

# Supercooling super-droplets: on particle-based modelling of immersion freezing

S. Arabas<sup>1</sup>, J.H. Curtis<sup>2</sup>, I. Silber<sup>3</sup>, A. Fridlind<sup>4</sup>, D.A Knopf<sup>5</sup>, M. West<sup>2</sup> & N. Riemer<sup>2</sup>



funding:



# aerosol-cloud interactions: a conceptual picture

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background image: [vitsly.ru/](http://vitsly.ru/) / Hokusai

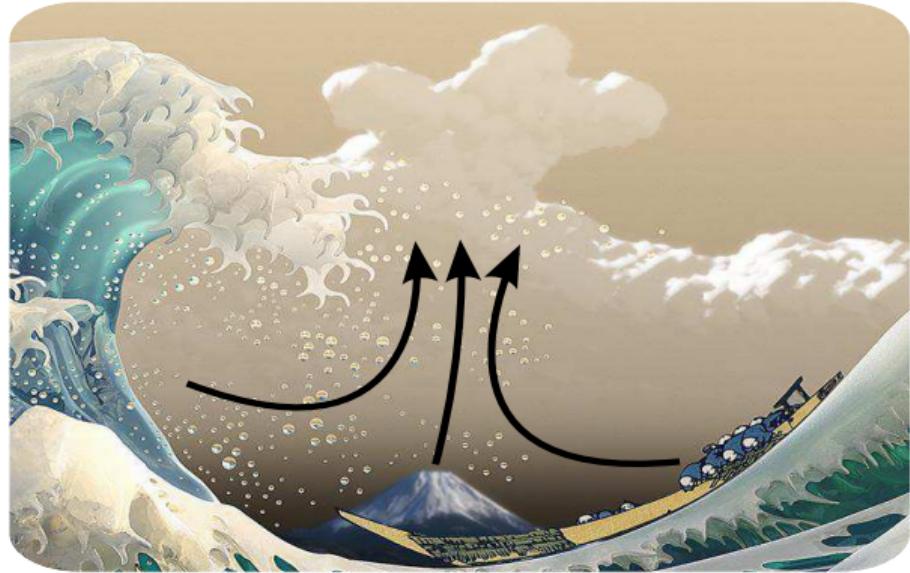
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# aerosol-cloud interactions: a conceptual picture

- ▶ aerosol particles of natural and anthropogenic origin act as condensation/crystallisation nuclei



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super-particles as a probabilistic alternative to bulk or bin  $\mu$ -physics

JAMES

Journal of Advances in  
Modeling Earth Systems

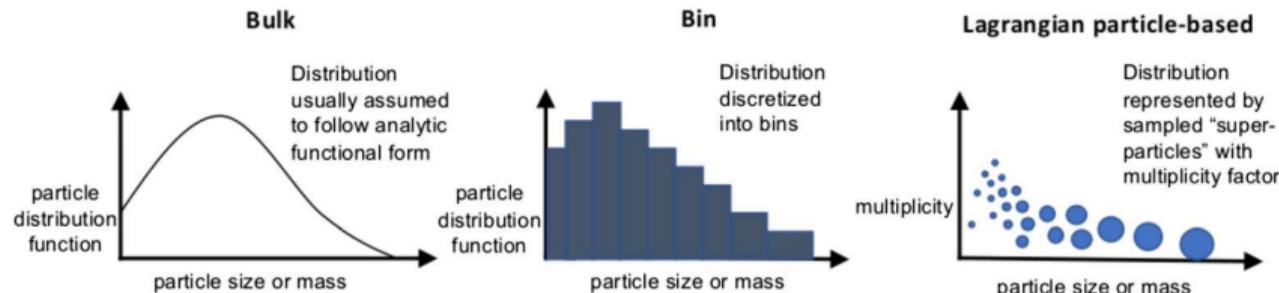
**COMMISSIONED  
MANUSCRIPT**  
10.1029/2019MS001689

## Key Points

- Microphysics is an important component of weather and climate models, but its representation in current models is highly uncertain

## Confronting the Challenge of Modeling Cloud and Precipitation Microphysics

Hugh Morrison<sup>1</sup> , Marcus van Lier-Walqui<sup>2</sup> , Ann M. Fridlind<sup>3</sup> , Wojciech W. Grabowski<sup>1</sup> , Jerry Y. Harrington<sup>4</sup>, Corinna Hoose<sup>5</sup> , Alexei Korolev<sup>6</sup> , Matthew R. Kumjian<sup>4</sup> , Jason A. Milbrandt<sup>7</sup>, Hanna Pawlowska<sup>8</sup> , Derek J. Posselt<sup>9</sup>, Olivier P. Prat<sup>10</sup>, Karly J. Reimel<sup>4</sup>, Shin-Ichiro Shima<sup>11</sup> , Bastiaan van Diedenhoven<sup>2</sup> , and Lulin Xue<sup>1</sup> 



**Figure 3.** Representation of cloud and precipitation particle distributions in the three main types of microphysics

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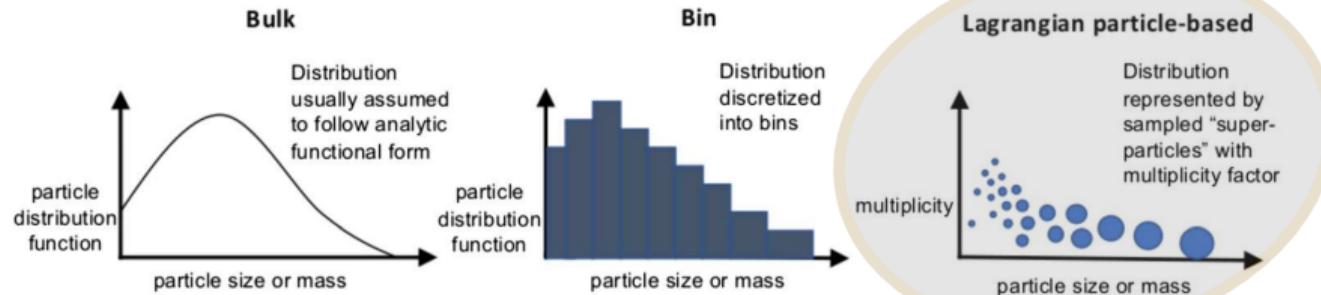
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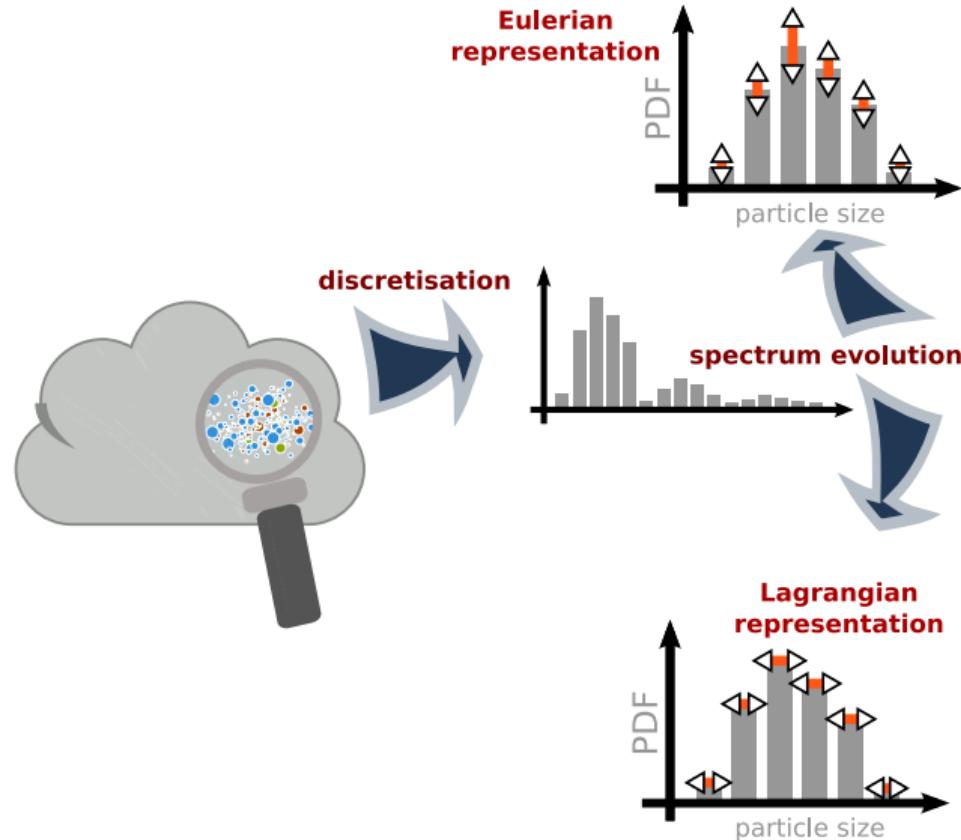
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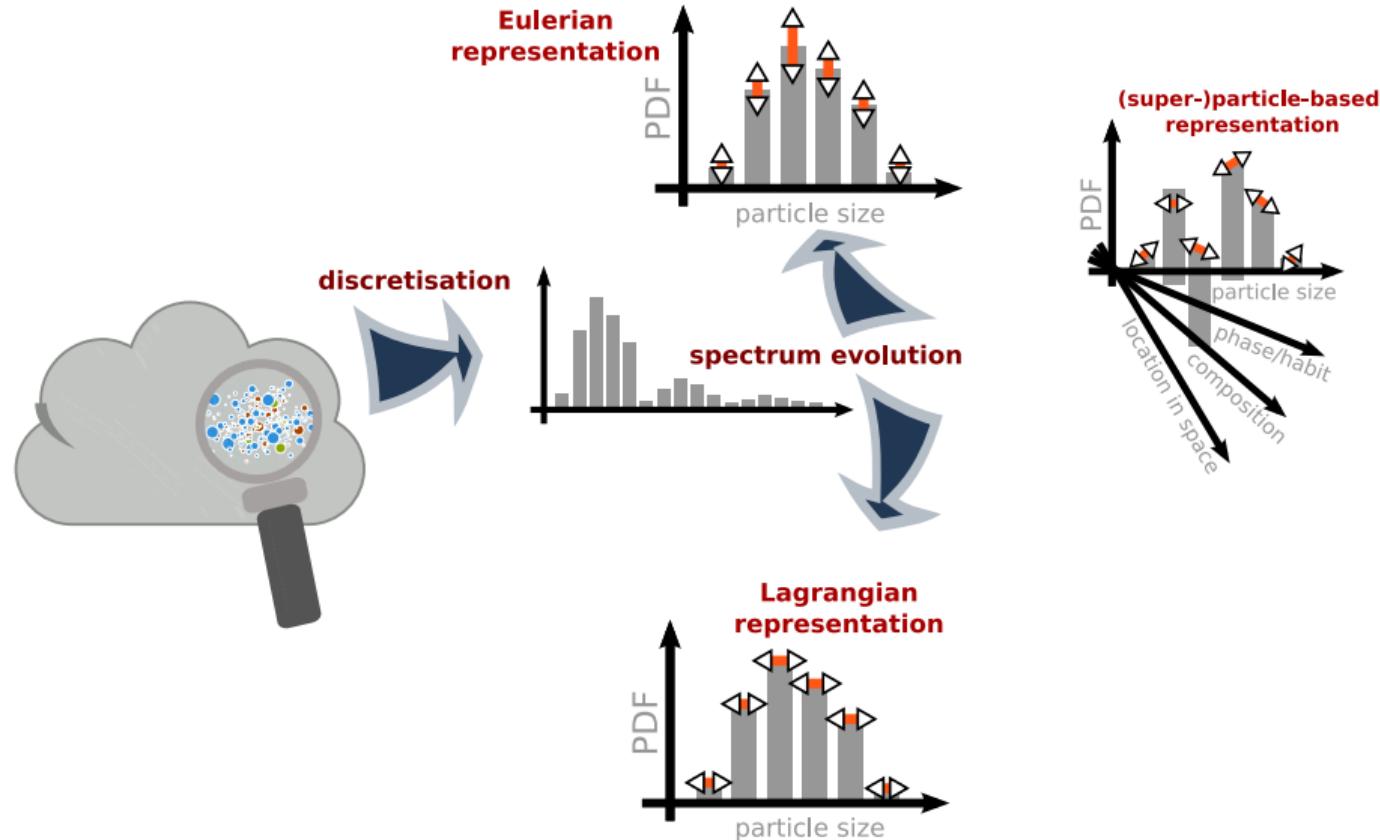


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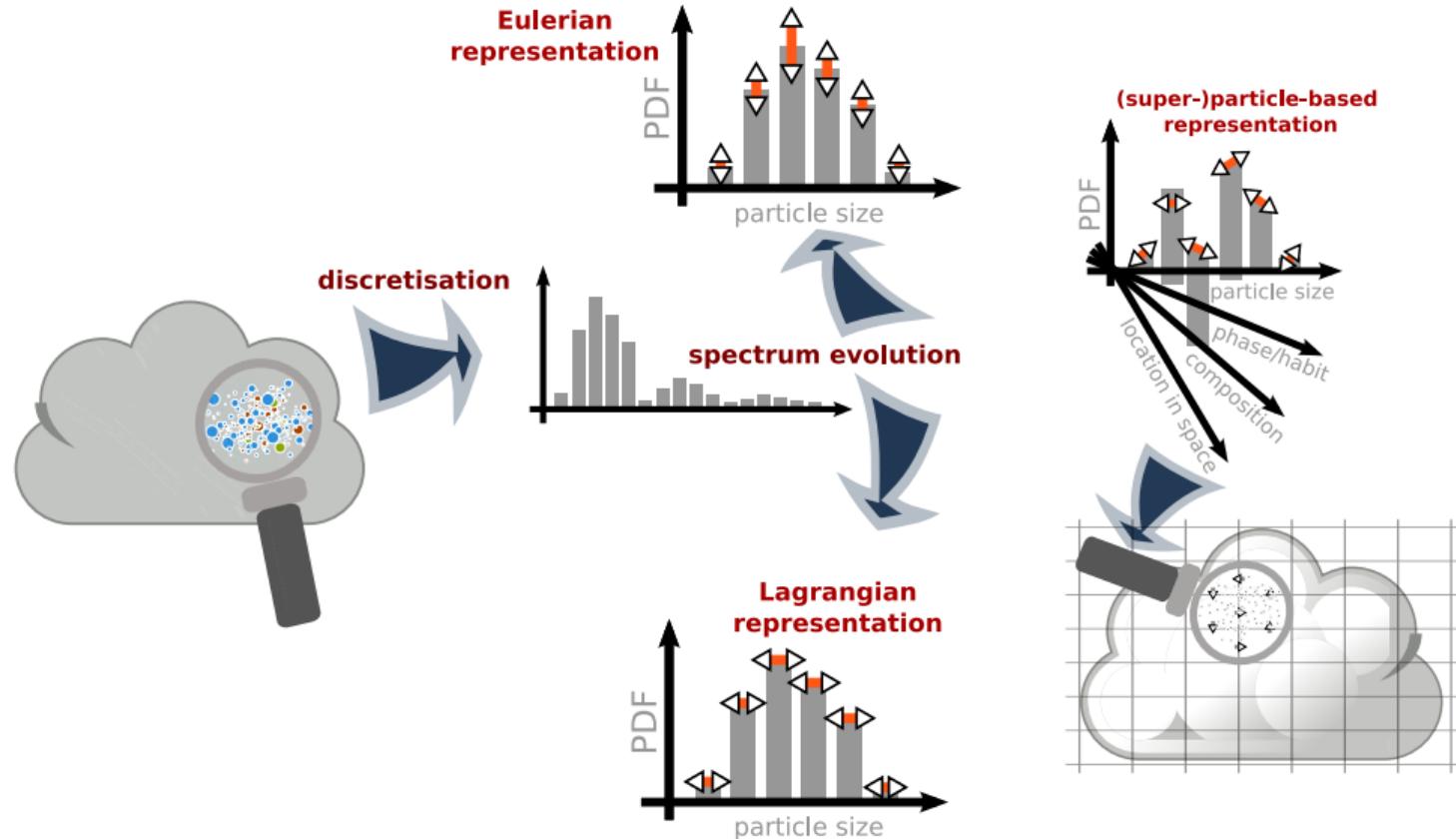
modelling cloud  $\mu$ -physics: Eulerian vs. Lagrangian approaches



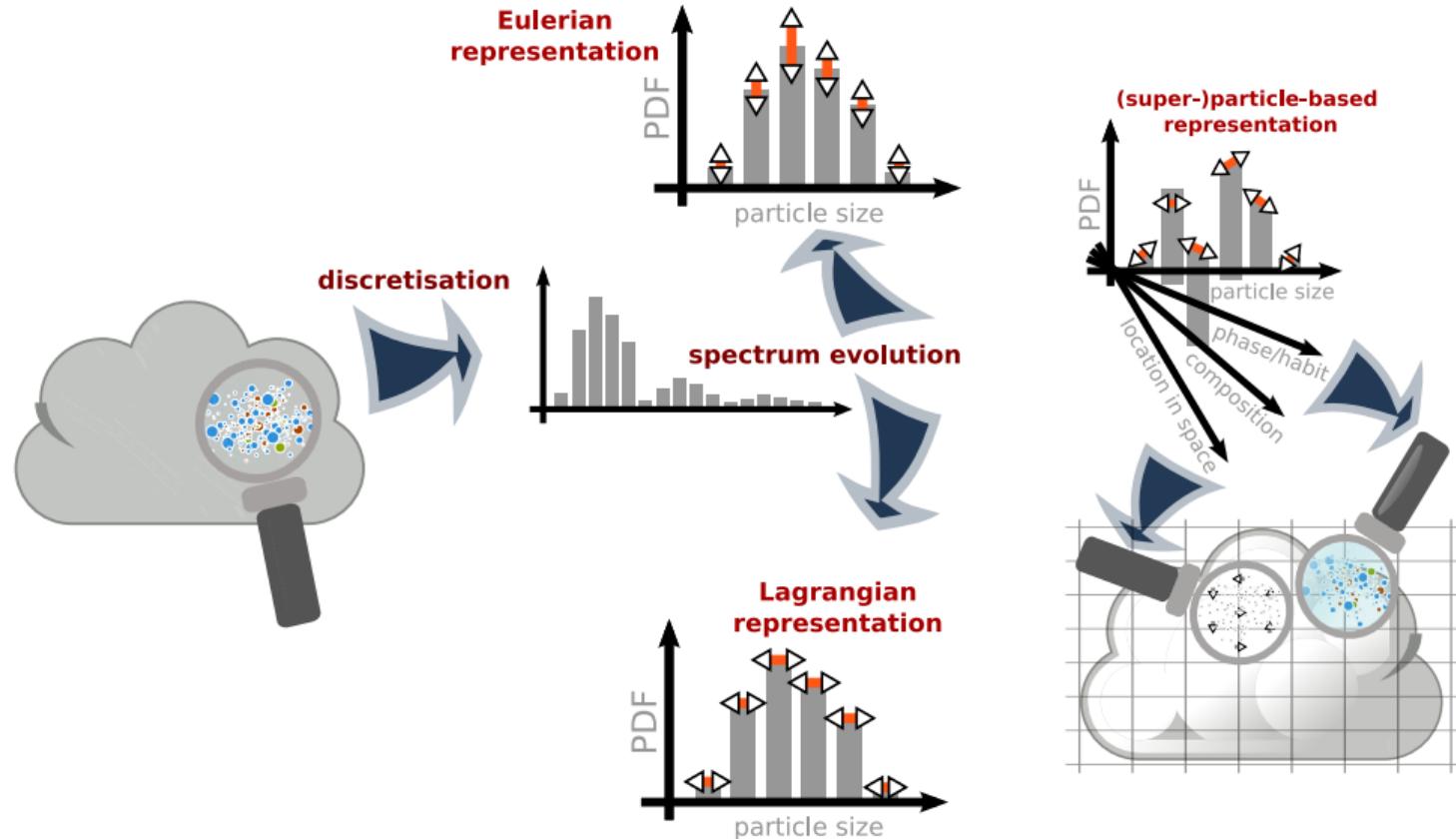
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two-way interactions:

- aerosol characteristics influence cloud microstructure
- cloud processes influence aerosol size and composition

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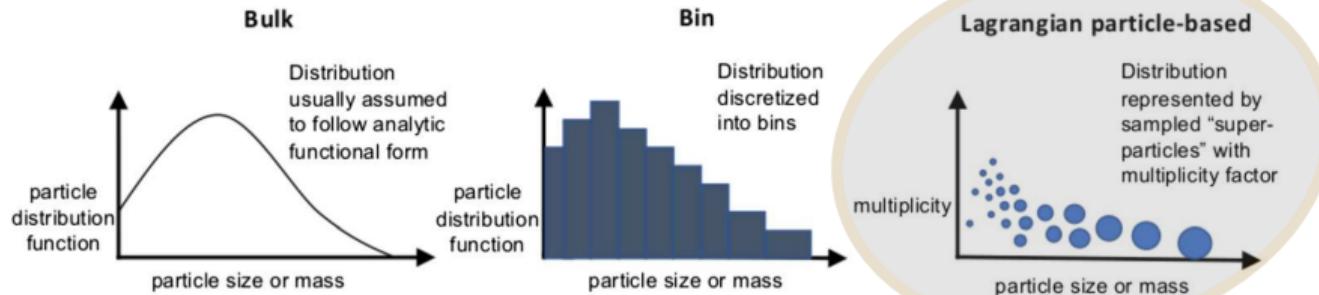
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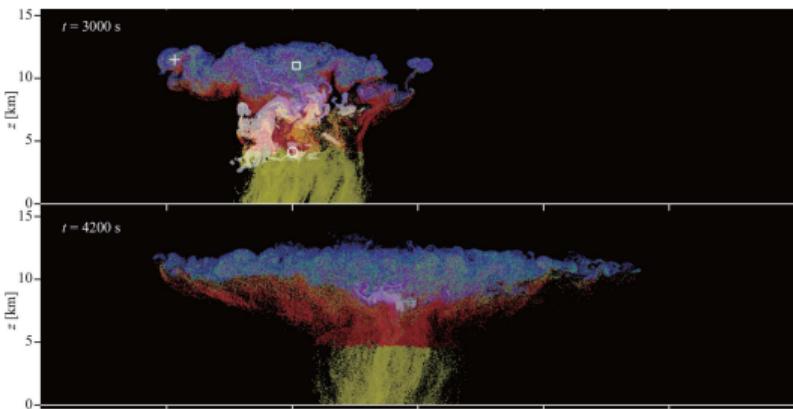
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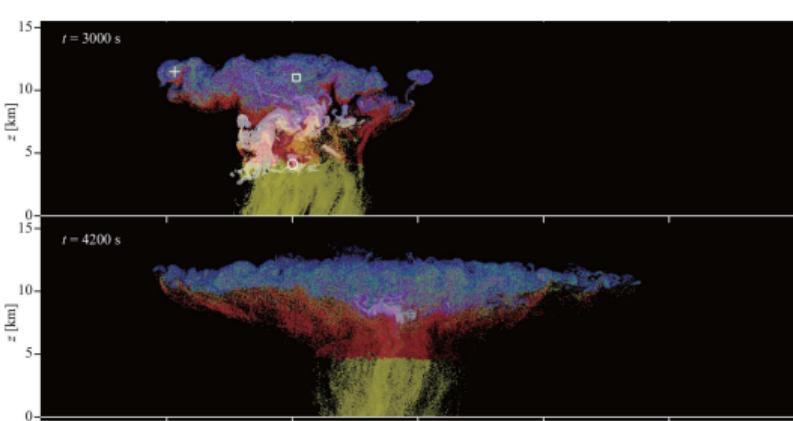
*Predicting the morphology of ice particles in deep convection using the super-droplet method*



**Figure 1.** Typical realization of CTRL cloud spatial structures at  $t = 2040, 2460, 3000, 4200$ , and  $5400$  s. The mixing ratio of cloud water, rainwater, cloud ice, graupel, and snow aggregates are plotted in fading white, yellow, blue, red, and green, respectively. The symbols indicate examples of unrealistic predicted ice particles (Sects. 7.3 and 9.1). See also Movie 1 in the video supplement.

