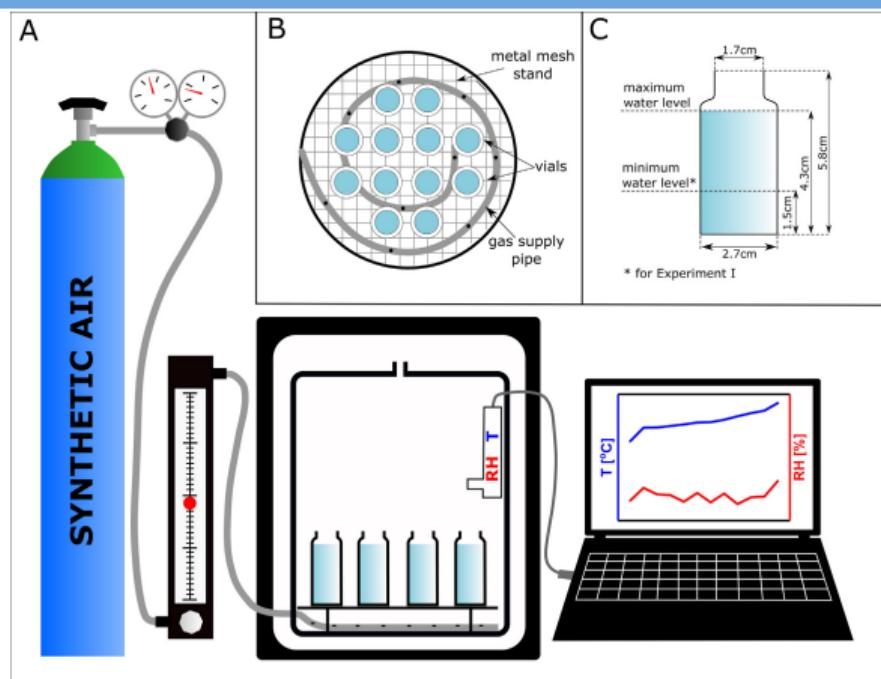
Fig. 1 (paper): lab experiment setup



# Pierchala et al. '22 – triple isotope / kinetic fract. PySDM setup<sup>a</sup>

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Fig. 1 (paper): lab experiment setup

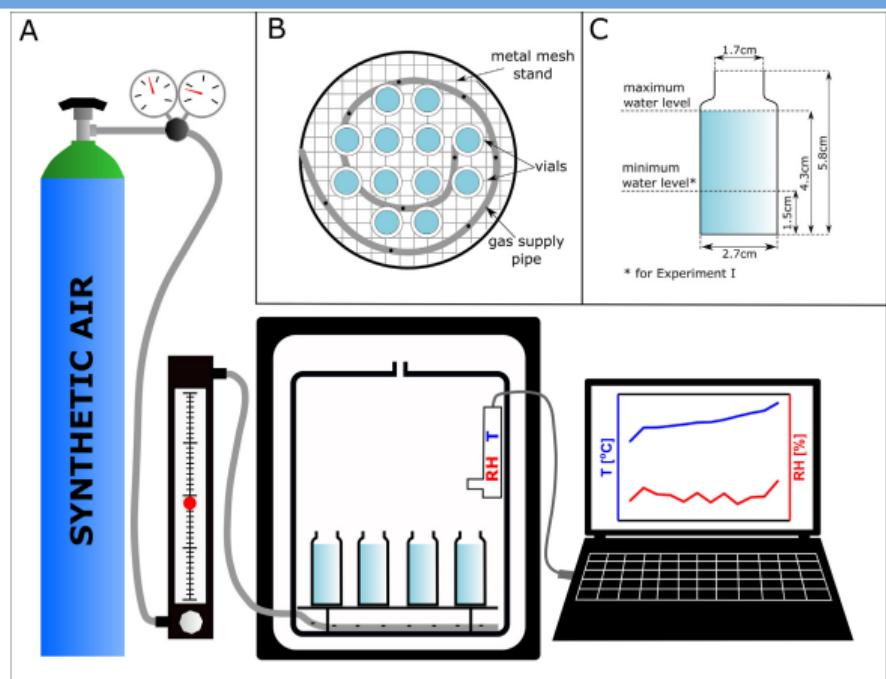


- fractionation upon evaporation (incl. kinetic effects)

