



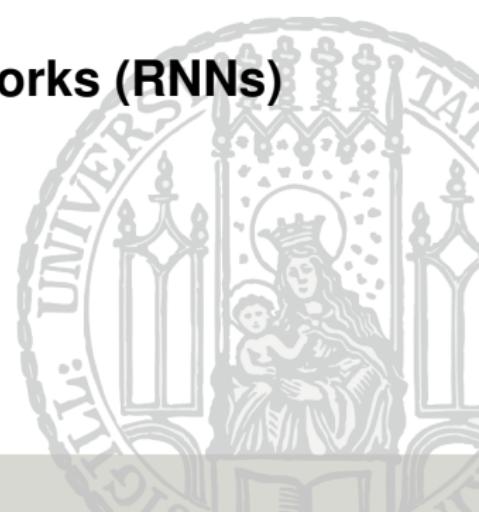
# Deep Learning

## Chapter 7: Recurrent Neural Networks (RNNs)

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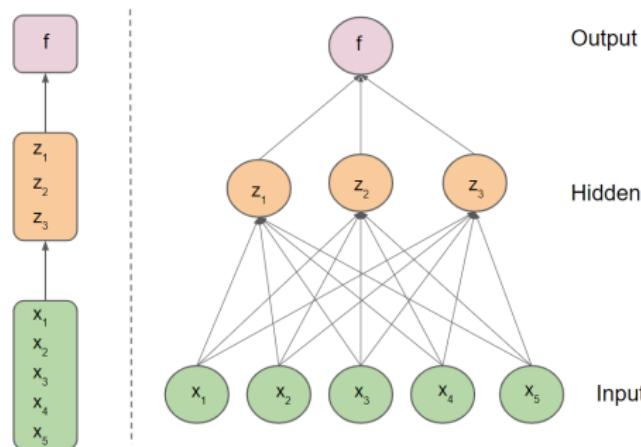
# MOTIVATION FOR RNNs

- The two major types of neural network architectures that we've seen so far are fully-connected networks and Convolutional Neural Networks (CNNs).
- In both cases, the input layers have a fixed size and, therefore, these networks can (typically) only handle fixed-length inputs.
- The primary reason for this is that it is not possible to vary the size of the input layer without also varying the number of learnable parameters/weights in the network.
- However, in many cases, we would like to feed **variable length inputs** to the network.
- Common examples of this are **sequence data** such as time-series, audio and text.
- Therefore, we need a new class of neural network architectures that are able to handle such variable length inputs: **Recurrent Neural Networks (RNNs)**.

# RNNs – The basic idea

# RNNS - INTRODUCTION

- Let's say we have some text data and our task is to analyse the *sentiment* in the text.
- For example, given an input sentence, such as "This is good news.", the network has to classify it as either 'positive' or 'negative'.
- We would like to train a simple neural network (such as the one below) to perform the task.



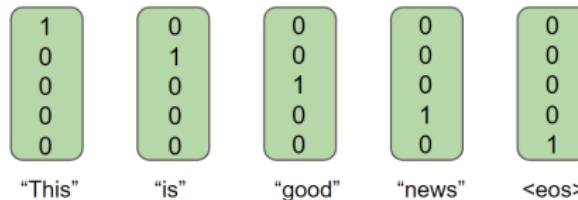
**Figure:** Two equivalent visualizations of a dense net with a single hidden layer.

# RNNs - INTRODUCTION

- Because sentences can be of varying lengths, we need to modify the dense net architecture to handle such a scenario.
- One approach is to draw inspiration from the way a human reads a sentence; that is, one word at a time.
- An important cognitive mechanism that makes this possible is "**short-term memory**".
- As we read a sentence from beginning to end, we retain some information about the words that we've already read and use this information to understand the meaning of the entire sentence.
- Therefore, in order to feed the words in a sentence sequentially to a neural network, we need to give it the ability to retain some information about past inputs.

# RNNs - INTRODUCTION

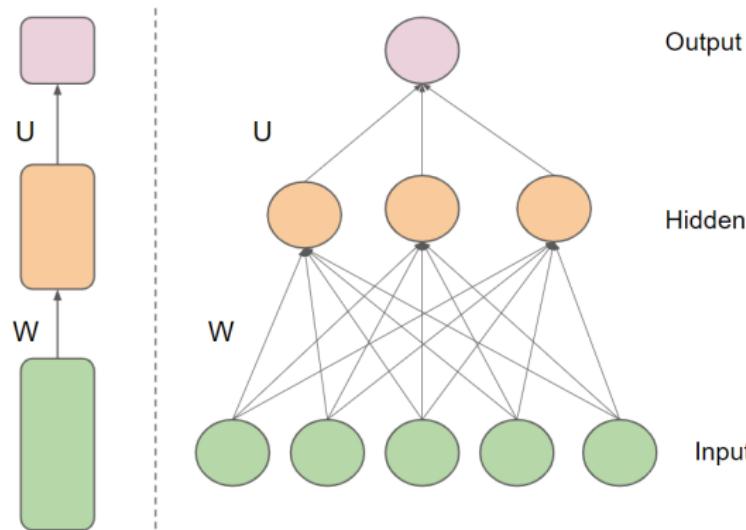
- When words in a sentence are fed to the network one at a time, the inputs are no longer independent. For example, it is much more likely that the word "good" is followed by "morning" rather than "plastic". We need to model this dependence.
- Each word must still be encoded as a fixed-length vector because the size of the input layer will remain fixed.
- Here, for the sake of the visualization, each word is represented as a 'one-hot coded' vector of length 5. (<eos> = 'end of sequence')



(The standard approach is to use word embeddings (more on this later)).

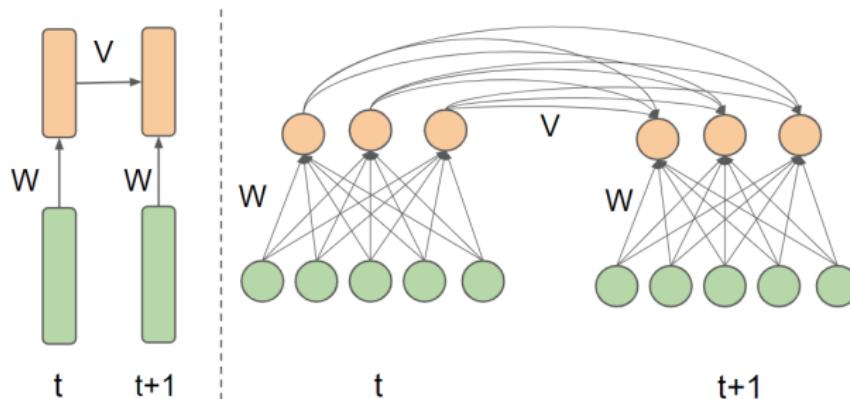
# RNNs - INTRODUCTION

- Our goal is to feed the words to the network sequentially in discrete time-steps.
- A regular dense neural network with a single hidden layer only has two sets of weights : 'input-to-hidden' weights  $W$  and 'hidden-to-output' weights  $U$ .



