Lab 10

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Imports

In [1]:

```
import string
from collections import Counter
from math import ceil
from typing import List, Optional, Tuple, Dict

import matplotlib.pyplot as plt
import torch
from matplotlib_inline.backend_inline import set_matplotlib_formats
from torch import nn, Tensor
from torch.nn.utils.rnn import pad_sequence
from torch.optim import Adam, Optimizer
from torch.utils.data import DataLoader, Dataset
from torchtext.datasets import IMDB
from torchvision.datasets import make_grid

set_matplotlib_formats('png', 'pdf')
```

Exercise 1

In this exercise, we are going to revise the sentiment classifier for IMDB reviews we developed in a previous lab. Earlier, we encoded each review as a single "bag-of-words" vector which had one element for each word in our dictionary set to one if that word was found in the review, zero otherwise. This allowed us to use a simple fully-connected neural network but, on the flip side, we lost all information contained in the ordering and of the words and possible multiple repetitions. Recurrent neural networks, however, are able to process reviews directly. Let's see how!

The first step is to load the data and preprocess it like it in exercise 6, so if you still remember what we did there, feel free to skip this part. For brevity, we only use the 10000 most common words and truncate reviews to 250 words, but if you can use a GPU then feel free to use the full length reviews and all words!

```
In [2]:
```

```
train_iterator, test_iterator = IMDB();
```

In [3]:

```
# Feed iterator to list
train_x = []
train_y = []
test_x = []
test_y = []

for label, line in train_iterator:
    train_x.append(line)
    train_y.append(label)

for label, line in test_iterator:
    test_x.append(line)
    test_y.append(label)
```

In [4]:

```
# Tokenize sentences.

def tokenize(data_list: List[str]) -> List[List[str]]:
    """
    Tokenize a list of strings.
    :param data_list: A list of strings.
    :return: A list where each entry is a list including the tokenized elements.
    """
    token_list: List[List[str]] = []
    for data_string in data_list:
        # Remove punctuation.
        data_string = data_string.translate(str.maketrans('', '', string.punctuatio
        # Split by space.
        token_list.append(data_string.split())
    return token_list

train_x = tokenize(train_x)
test_x = tokenize(test_x)
```

```
# Count-vectorize sentences.
class CountVectorizer:
   def init (self):
        self.vec to str map: Dict[int, str] = {}
        self.str to vec map: Dict[str, int] = {}
    def fit(self, token list: List[str]) -> None:
        # The `Counter` object from the `collections` library gives us efficient co
        # in large lists out of box.
        cnt = Counter(token list)
        sorted cnt = sorted(cnt.items(), key=lambda item: item[1], reverse=True)
        sorted words = [key for key, val in sorted cnt]
        # Python does not know a bidirectional mapping by default.
        # We trick a bit by simply creating two dicts, but note that this is ineffi
        self.str to vec map = {sorted words[i]: i + 1 for i in range(len(sorted wor
        self.vec to str map = {i + 1: sorted words[i] for i in range(len(sorted wor
   def transform to vec(self, token list: List[str]) -> List[int]:
        return [self.str to vec map.get(word) for word in token list]
    def transform to str(self, token list: List[int]) -> List[str]:
        return [self.vec to str map.get(rank) for rank in token list]
train words = [word for word list in train x for word in word list]
test words = [word for word list in test x for word in word list]
count vectorizer = CountVectorizer()
counter = count vectorizer.fit(train words)
train x = [count vectorizer.transform to vec(word list) for word list in train x]
test x = [count vectorizer.transform to vec(word list) for word list in test x]
```

In [6]:

```
# Discard words that are not in the top 10000
# Truncate sequences to a length of 250
# Remove Nones
def filter word ranks(
        word list: List[Optional[int]],
        max rank: int = 10000,
        max seq len: int = 250
) -> List[int]:
    output = []
    seq len = 0
    for word rank in word list:
        if seq len >= max seq len:
            return output
        elif word rank is None:
            continue
        elif word rank <= max rank:</pre>
            output.append(word rank)
            seq_len += 1
    return output
train x = [filter word ranks(word list) for word list in train x]
test x = [filter word ranks(word list) for word list in test x]
```

