INDEPENDENT MODELS

The most naive way to make multi-target predictions: learning a model for each target independently.

- In multi-label classification this approach is also known as binary relevance learning.

 Mean regularization
- Advantage: easy to realize, as for single-target prediction we have a wealth of methods available.
 Weight sharing in DL



INDEPENDENT MODELS

- Assume arlinear basis function model for the meth-target rning a model for each target independently $f_k(\mathbf{x}) = \theta_k^{\text{tr}} \phi(\mathbf{x})$,
 - θ_k is target-specific parameter and ϕ some feature mapping.
- Use this with with large nr of targets.
- We optimize jointly:
 - $\min_{\Theta} \|Y \Phi\Theta\|_F^2 + \sum_{h=1}^{n} \lambda_m \|\theta_m\|^2,$
- In multi-label classification this approximate is also known as binary $\|\vec{B}\|_F^2 = \sqrt{\sum_{i=1}^m \sum_{m=1}^l B_{i,m}^2} \text{ is Frobenius norm for } B \in \mathbb{R}^{n \times l} \text{ and }$
- Advantage: easy to realize, as for single-target prediction we have a wealth of method (XVallable).

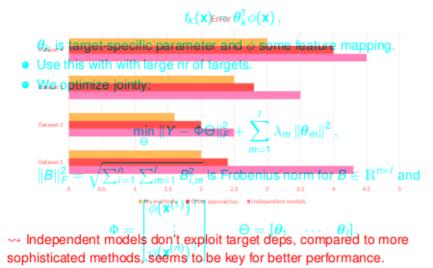
$$\Phi = \begin{bmatrix} \vdots \\ \phi(\mathbf{x}^{(n)})^{\top} \end{bmatrix} \qquad \Theta = [\boldsymbol{\theta}_1 \quad \cdots \quad \boldsymbol{\theta}_l].$$

Frobenius norm = sum of SSE-s of all targets



INDEPENDENT MODELS

The experimental results section of a typical MTP paperarget:

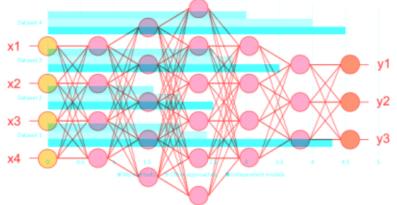




Frobenius norm = sum of SSE-s of all targets

ENFORCING SIMILARITY IN DEEP LEARNING

The experimental results section of a typical MTP paper:
Commonly-used architecture: weight sharing in the final layer with *m*nodes, i.e., weight sharing among the targets



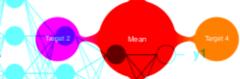




MEAN-REGULARIZED MULTI-TASK LEARNING

Commonly-used architecture: weight sharing in the final layer with m nodes, i.e., weight sharing among the targets

- Models for similar targets
 x should behave similarly
- So params should be similar







$$\min_{\Theta} \|Y - \Phi\Theta\|_F^2 + \lambda \sum_{m=1}^{I} \|\theta_m - \frac{1}{I} \sum_{m'=1}^{I} \theta_{m'}\|^2$$



➤ Evgeniou and Pontil, 2004



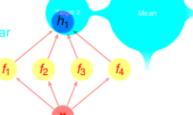
STACKING ULARIZED MULTI-TASK LEARNING

- Originally, general ensemble learning technique.
- Level 1: apply series of ML methods on the same dataset
- Level 2: apply ML method to a new dataset consisting of the

predictions obtained at level 1 should behave similarly

So params should be similar

Level 1







$$\min_{\Theta} \|Y - \Phi\Theta\|_F^2 + \lambda \sum_{m=1}^{I} \|\theta_m - \frac{1}{I} \sum_{m'=1}^{I} \theta_{m'}\|^2$$





STACKING APPLIED TO MTP

- Levenathearmann
- g_2 g_3 g
- independently series of ML methods on the same value.
- Level 2: learly model forceach a new dataset consisting of target independently assing 1.

predictions of level 1 ~







$$f(\mathbf{x}) = g(f_1(\mathbf{x}), \dots, f_l(\mathbf{x}))$$



$$f(\mathbf{x}) = g(f_1(\mathbf{x})_{\text{Level}} f_1(\mathbf{x}), \mathbf{x})$$











- Advantages: easy to implement and general
- Has been shown to avoid overfitting in multivariate regression
- If level 2 learner uses regularization → models are forced to learn similar parameters for different targets.

Cheng and Hüllermeier, 2009

STACKING VS BINARY RELEVANCE: EXAMPLE

 Compare E1 Score of random forest with stacking vs random forest with binary relevance on different multilabel datasets:



- Fil-Score is decomposed over targets.
- NB) Stacking slightly outperforms binary relevance on average.
- For more details, please refer to Probst of al., 2017 $f(\mathbf{x}) = g(f_1(\mathbf{x}), \dots, f_l(\mathbf{x}), \mathbf{x})$



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. Chieng and Hüllermeier, 2009



STACKING VS BINARY RELEVANCE: EXAMPLE

 Compare F1-Score of random forest with stacking vs random forest with binary relevance on different multilabel datasets:

	birds	emotions	enron	genbase	image	langLog	reuters	scene	slashdot	yeast
BR(rf) F1-Score										
STA(rf) F1-Score	0.646	0.634	0.583	0.986	0.446	0.317	0.685	0.633	0.453	0.624

- F1-Score is decomposed over targets.
- NB: Stacking slightly outperforms binary relevance on average.
- For more details, please refer to Probst et al., 2017).