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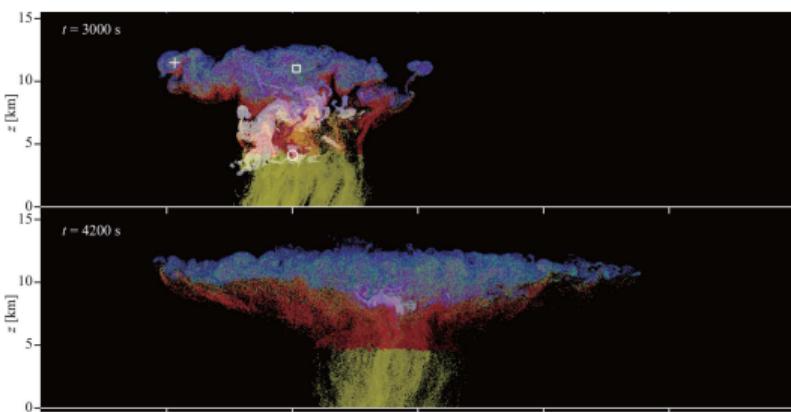


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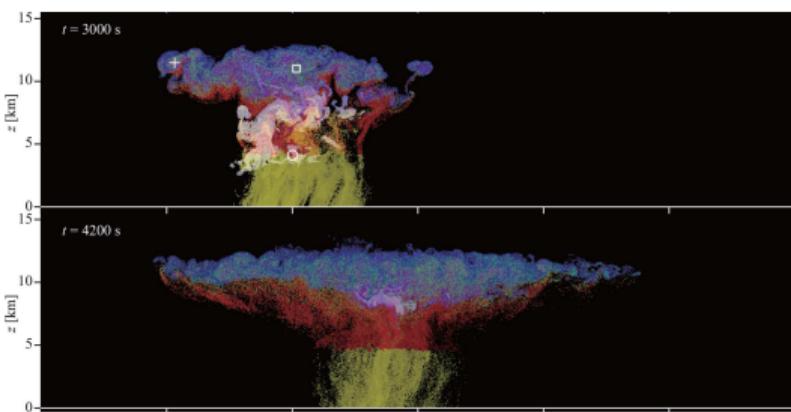


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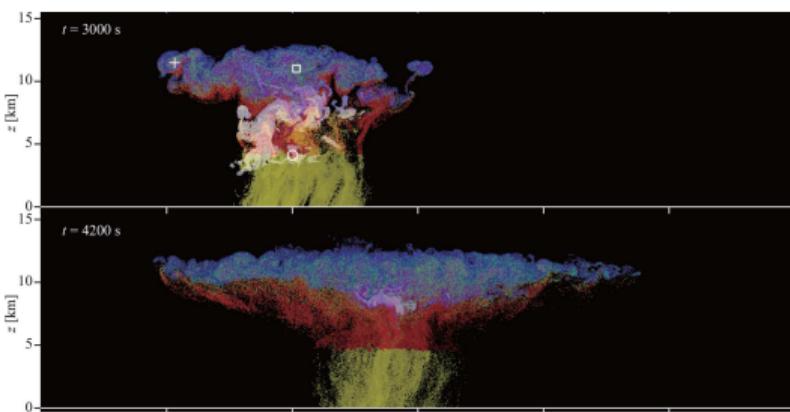


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  - homogeneous and immersion freezing (singular)
  - melting
  - condensation and evaporation (incl. CCN [de]activation)
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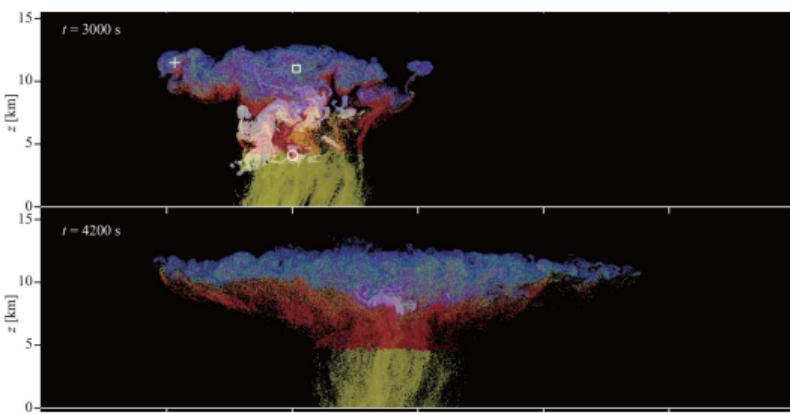


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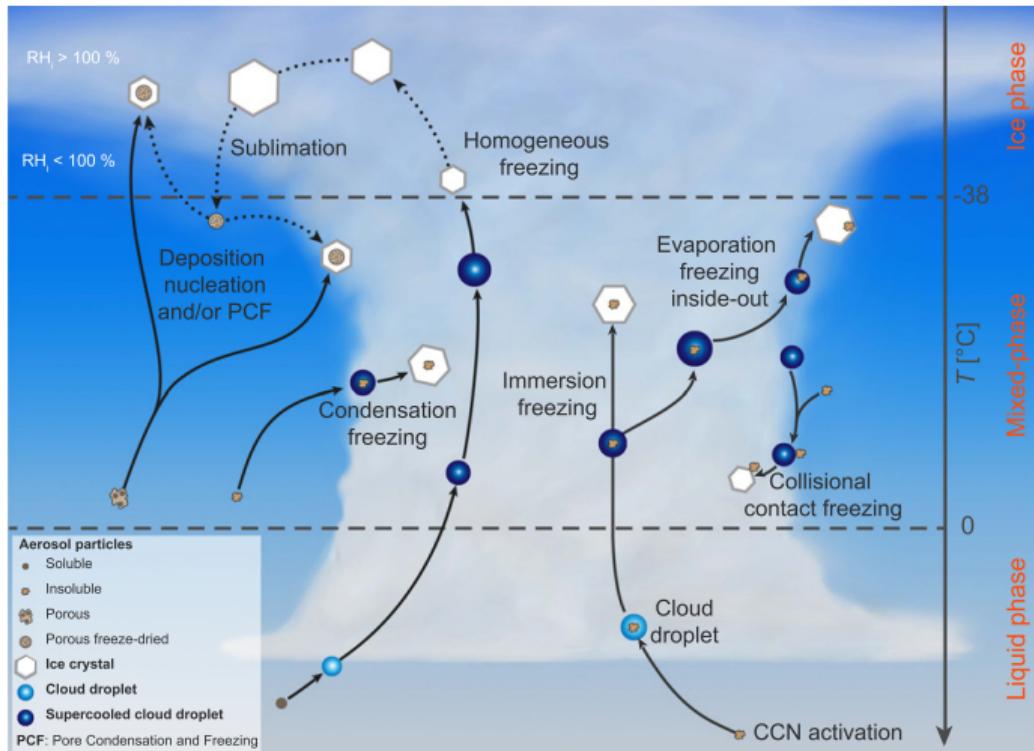
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# immersion freezing and other ice crystal formation pathways in clouds



Kanji et al. 2017, graphics F. Mahrt, <https://doi.org/10.1175/AMSMONOGRAPHS-D-16-0006.1>

# immersion freezing: bacteria and the Olympics

## Journal of Geophysical Research: Atmospheres

### RESEARCH ARTICLE

10.1002/2016JD025251

#### Key Points:

- Very ice active Snomax protein aggregates are fragile and their ice nucleation ability decreases over months of freezer storage
  - Partitioning of ice active protein aggregates into the immersion oil reduces the droplet's measured freezing temperature
- Freezing is measured in the core of

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<sup>1</sup>Center for Atmospheric Particle Studies, Carnegie Mellon University, Pittsburgh, Pennsylvania, USA

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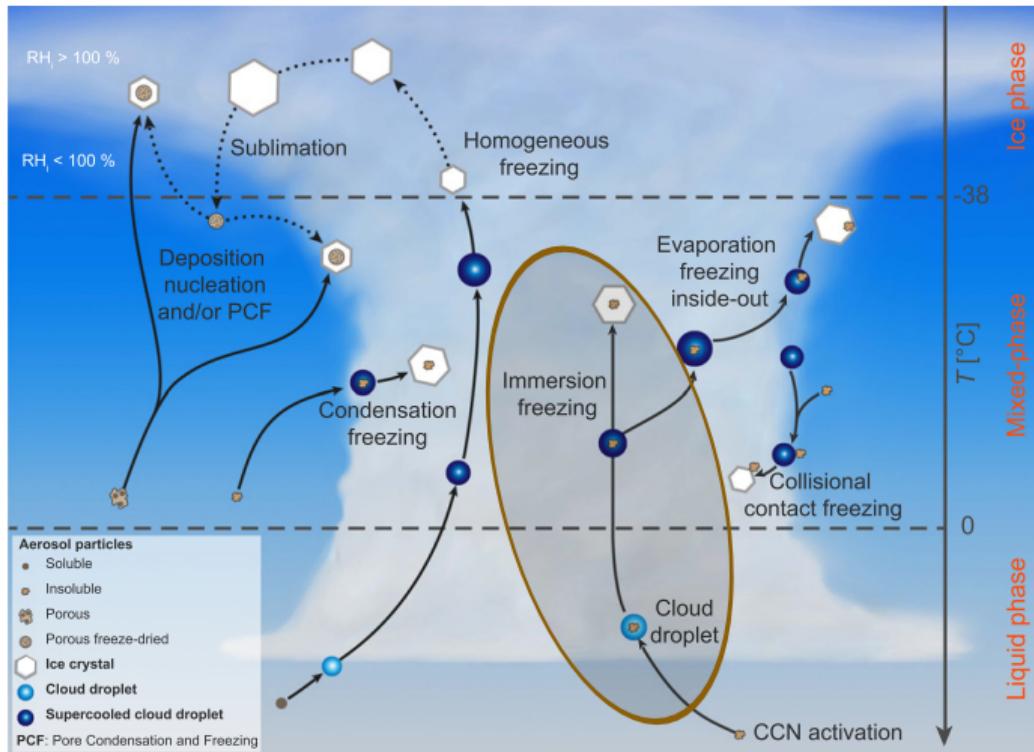
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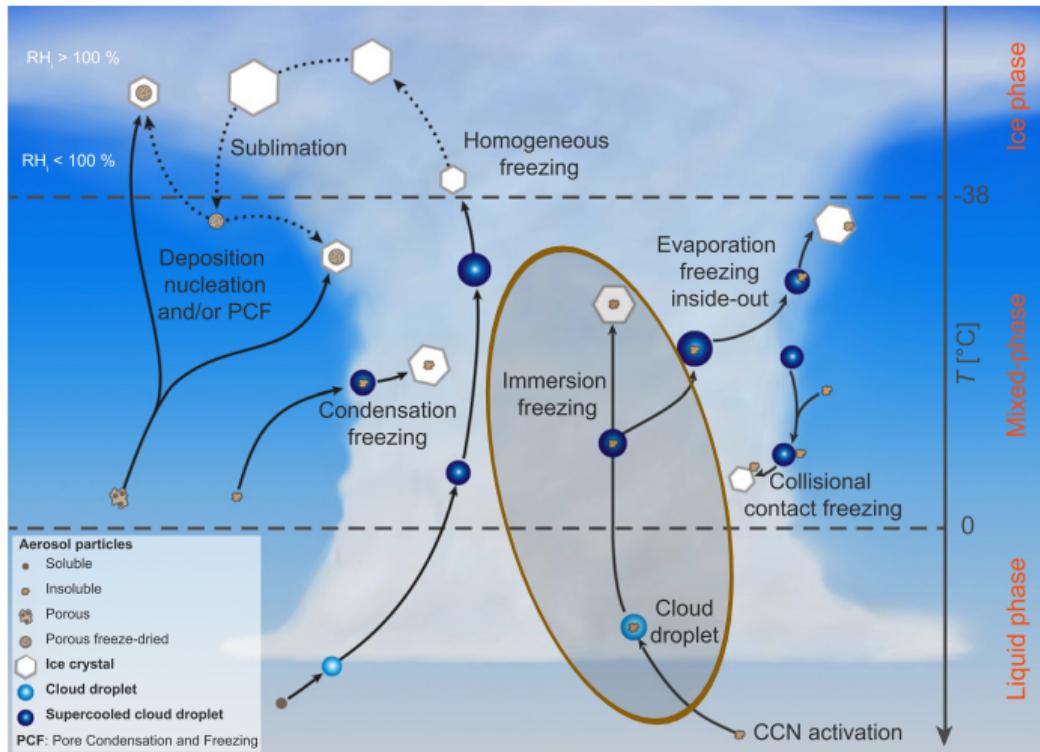
<https://www.reuters.com/markets/commodities/making-snow-stick-wind-challenges-winter-games-slope-makers-2021-11-29/>

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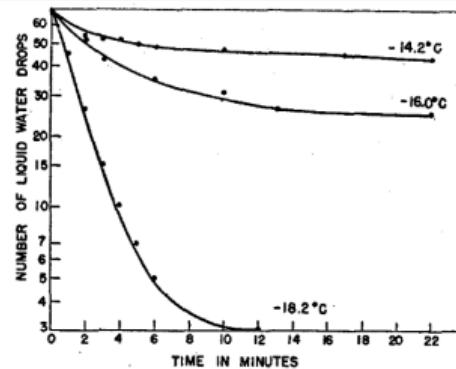


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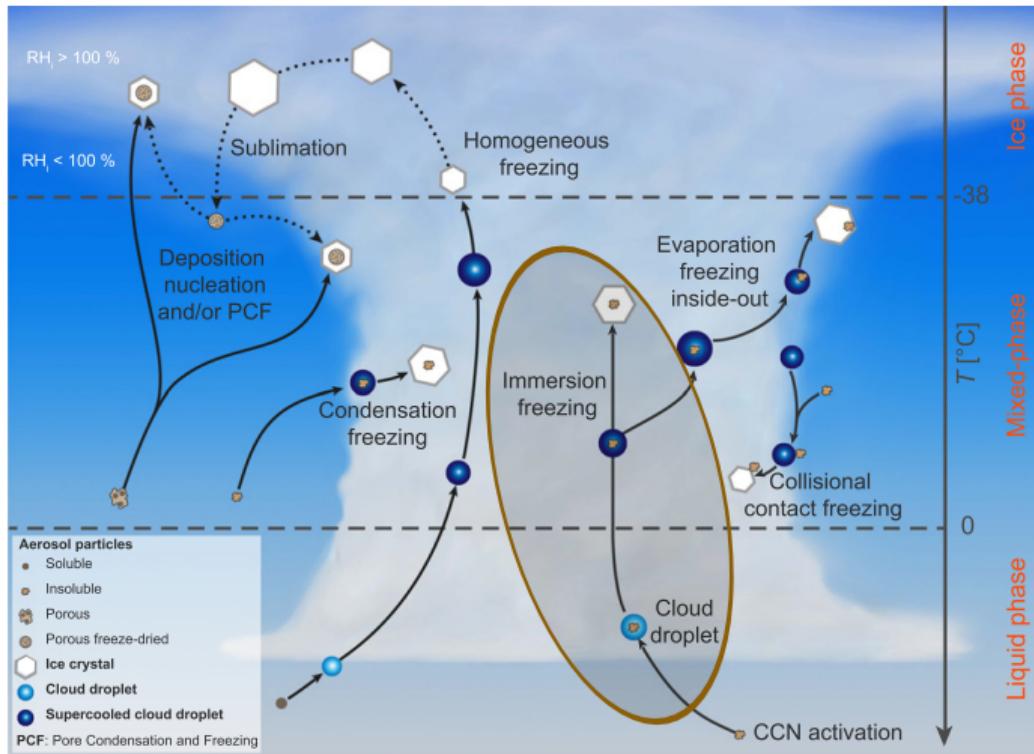
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Fraction of water drops remaining unfrozen as a function of time.

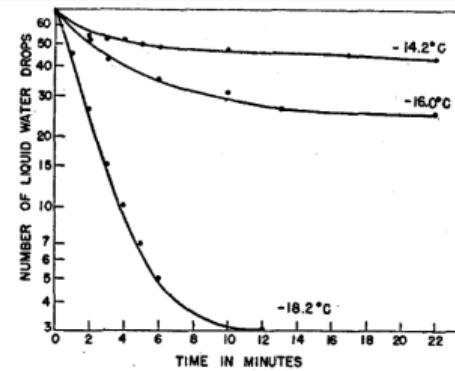
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Vali 2014 (ACP)

*"Interpretations of the experimental results face considerable difficulties ... two separate ways of interpreting the same observations; one assigned primacy to time the other emphasized the temperature-dependent impacts of the impurities ... dichotomy – the stochastic and singular models"*

# Heterogeneous Nucleations is a Stochastic Process

by

J. S. MARSHALL

McGill University, Montreal, Canad.

*Presented at the International Congress on the Physics of Clouds (Hailstorms)  
at Verona 9-13 August 1960.*

[http://cma.entepra.it/Astro2\\_sito/doc/Nubila\\_1\\_1961.pdf](http://cma.entepra.it/Astro2_sito/doc/Nubila_1_1961.pdf)

# Poissonian model of freezing & Ice Nucleation Active Sites (INAS)

theory (in modern notation)

(Bigg '53, Langham & Mason '58, Carte '59, Marshall '61)

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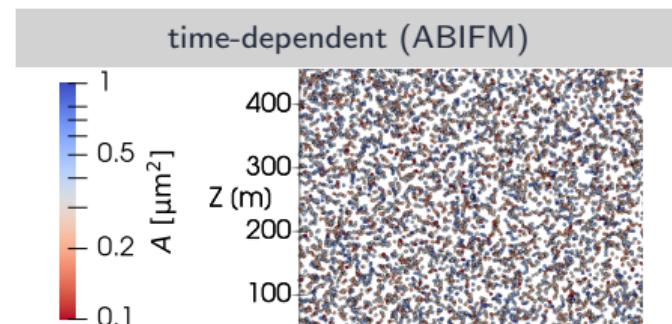
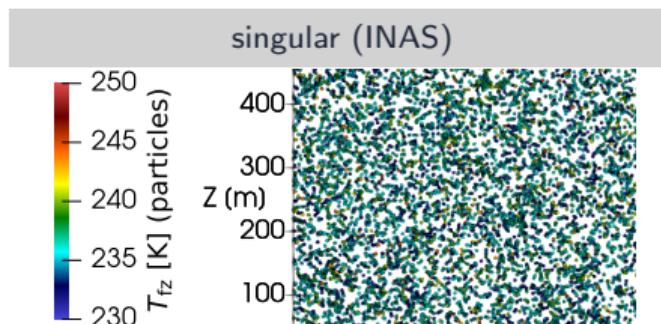
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experimental  $n_s(T)$  fits: e.g., Niemand et al. 2012

# particle-based Monte-Carlo freezing: singular vs. time-dependent

**singular<sup>1</sup>:** INAS  $T_{fz}$  as attribute; initialisation by random sampling from  $P(T_{fz}, A)$  with lognormal  $A$  (A is not an attribute, initialisation only); freezing if  $T(t) < T_{fz}(t = 0)$

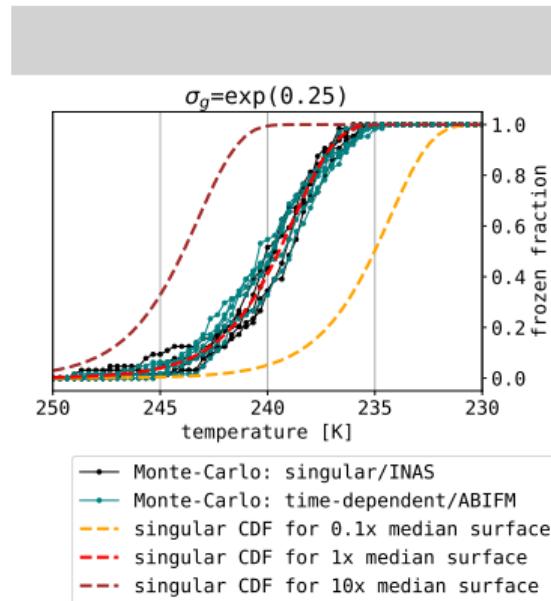
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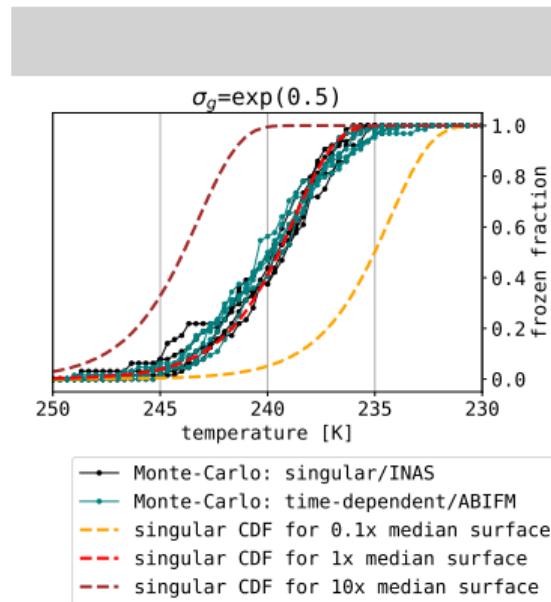
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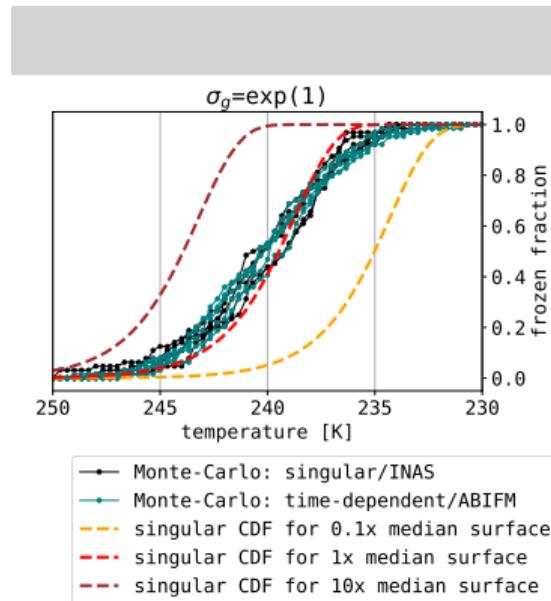
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singular<sup>1</sup>: INAS  $T_{fz}$  as attribute; initialisation by random sampling from  $P(T_{fz}, A)$  with lognormal  $A$  ( $A$  is not an attribute, initialisation only); freezing if  $T(t) < T_{fz}(t = 0)$