In [7]:

```
# Encode labels to binary targets
train_y = [1 if label == 'pos' else 0 for label in train_y]
test_y = [1 if label == 'pos' else 0 for label in test_y]
```

Now, each review is a vector of numbers, each corresponding to a different word:

In [8]:

```
print(train_x[0])
```

```
[8, 1595, 8, 35, 70, 434, 1191, 80, 4, 32, 1, 7739, 9, 3423, 10, 55, 1
0, 13, 89, 654, 7, 7978, 8, 91, 559, 9, 30, 89, 10, 13, 31, 835, 60, 1
0, 129, 787, 5, 3578, 11, 783, 2044, 110, 2, 341, 4, 94, 1165, 3150,
8, 59, 61, 5, 66, 11, 17, 12, 14, 114, 6, 6504, 187, 2, 199, 4239, 50
0, 1612, 777, 5011, 34, 481, 5, 847, 330, 72, 67, 41, 128, 121, 826, 7
2, 481, 5, 1139, 39, 5, 255, 47, 439, 4, 701, 21, 51, 1, 895, 196, 41,
809, 1008, 1328, 141, 15, 1, 2757, 969, 3, 1672, 1328, 7, 1, 2535, 253
2, 121, 194, 2193, 7740, 3, 1999, 4, 41, 64, 5012, 21, 2549, 72, 43, 4
23, 16, 39, 500, 1774, 8513, 3, 1052, 12, 216, 1116, 71, 41, 8, 6, 9,
1831, 154, 614, 11, 13, 1165, 8972, 2069, 1, 423, 3, 1048, 139, 22, 16
4, 3, 243, 194, 65, 107, 37, 24, 333, 36, 47, 6972, 88, 5058, 441, 70,
357, 162, 10, 1635, 7, 677, 423, 3, 1048, 22, 2, 723, 7, 4239, 496, 38
0, 5218, 5059, 64, 1564, 5, 48, 175, 522, 305, 2092, 61, 423, 139, 7,
23, 3817, 12, 8, 84, 1, 902, 17, 1, 189, 9, 100, 423, 613, 7, 1, 19,
6, 613, 17, 1618, 5555, 250, 73, 44, 5, 1579, 82, 3, 93, 291, 5, 27, 6
13, 7, 8972, 2245, 7, 949, 8, 6, 2, 48, 19, 17, 278, 1786, 5, 2093]
```

Even though RNNs can process sequences of arbitrary length, all sequences in the same batch must be of the same length, while sequences in different batches can have different length. In this case, however, we pad all

sequences to the same length as this makes for much simpler code. PyTorch provides a function to do so for you called pad_sequence (read the documentation!). Hint: It might be good to set the argument batch_first to `True. Beforehand, we need to convert the data to tensors. Let's also define our device and push the newly created padded tensor to it.

In [9]:

```
device = (
# TODO: Define the device you want to use.
)

train_x = [torch.tensor(word_list, dtype=torch.int) for word_list in train_x]
test_x = [torch.tensor(word_list, dtype=torch.int) for word_list in test_x]

train_x = (
# TODO: Pad the sequences and push the result to your device.
)

test_x = (
# TODO: Pad the sequences and push the result to your device.
)

train_y = torch.tensor(train_y, dtype=torch.float, device=device)
test_y = torch.tensor(test_y, dtype=torch.float, device=device)
```

In [10]:

```
print(train_x.shape)
```

The data is now an array of shape (num_samples x seq_len). A PyTorch RNN with batch_first=True option expects the input to be of shape (num_samples x seq_len x features). Although we have a univariate timeseries, we still need to add this additional last dimension.