# RNNs - INTRODUCTION

- In order to enable the network to retain information about past inputs, we introduce an **additional set of weights  $V$** , from the hidden neurons at time-step  $t$  to the hidden neurons at time-step  $t + 1$ .
- Having this additional set of weights makes the activations of the hidden layer depend on **both** the current input and the activations for the *previous* input.



**Figure:** Input-to-hidden weights  $W$  and **hidden-to-hidden** weights  $V$ . The hidden-to-output weights  $U$  are not shown in the figure.

# RNNs - INTRODUCTION

- With this additional set of hidden-to-hidden weights  $V$ , the network is now a Recurrent Neural Network (RNN).
- In a regular feed-forward network, the activations of the hidden layer are only computed using the input-hidden weights  $W$  (and bias  $b$ ).

$$z = \sigma(W^T x + b)$$

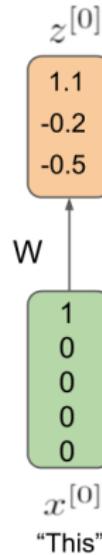
- In an RNN, the activations of the hidden layer (at time-step  $t$ ) are computed using *both* the input-to-hidden weights  $W$  and the hidden-to-hidden weights  $V$ .

$$z^{[t]} = \sigma(V^T z^{[t-1]} + W^T x^{[t]} + b)$$

- The vector  $z^{[t]}$  represents the short-term memory of the RNN because it is a function of the current input  $x^{[t]}$  and the activations  $z^{[t-1]}$  of the previous time-step.
- Therefore, by recurrence, it contains a "summary" of *all* previous inputs.

# APPLICATION EXAMPLE — SENTIMENT ANALYSIS

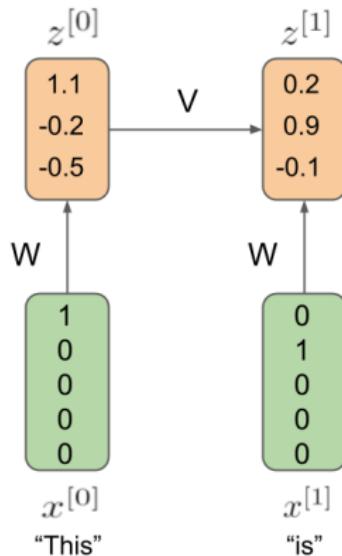
- At  $t = 0$ , we feed the word "This" to the network and obtain  $z^{[0]}$ .
- $z^{[0]} = \sigma(W^T x^{[0]} + b)$



Because this is the very first input, there is no past state. (Or, equivalently, the state is initialized to 0).

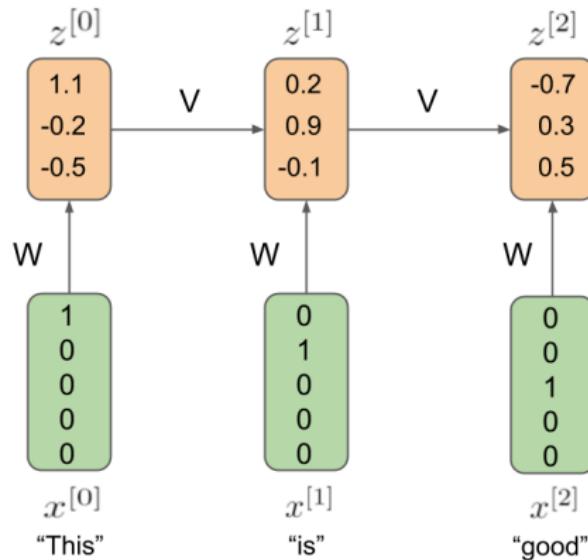
# APPLICATION EXAMPLE - SENTIMENT ANALYSIS

- At  $t = 1$ , we feed the second word to the network to obtain  $z^{[1]}$ .
- $z^{[1]} = \sigma(V^T z^{[0]} + W^T x^{[1]} + b)$



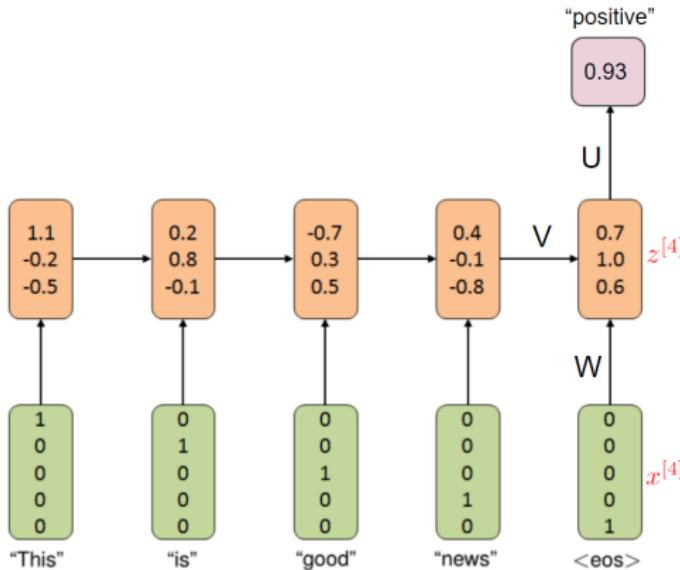
# APPLICATION EXAMPLE - SENTIMENT ANALYSIS

- At  $t = 2$ , we feed the next word in the sentence.
- $z^{[2]} = \sigma(V^T z^{[1]} + W^T x^{[2]} + b)$



# APPLICATION EXAMPLE - SENTIMENT ANALYSIS

- Once the entire input sequence has been processed, the prediction of the network can be generated by feeding the activations of the final time-step to the output neuron(s).
- $f = \sigma(U^T z^{[4]} + c)$ , where  $c$  is the bias of the output neuron.

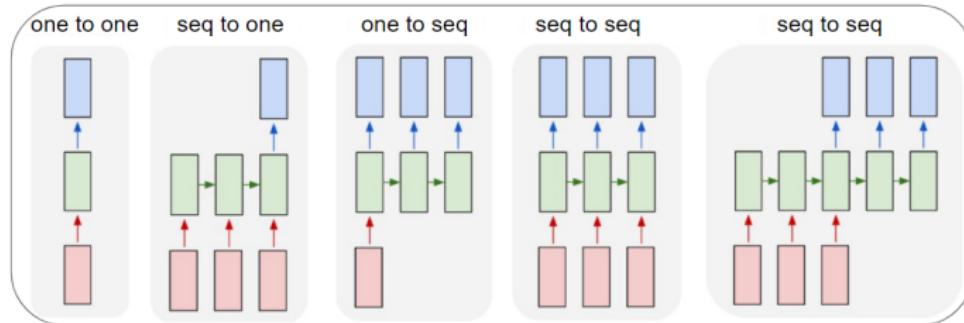


# PARAMETER SHARING

- This way, the network can process the sentence one word at a time and the length of the network can vary based on the length of the sequence.
- It's important to note that no matter how long the input sequence is, the matrices  $W$  and  $V$  are the same in every time-step. This is another example of **parameter sharing**.
- Therefore, the number of weights in the network is independent of the length of the input sequence.