# Pierchala et al. '22 – triple isotope / kinetic fract. PySDM setup<sup>a</sup>

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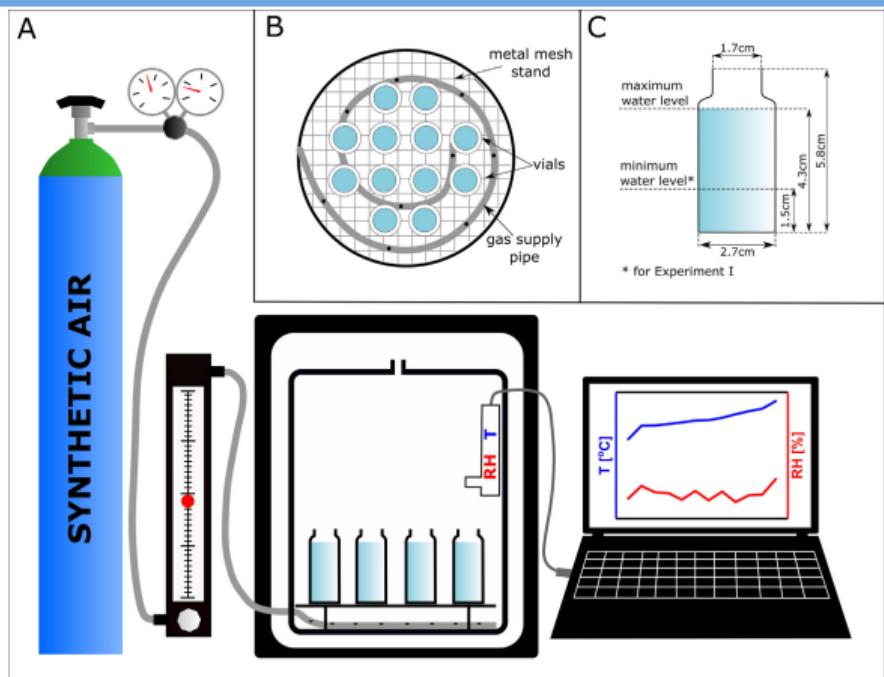


- ❖ fractionation upon evaporation (incl. kinetic effects)
- ❖ multi-day experiments (up to two weeks)

# Pierchala et al. '22 – triple isotope / kinetic fract. PySDM setup<sup>a</sup>

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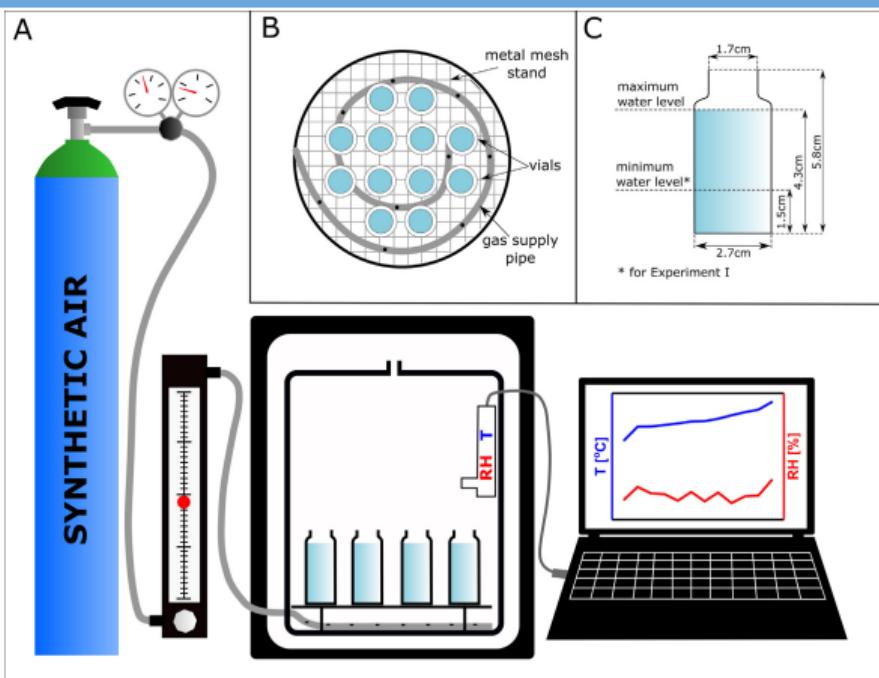