In [11]:

```
train_x = (
# TODO: Add the feature dimension.
)

test_x = (
# TODO: Add the feature dimension.
)
```

Finally let's create our IMDBDataset object:

In [12]:

```
class IMDBDataset(Dataset):
    def __init__(self, data: Tensor, labels: Tensor):
        self.data = data
        self.labels = labels

@property
    def shape(self) -> Tuple:
        return self.data.shape

def __len__(self) -> int:
        return len(self.labels)

def __getitem__(self, idx: int) -> Tuple[Tensor, Tensor]:
# TODO: Return the correct review and label for the index.
```

Next, we define our sequential model. The first layer is an *Embedding* layer that associates a vector of numbers to each word in the vocabulary. These numbers are updated during training just like all other weights in the network. Crucially, thanks to this embedding layer we do not have to one-hot-encode the reviews but we can use the word indices directly, making the process much more efficient.

Note the parameter <code>padding_idx</code>: this indicates that zeros in the input sequences are used for padding (verify that this is the case!). Internally, this is used by the RNN to ignore padding tokens, preventing them from contributing to the gradients (read more in the user guide, <code>link</code> link (https://pytorch.org/docs/stable/generated/torch.nn.Embedding.html/)!)

We also make use of a <code>nn.Module</code> container, where we will define our model. This gives us more flexibility in the flow of the network. Here we add the model blocks as class attributes and define a forward pass, which is enough for the autograd engine.

The shapes and dimensions of tensors can now be a bit tricky. It helps if you print the resulting shape of each transformation to console and investigate what happened!

In [13]:

```
class LSTMModel(nn.Module):
   def __init__(self):
       # A class that inherits from nn.Module needs to call the constructor from t
       # parent class
       super().__init__()
       self.embedding = nn.Embedding(
            num embeddings=10001,
            embedding dim=64,
            padding idx=0
       self.lstm = nn.LSTM(
            input size=64,
            hidden size=32,
            num layers=2,
            batch first=True
       )
       self.fc = nn.Linear(in features=32, out features=1)
       self.sigmoid = nn.Sigmoid()
   def forward(self, x: Tensor) -> Tensor:
       # The output needs to be reshaped or otherwise we have a dimension too much
       x = self.embedding(x).squeeze(2)
       # The LSTM module gives a variety of outputs. Please refer to the official
       # docs for a detailed description. Here `hidden` contains the final hidden
       # from the last layer for every sample in the batch.
       _, (hidden, _) = self.lstm(x)
       # We need to extract the last hidden state
       y score = self.fc(hidden[-1])
       y hat = self.sigmoid(y score).squeeze(-1)
       return y hat
```

In the next step, we once again need our beloved training loop.

```
def train(
      model: nn.Module,
      loss: nn.Module,
      optimizer: Optimizer,
      train_dataset: Dataset,
      test dataset: Dataset,
      epochs: int,
      batch size: int
) -> Dict:
   metrics: Dict = {
      'train loss': [],
      'train acc': [],
      'test loss': [],
      'test acc': [],
   }
   num train batches = ceil(len(train dataset) / batch size)
   num test batches = ceil(len(test dataset) / batch size)
   train loader = DataLoader(train dataset, batch size, shuffle=True)
   test loader = DataLoader(test dataset, batch size)
   for ep in range(1, epochs + 1):
      total loss = 0
      num correct = 0
      # TRAINING LOOP
      for batch idx, (x, y) in enumerate(train loader):
# TODO: Add forward pass + batch loss, backpropagation and apply gradients
         if batch idx % 10 == 0:
             print('TRAINING BATCH:\t({:5} / {:5})\tLOSS:\t{:.3f}'
                  .format(batch idx, num train batches, float(batch loss)),
                  end='\r'
         total loss += float(batch loss)
         num correct += int(torch.sum(torch.where(y hat > 0.5, 1, 0) == y))
      ep_train_loss = total_loss / len(train_dataset)
      ep_train_acc = num_correct / len(train_dataset)
      total loss = 0
      num correct = 0
      # TEST LOOP
      for batch idx, (x, y) in enumerate(test loader):
         with torch.no_grad():
# TODO: Do a forward pass and get the batch loss
         if batch idx % 50 == 0:
```

We declare model, optimizer, datasets, loss, epochs, batch size and then start training!