time-dependent<sup>2</sup>:  $A$  as attribute (randomly sampled from the same lognormal)  
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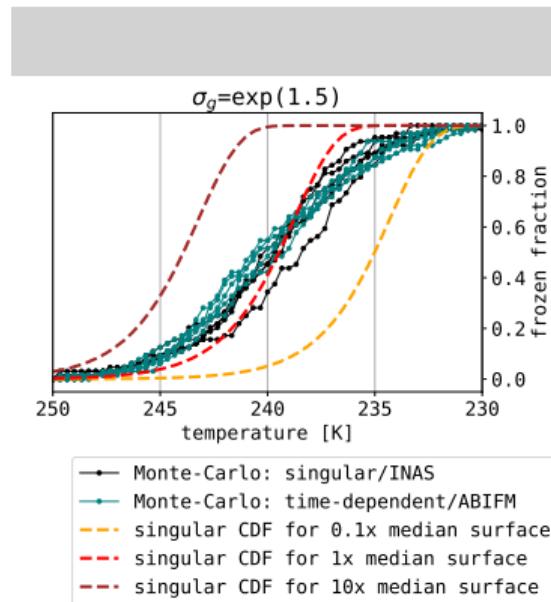
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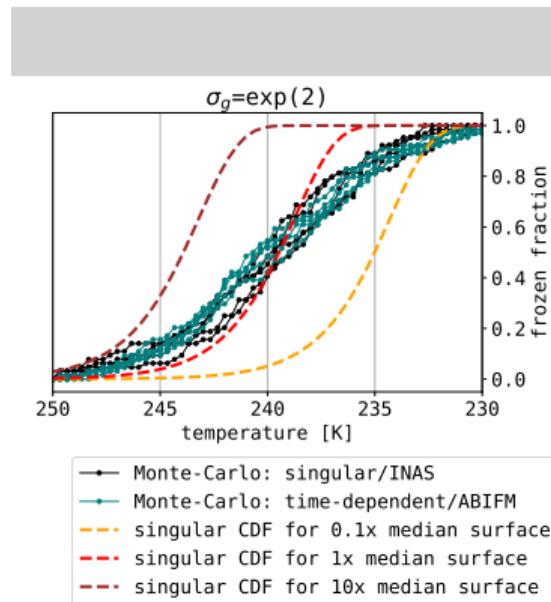
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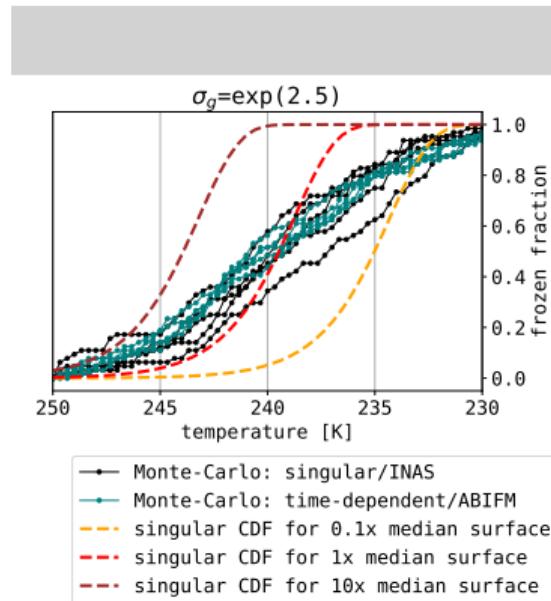
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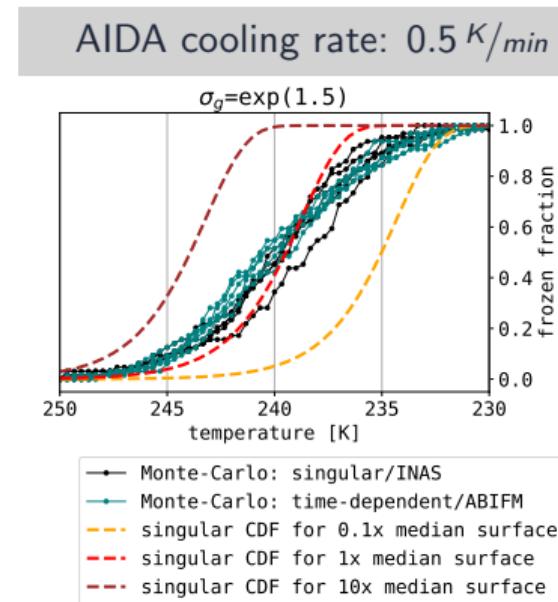
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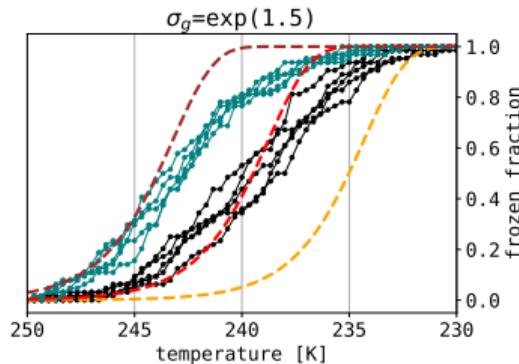
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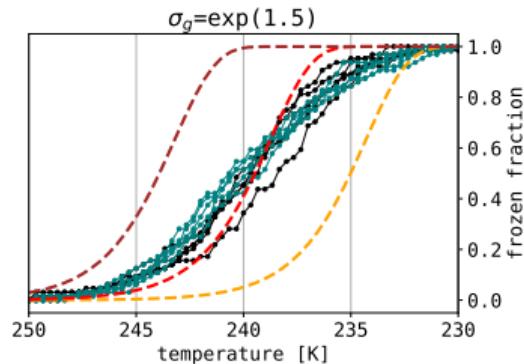
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cooling rate:  $0.1 \text{ K/min}$



AIDA cooling rate:  $0.5 \text{ K/min}$



- Monte-Carlo: singular/INAS
- Monte-Carlo: time-dependent/ABIFM
- singular CDF for  $0.1x$  median surface
- - singular CDF for  $1x$  median surface
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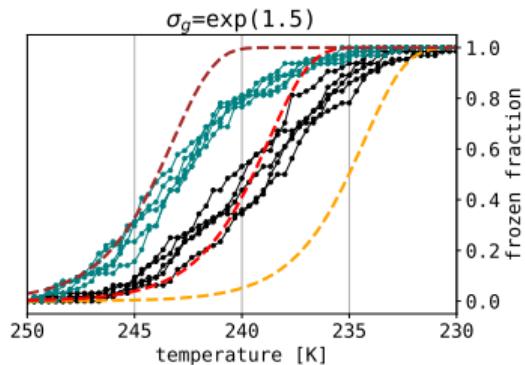
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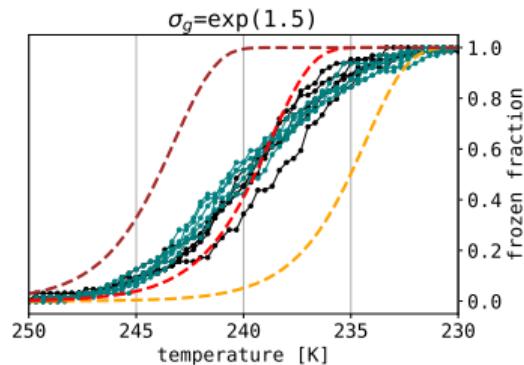
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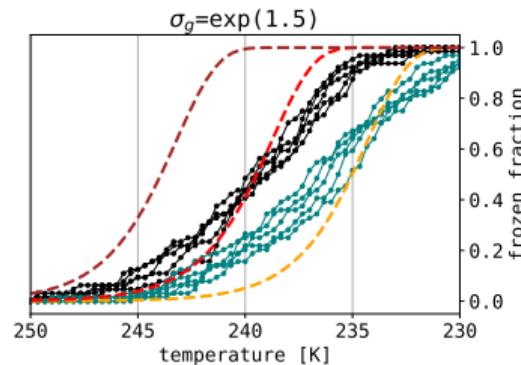
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# Poissonian model of freezing & Ice Nucleation Active Sites (INAS)

theory (in modern notation)

(Bigg '53, Langham & Mason '58, Carte '59, Marshall '61)

Poisson counting process with rate  $r$ :

$$P^*(k \text{ events in time } t) = \frac{(rt)^k \exp(-rt)}{k!}$$

$$P(\text{one or more events in time } t) = 1 - P^*(k = 0, t)$$

$$\ln(1 - P) = -rt$$

introducing  $J_{\text{het}}(T)$ ,  $T(t)$  and INP surface  $A$ :

$$\ln(1 - P(A, t)) = -A \underbrace{\int_0^t J_{\text{het}}(T(t')) dt'}_{I(T)}$$

INAS:  $I(T) = n_s(T) = \exp(a \cdot (T - T_0^{\circ}C) + b)$

experimental  $n_s(T)$  fits: e.g., Niemand et al. 2012

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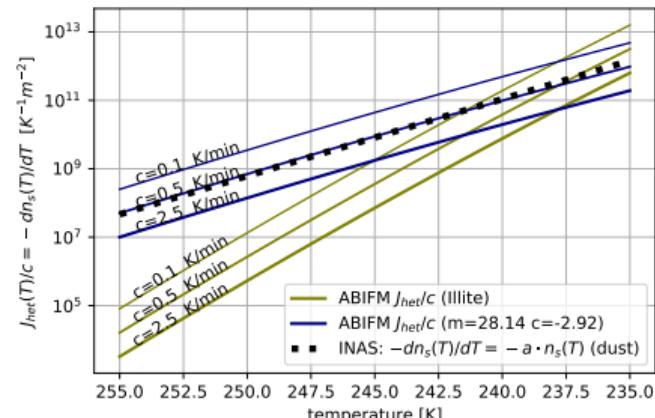
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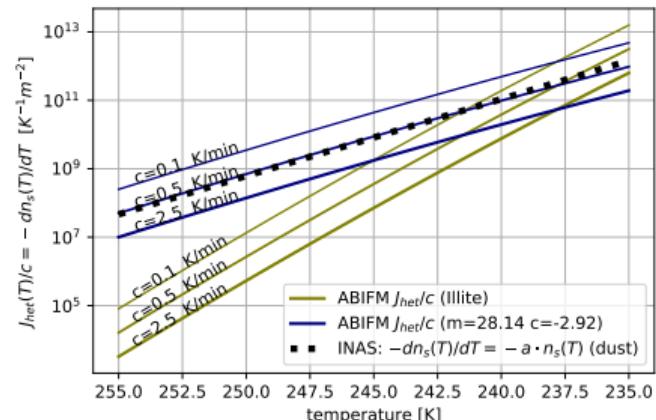
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cf. Vali & Stansbury '66; modified singular model (Vali '94, Murray et al. '11)  
but the **singular ansatz limitation of sampling  $T_F$  at  $t=0$**  remains

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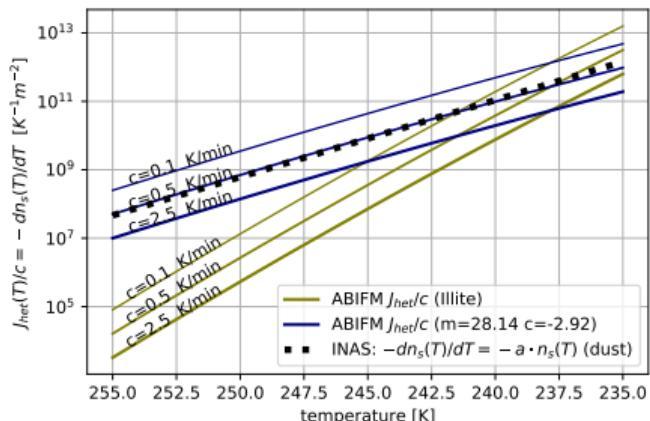
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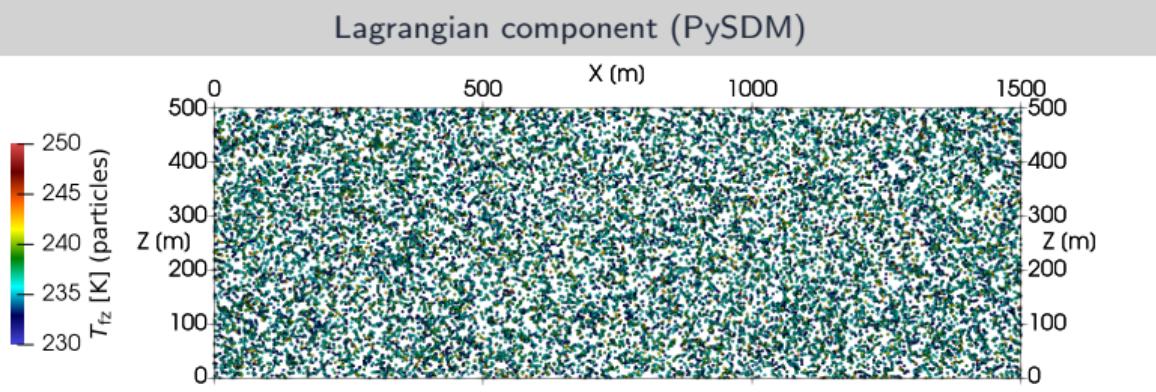
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## Is it a problem?



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particle-based  $\mu$ -physics + prescribed-flow test (aka KiD-2D)<sup>a,b,c,d,e,f</sup>



concept: Gedzelman & Arnold '93

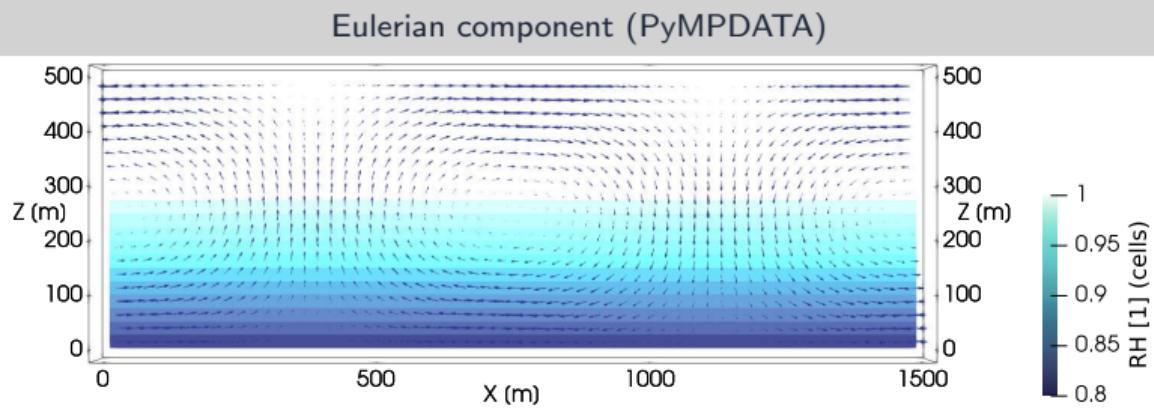
<sup>b</sup>stratiform: Morrison & Grabowski '07

**ice phase**: e.g., Yang et al. '15

<sup>d</sup> particle-based: e.g., Arabas et al. '15

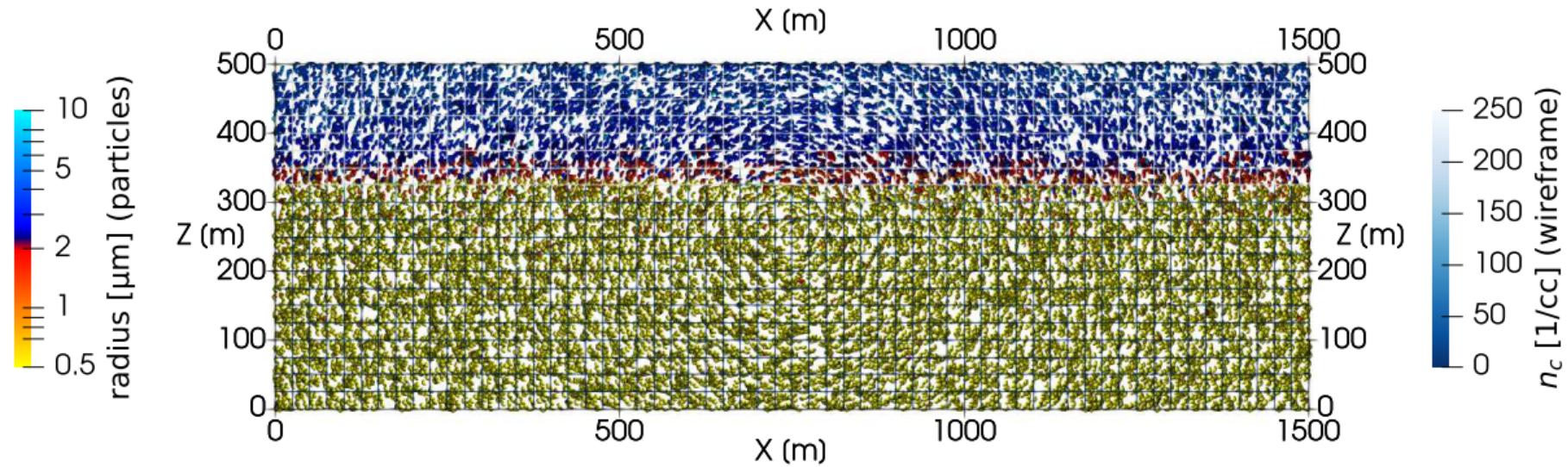
**KiD-2D**: [github.com/BShipway/KiD](https://github.com/BShipway/KiD)

<sup>f</sup>here: SHEBA case (Fridlind et al. '12)



## particle-based $\mu$ -physics + prescribed-flow test

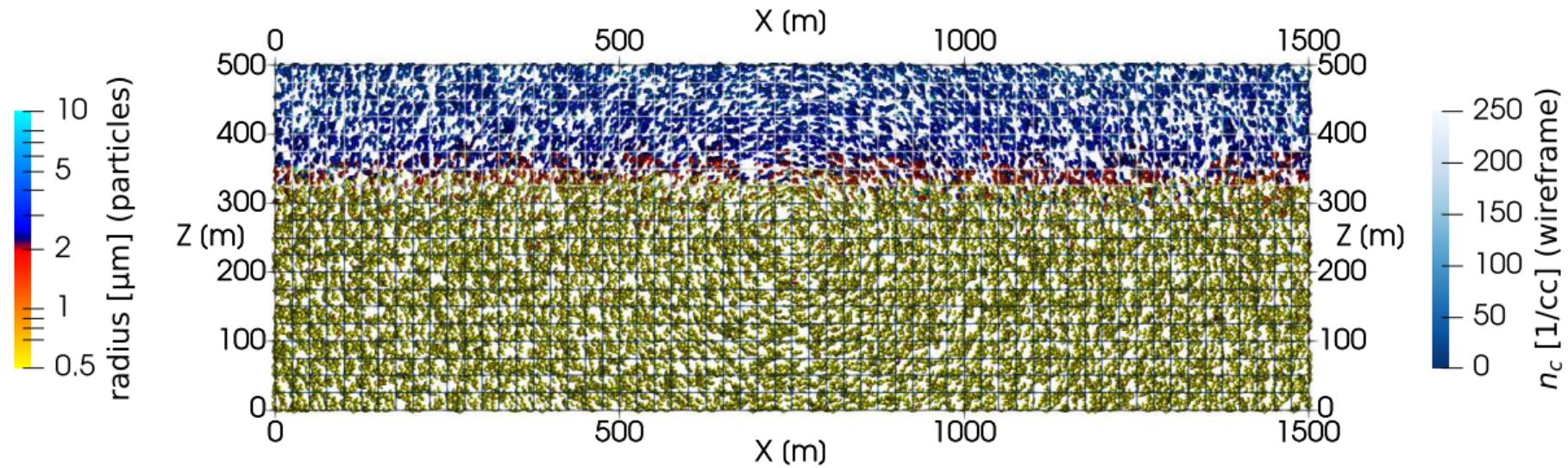
Time: 30 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