# RNNS - USE CASE SPECIFIC ARCHITECTURES

RNNs are very versatile. They can be applied to a wide range of tasks.



credit: Andrej Karpathy

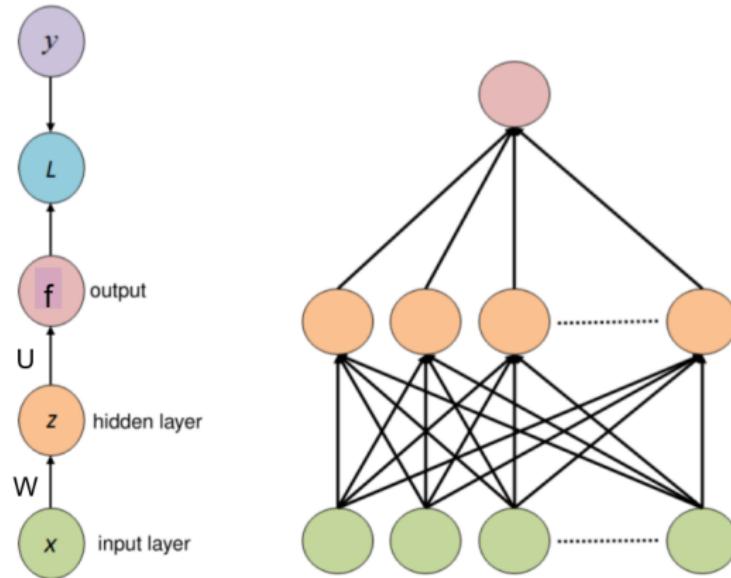
**Figure:** RNNs can be used in tasks that involve multiple inputs and/or multiple outputs.

Examples:

- Many-to-One: Sentiment analysis, document classification.
- One-to-Many: Image captioning.
- Many-to-Many: Language modelling, machine translation, time-series prediction.

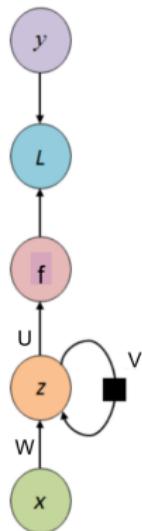
# RNNs - Computational Graph

# RNNs - COMPUTATIONAL GRAPH



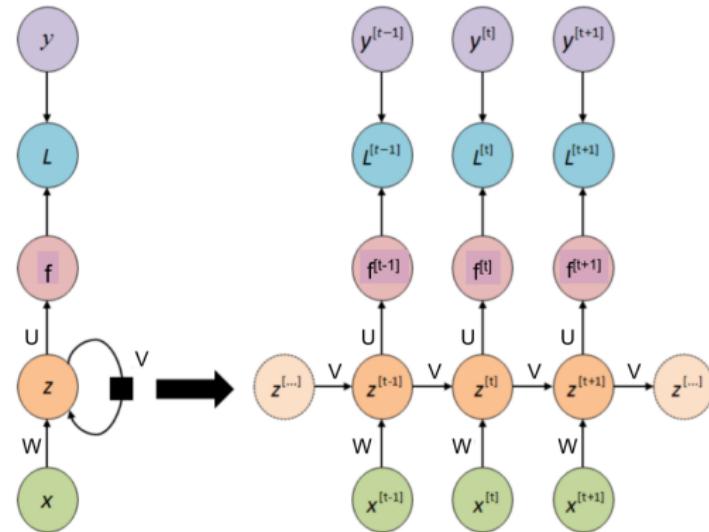
- On the left is the computational graph for the dense net on the right. A loss function  $L$  measures how far each output  $f$  is from the corresponding training target  $y$ .

# RNNs - COMPUTATIONAL GRAPH



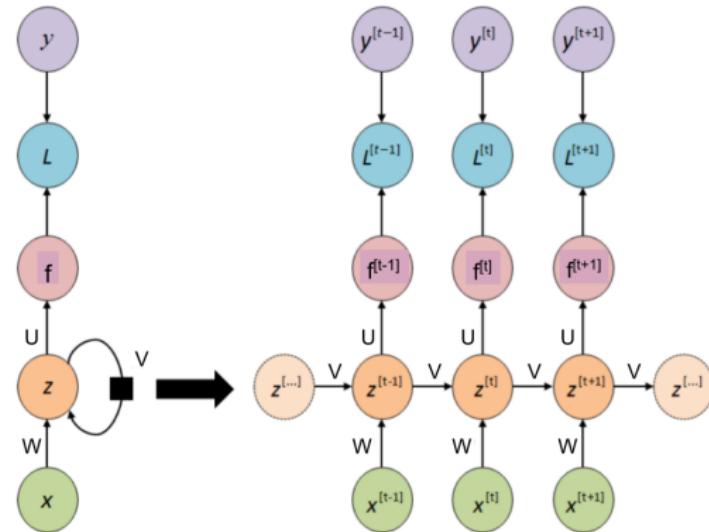
- A helpful way to think of an RNN is as multiple copies of the same network, each passing a message to a successor.
- RNNs are networks with loops, allowing information to persist.

# RNNs - COMPUTATIONAL GRAPH



- Things might become more clear if we unfold the architecture.
- We call  $z^{[t]}$  the *state* of the system at time  $t$ .
- Recall, the state contains information about the whole past sequence.