In [15]:

```
epochs = 10
batch_size = 32

model = (
# Initialize the model and push it to your device.
)

optimizer = (
# TODO: Define an optimizer.
)

loss = (
# TODO: Define the matching loss function.
)

train_dataset = (
# TODO: Define the train dataset.
)

test_dataset = (
# TODO: Define the train dataset.
)

metrics = train(model, loss, optimizer, train_dataset, test_dataset, epochs, batch_
```

```
def get_training_progress_plot(
        train losses: List[float],
        train accs: List[float],
        val losses: List[float],
        val accs: List[float],
) -> None:
    fig, (ax1, ax2) = plt.subplots(1, 2, figsize=(7, 2))
    ax1.set title('Loss')
    ax1.plot(train losses, label='Train Loss')
    ax1.plot(val losses, label='Test Loss')
    ax1.legend()
    ax2.set title('Accuracy')
    ax2.plot(train accs, label='Train Accuracy')
    ax2.plot(val_accs, label='Test Accuracy')
    ax2.set ylim(0, 1)
    ax2.legend()
get training progress plot(
    metrics['train loss'],
    metrics['train_acc'],
    metrics['test loss'],
    metrics['test acc'],
)
```

The model seems to be learning more easily than the simple baseline we created time ago, which had an accuracy of 85-88% on the test data. Let it train for longer and tune the architecture above to reach as high accuracy as possible! (note that evaluating on the same data that you used for early stopping is cheating).

Exercise 2

In this exercise, we are going to build a model that is able to sum two numbers, each given as a sequence of images of handwritten digits. The network will first use a convolutional encoder to transform each digit into a feature vector. These feature vectors will then be processed by a LSTM that will produce as output each digit of the sum.

Dataset

We are now going to create a synthetic dataset using images from MNIST.

First, we define some auxiliary functions. We need a function that converts an integer to a padded tensor.

In [17]:

```
def convert_int_to_vector(num: int, length: int) -> Tensor:
    Take an integer and convert it to a vector.

Example: 123 with a length of 3 returns a tensor with [1, 2, 3].
5 with a length of 3 returns [0, 0, 5]
# TODO: Fill the function.
```

Then, we need a function that generates our training labels. The result of the function should be a dictionary that contains 3 tensors (first numbers, second numbers, sum of first + second) of shape (num_samples, max_length). We need the summands for drawing matching images later, while the latter is our actual label.

In [18]:

```
def generate labels(num samples: int, max length: int) -> Dict:
    Generate random numbers, whose sum does not exceed maximum length.
   We will pad numbers that are less than max length with zeros.
   num 1s = []
   num 2s = []
    sums = []
   for in range(num samples):
        # Ensure the sum always has at most max len digits
        num 1 = torch.randint(10**max_length // 2 - 1, (1,))
        num_2 = torch.randint(10**max_length // 2 - 1, (1,))
        num ls.append(convert int to vector(int(num 1), max length))
        num_2s.append(convert_int_to_vector(int(num_2), max_length))
# TODO: Add the two numbers and save the result as padded tensor
    return {
        'num_1': torch.stack(num_1s),
        'num 2': torch.stack(num 2s),
        'sum': torch.stack(sums)
    }
```

