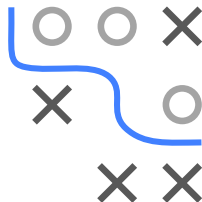


MULTI-TARGET PREDICTION: MOTIVATION

- Conventional supervised learning: Label space \mathcal{Y} is 1-D.
- Multi-target prediction (MTP): multiple targets of mixed types (binary, nominal, ordinal, real-valued).
- Learn one model per target independently? \rightsquigarrow Targets can be *statistically dependent*.
- Multi-label Emotions Dataset: 4 emotions of a music piece. Multiple emotions may be attributed to a single piece. Mutual information of the labels are:

| | Calm | Quiet | Sad | Angry |
|-------|--------------|--------------|--------------|--------------|
| Calm | 1.000 | 0.073 | 0.018 | 0.290 |
| Quiet | 0.073 | 1.000 | 0.241 | 0.164 |
| Sad | 0.018 | 0.241 | 1.000 | 0.067 |
| Angry | 0.290 | 0.164 | 0.067 | 1.000 |

- It might be better to tackle targets *simultaneously*.

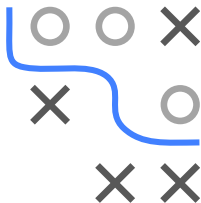


MULTI-TARGET PREDICTION: CHARACTERISTICS

Characterized by instances $\mathbf{x} \in \mathcal{X}$ and targets $m \in \{1, 2, \dots, l\}$ with following properties:







- A training set $\mathcal{D} = \{(\mathbf{x}^{(i)}, \mathbf{y}^{(i)})\}_{i=1}^n$, where $\mathbf{y}^{(i)} = (y_1^{(i)}, \dots, y_l^{(i)})$, with $y_m^{(i)} \in \mathcal{Y}_m$ is label for target m .
- n instances and l targets \rightsquigarrow Labels $y_m^{(i)}$ can be arranged in an $n \times l$ matrix \mathbf{Y} . Note \mathbf{Y} may have missing values.
- Target spaces \mathcal{Y}_m can be nominal, ordinal or real-valued.
- Goal: predict scores for any pair $(\mathbf{x}, m) \in \mathcal{X} \times \{1, 2, \dots, l\}$.

In conventional MTP setting: no available side information for targets.



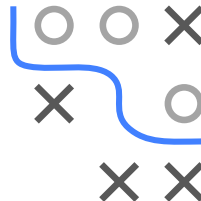
MULTIVARIATE REGRESSION

Target space $\mathcal{Y}_m = \mathbb{R} \forall m \in \{1, 2, \dots, l\}$.

| | | Mol1 | Mol2 | Mol3 | Mol4 | Mol5 | Mol6 |
|-------|---|------|------|------|------|------|------|
| 01101 |  | 1,3 | 0,2 | 1,4 | 1,7 | 3,5 | 1,3 |
| 00111 |  | 2 | 1,7 | 1,5 | 7,5 | 8,2 | 7,6 |
| 01110 |  | 0,2 | 0 | 0,3 | 0,4 | 1,2 | 2,2 |
| 10001 |  | 3,1 | 1,1 | 1,3 | 1,1 | 1,7 | 5,2 |
| 01011 |  | 4,7 | 2,1 | 2,5 | 1,5 | 2,3 | 8,5 |
| 11110 |  | ? | ? | ? | ? | ? | ? |

Waegeman et al. (2019), Multi-target prediction: A unifying view on problems and methods ([URL](#)).

Example: Predict binding strength between proteins (rows) and molecules (columns).



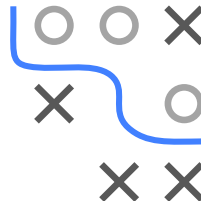
MULTI-LABEL CLASSIFICATION

Target space $\mathcal{Y}_m = \{0, 1\} \forall m \in \{1, 2, \dots, l\}$

| | | Tennis | Football | Biking | Movies | TV | Belgium |
|-------|-------|--------|----------|--------|--------|----|---------|
| 01101 | Text1 | 0 | 1 | 0 | 0 | 1 | 1 |
| 00111 | Text2 | 1 | 0 | 0 | 0 | 0 | 1 |
| 01110 | Text3 | 0 | 0 | 0 | 1 | 1 | 0 |
| 10001 | Text4 | 0 | 0 | 1 | 0 | 1 | 0 |
| 01011 | Text5 | 1 | 0 | 0 | 1 | 0 | 0 |
| 11110 | Text6 | ? | ? | ? | ? | ? | ? |

Waegeman et al. (2019), Multi-target prediction: A unifying view on problems and methods ([URL](#)).

Example: Assign documents (rows) to category tags (columns).



LABEL RANKING

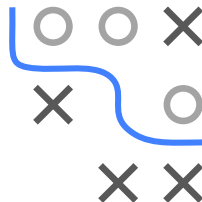
In *label ranking*, each instance is associated with a ranking of targets.

$\mathcal{Y}_m = \{1, \dots, l\} \forall m$, and labels (i.e., ranks) $y_m^{(i)} \neq y_k^{(i)} \forall m \neq k$.

| | | Tennis | Football | Biking | Skating | Running | Walking |
|-------|---------|--------|----------|--------|---------|---------|---------|
| 01101 | User 1 | 2 | 1 | 4 | 3 | 5 | 6 |
| 00111 | User 2 | 1 | 4 | 3 | 5 | 6 | 2 |
| 01110 | User 3 | 4 | 5 | 1 | 2 | 3 | 6 |
| 10001 | User 4 | 4 | 3 | 2 | 6 | 1 | 5 |
| 01011 | User t5 | 1 | 3 | 5 | 2 | 6 | 4 |
| 11110 | User 6 | ? | ? | ? | ? | ? | ? |

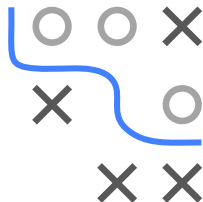
Waegeman et al. (2019), Multi-target prediction: A unifying view on problems and methods ([URL](#)).