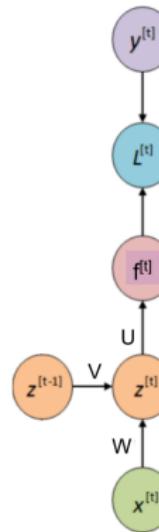
# RNNs - COMPUTATIONAL GRAPH



- We went from

$$\begin{aligned} f &= \tau(c + U^T \sigma(b + W^T x)) \text{ for the dense net, to} \\ f^{[t]} &= \tau(c + U^T \sigma(b + V^T z^{[t-1]} + W^T x^{[t]})) \text{ for the RNN.} \end{aligned}$$

# RNNs - COMPUTATIONAL GRAPH

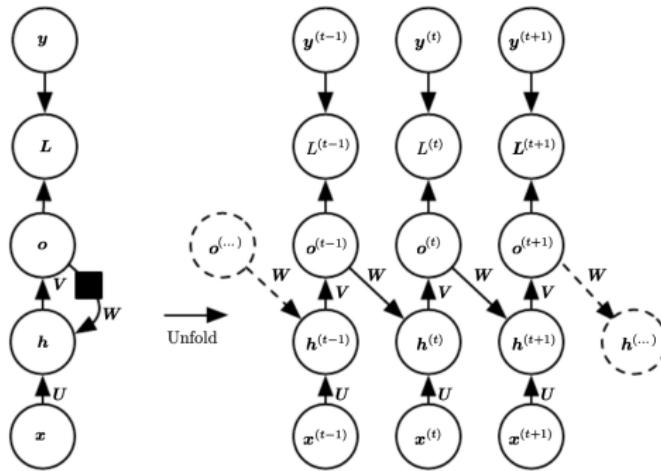


- Potential computational graph for time-step  $t$ :

$$f^{[t]} = \tau(c + U^T \sigma(b + V^T z^{[t-1]} + W^T x^{[t]}))$$

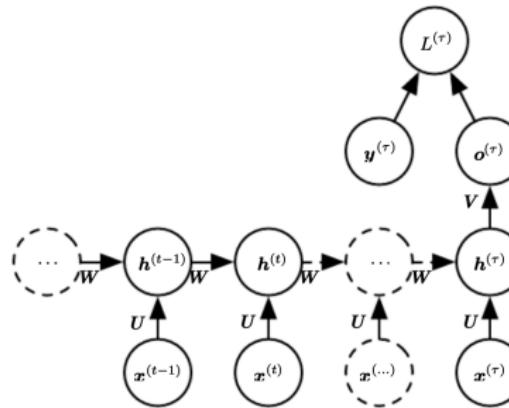
# RNNs - COMPUTATIONAL GRAPH WITH RECURRENT OUTPUT-HIDDEN CONNECTIONS

Recurrent connections do not need to map from hidden to hidden neurons!



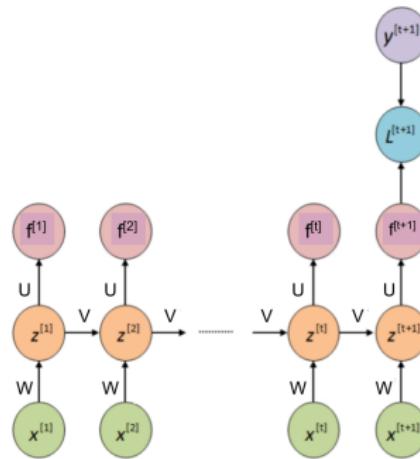
# RNNs - COMPUTATIONAL GRAPH FOR MANY TO ONE MAPPING

RNNs do not need to produce an output at each time step. Often only one output is produced after processing the whole sequence.



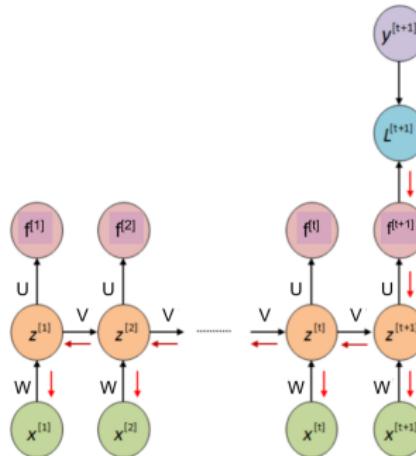
# Computing the Loss Gradient in RNNs

# BACKPROPAGATION THROUGH TIME



- For training the RNN we need to compute  $\frac{dL}{du_{i,j}}$ ,  $\frac{dL}{dv_{i,j}}$ , and  $\frac{dL}{dw_{i,j}}$ .
- To do so, during backpropagation at time step  $t$  we need to compute

# BACKPROPAGATION THROUGH TIME



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- To do so, during backpropagation at time step  $t$  we need to compute

$$\frac{dL}{dz^1} = \frac{dL}{dz^t} \frac{z^t}{dz^{t-1}} \cdots \frac{dz^2}{dz^1}$$

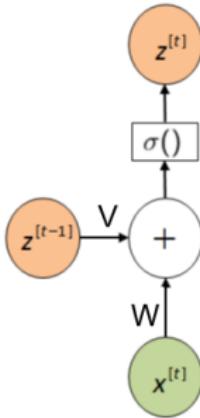
# LONG-TERM DEPENDENCIES

- In practice, it is quite challenging for RNNs to learn long-term dependencies. The gradients either **vanish** (most of the time) or **explode** (rarely, but with much damage to the optimization).
- That happens simply because we propagate errors over very many stages backwards.
- Recall, that we can counteract vanishing/exploding gradients, by using activation functions like RELU/gradient clipping.
- Even if we assume that the parameters are such that the recurrent network is stable (can store memories, with gradients not exploding), the difficulty with long-term dependencies arises from the exponentially smaller weights given to long-term interactions (involving the multiplication of many Jacobians) compared to short-term ones.

# Gated units: LSTMs and GRUs

# LONG SHORT-TERM MEMORY (LSTM)

The LSTM provides a different way of dealing with vanishing gradients and modelling long-term dependencies.



- Until now, we simply computed

$$z^{[t]} = \sigma(b + V^T z^{[t-1]} + W^T x^{[t]})$$

# LONG SHORT-TERM MEMORY (LSTM)

The LSTM provides a different way of dealing with vanishing gradients and modelling long-term dependencies.

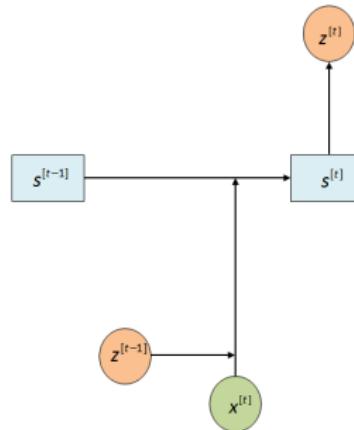


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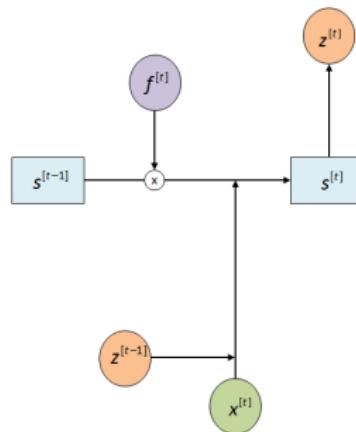
- Now we introduce the LSTM cell (which is a small network on its own)

# LONG SHORT-TERM MEMORY (LSTM)



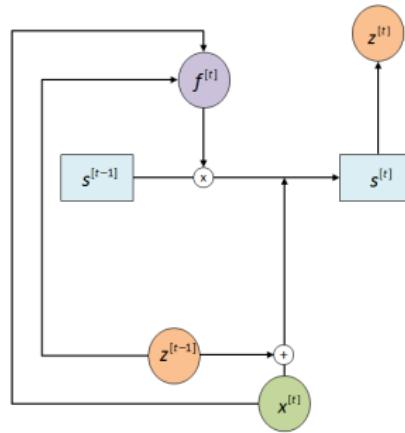
- The key to LSTMs is the **cell state**  $s^t$ .
- $s^t$  can be manipulated by different **gates** to forget old information, add new information, and read information out of it.
- Each gate is a vector of the same size as the  $s^t$  with elements between 0 (â€œlet nothing passâ€) and 1 (â€œlet everything passâ€).