- fractionation upon evaporation (incl. kinetic effects)
- multi-day experiments (up to two weeks)
- Picarro L2140-i cavity ring-down laser spectrometer @AGH ( $D$ ,  $^{18}O$ ,  $^{17}O$ ) (probing vaporized water)

# Pierchala et al. '22 – triple isotope / kinetic fract. PySDM setup<sup>a</sup>

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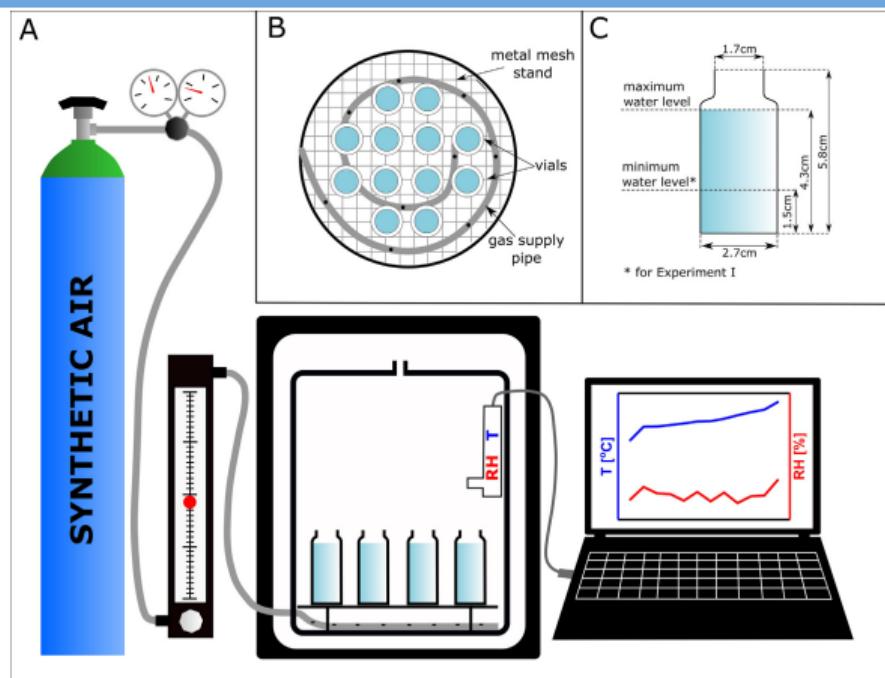


- ❖ fractionation upon evaporation (incl. kinetic effects)
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- ❖ constant T/RH, variable T or variable RH setups