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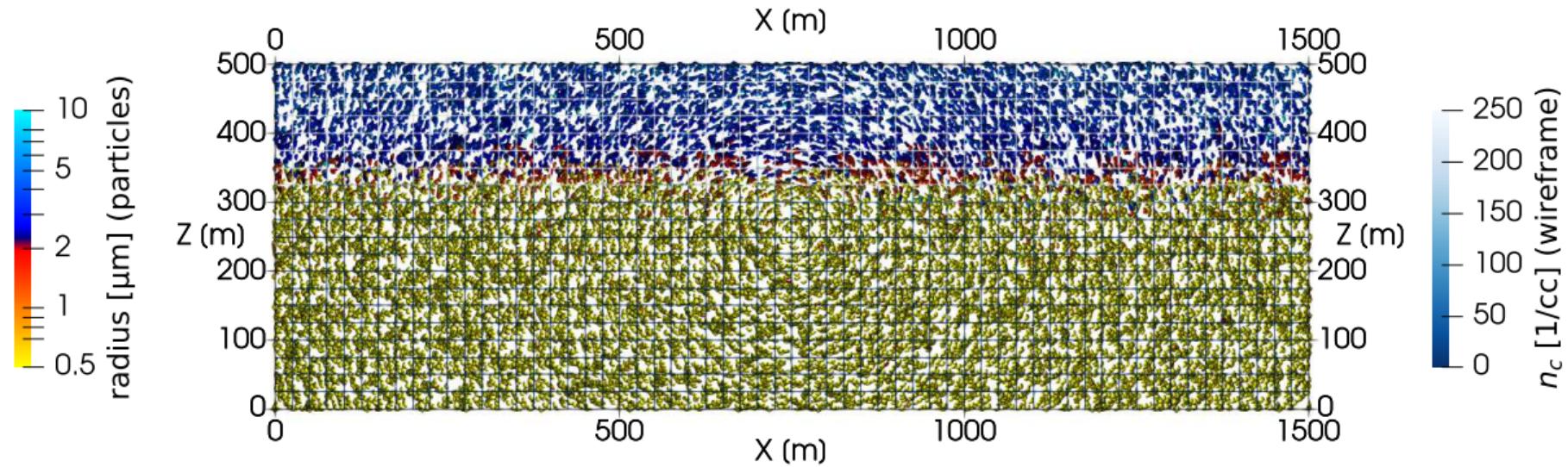
Time: 60 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
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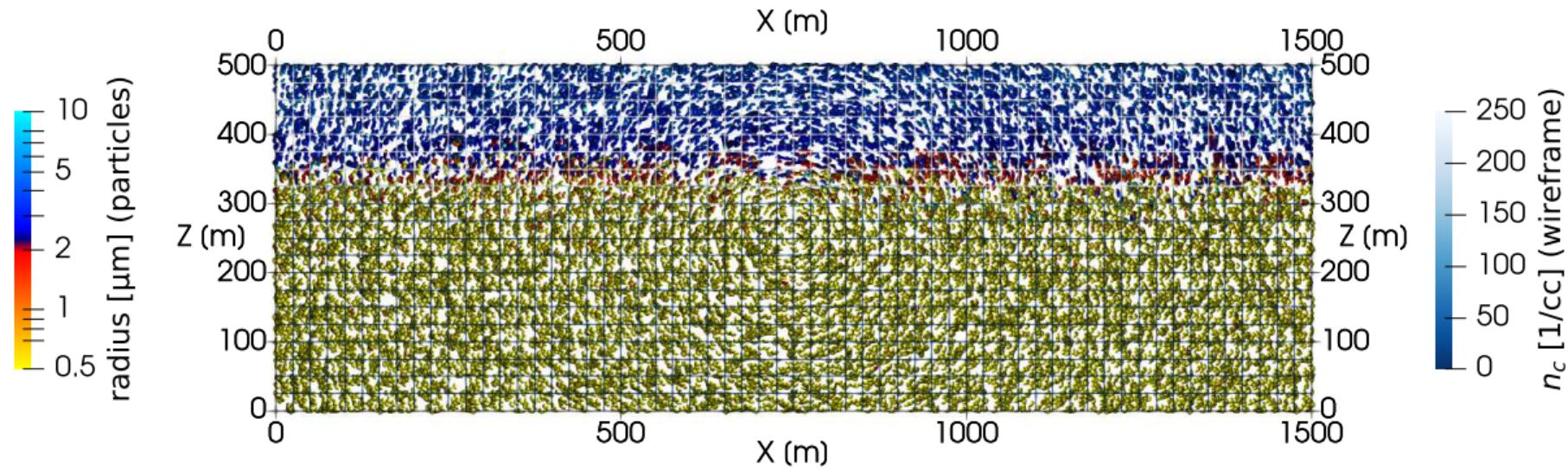
Time: 90 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
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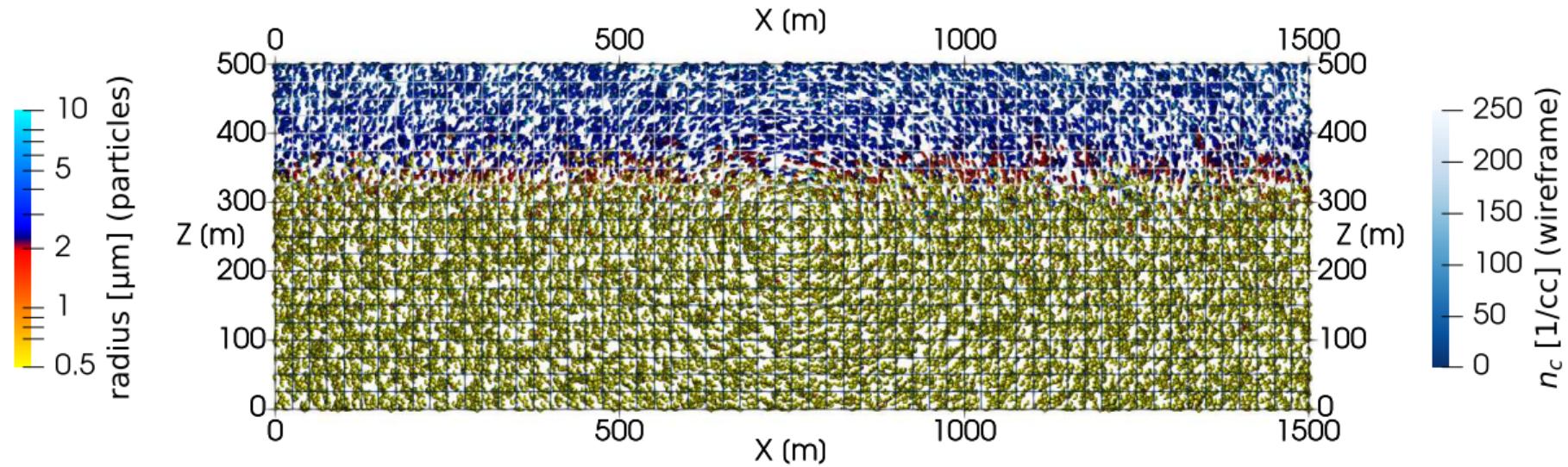
Time: 120 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \text{ } \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
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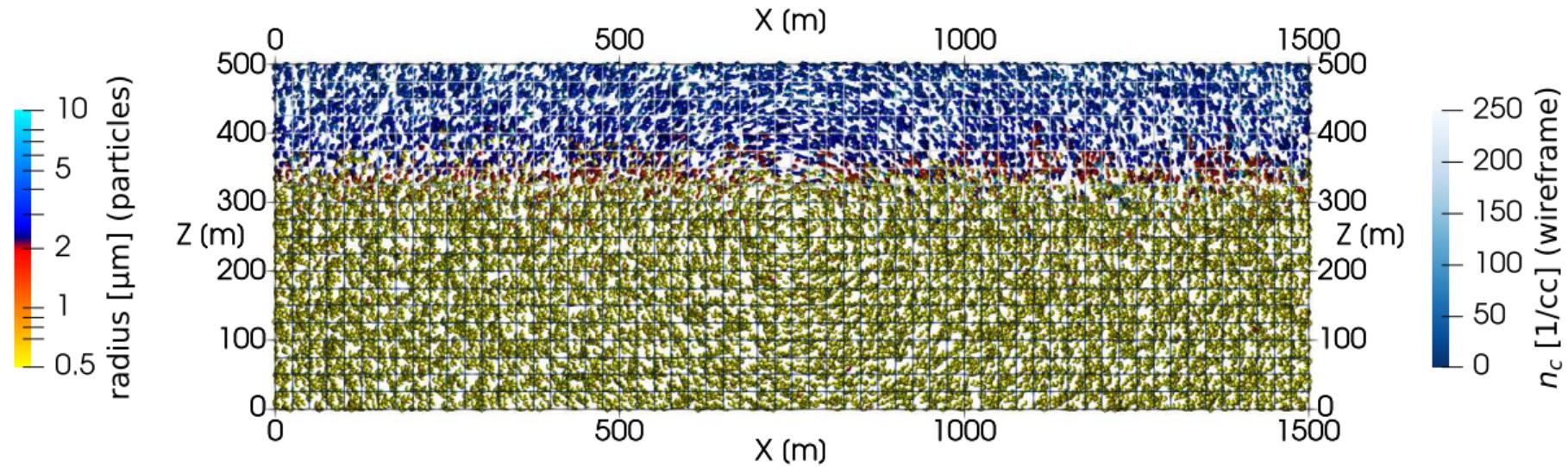
Time: 150 s (spin-up till 600.0 s)



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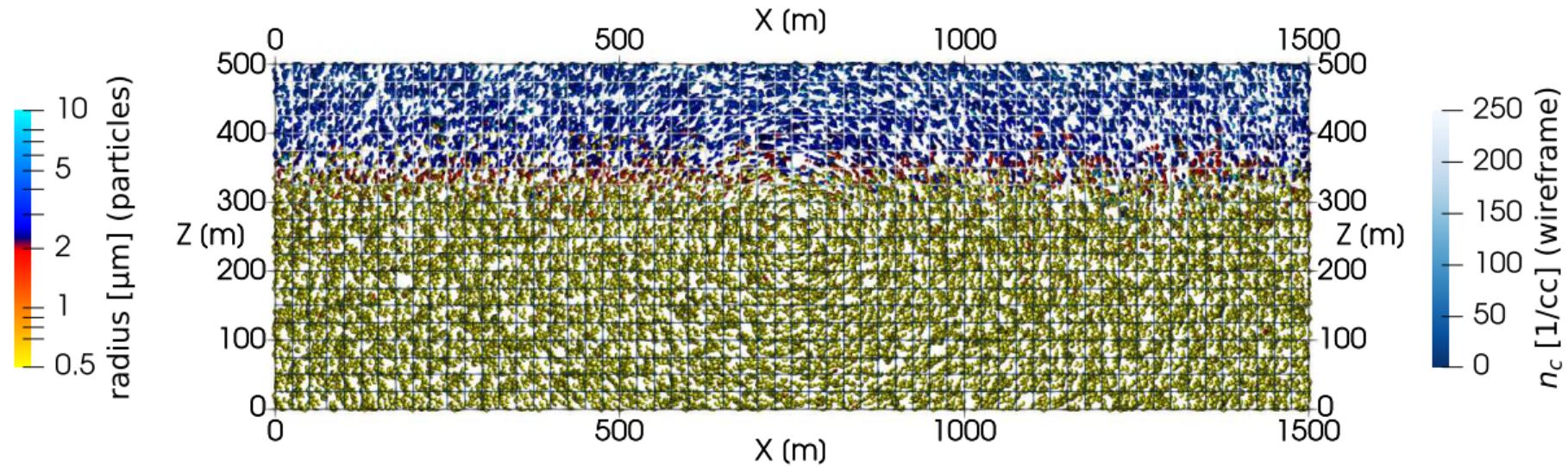
Time: 180 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
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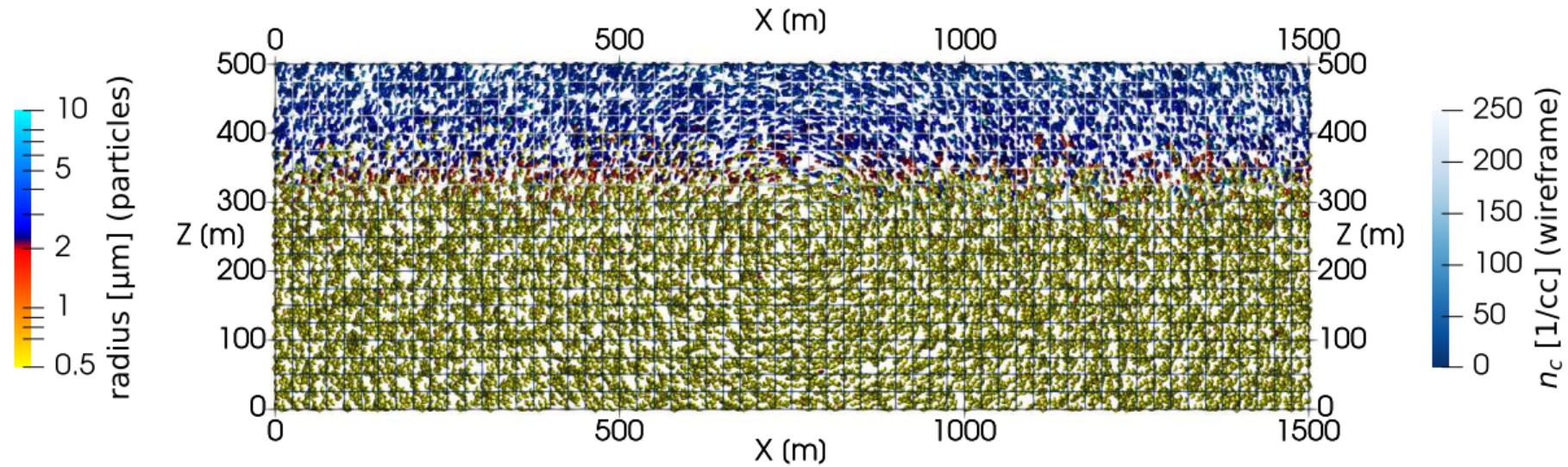
Time: 210 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
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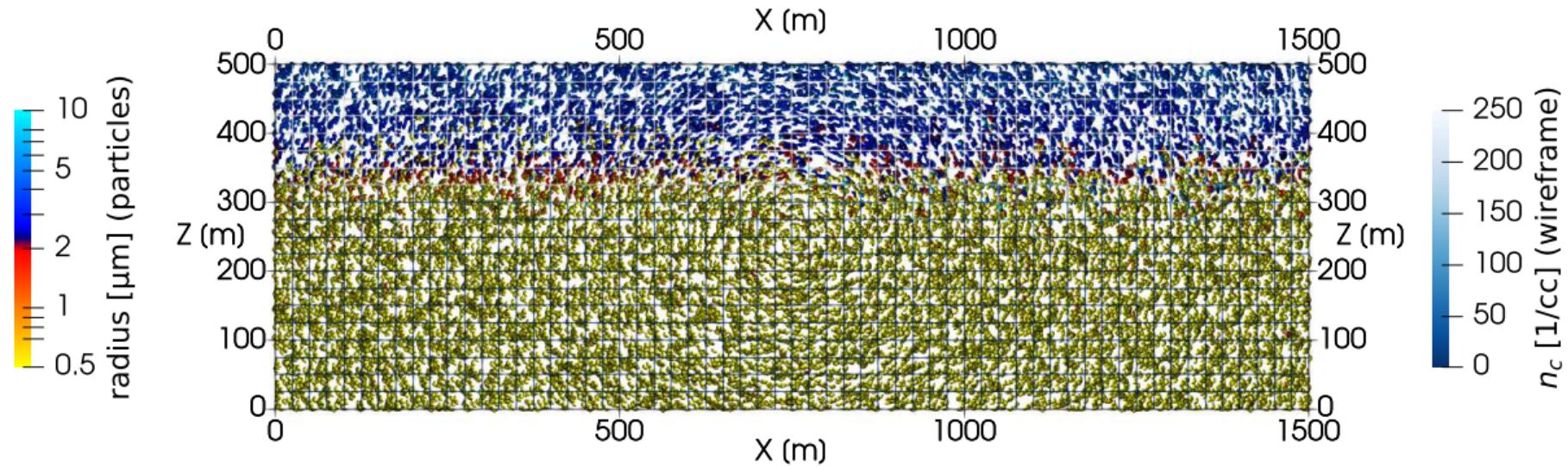
Time: 240 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
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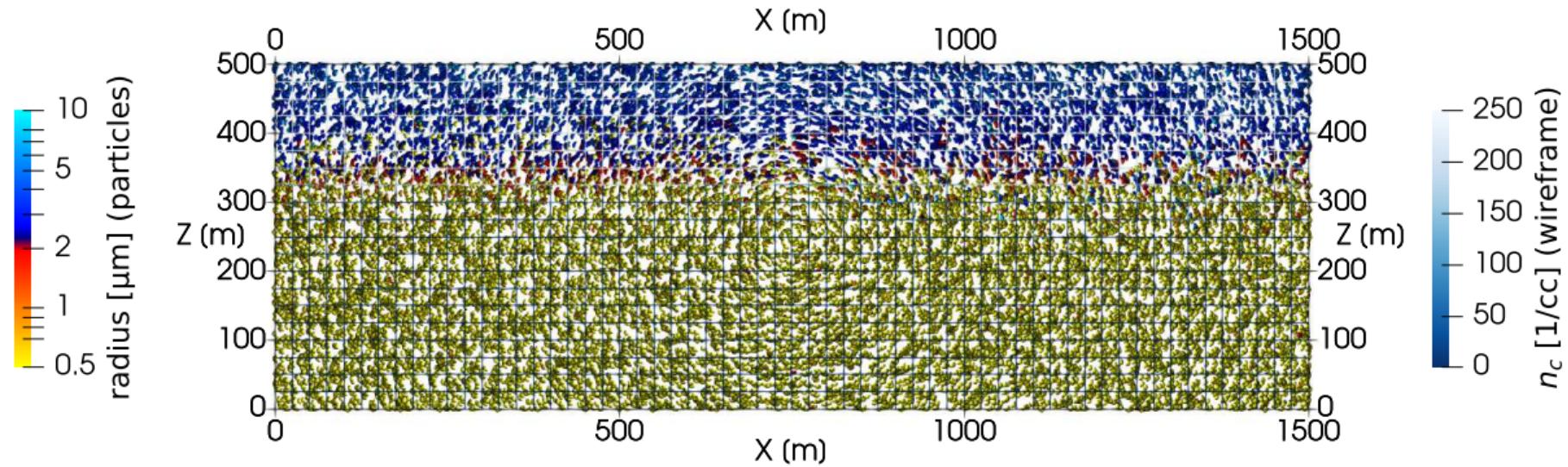
Time: 270 s (spin-up till 600.0 s)



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 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
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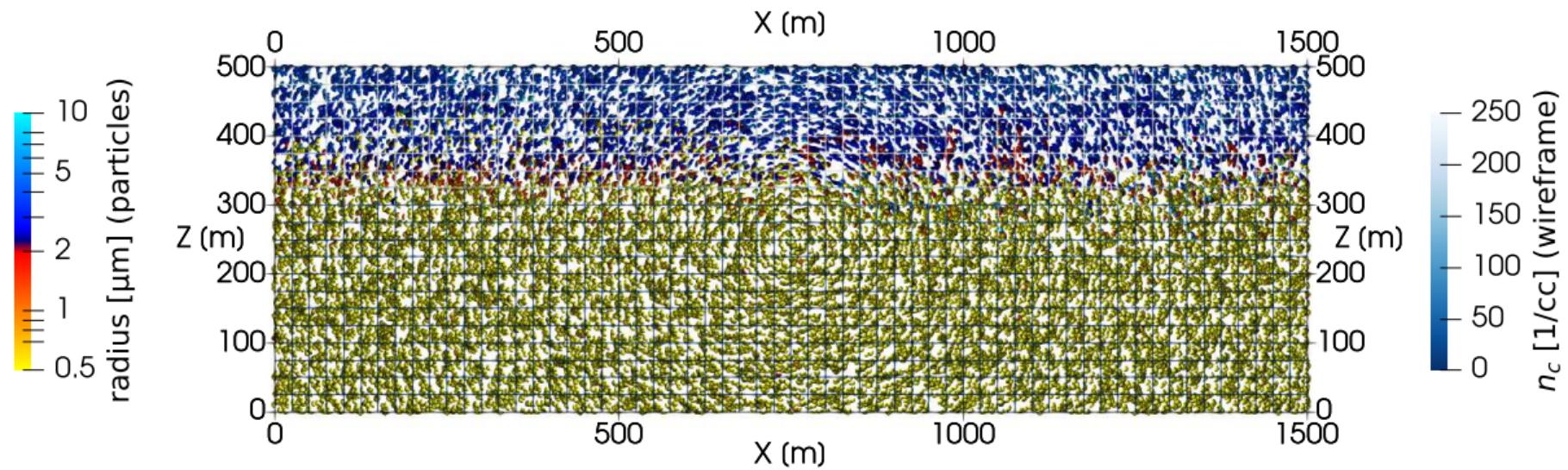
Time: 300 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \text{ } \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
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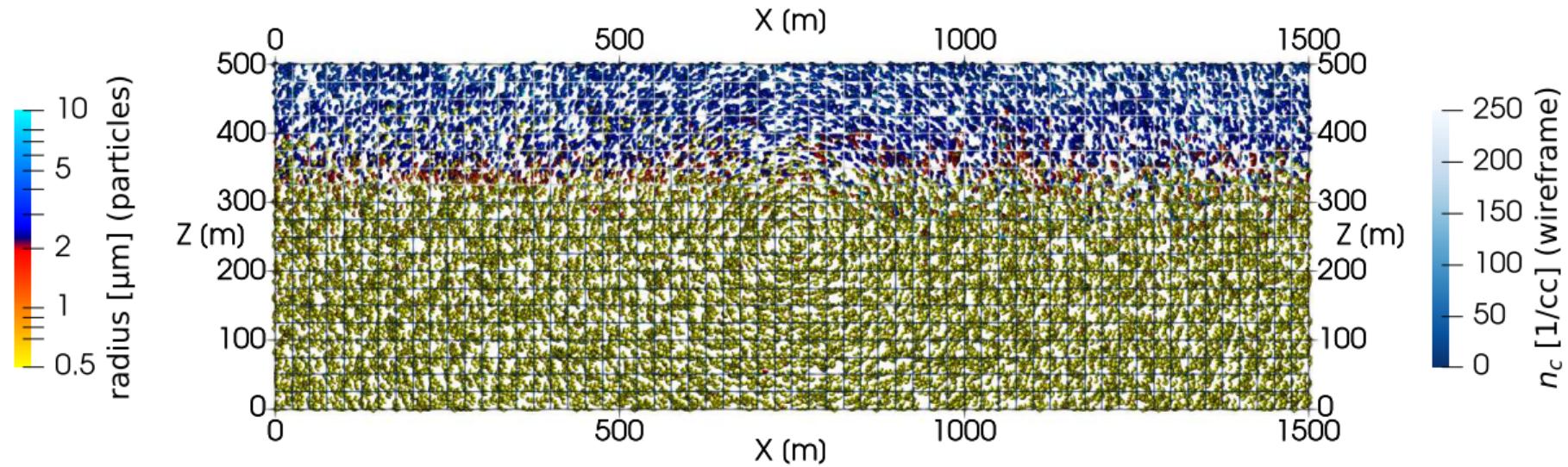
Time: 330 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
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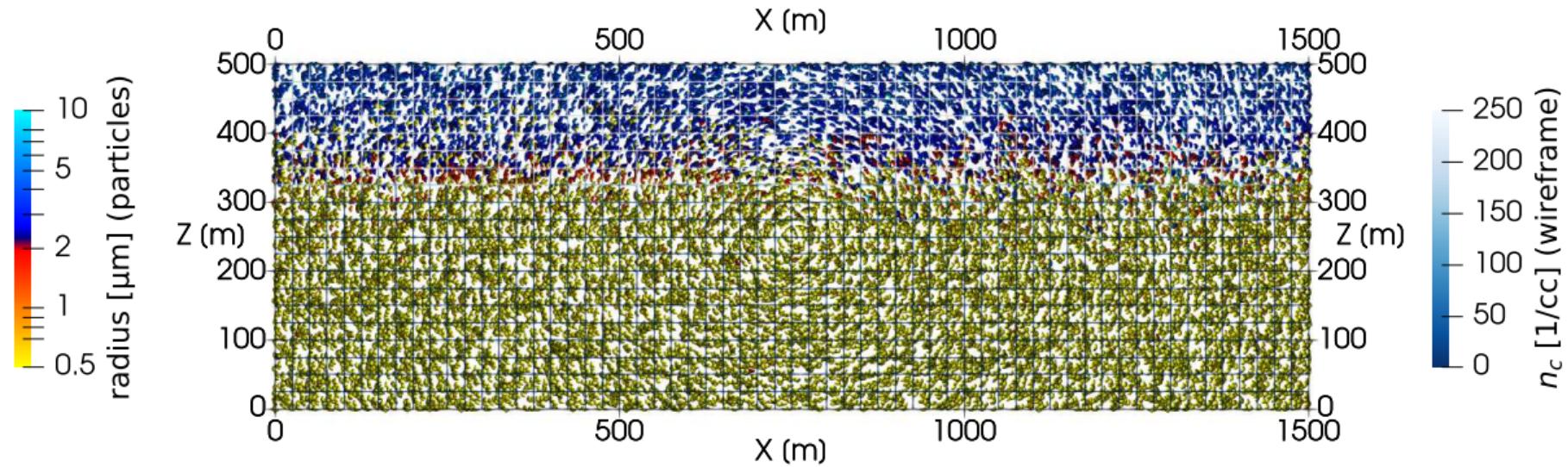
Time: 360 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

