Assignment 7 By Team 1

Odianosen Akhibi, Shun-Lung Chang, Juliana Nair

This study was conducted in R, and the source code can be found here.

1. Generate a simulated data set with 20 observations in each of three classes (i.e. 60 observations total), and 50 variables.

```
# set the random number seed
set.seed(45)

normal <- rnorm(1000, mean = 100, sd = 1) %>%
    matrix(20, 50) %>%
    data.frame()

uniform <- runif(1000, min = -100, max = -50) %>%
    matrix(20, 50) %>%
    data.frame()

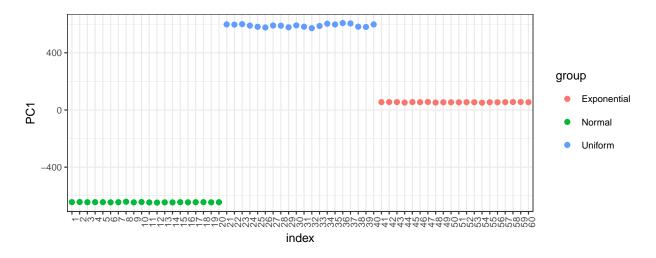
exponential <- rexp(1000, rate = 1) %>%
    matrix(20, 50) %>%
    data.frame()

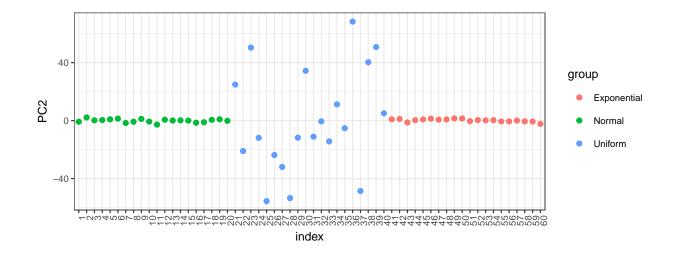
dat <- rbind(normal, uniform, exponential)

dim(dat)

[1] 60 50</pre>
```

2. Perform PCA on the 60 observations and plot the first two principal component score vectors. Use a different color to indicate the observations in each of the three classes.





3. Perform K-means clustering of the observations with K=3. How well do the clusters that you obtained in K-means clustering compare to the true class labels?

4. Perform K-means clustering with K = 2. Describe your results.

```
kc_2 <- kmeans(dat, center = 2)

table(kc_2$cluster, c(rep(1, 20), rep(2, 20), rep(3, 20))) %>% kable()

\[ \frac{1 2 3}{20 0 20} \\
 0 20 0
\]
```

5. Now perform K-means clustering with K=4, and describe your results.

```
kc_4 <- kmeans(dat, center = 4)</pre>
```

```
table(kc_4$cluster, c(rep(1, 20), rep(2, 20), rep(3, 20))) %>% kable()

1 2 3
9 0 0
5 0 0
6 0 0
0 20 20
```

6. Now perform K-means clustering with K=3 on the first two principal component score vectors, rather than on the raw data. That is, pserform K-means clustering on the 60×2 matrix of which the first column is the first principal component score vector, and the second column is the second principal component score vector. Comment on the results.

7. Using the scale() function, perform K-means clustering with K=3 on the data after scaling each variable to have standard deviation one. How do these results compare to those obtained in (3)? Explain.

```
dat_scaled <- scale(dat)
kc_3 <- kmeans(dat_scaled, center = 3)
table(kc_3$cluster, c(rep(1, 20), rep(2, 20), rep(3, 20))) %>% kable()
```

1	2	3
0	0	20
0	20	(
20	0	(

8. Use the scaled variables and run a PCA on them. Now perform K-means clustering with K=3 on the first two principal component score vectors, rather than on the raw data. How do these results compare to those obtained in (3) and (7)? Explain.

```
pca_scaled <- prcomp(dat, center = TRUE, scale. = TRUE)
kc_pc_scaled_3 <- kmeans(data.frame(pca_scaled$x[, 1], pca_scaled$x[, 2]), centers = 3)
table(kc_pc_scaled_3$cluster, c(rep(1, 20), rep(2, 20), rep(3, 20))) %>% kable()
```

1	2	٩
0	0	20
20	0	(
0	20	(