# LONG SHORT-TERM MEMORY (LSTM)



- **Forget gate  $f^{[t]}$ :** indicates which information of the old cell state we should forget.
- Intuition: Think of a model trying to predict the next word based on all the previous. The cell state might include the gender of the present subject, so that the correct pronouns can be used. When we now see a new subject, we want to forget the gender of the old one.

# LONG SHORT-TERM MEMORY (LSTM)

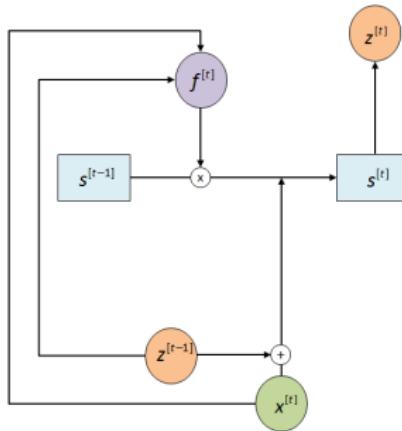


- We obtain the forget gate by computing

$$f^{[t]} = \sigma(b_f + V_f^T z^{[t-1]} + W_f^T x^{[t]})$$

- $\sigma()$  is a sigmoid, squashing the values to  $[0, 1]$ , and  $V_f, W_f$  are forget gate specific weights.

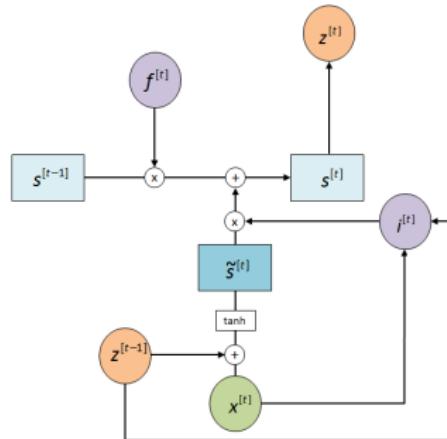
# LONG SHORT-TERM MEMORY (LSTM)



- To compute the cell state  $s^t$ , the first step is to multiply (element-wise) the previous cell state  $s^{t-1}$  by the forget gate  $f^t$ .

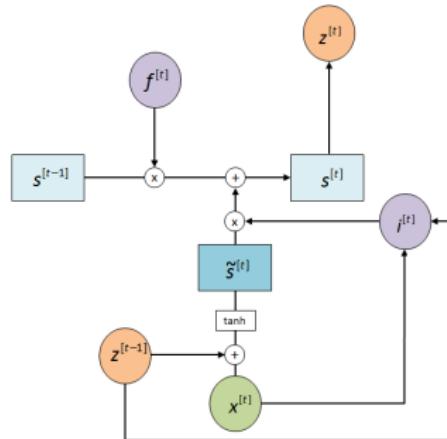
$$f^t \odot s^{t-1}, \text{ with } f^t \in [0, 1]$$

# LONG SHORT-TERM MEMORY (LSTM)



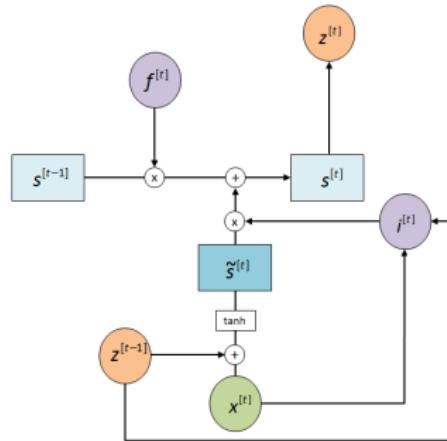
- **Input gate  $i^{[t]}$ :** indicates which new information should be added to  $s^{[t]}$ .
- Intuition: in the example of the language model, this is where we add the new information about the gender of the new subject.

# LONG SHORT-TERM MEMORY (LSTM)



- The new information is given by  
$$\tilde{s}^{[t]} = \tanh(b + V^T z^{[t-1]} + W^T x^{[t]}) \in [-1, 1].$$
- The input gate is given by  
$$i^{[t]} = \sigma(b_i + V_i^T z^{[t-1]} + W_i^T x^{[t]}) \in [0, 1].$$
- $W$  and  $V$  are weights of the new information,  $W_i$  and  $V_i$  the weights of the input gate.

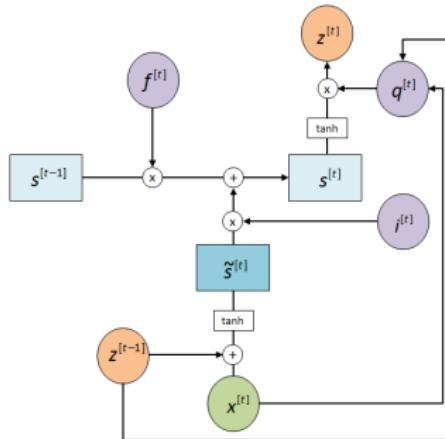
# LONG SHORT-TERM MEMORY (LSTM)



- Now we can finally compute the cell state  $s^{[t]}$ :

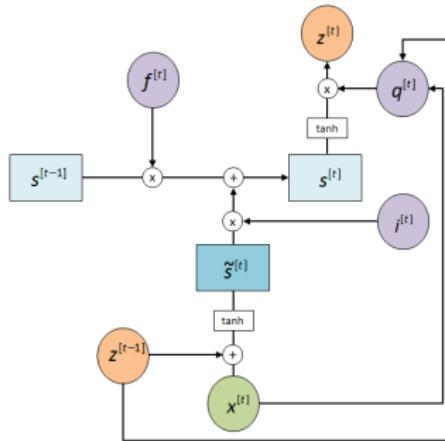
$$s^{[t]} = f^{[t]} \odot s^{[t-1]} + i^{[t]} \odot \tilde{s}^{[t]}$$

# LONG SHORT-TERM MEMORY (LSTM)



- **Output gate  $q^{[t]}$ :** Indicates which information from the cell state is filtered.
- It is given by  $q^{[t]} = \sigma(b_q + V_q^T z^{[t-1]} + W_q^T x^{[t]})$ , with specific weights  $W_q$ ,  $V_q$ .