## particle-based $\mu$ -physics + prescribed-flow test

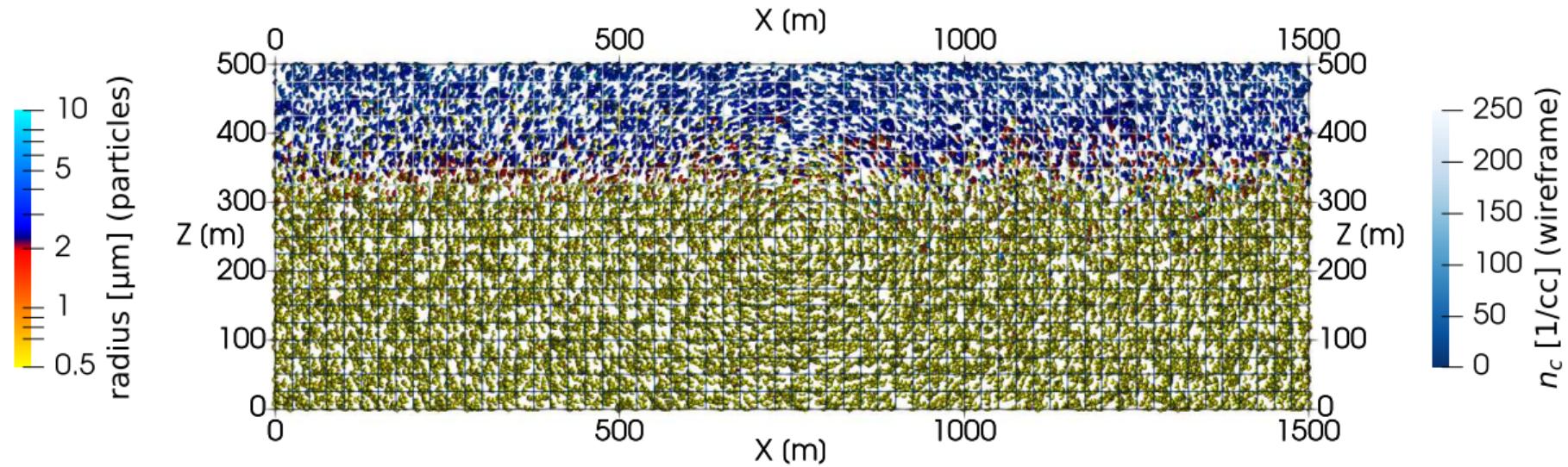
Time: 390 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

## particle-based $\mu$ -physics + prescribed-flow test

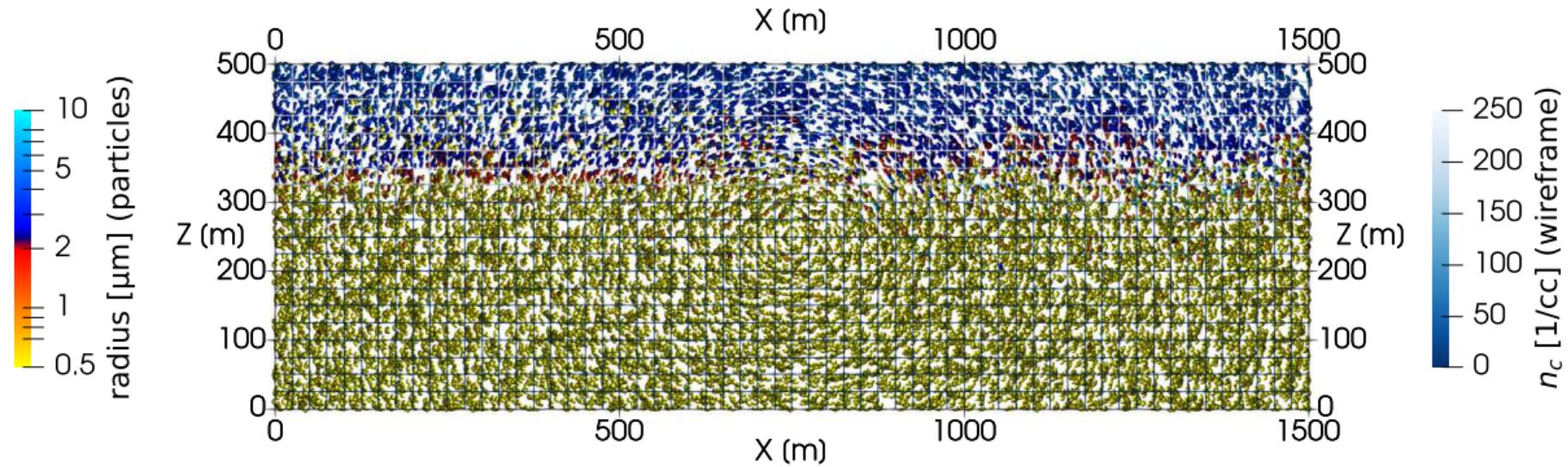
Time: 420 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

## particle-based $\mu$ -physics + prescribed-flow test

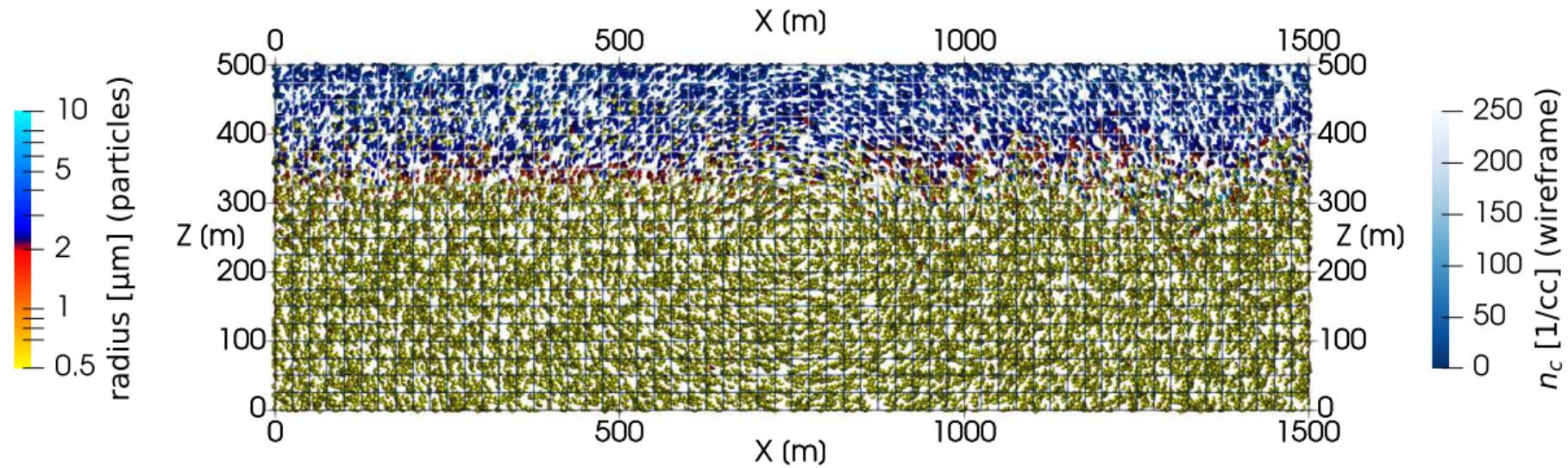
Time: 450 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

## particle-based $\mu$ -physics + prescribed-flow test

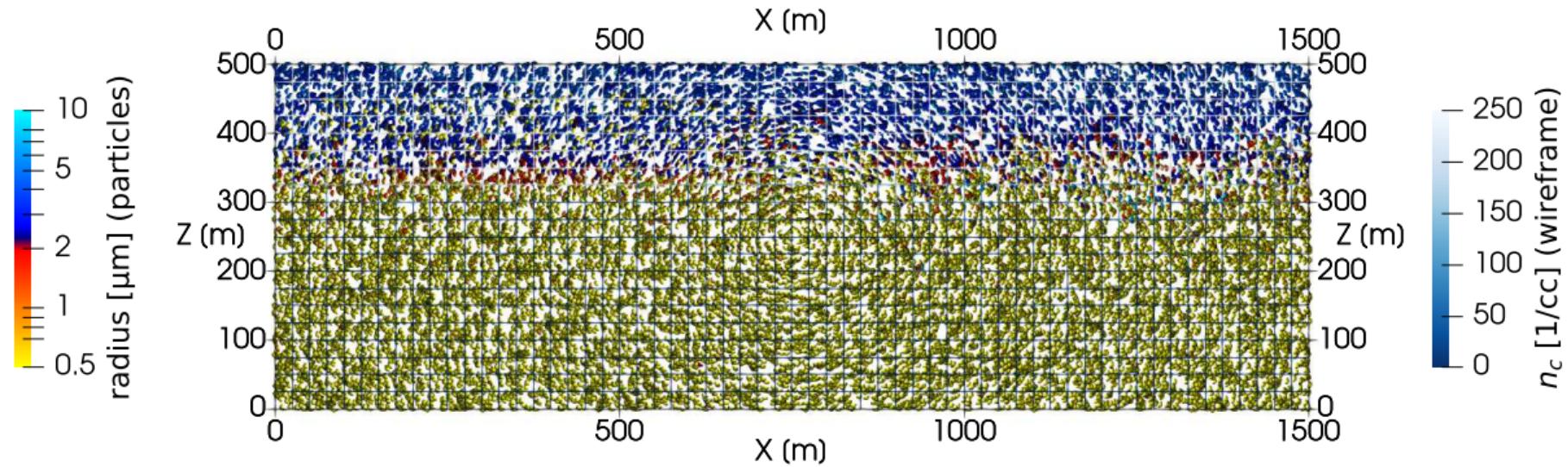
Time: 480 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

## particle-based $\mu$ -physics + prescribed-flow test

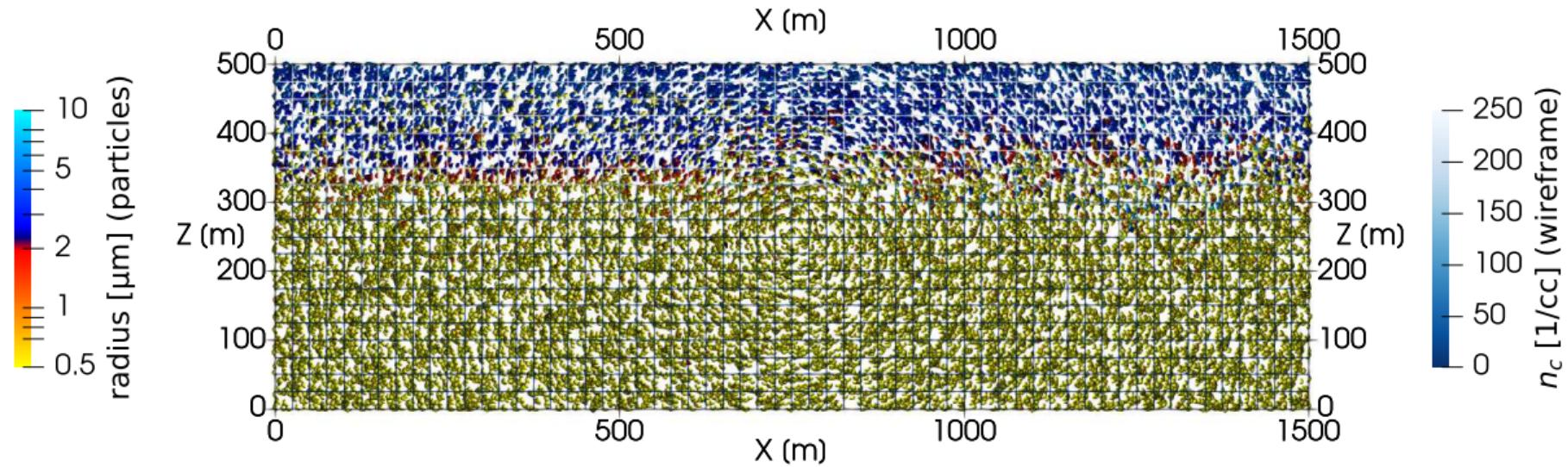
Time: 510 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

## particle-based $\mu$ -physics + prescribed-flow test

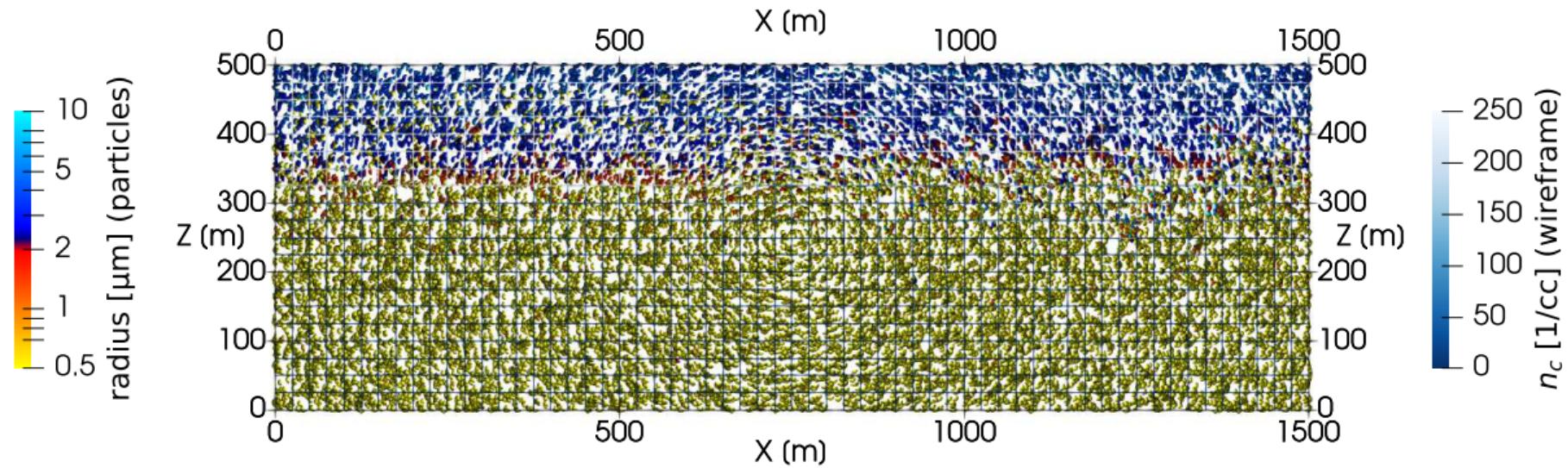
Time: 540 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

## particle-based $\mu$ -physics + prescribed-flow test

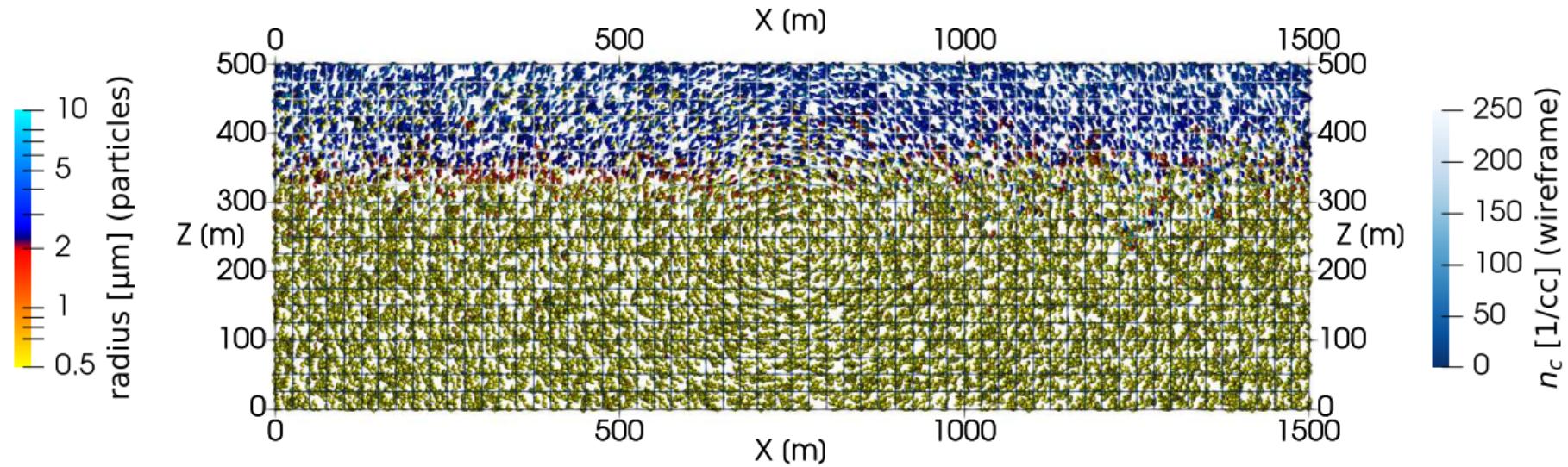
Time: 570 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

## particle-based $\mu$ -physics + prescribed-flow test

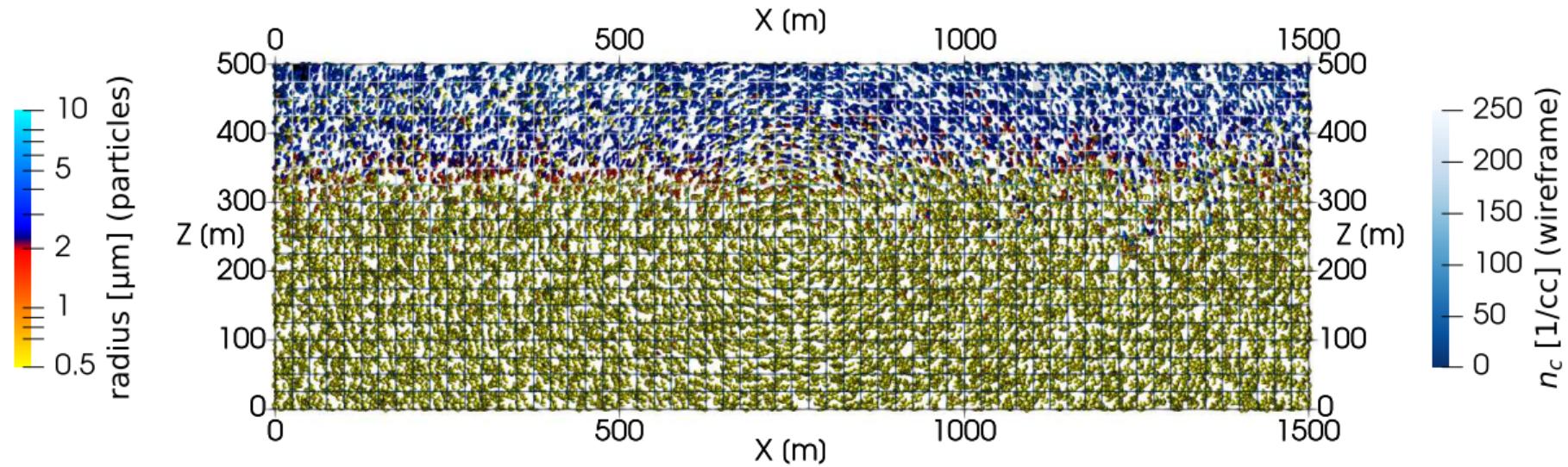
Time: 600 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)    $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

## particle-based $\mu$ -physics + prescribed-flow test

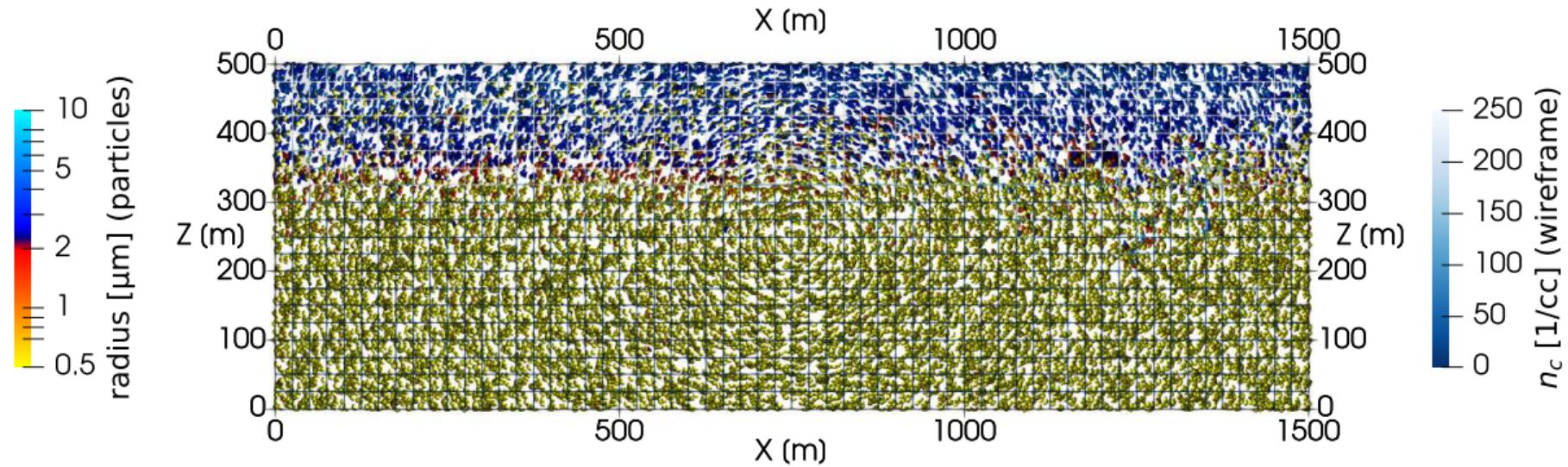
Time: 630 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

## particle-based $\mu$ -physics + prescribed-flow test

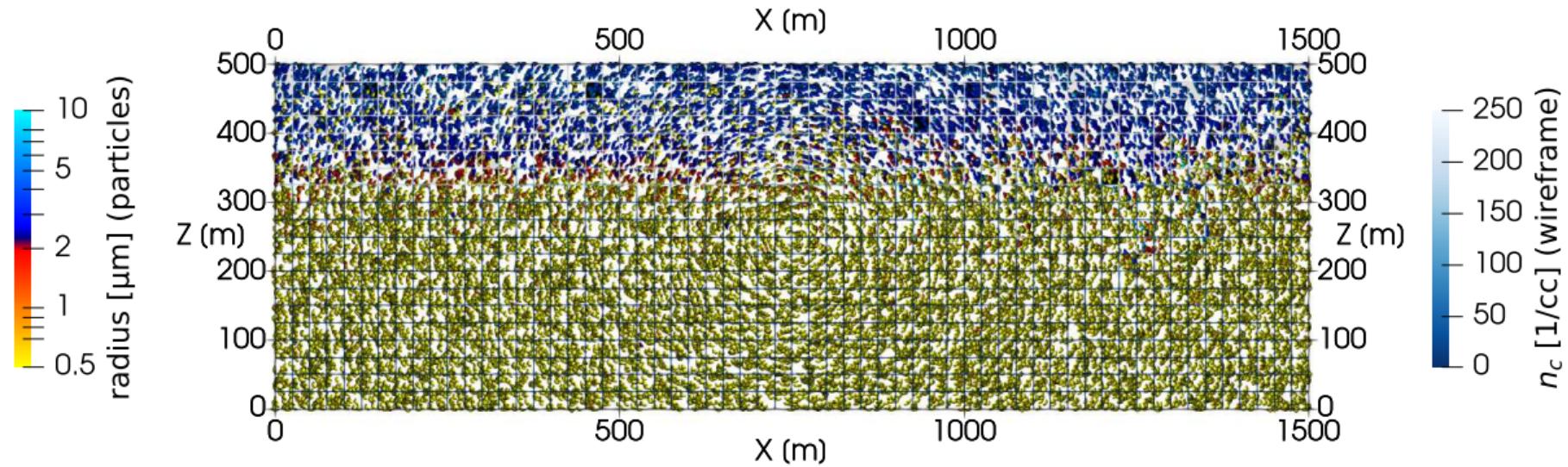
Time: 660 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