For our training, we need our Dataset object. Here, we will also draw the images to create our input tensors. One image is of shape $(1 \times 28 \times 28)$. Thus, a constructed input tensor is of shape $(max_length \times 1 \times 28 \times 28)$

```
class NumberMNIST(Dataset):
   def init (
            self,
            max length: int = 3,
            train: bool = True
    ) -> None:
        mnist base = MNIST('.data', train=train, download=True)
        mnist base.data = mnist base.data.float() / 255
        self.max length = max length
        # We choose 20k samples for training and 5k for testing.
        self.num samples = 20000 if train else 5000
        self.digit idxs = NumberMNIST. generate digit groups(mnist base.targets)
        self.labels = generate labels(self.num samples, self.max length)
        self.num 1s = torch.zeros(self.num samples, self.max length, 1, 28, 28)
        self.num 2s = torch.zeros(self.num samples, self.max length, 1, 28, 28)
        for i in range(self.num samples):
            imgs = []
            for num 1 digit in self.labels['num 1'][i]:
                # Get corresponding index group
                digit idxs = self.digit idxs[int(num 1 digit)]
                # Sample a random index from the digit class
                rand idx = digit idxs[torch.randint(len(digit idxs), (1, ))]
                # Obtain image for the sampled index
                imgs.append(mnist base.data[rand idx])
            # Add images to main tensor.
            self.num 1s[i] = torch.stack(imgs)
# TODO: Repeat the procedure for the second number
   @staticmethod
    def _generate_digit_groups(targets: Tensor) -> Dict:
        """Separates the dataset in groups based on the label. Returns a Dict with
        res = \{\}
        for i in range(10):
            idxs = (targets == i).nonzero().squeeze(-1)
            res.update({i: idxs})
        return res
   @property
    def shape(self) -> Tuple:
        return self.data.shape
    def len (self) -> int:
        return len(self.num 1s)
   def __getitem__(self, idx: int) -> Dict:
# TODO: Given an index return a dictionary with images
# for the first and second digit (Keys: 'num_1' and 'num_2') & sum as label (Key:
```

Let's initialize our datasets and see if everything works as expected.

In [20]:

```
train_dataset = NumberMNIST(train=True, max_length=3)
test_dataset = NumberMNIST(train=False, max_length=3)
```

In [21]:

```
def plot_digits(num_1: Tensor, num_2: Tensor) -> None:
    grid_img = make_grid(torch.cat([num_1, num_2]), nrow=3)
    plt.imshow(grid_img.permute(1, 2, 0))
    plt.show()

idx = int(torch.randint(len(test_dataset), (1,)))
sample = test_dataset[idx]

print('Sum:', [int(i) for i in sample['label']])
plot_digits(sample['num_1'], sample['num_2'])
```

The model

Let's now see how to create the model.

This network will have two inputs, one for each number. The numbers have three digits, each of which is an image of size $1 \times 28 \times 28$.

```
class AdditionModel(nn.Module):
   def __init__(self):
        super(). init ()
        self.latent_dim = 128
        # The network will use the same convolutional encoder for all digits in bot
        # Let us first define this encoder as its own submodule, a normal CNN:
        self.digit encoder = nn.Sequential(
# TODO: Add some convolutional and pooling layers as you see fit.
# Note: We will encode each digit on its own. Expect an input one single grayscale
            nn.AdaptiveAvgPool2d((1, 1))
        # Our second model in this szenario will be a bidrectional LSTM.
        # The input for this model are the concatenated latent vectors that we obta
        # the digit encoder.
        # For flexibility, we do not use a sequential but have the final layers as
        # Let's also apply a bit of dropout to prevent overfitting too much.
        self.dropout = (
# TODO: Add a dropout layer.
        self.lstm = (
# TODO: Add a bidirectional LSTM.
        # Finally, we add a fully connected layer as output.
        # Note that the input size of the linear layer should be twice the hidden s
        # of the LSTM (bidirectional).
        self.fc = (
# TODO: Add an output linear layer.
   def forward(self, num 1: Tensor, num 2: Tensor) -> Tensor:
        # Note: num_1 and num_2 are of shape (batch_size x max_length x 1 x 28 x 28
        batch_size = num_1.shape[0]
        max length = num 1.shape[1]
        enc_1 = torch.zeros(batch_size, max_length, self.latent_dim, device=num_1.d
        enc_2 = torch.zeros(batch_size, max_length, self.latent_dim, device=num_1.d
# TODO: Encode each digit of the batched tensors with the encoder.
# TODO: Fill enc_1 and enc_2 with the results
        # After we apply the CNN to both numbers, we need to "merge" the two sequen
        # There are several options here, here we choose to concatenate the two ten
        # to produce a single tensor of shape (batch size, max len, latent dim * 2)
        enc total = (
# TODO: Concat enc_1 and enc_2 as described above
        # Now, we pass the total encoded tensor through the dropout, lstm and outpu
        enc total = self.dropout(enc total)
        # We obtain all hidden states from each timestep resulting in a tensor of s
        out, = self.lstm(enc total)
        # Due to broadcasting, we can feed this tensor directly to the fully connec
```

```
out = self.fc(out)
# Our loss function does accept a tensor of shape (batch_size, num_classes,
# So we reshape before returning the network output.
return out.permute(0, 2, 1)
```