# LONG SHORT-TERM MEMORY (LSTM)

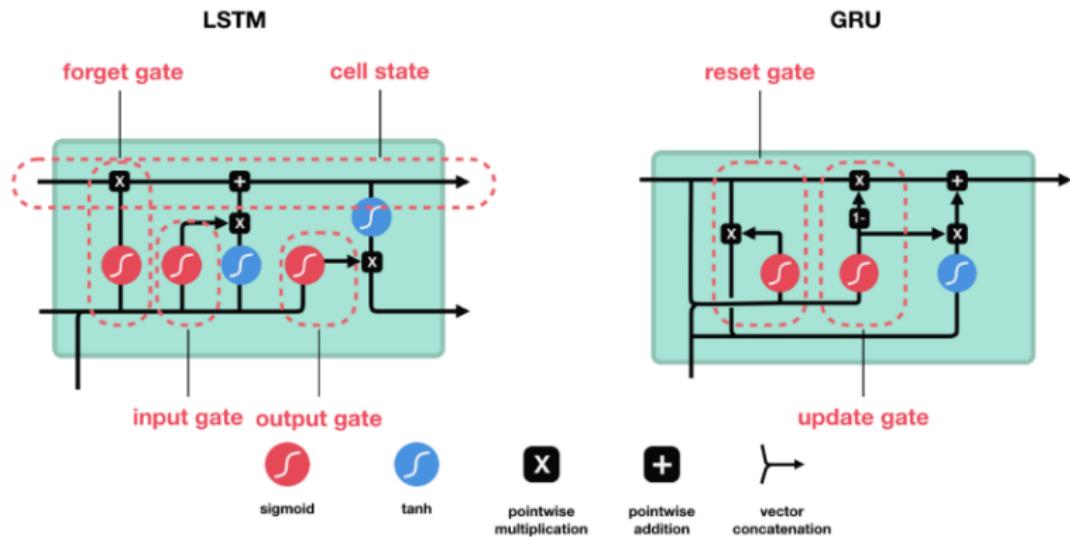


- Finally, the new state  $z^{[t]}$  of the LSTM is a function of the cell state, multiplied by the output gate:

$$z^{[t]} = q^{[t]} \odot \tanh(s^{[t]})$$

# GATED RECURRENT UNIT (GRU)

A popular alternative to LSTM is the Gated Recurrent Unit (GRU). Its performance can match and sometimes exceed that of an LSTM.

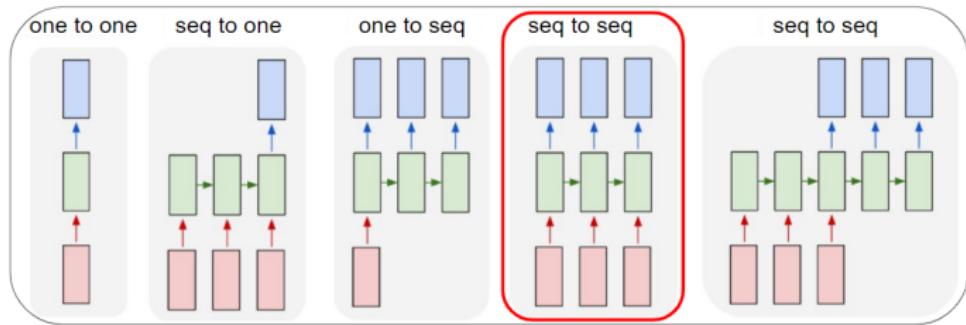


credit: Michael Nguyen

**Figure:** A GRU has fewer gates and is faster to train.

# **Application: Language modelling**

# Many-to-Many (Type I)



# RNNS - LANGUAGE MODELLING

- In the previous example, we built a 'many-to-one' RNN model to perform 'sentiment analysis'.
- Another common task in Natural Language Processing (NLP) is '**language modelling**'.
- Input: word/character, encoded as a one-hot vector.
- Output: probability distribution over words/characters given previous words

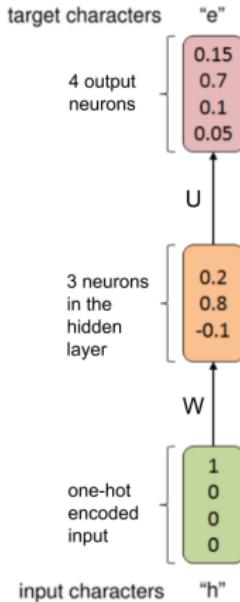
$$P(y^{[1]}, \dots, y^{[\tau]}) = \prod_{i=1}^{\tau} P(y^{[i]} | y^{[1]}, \dots, y^{[i-1]})$$

⇒ given a sequence of previous characters, ask the RNN to model the probability distribution of the next character in the sequence!

# RNNs - LANGUAGE MODELLING

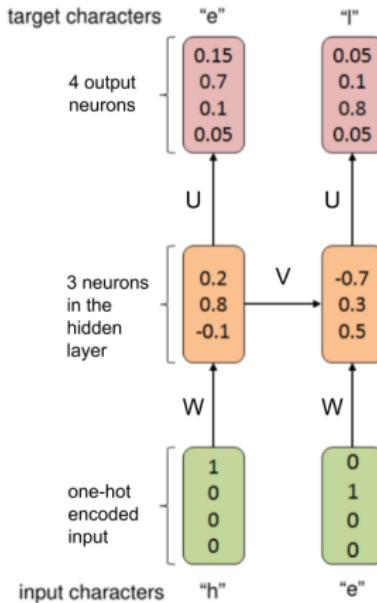
- In this example, we'll feed the characters in the word "hello" one at a time to a 'many-to-many' RNN.
- For the sake of the visualization, the characters "h", "e", "l" and "o" are one-hot coded as vectors of length 4 and the output layer only has 4 neurons, one for each character (we'll ignore the <eos> token).
- At each time step, the RNN has to output a probability distribution (softmax) over the 4 possible characters that might follow the current input.
- Naturally, if the RNN has been trained on words in the English language:
  - The probability of "e" should be likely, given the context of "h".
  - "l" should be likely in the context of "he".
  - "l" should **also** be likely, given the context of "hel".
  - and, finally, "o" should be likely, given the context of "hell".