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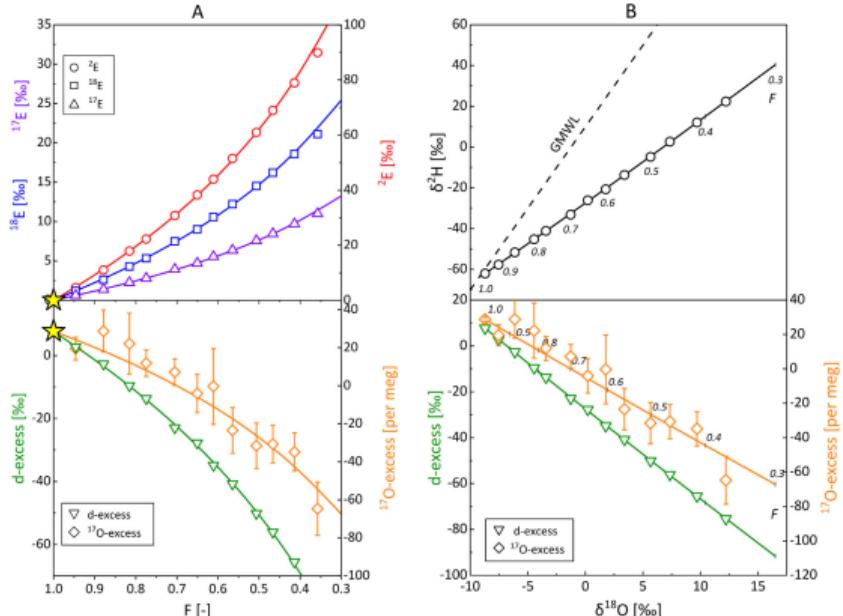


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Fig. 3 (paper): measurements + model



$$E = \left[ \frac{\text{heavy iso.}}{\text{light iso.}} \right] / \left[ \frac{\text{heavy iso.}}{\text{light iso.}} \right]_{t=0} - 1$$

$$\delta = \left[ \frac{\text{heavy iso.}}{\text{light iso.}} \right] / \left[ \frac{\text{heavy iso.}}{\text{light iso.}} \right]_{\text{VSMOW}} - 1$$

F: fraction of water remaining

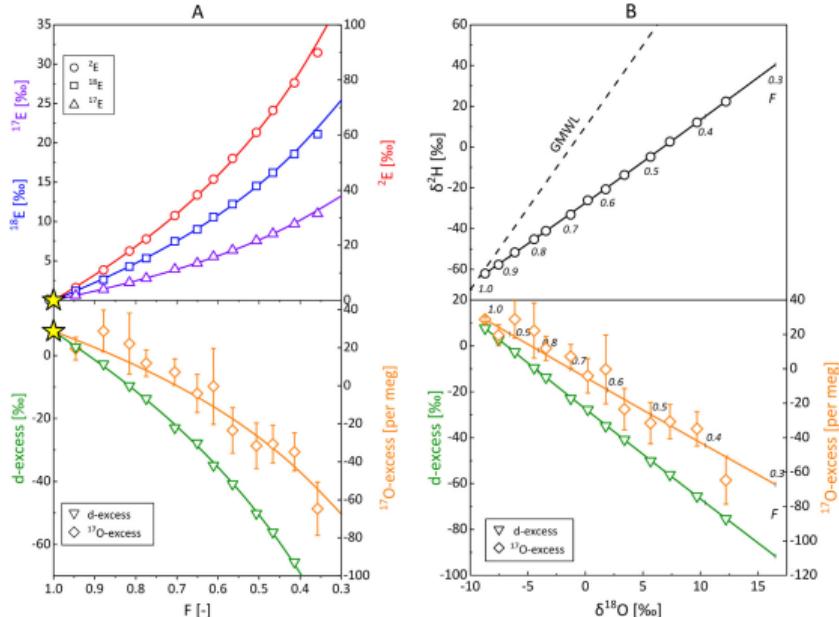
d-excess:  $\delta^2\text{H} - 8 \cdot \delta^{18}\text{O}$

$^{17}\text{O}$ -excess:  $\ln(\delta^{17}\text{O} + 1) - 0.528 \cdot \ln(\delta^{18}\text{O} + 1)$