## particle-based $\mu$ -physics + prescribed-flow test

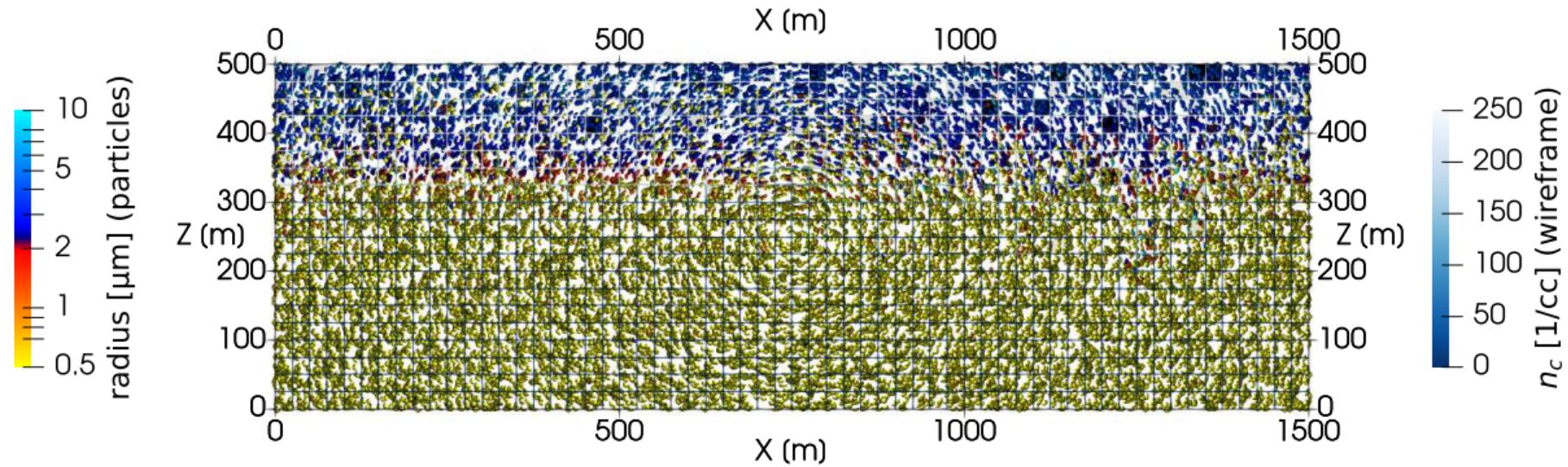
Time: 690 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

## particle-based $\mu$ -physics + prescribed-flow test

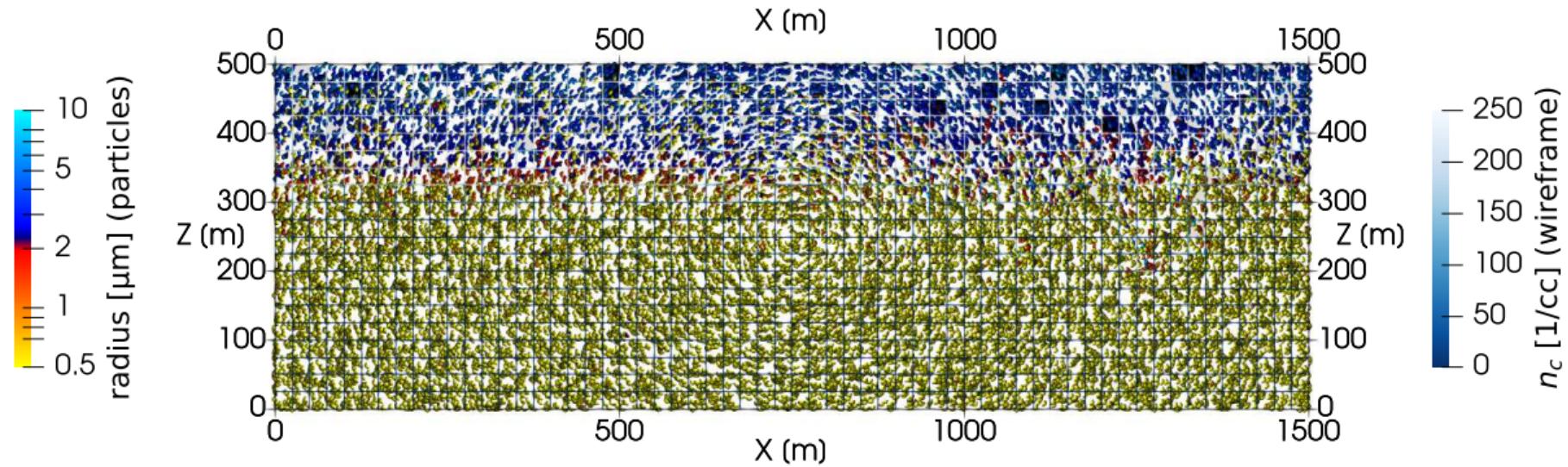
Time: 720 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

## particle-based $\mu$ -physics + prescribed-flow test

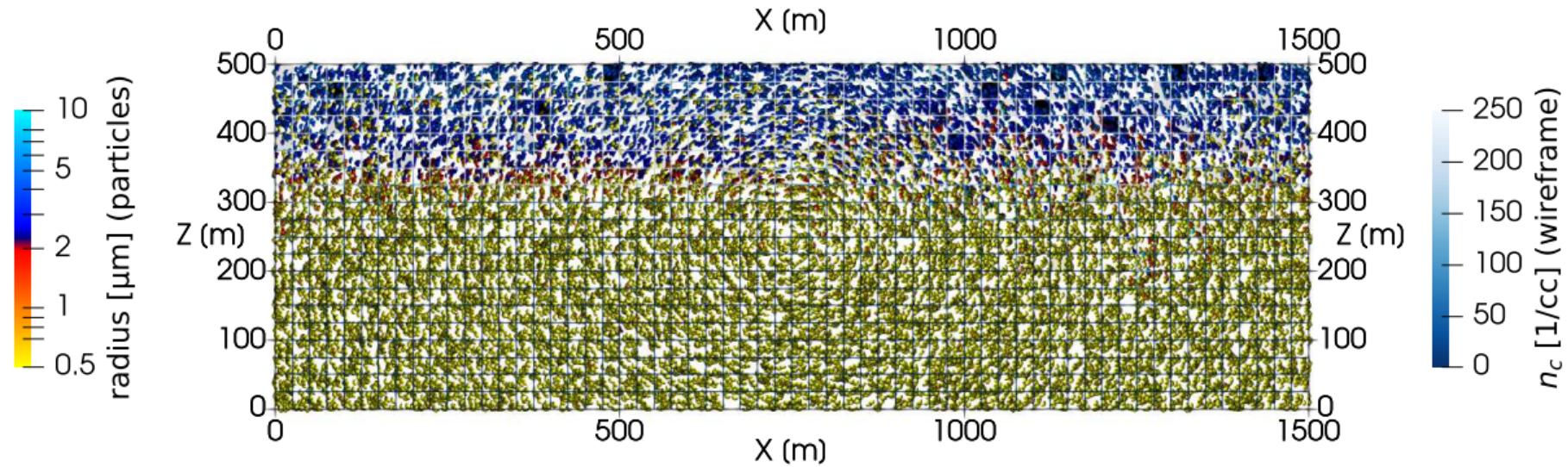
Time: 750 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

## particle-based $\mu$ -physics + prescribed-flow test

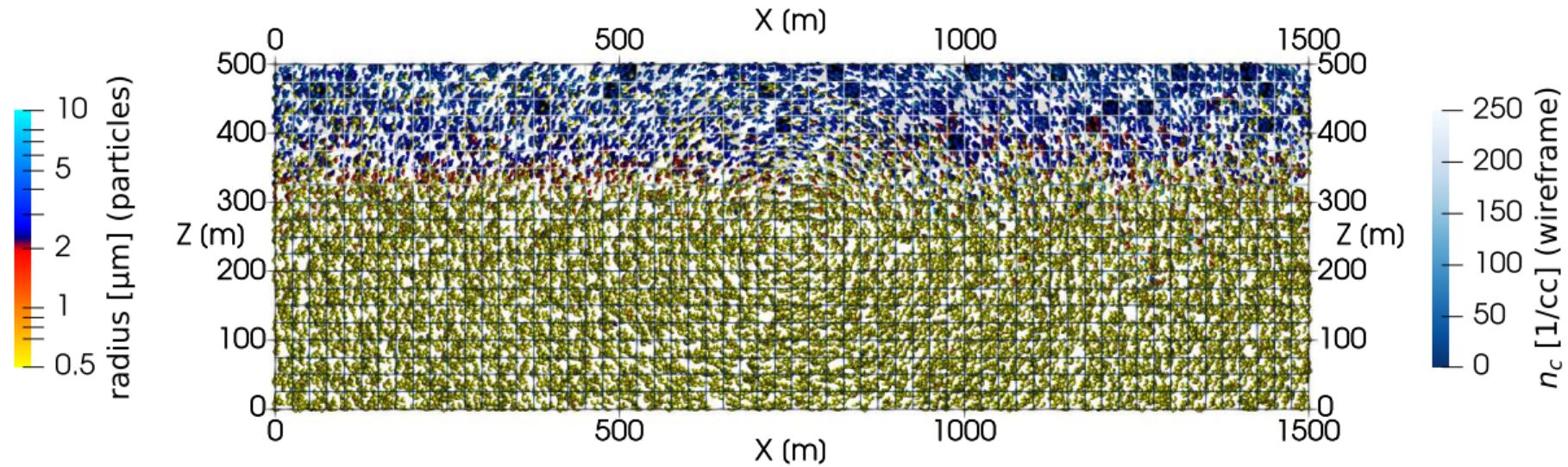
Time: 780 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

## particle-based $\mu$ -physics + prescribed-flow test

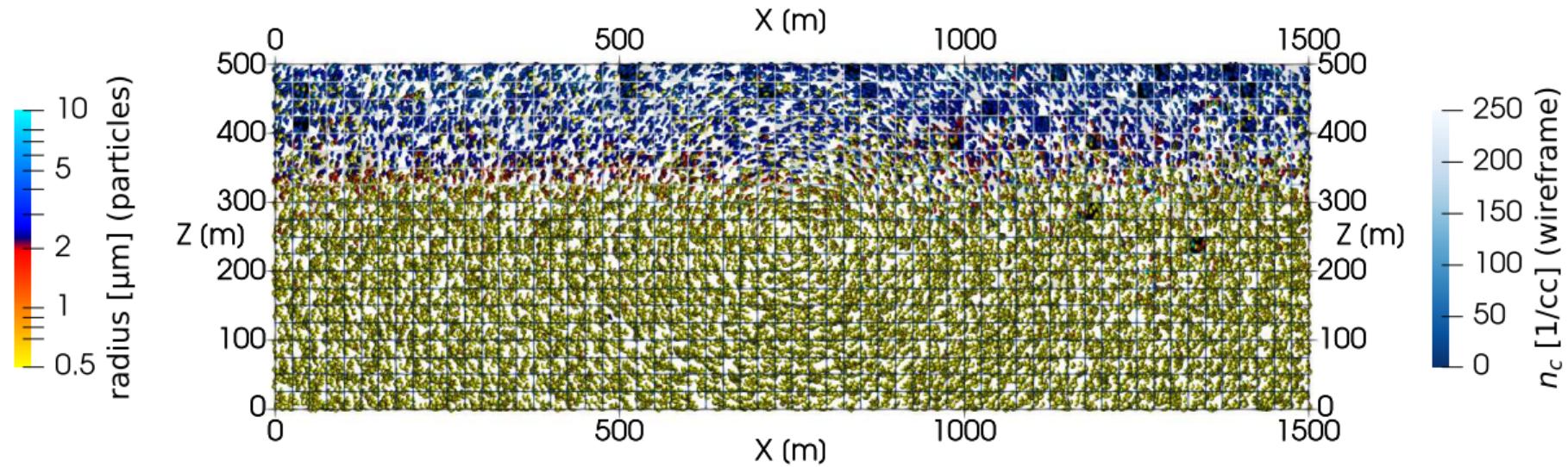
Time: 810 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

## particle-based $\mu$ -physics + prescribed-flow test

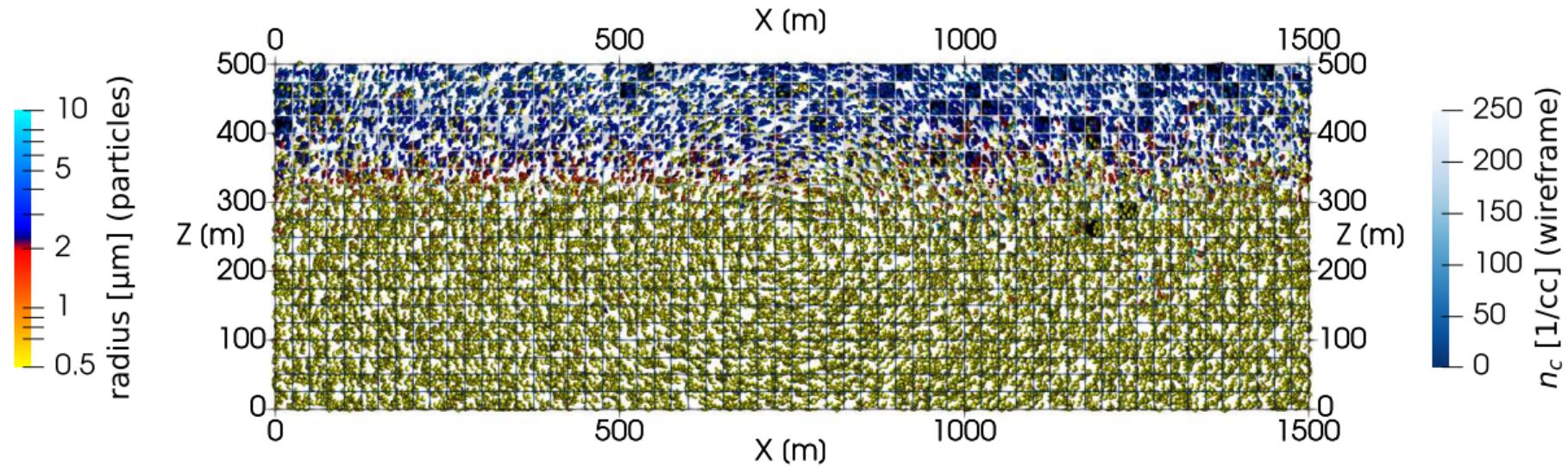
Time: 840 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

## particle-based $\mu$ -physics + prescribed-flow test

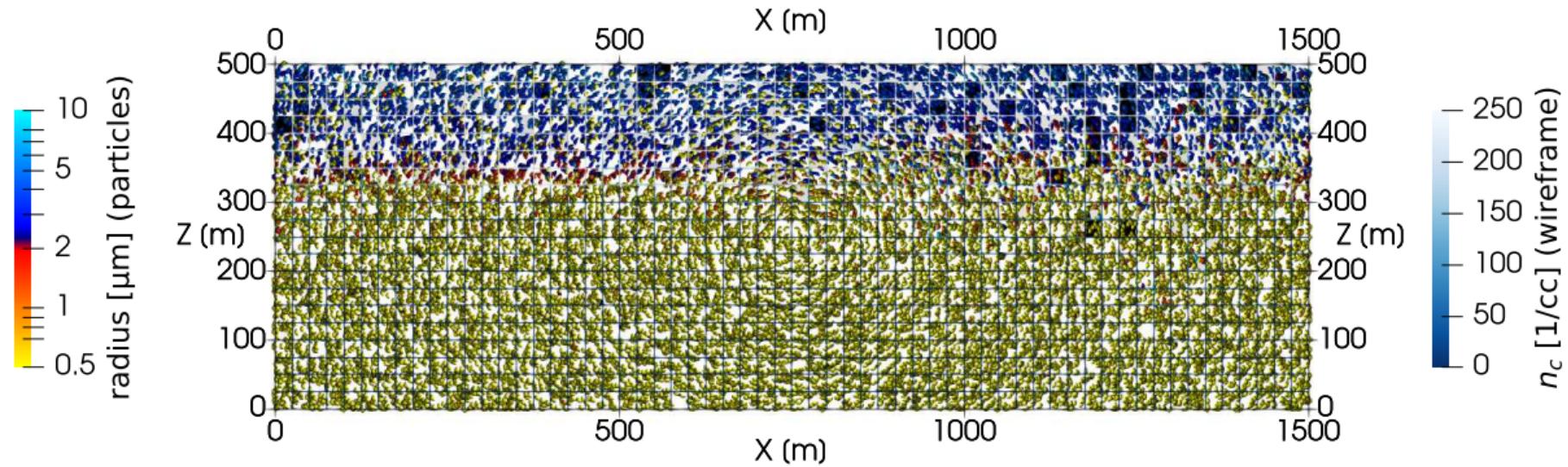
Time: 870 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

## particle-based $\mu$ -physics + prescribed-flow test

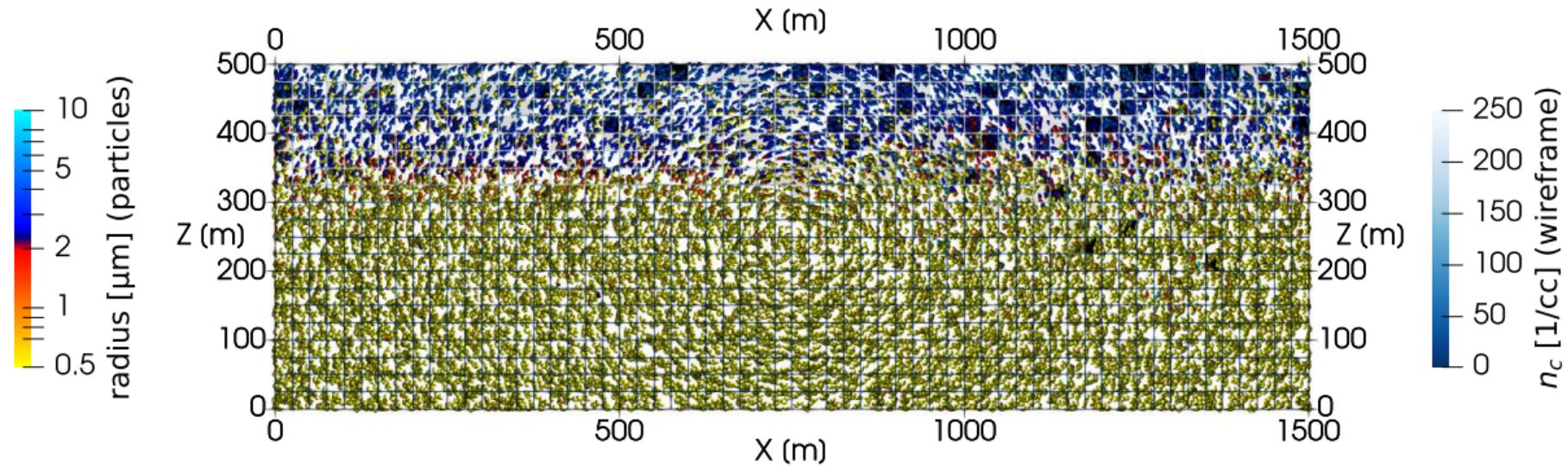
Time: 900 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

## particle-based $\mu$ -physics + prescribed-flow test

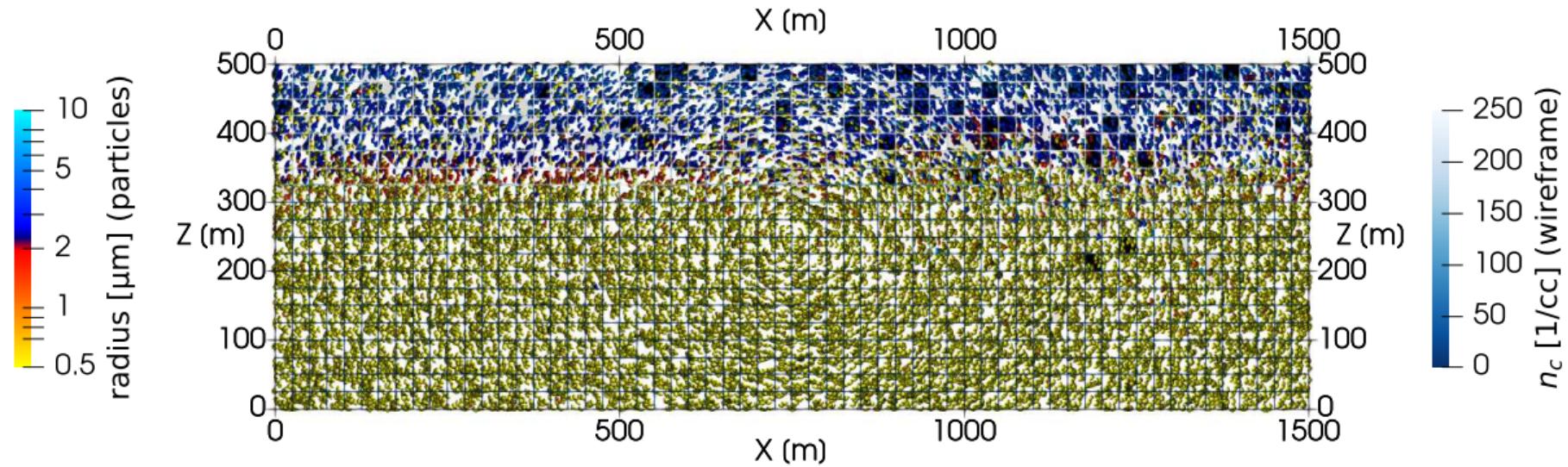
Time: 930 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

## particle-based $\mu$ -physics + prescribed-flow test

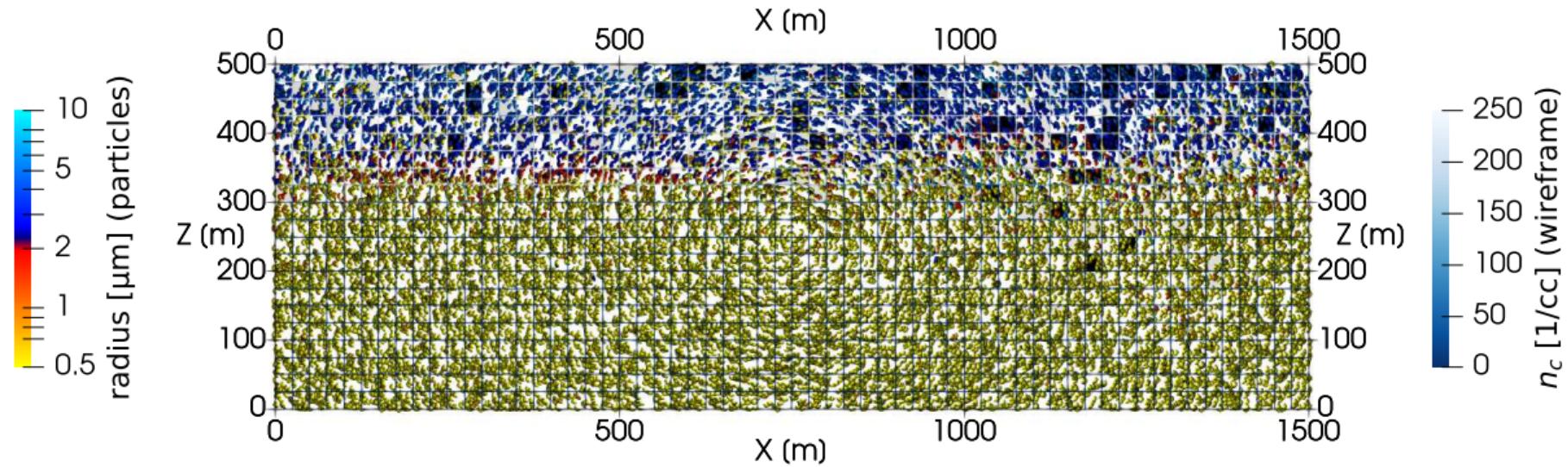
Time: 960 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