# RNNs - LANGUAGE MODELLING



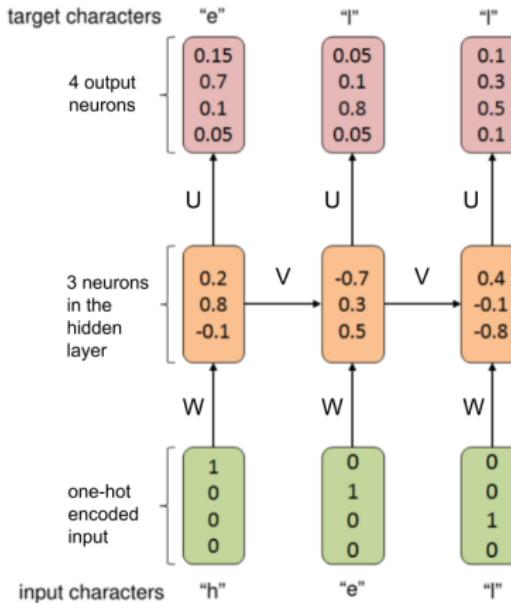
The probability of “e” should be high, given the context of “h”.

# RNNs - LANGUAGE MODELLING



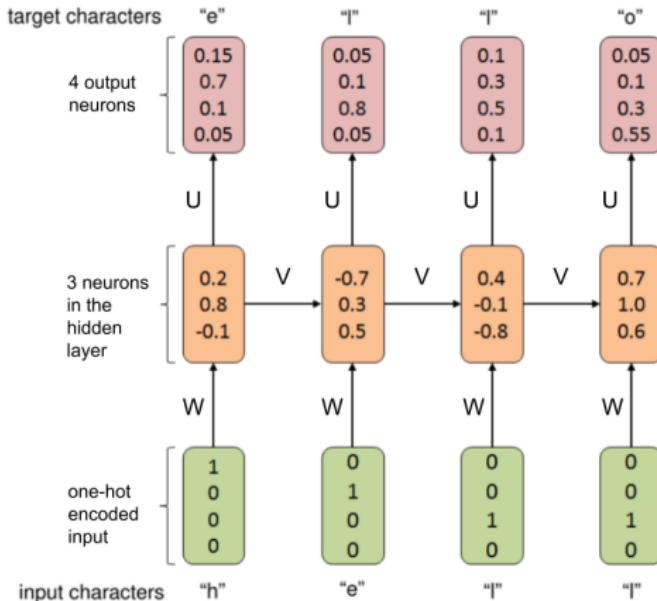
The probability of "l" should be high, given in the context of "he".

# RNNs - LANGUAGE MODELLING



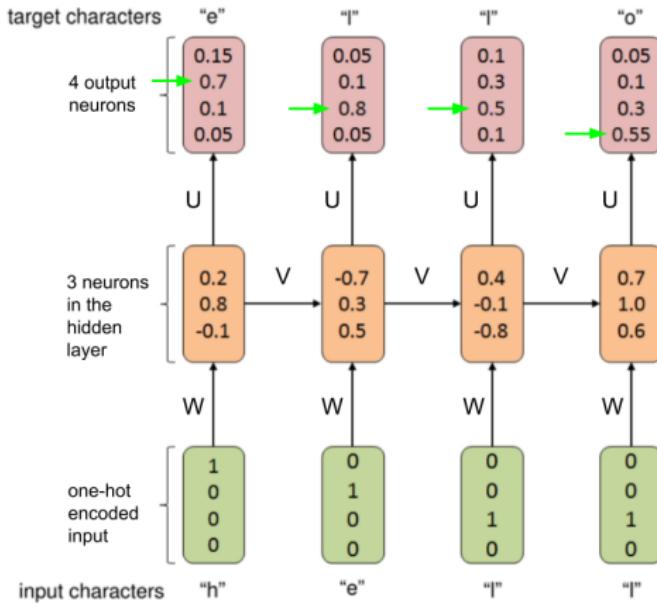
The probability of "l" should **also** be high, given in the context of "hel".

# RNNs - LANGUAGE MODELLING



The probability of "o" should be high, given the context of "hell".

# RNNs - LANGUAGE MODELLING

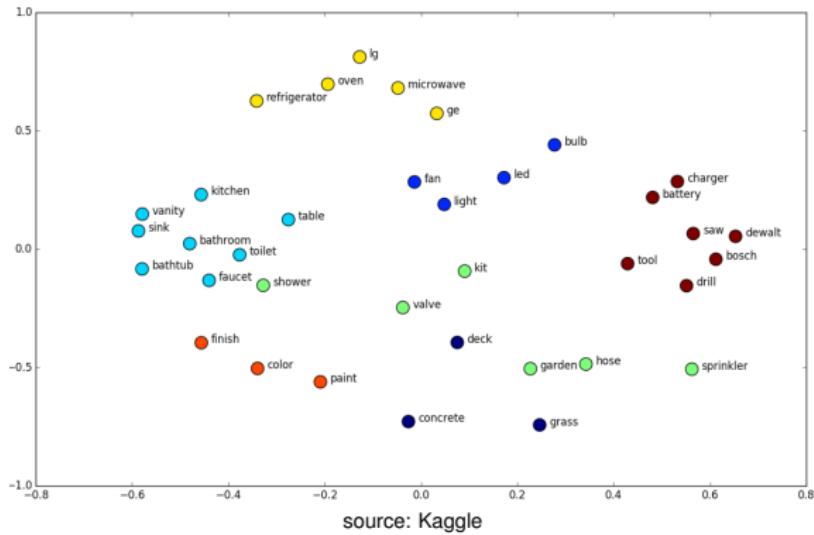


During training, our goal would be to increase the confidence for the correct letters (indicated by the green arrows) and decrease the confidence of all others.

# WORD EMBEDDINGS

- In the example in the beginning, words were encoded as sparse one-hot vectors.
- However, this is simply not practical as it would require that the size of the input layer = # of words in the dictionary.
- More importantly, the one-hot representations do not capture the meanings/semantics of the words because all words would be equidistant from one another.
- For example, the word "pineapple" would be equidistant from the words "apple" and "weather".
- Therefore, it is standard practice to encode each word as a dense (as opposed to sparse) vector of fixed size that captures its underlying semantic content.
- The dimensionality of these embeddings is typically much smaller than the number of words in the dictionary.

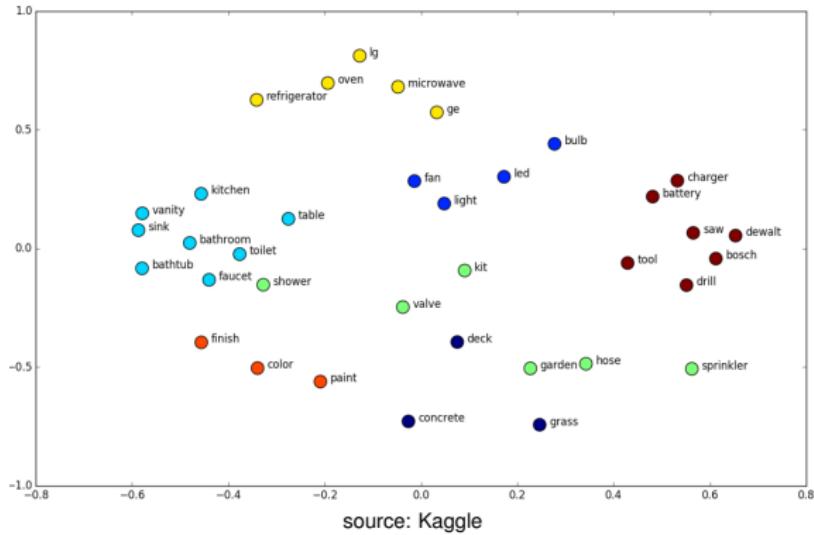
# WORD EMBEDDINGS



**Figure:** A two-dimensional embedding space is shown here for the sake of visualization. Typically, the embedding space is much higher dimensional.