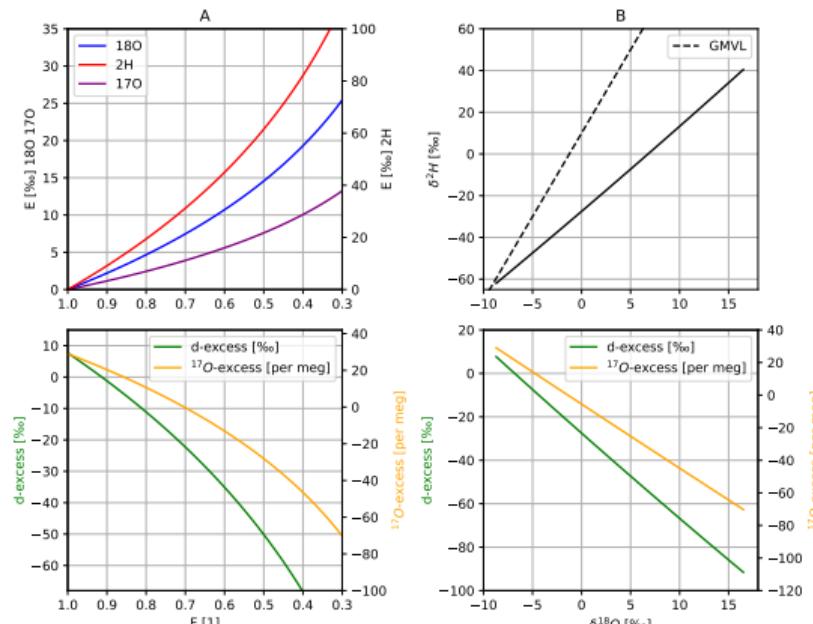
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PySDM: theoretical curves



$$E = \frac{[\text{heavy iso.}]}{[\text{light iso.}]} / \frac{[\text{heavy iso.}]}{[\text{light iso.}]} \Big|_{t=0} - 1$$

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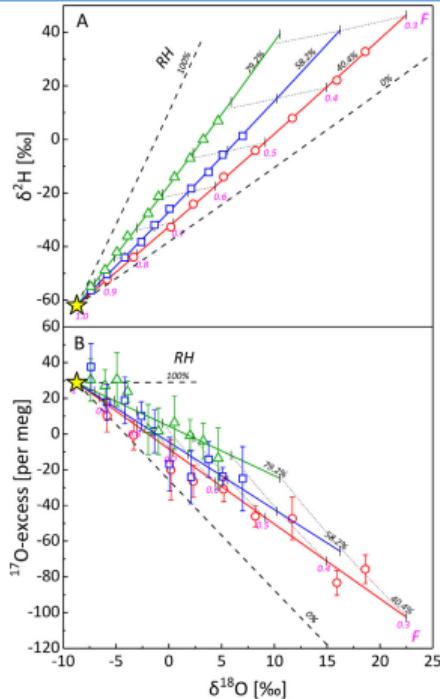
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$$d\text{-excess: } \delta^{2}\text{H} - 8 \cdot \delta^{18}\text{O}$$

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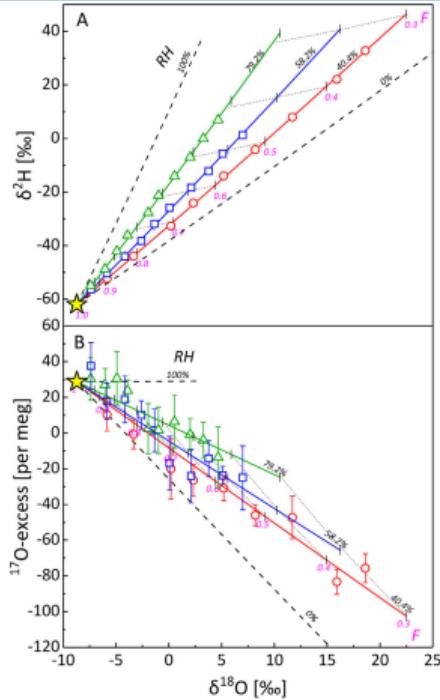
Fig. 4 (paper): RH varied