Example: Predict for users (rows) their preferences over specific activities (columns).



REMARKS






- It is also possible when the m -th task is multiclass classification. That is, $f(\mathbf{x})_m \in \mathbb{R}^{g_m}$ is the probability predictions for g_m classes.
~> The techniques for multi-target learning are also applicable under this setting, notation becomes cumbersome.
- Target space can be inhomogeneous, e.g. $\mathcal{Y}_m = \{0, 1\}$ and $\mathcal{Y}_k = \mathbb{R}$.
~> A mixture of multi-label classification and multivariate regression.



SIDE INFORMATION ON TARGETS

- Sometimes, additional side information about targets is available.

- Extra representation for target molecules in drug design (*structured representation*).

| | | Mol1 | Mol2 | Mol3 | Mol4 | Mol5 | Mol6 |
|-------|---|------|------|------|------|------|------|
| 01101 |  | 1,3 | 0,2 | 1,4 | 1,7 | 3,5 | 1,3 |
| 00111 |  | 2 | 1,7 | 1,5 | 7,5 | 8,2 | 7,6 |
| 01110 |  | 0,2 | 0 | 0,3 | 0,4 | 1,2 | 2,2 |
| 10001 |  | 3,1 | 1,1 | 1,3 | 1,1 | 1,7 | 5,2 |
| 01011 |  | 4,7 | 2,1 | 2,5 | 1,5 | 2,3 | 8,5 |

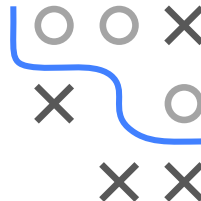
| | | | | | | | |
|-------|---|---|---|---|---|---|---|
| 11110 |  | ? | ? | ? | ? | ? | ? |
|-------|---|---|---|---|---|---|---|



| | | | | | | | |
|-------|-------|---|---|---|---|---|---|
| 01101 | Text1 | 0 | 0 | 0 | 0 | 0 | 1 |
| 00111 | Text2 | 0 | 0 | 1 | 0 | 1 | 1 |
| 01110 | Text3 | 0 | 0 | 0 | 1 | 1 | 0 |
| 10001 | Text4 | 0 | 0 | 1 | 0 | 1 | 0 |
| 01011 | Text5 | 1 | 0 | 0 | 1 | 0 | 0 |

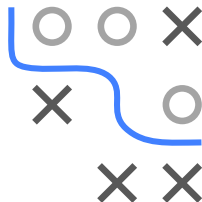
| | | | | | | | |
|-------|-------|---|---|---|---|---|---|
| 11110 | Text6 | ? | ? | ? | ? | ? | ? |
|-------|-------|---|---|---|---|---|---|

- Taxonomy on document categories (*hierarchy*).



INDUCTIVE VS. TRANSDUCTIVE LEARNING

- In previous problems,
 - 1 predictions need to be generated for novel instances,
 - 2 targets are known beforehand and observed during training.
- These problems are *inductive* w.r.t. instances and *transductive* w.r.t. targets.



- Side information is important for generalizing to novel targets.

- a novel target molecule in the drug design,
- a novel tag in the document annotation,

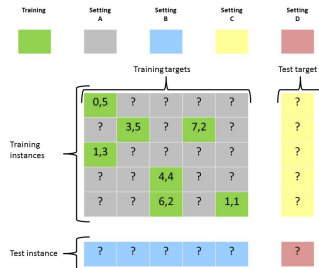
$g(\cdot, \cdot)$: target similarity

| | Mol1 | Mol2 | Mol3 | Mol4 | Mol5 | Mol6 | Mol7 |
|-------|------|------|------|------|------|------|------|
| 01101 | 1,3 | 0,2 | 1,4 | 1,7 | 3,5 | 1,3 | ? |
| 00111 | 2 | 1,7 | 1,5 | 7,5 | 8,2 | 7,6 | ? |
| 01110 | 0,2 | 0 | 0,3 | 0,4 | 1,2 | 2,2 | ? |
| 10001 | 3,1 | 1,1 | 1,3 | 1,1 | 1,7 | 5,2 | ? |
| 01011 | 4,7 | 2,1 | 2,5 | 1,5 | 2,3 | 8,5 | ? |
| 11110 | ? | ? | ? | ? | ? | ? | ? |

Waegeman et al. (2019), Multi-target prediction: A unifying view on problems and methods ([URL](#)).

SUBDIVISION OF DIFFERENT LEARNING SETTINGS

- Setting A — transductive w.r.t. targets and instances. Goal: predict missing values of score matrix (*matrix completion*).
- Setting B — transductive w.r.t. targets and inductive w.r.t. instances (*classical supervised learning*).
- Setting C — inductive w.r.t. targets and transductive w.r.t. instances.
~> Some targets are unobserved during training but may appear at prediction time.
- Setting D — inductive w.r.t. both targets and instances (*zero-shot learning*).



Waegeman et al. (2019), Multi-target prediction: A unifying view on problems and methods ([URL](#)).