## particle-based $\mu$ -physics + prescribed-flow test

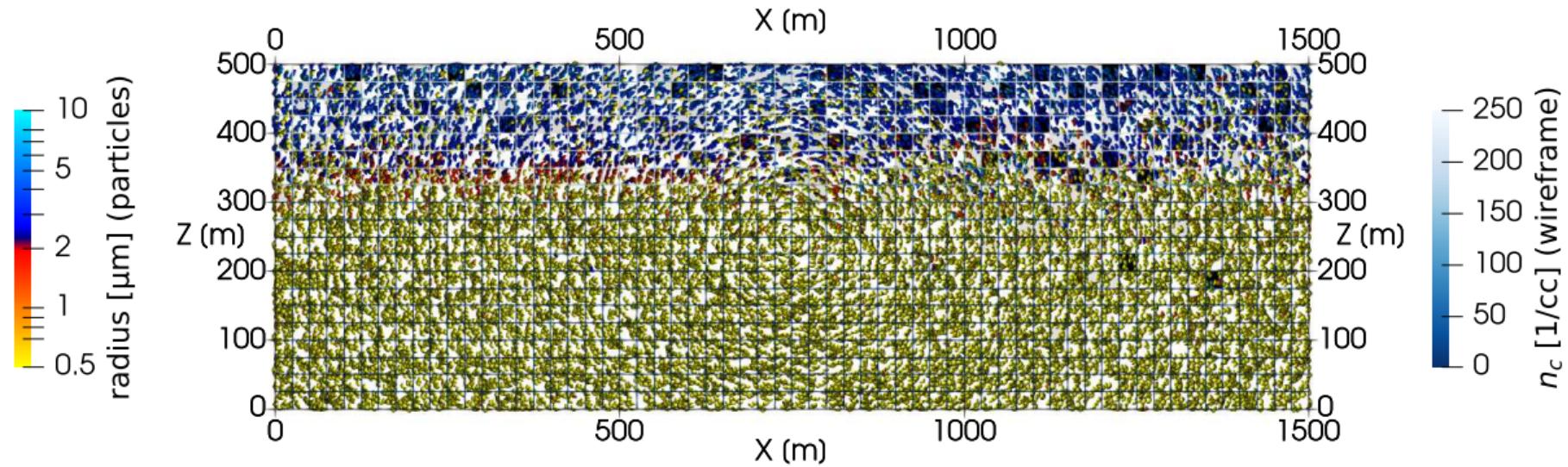
Time: 990 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

## particle-based $\mu$ -physics + prescribed-flow test

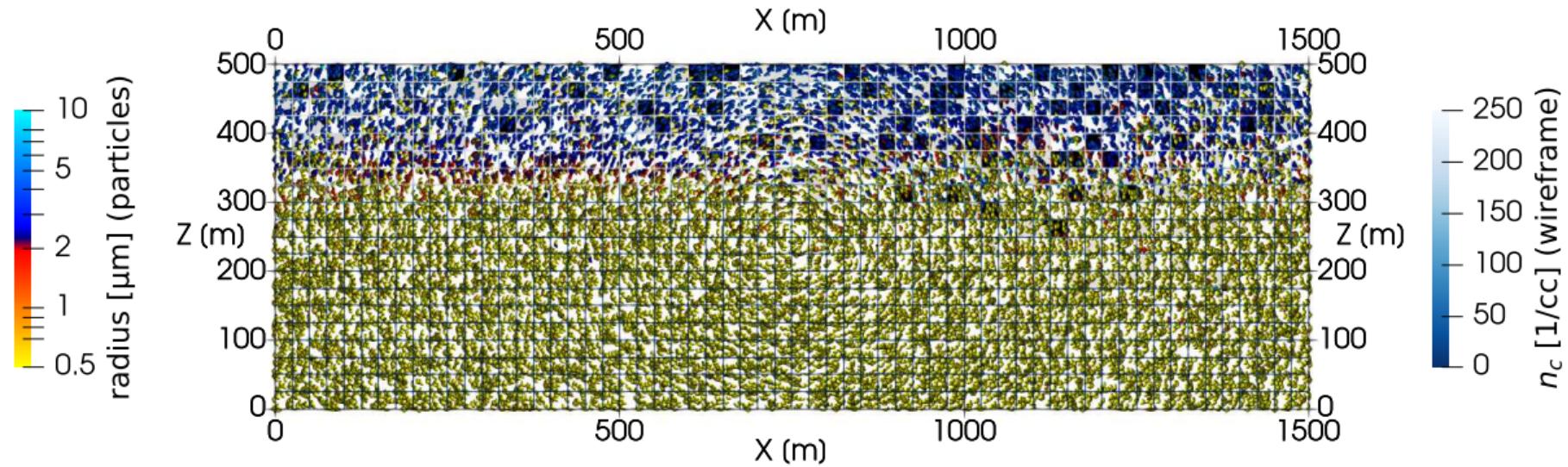
Time: 1020 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

## particle-based $\mu$ -physics + prescribed-flow test

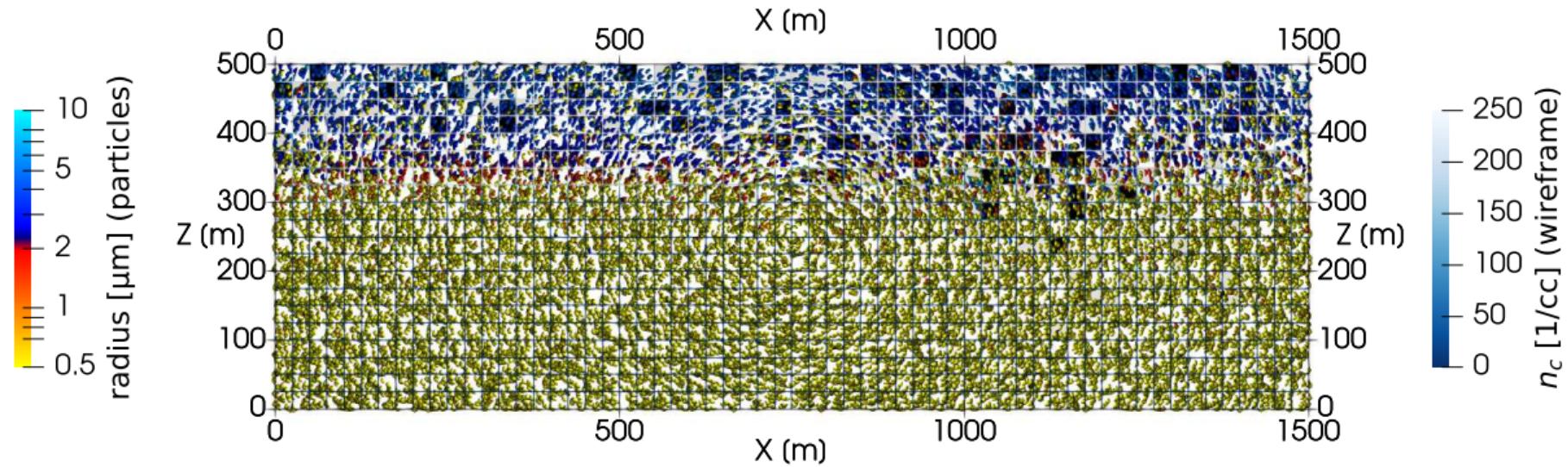
Time: 1050 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

## particle-based $\mu$ -physics + prescribed-flow test

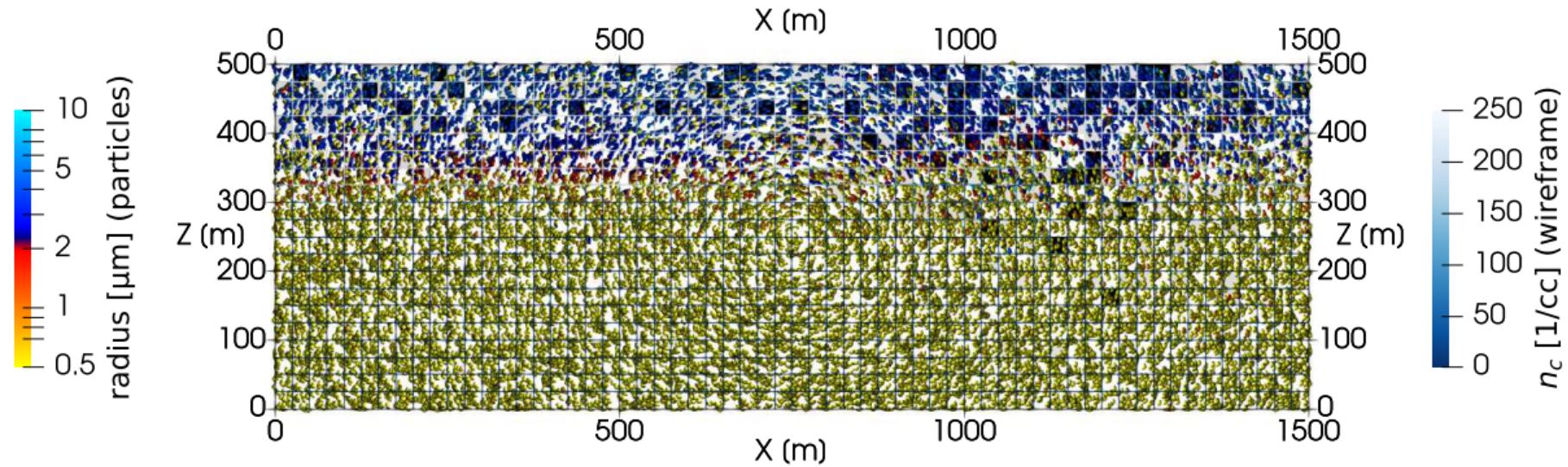
Time: 1080 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

## particle-based $\mu$ -physics + prescribed-flow test

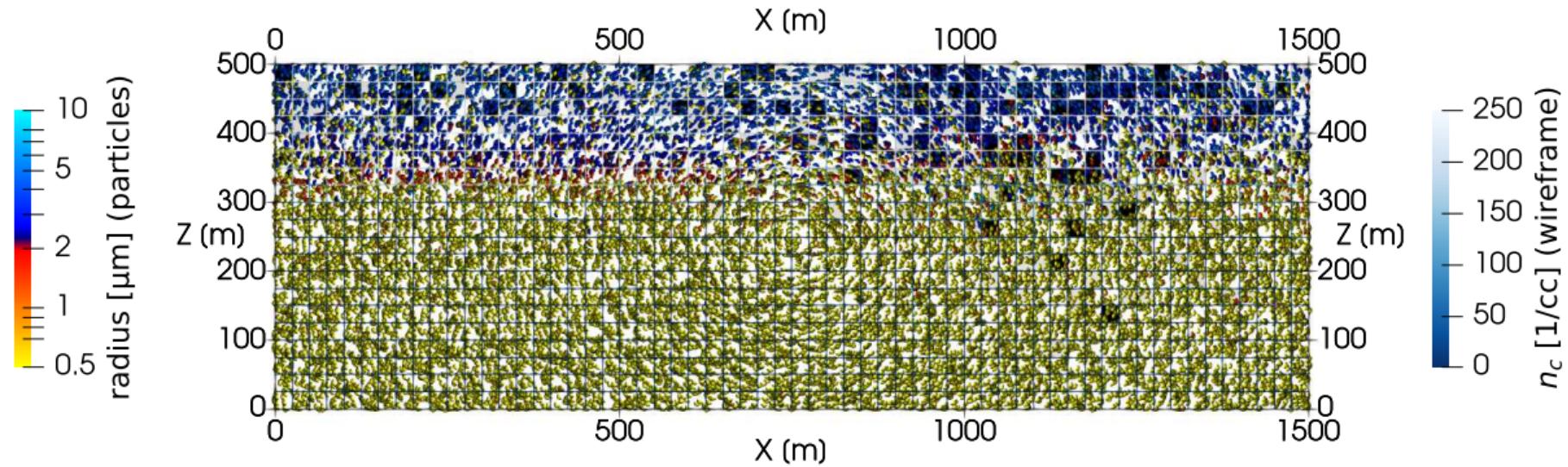
Time: 1110 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

## particle-based $\mu$ -physics + prescribed-flow test

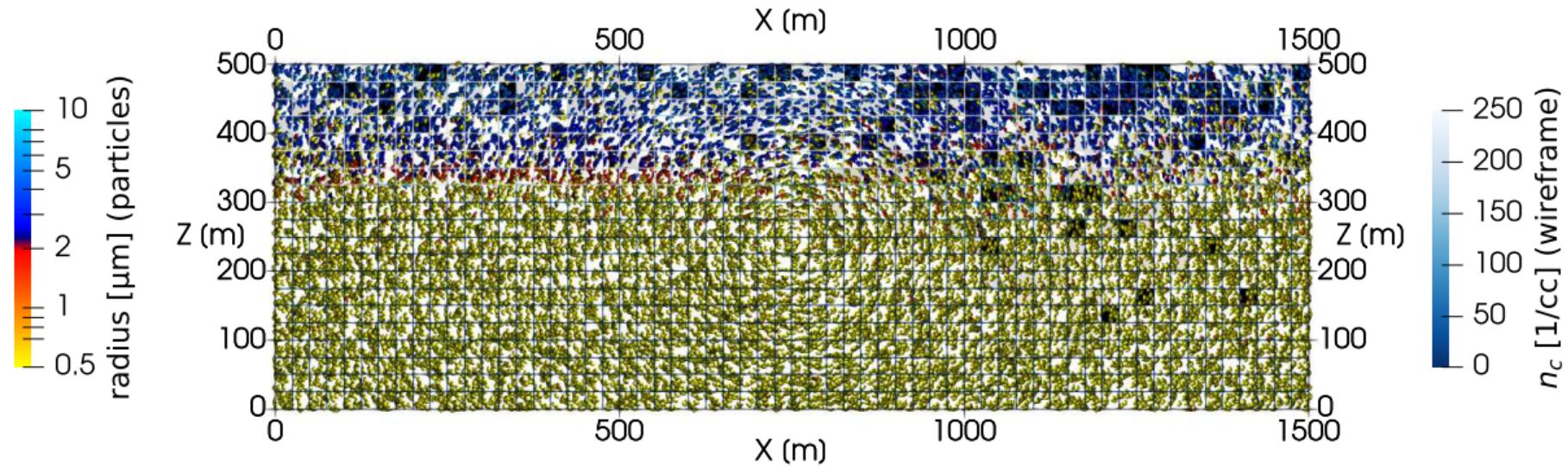
Time: 1140 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

## particle-based $\mu$ -physics + prescribed-flow test

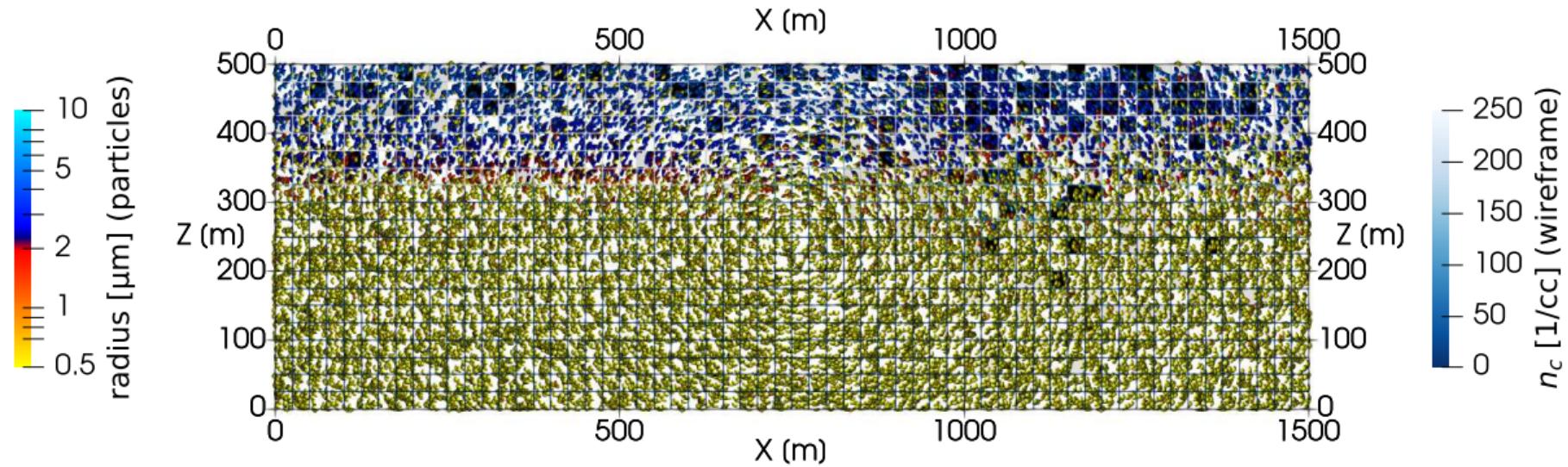
Time: 1170 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

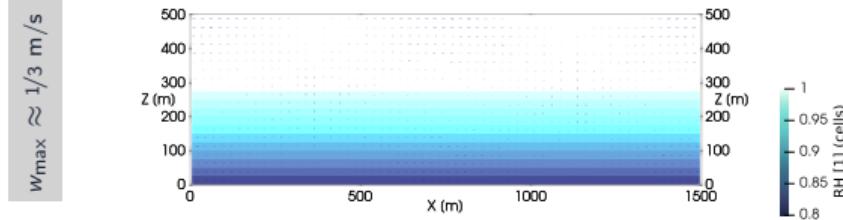
## particle-based $\mu$ -physics + prescribed-flow test

Time: 1200 s (spin-up till 600.0 s)



16+16 super-particles/cell for INP-rich + INP-free particles  
 $N_{\text{aer}} = 300/\text{cc}$  (two-mode lognormal)     $N_{\text{INP}} = 150/L$  (lognormal,  $D_g = 0.74 \mu\text{m}$ ,  $\sigma_g = 2.55$ )  
 spin-up = freezing off; subsequently frozen particles act as tracers

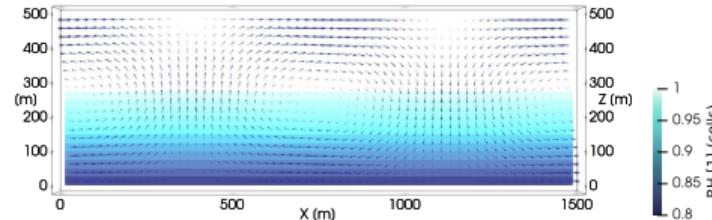
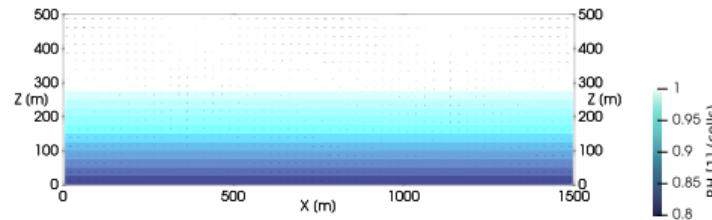
testing three flow regimes and two immersion freezing representations



$$w_{\max} \approx 1 \text{ m/s}$$

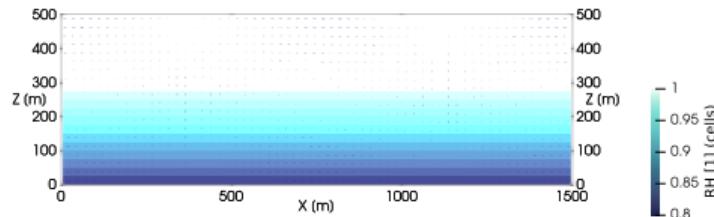
$$w_{\max} \approx 3 \text{ m/s}$$

testing three flow regimes and two immersion freezing representations

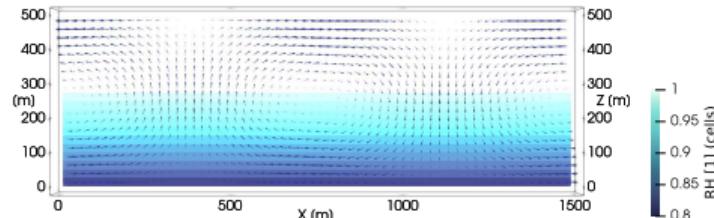


# testing three flow regimes and two immersion freezing representations

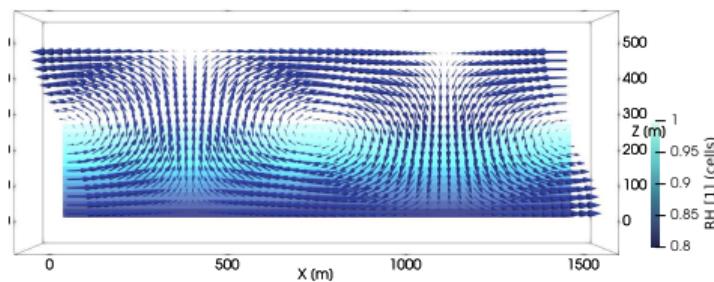
$w_{\max} \approx 1/3 \text{ m/s}$



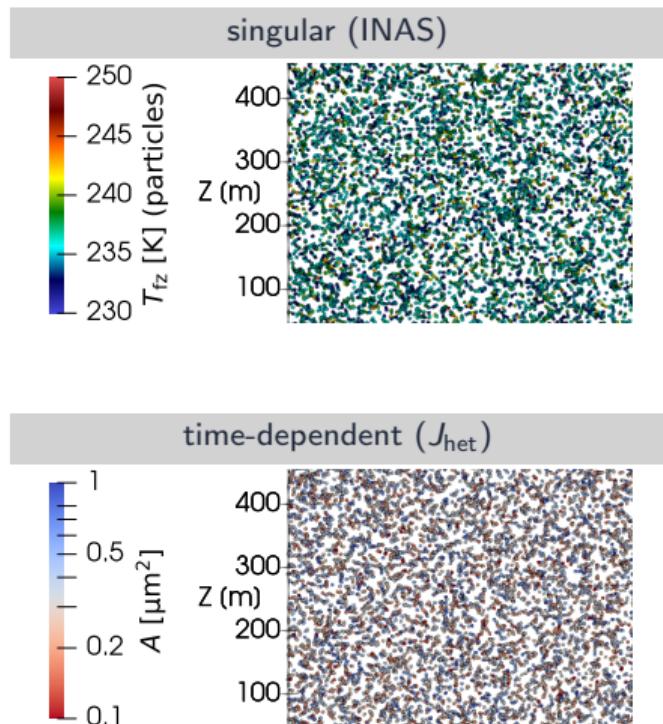
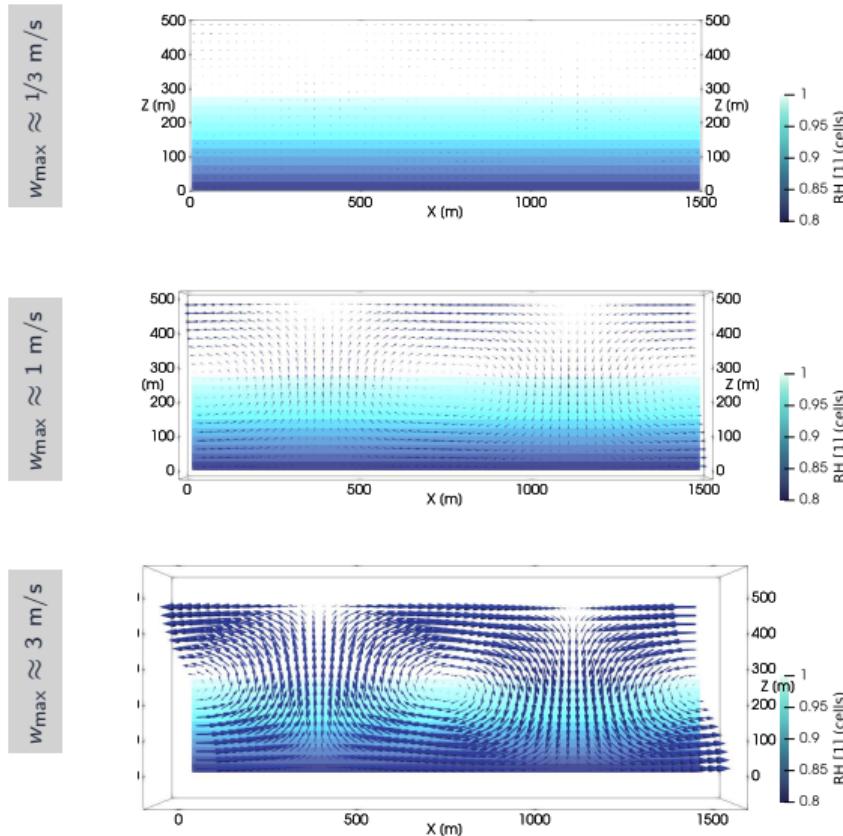
$w_{\max} \approx 1 \text{ m/s}$