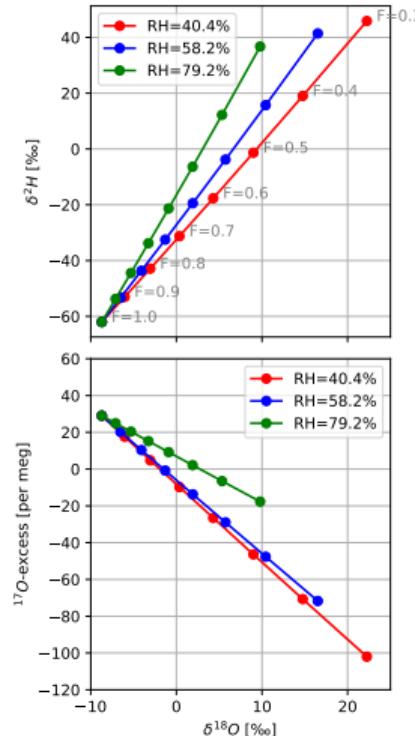
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PySDM: model curves



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Shipway & Hill 2012	x	x			x			#KiD
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Arabas et al. 2023 (figure 11)	x	x			x	x		#Paraview

# Gedzelman & Arnold 1994: drop evaporation dynamics<sup>a</sup>

<sup>a</sup>[https://github.com/open-atmos/PySDM/tree/main/examples/PySDM\\_examples/Gedzelman\\_and\\_Arnold\\_1994](https://github.com/open-atmos/PySDM/tree/main/examples/PySDM_examples/Gedzelman_and_Arnold_1994)

$$\frac{d}{dt} \begin{bmatrix} m_{\text{rain}}^{\text{total}} \\ m_{\text{vap}}^{\text{total}} \end{bmatrix} / A(m_{\text{rain}}^{\text{total}}) = F(\underbrace{T, m_{\text{vap}}^{\text{total}}}_{\text{RH}}, \dots, \underbrace{\text{Re}, \text{Sc}, \text{Pr}}_{})$$

# Gedzelman & Arnold 1994: drop evaporation dynamics<sup>a</sup>

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$$\frac{d}{dt} \begin{bmatrix} m_{\text{rain}}^{\text{total}} \\ m_{\text{vap}}^{\text{total}} \\ m_{\text{vap}}^{\text{heavy}} \\ \color{red} m_{\text{rain}}^{\text{heavy}} \\ \color{red} m_{\text{vap}}^{\text{heavy}} \\ \vdots \end{bmatrix} / A(m_{\text{rain}}^{\text{total}}) = F(\underbrace{T, m_{\text{vap}}^{\text{total}},}_{\text{RH}} \underbrace{m_{\text{vap}}^{\text{heavy}}, m_{\text{rain}}^{\text{heavy}},}_{\text{Re, Sc, Pr}} \dots)$$

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$T_{\text{rain}} \neq T$   
 $\text{RH} < 1$

# Gedzelman & Arnold 1994: drop evaporation dynamics<sup>a</sup>

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$$\frac{d}{dt} \begin{bmatrix} m_{\text{rain}}^{\text{total}} \\ m_{\text{vap}}^{\text{total}} \\ m_{\text{vap}}^{\text{heavy}} \\ \textcolor{red}{m_{\text{rain}}^{\text{heavy}}} \\ \textcolor{red}{M_{\text{vap}}} \\ \vdots \end{bmatrix} / A(m_{\text{rain}}^{\text{total}}) = F(\underbrace{T, m_{\text{vap}}^{\text{total}}}_{\text{RH}}, \underbrace{m_{\text{vap}}^{\text{heavy}}, m_{\text{rain}}^{\text{heavy}}}_{\text{Re, Sc, Pr}}, \dots)$$

$T_{\text{rain}} \neq T$   
 $\text{RH} < 1$

$$\delta_{\text{rain}} + 1 = \frac{M^{\text{light}}}{M^{\text{heavy}}} \frac{m_{\text{rain}}^{\text{heavy}}}{m_{\text{rain}}^{\text{total}} - m_{\text{rain}}^{\text{heavy}}} / R_{\text{SMOW}}$$
$$\delta_{\text{vap}} + 1 = \dots$$