We can mainly reuse the training loop from the exercise before, but we need to change the computation of the accuracy and dataloading. Let's initialize our modules and start training!

```
In [23]:
```

```
device = (
# TODO: Define the device you want to use.
)
def train(
      model: AdditionModel,
      loss: nn.Module,
      optimizer: Optimizer,
      train dataset: Dataset,
      test dataset: Dataset,
      epochs: int,
      batch size: int
) -> Dict:
   metrics: Dict = {
       'train_loss': [],
       'train acc': [],
       'test loss': [],
       'test acc': [],
   }
   num train batches = ceil(len(train dataset) / batch size)
   num test batches = ceil(len(test dataset) / batch size)
   train loader = DataLoader(train dataset, batch size, shuffle=True)
   test_loader = DataLoader(test_dataset, batch_size)
   for ep in range(1, epochs + 1):
      total loss = 0
      num correct = 0
      # TRAINING LOOP
      for batch idx, sample in enumerate(train loader):
          num_1 = sample['num_1'].to(device)
          num_2 = sample['num_2'].to(device)
          y = sample['label'].to(device)
# TODO: Add forward pass + batch loss, backpropagation and apply gradients
          if batch idx % 10 == 0:
             print('TRAINING BATCH:\t({:5} / {:5})\tLOSS:\t{:.3f}'
                   .format(batch idx, num train batches, float(batch loss)),
                  end='\r')
          total loss += float(batch loss)
          num_correct += int(torch.sum(torch.all(torch.eq(torch.argmax(y hat, dim
      ep train loss = total loss / len(train dataset)
      ep_train_acc = num_correct / len(train_dataset)
      total loss = 0
      num_correct = 0
```

```
# TEST LOOP
       for batch idx, sample in enumerate(test loader):
           num_1 = sample['num_1'].to(device)
           num 2 = sample['num 2'].to(device)
           y = sample['label'].to(device)
           with torch.no grad():
# TODO: Do a forward pass and get the batch loss
           if batch idx % 50 == 0:
               print('TEST BATCH:\t({:5} / {:5})\tLOSS:\t{:.3f}'
                    .format(batch idx, num test batches, float(batch loss)), end=
           total loss += float(batch loss)
           num correct += int(torch.sum(torch.all(torch.eq(torch.argmax(y hat, dim
       ep test loss = total loss / len(test dataset)
       ep test acc = num correct / len(test dataset)
       metrics['train loss'].append(ep train loss)
       metrics['train acc'].append(ep train acc)
       metrics['test loss'].append(ep test loss)
       metrics['test_acc'].append(ep_test_acc)
       print('EPOCH:\t{:5}\tTRAIN LOSS:\t{:.3f}\tTRAIN ACCURACY:\t{:.3f}\tTEST LOS
             '{:.3f}\tTEST ACCURACY:\t{:.3f}'
             .format(ep, ep train loss, ep train acc, ep test loss, ep test acc))
   return metrics
```

Let's initialize our modules and start training!

In [24]:

```
epochs = 20
batch_size = 32

model = (
# Initialize the model and push it to your device.
)

optimizer = (
# TODO: Define an optimizer.
)

loss = (
# TODO: Define the matching loss function.
)

metrics = train(model, loss, optimizer, train_dataset, test_dataset, epochs, batch_
```

In [25]:

```
get_training_progress_plot(
    metrics['train_loss'],
    metrics['train_acc'],
    metrics['test_loss'],
    metrics['test_acc'],
)
```

It is amazing what we achieved with such a small (for the standard of deep learning) model and dataset!