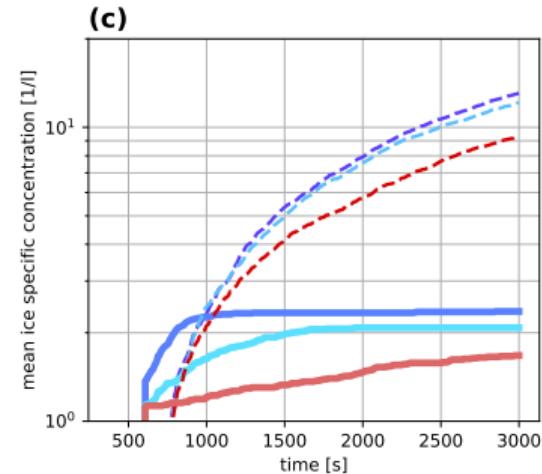
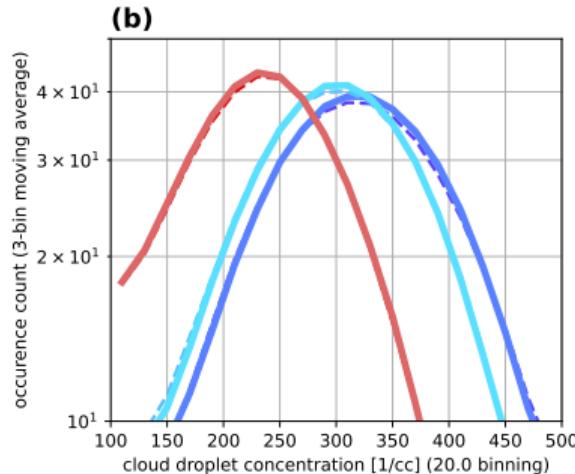
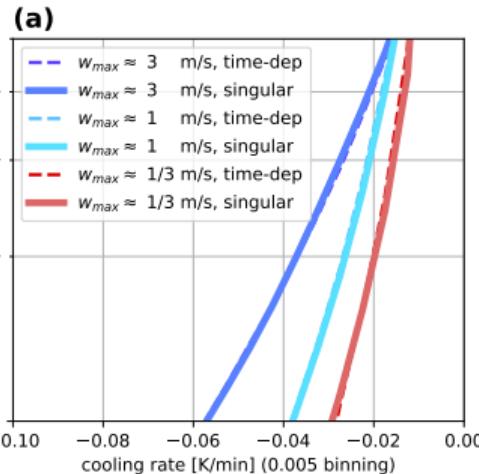
$w_{\max} \approx 3 \text{ m/s}$



testing three flow regimes and two immersion freezing representations

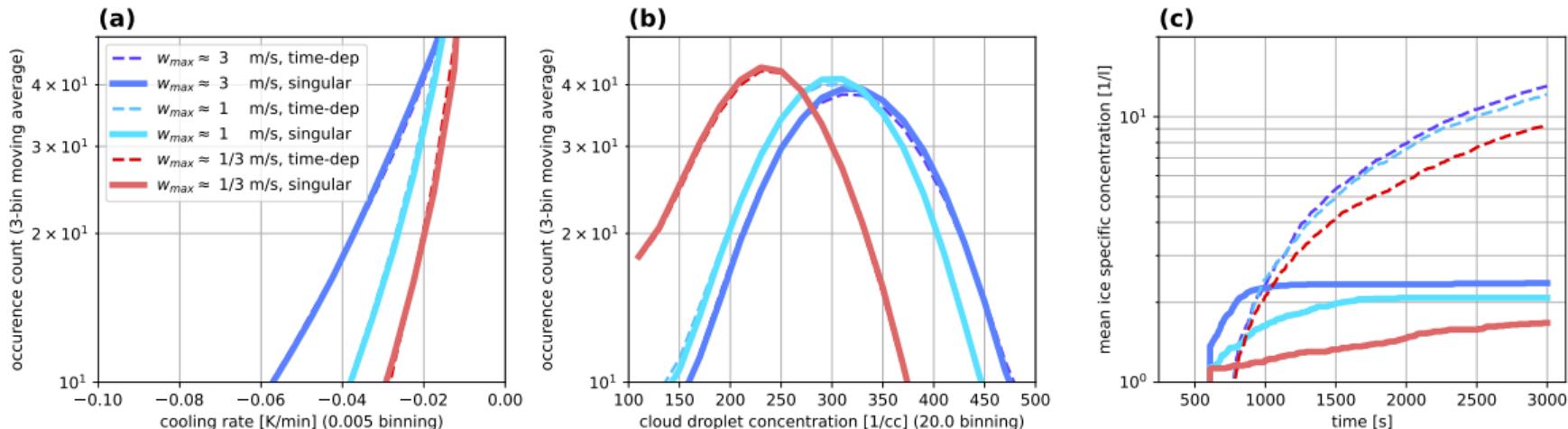


# testing three flow regimes and two immersion freezing representations



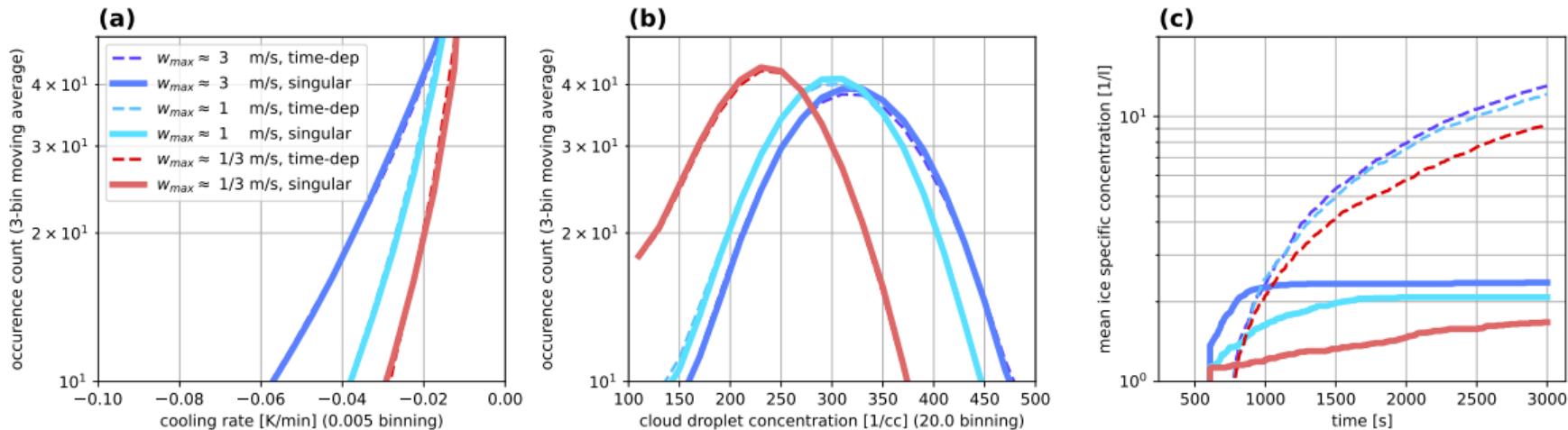
- range of cooling rates in simple flow (far from  $c \sim 1$  K/min for AIDA as in Niemand et al. 2012)

testing three flow regimes and two immersion freezing representations



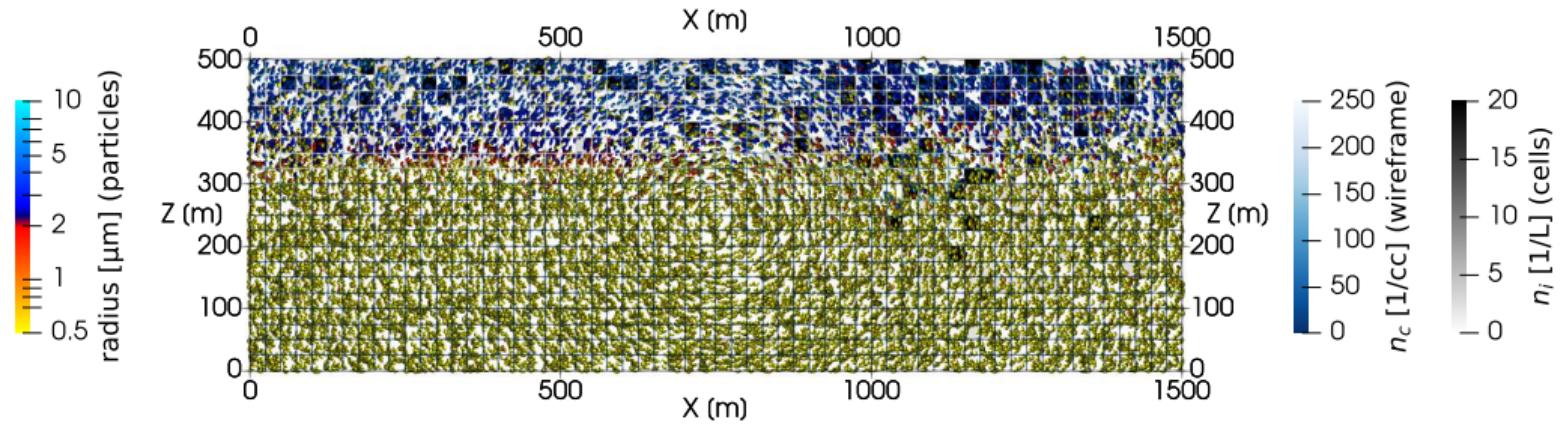
- ▶ range of cooling rates in simple flow (far from  $c \sim 1$  K/min for AIDA as in Niemand et al. 2012)
  - ▶ singular vs. time-dependent markedly different (consistent with box model for  $c \ll 1$  K/min)

testing three flow regimes and two immersion freezing representations



- ▶ range of cooling rates in simple flow (far from  $c \sim 1$  K/min for AIDA as in Niemand et al. 2012)
  - ▶ singular vs. time-dependent markedly different (consistent with box model for  $c \ll 1$  K/min)
  - ▶ CPU time trade off: time dependent ca. 3-4 times costlier

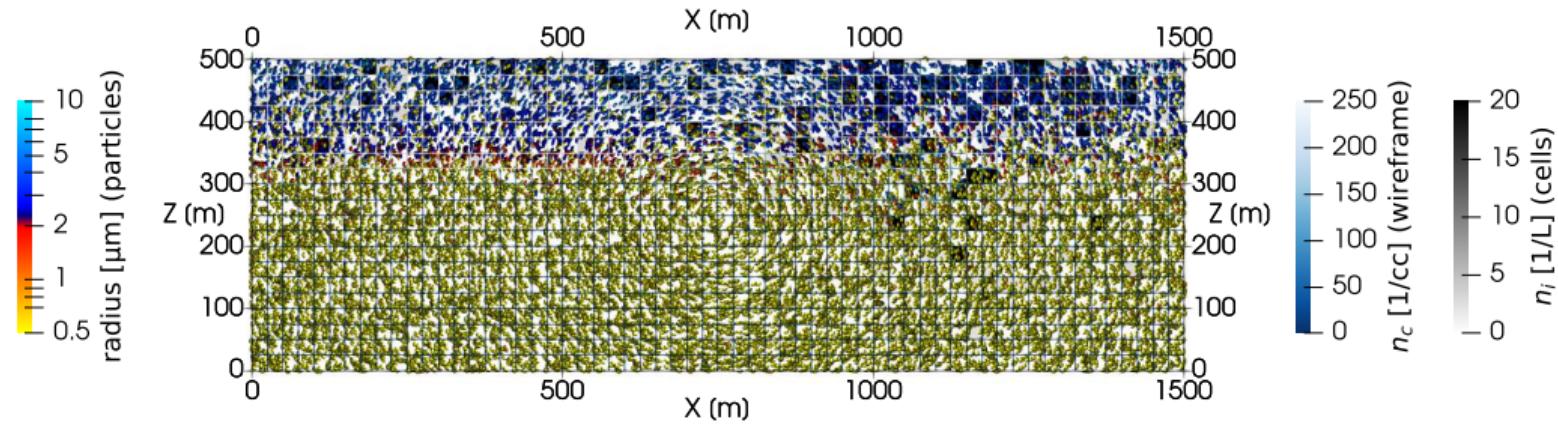
Time: 1200 s (spin-up till 600.0 s)



## **key messages:**

- emergence of comprehensive mixed-phase particle-based aerosol/cloud  $\mu$ -physics models
  - cooling rate embedded in INAS fits  $\rightsquigarrow$  limited robustness to different flow regimes

Time: 1200 s (spin-up till 600.0 s)

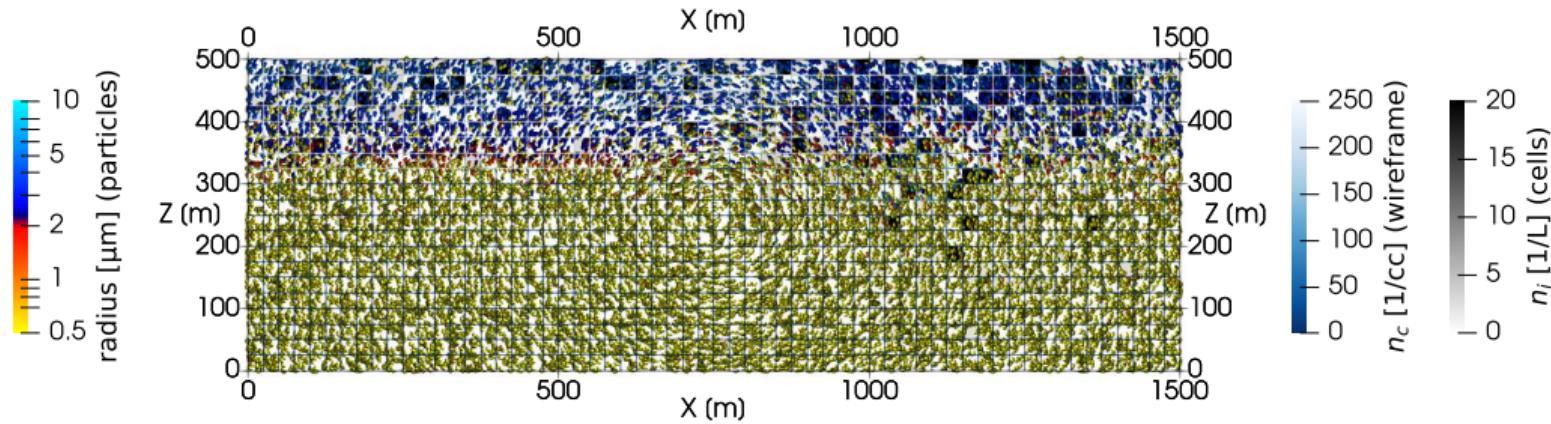


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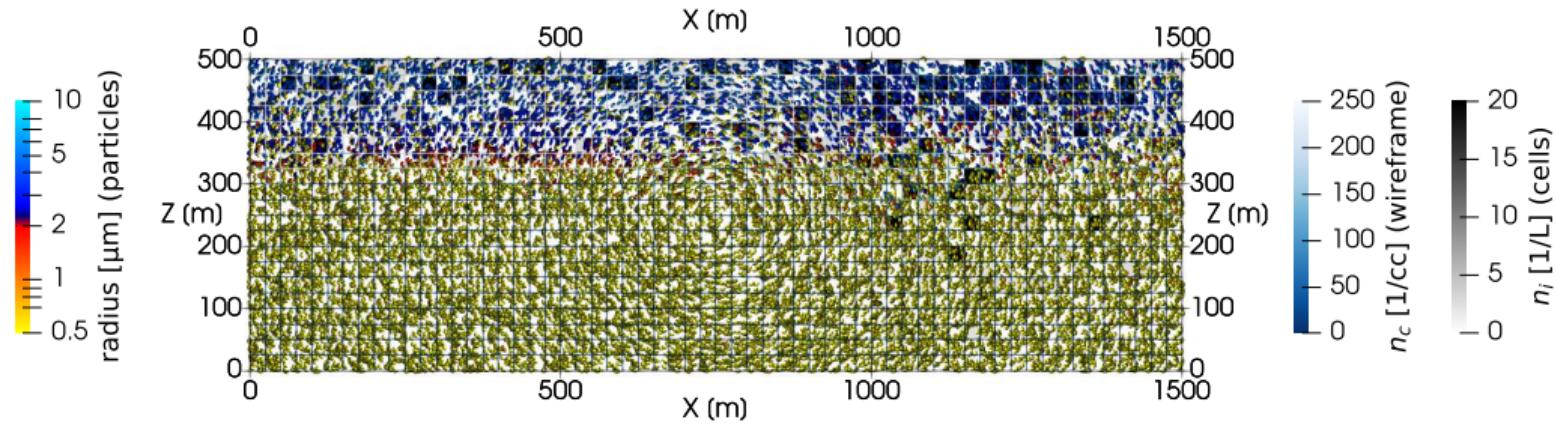
ASR  
Atmospheric  
System Research

DOE ASR grant no.  
DE-SC0021034

project hosted at:



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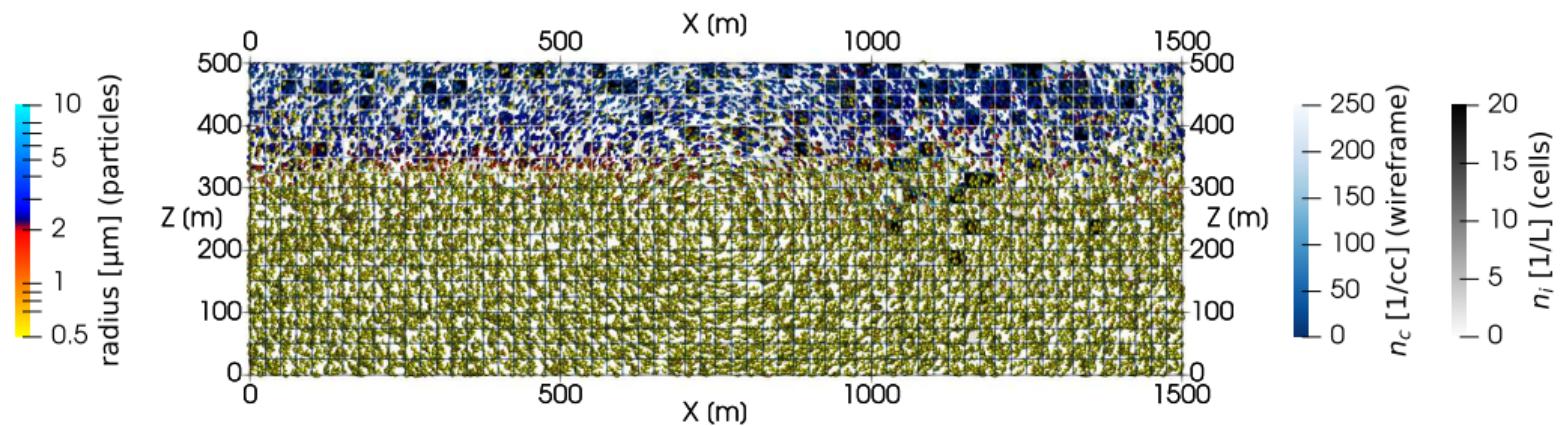


**ASR**  
Atmospheric  
System Research

DOE ASR grant no.  
DE-SC0021034

project hosted at:  
**ILLINOIS**

open python™ code:  
[o/atmos-cloud-sim-uj](https://github.com/atmos-cloud-sim-uj)



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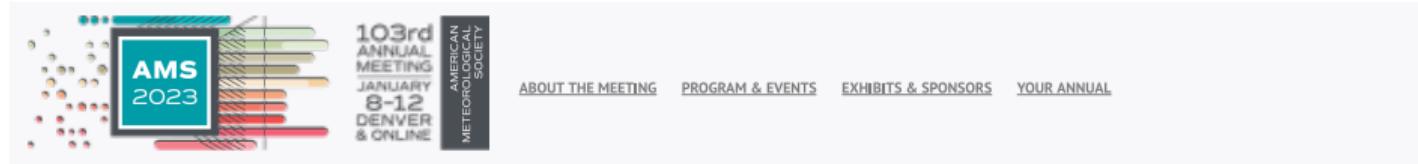
project hosted at:



open  python™ code:  
Q/atmos-cloud-sim-u

 Thank you  
for your attention!

<https://annual.ametsoc.org/index.cfm/2023/program-events/call-for-papers/>



## 15th Symposium on Aerosol–Cloud–Climate Interactions

The 15th Symposium on Aerosol–Cloud–Climate Interactions is sponsored by the American Meteorological Society and organized by the [AMS Committee on Atmospheric Chemistry](#).

### Call for Papers

Papers for the 15th Symposium on Aerosol–Cloud–Climate Interactions are solicited on the following:

- Advances in observational and modeling studies of mineral dust in the Earth system;
- Aerosol-Cloud Interactions in Deep Convective Clouds;
- Aerosol-Cloud interactions over the North Atlantic Ocean: insights from recent field campaigns;
- Aerosol-climate interactions from regional to global scale;
- Aerosol-cloud interactions in mixed-phase clouds;
- Aerosol-radiation interactions;
- Atmospheric ice-nucleating particles and ice formation processes in clouds;
- Challenges and progress in understanding, simulating and forecasting fog;
- Measurement and modeling of atmospheric cloud condensation nuclei and related chemistry;
- Mesoscale cloud organization and transition: the role of meteorology and aerosols;
- Probabilistic Particle-Based Methods in Aerosol-Cloud Microphysics Modeling.

### Abstract Information

Abstracts are due by **24 August 2022 at 11:59 PM EDT**

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