# Gedzelman & Arnold 1994: drop evaporation dynamics<sup>a</sup>

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$$\begin{bmatrix} \frac{d}{dt} \\ m_{\text{rain}}^{\text{total}} \\ m_{\text{vap}}^{\text{total}} \\ \textcolor{red}{m_{\text{rain}}^{\text{heavy}}} \\ \textcolor{red}{m_{\text{vap}}^{\text{heavy}}} \\ \vdots \end{bmatrix} / A(m_{\text{rain}}^{\text{total}}) = F(\underbrace{T, m_{\text{vap}}^{\text{total}}}_{\text{RH}}, \underbrace{m_{\text{vap}}^{\text{heavy}}, m_{\text{rain}}^{\text{heavy}}}_{\text{Re, Sc, Pr}}, \dots)$$

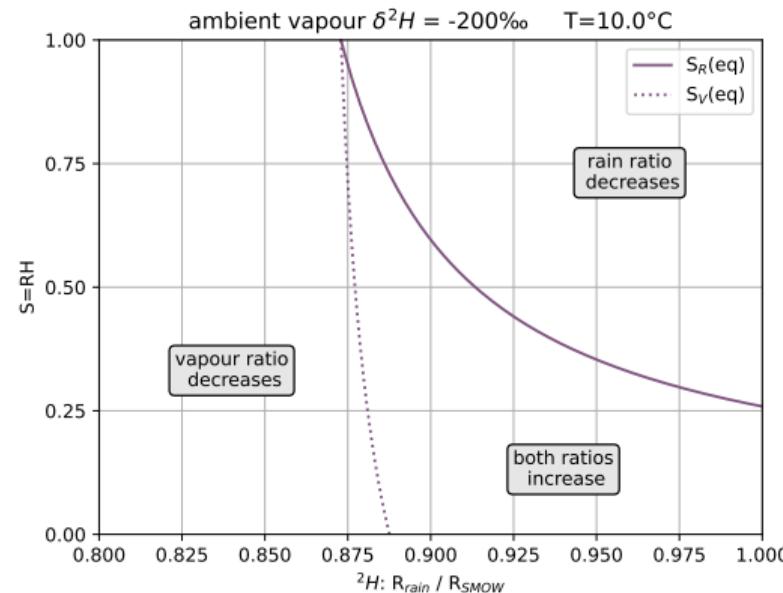
$T_{\text{rain}} \neq T$   
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$$\delta_{\text{vap}} + 1 = \dots$$

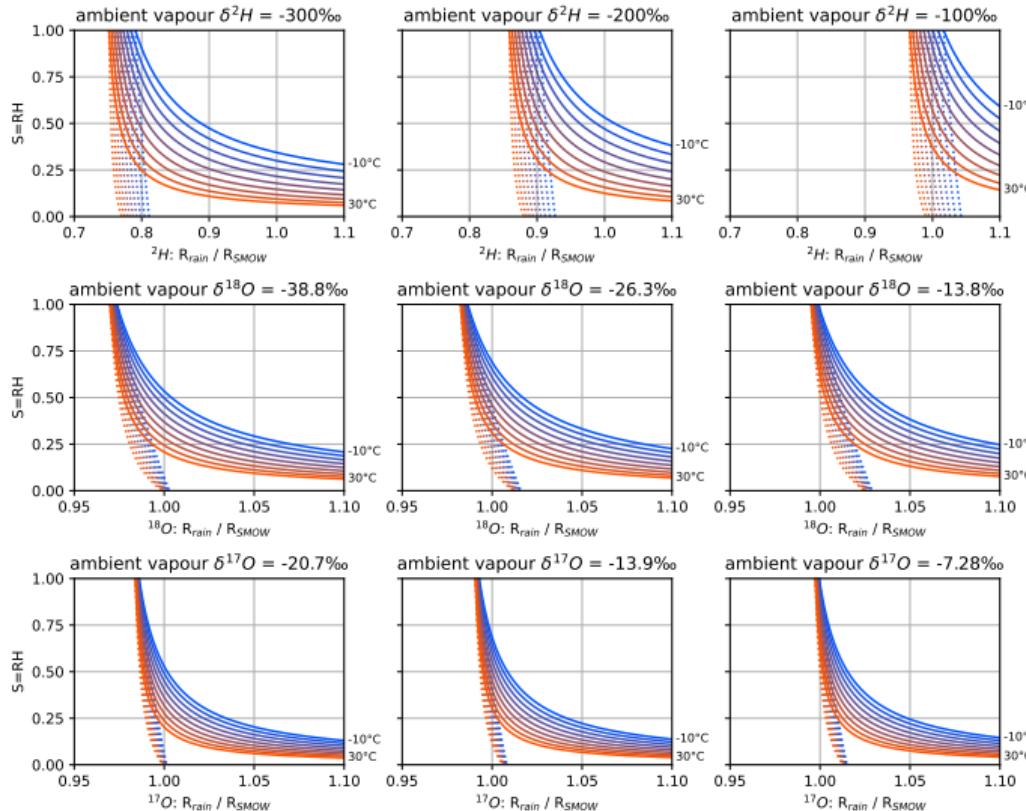
$$S_R \rightsquigarrow \frac{d\delta_{\text{rain}}}{dt} = 0$$

$$S_V \rightsquigarrow \frac{d\delta_{\text{vap}}}{dt} = 0$$



# Gedzelman & Arnold 1994: drop evaporation dynamics<sup>a</sup>

<sup>a</sup>[https://github.com/open-atmos/PySDM/tree/main/examples/PySDM\\_examples/Gedzelman\\_and\\_Arnold\\_1994](https://github.com/open-atmos/PySDM/tree/main/examples/PySDM_examples/Gedzelman_and_Arnold_1994)



# water isotopes in PySDM: summary, next steps

**implemented features** (incl. tests against lab and model literature data):

- base SD attributes: #moles of heavy isotopologue

# water isotopes in PySDM: summary, next steps

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- ☒ ice-phase processes

# motivation slide!

using water-isotope data to investigate turbulence

## Study of Mass Transfer at the Air-Water Interface by an Isotopic Method

L. MERLIVAT

*Departement de Recherche et Analyse, Centre d'Études Nucléaires de Saclay  
Gif Sur Yvette, France*

M. COANTIC

*Institut de Mécanique Statistique de la Turbulence, Marseille, France*

The calculation of the evaporation flux is based on certain assumptions concerning processes in the vicinity of the air-water interface. Most of the recently proposed evaporation theories differ mainly in the estimated contributions of molecular and turbulent mass transfer in the vapor phase just above the liquid surface. This paper will show that, by analyzing the hydrogen and oxygen stable isotope distribution in liquid and water vapor, the processes taking place on a very small scale near the liquid can be investigated. The effect of molecular mass transfer is directly obtained without having to perform difficult measurements in the air in the immediate vicinity of the water surface. Experiments are carried out in the Institut de Mécanique Statistique de la Turbulence air-water tunnel specially designed for the simulation

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supersaturation vs. temperature reconstructions

## Theory of isotopic fractionation on faceted ice crystals

J. Nelson

**Abstract.** The currently used "kinetic-fractionation" (KF) model of the differential incorporation of water-molecule isotopologues into vapor-grown ice omits surface processes on crystal facets that may be important in temperature reconstructions. This article introduces the "surface-kinetic" fractionation model, a model that includes such surface processes, and shows that differences in deposition coefficients for water isotopologues can produce isotopic fractionation coefficients that significantly differ from those of KF theory. For example, if the deposition coefficient of  $\text{H}_2^{18}\text{O}$  differs by just 5% from that of ordinary water ( $\text{H}_2^{16}\text{O}$ ), the resulting fractionation coefficient at 20% supersaturation may deviate from the KF value by up to about  $\pm 17\%$ , and even more at greater supersaturation. As a result, the surface-kinetic theory may significantly change how fractionation depends on supersaturation.

[github.com/open-atmos/PySDM](https://github.com/open-atmos/PySDM)

Acknowledgements:

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merci de votre attention