A major advantage of using word embeddings is that similar words are embedded close to each other in the lower-dimensional embedding space and, therefore, using them gives you a "warm start" for any NLP task.

# WORD EMBEDDINGS



**Figure:** A two-dimensional embedding space is shown here for the sake of visualization. Typically, the embedding space is much higher dimensional.

It is an easy way to incorporate prior knowledge into your model and a rudimentary form of **transfer learning**.

# WORD EMBEDDINGS

- Two very popular approaches to learn word embeddings are **word2vec** by Google and **GloVe** by Facebook. These embeddings are typically 100 to 1000 dimensional.
- Even though these embeddings capture the meaning of each word to an extent, they do not capture the *semantic* of the word in a given context because each word has a static precomputed representation. For example, depending on the context, the word "bank" might refer to a financial institution or to a river bank.
- Recently, there have been significant breakthroughs in context-based embeddings. One such example are the embeddings provided by BERT [Devlin et al., 2018], a **transformer model** which was trained on a corpus of 3.3 billion words.
- BERT (a non-recurrent model!) obtained new state-of-the-art performance on 11 NLP tasks.

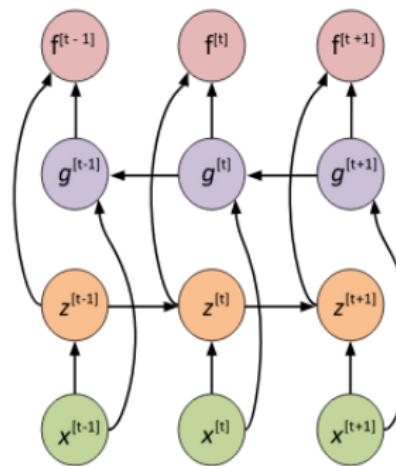
# **Bidirectional RNNs**

# BIDIRECTIONAL RNNs

- Another generalization of the simple RNN are bidirectional RNNs.
- These allow us to process sequential data depending on both past and future inputs, e.g. an application predicting missing words, which probably depend on both preceding and following words.
- One RNN processes inputs in the forward direction from  $x^{[1]}$  to  $x^{[T]}$  computing a sequence of hidden states  $(z^{[1]}, \dots, z^{(T)})$ , another RNN in the backward direction from  $x^{[T]}$  to  $x^{[1]}$  computing hidden states  $(g^{[T]}, \dots, g^{[1]})$
- Predictions are then based on both hidden states, which could be **concatenated**.
- With connections going back in time, the whole input sequence must be known in advance to train and infer from the model.
- Bidirectional RNNs are often used for the encoding of a sequence in machine translation.

# BIDIRECTIONAL RNNs

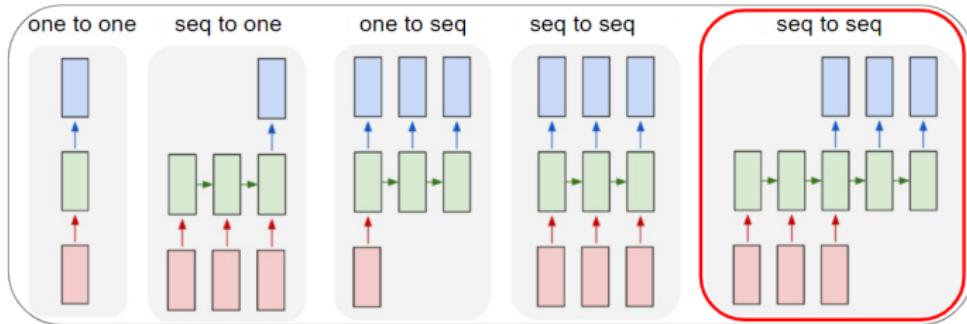
Computational graph of an bidirectional RNN:



**Figure:** A bidirectional RNN consists of a forward RNN processing inputs from left to right and a backward RNN processing inputs backwards in time.

# Encoder-Decoder Architectures

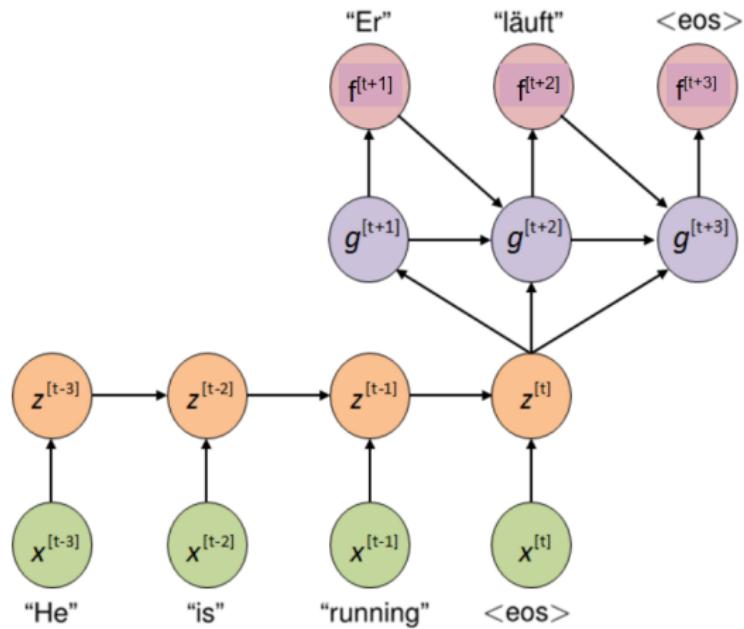
# Many-to-Many (Type II)



# ENCODER-DECODER NETWORK

- For many interesting applications such as question answering, dialogue systems, or machine translation, the network needs to map an input sequence to an output sequence of different length.
- This is what an encoder-decoder (also called sequence-to-sequence architecture) enables us to do!

# ENCODER-DECODER NETWORK



**Figure:** In the first part of the network, information from the input is encoded in the context vector, here the final hidden state, which is then passed on to every hidden state of the decoder, which produces the target sequence.

# ENCODER-DECODER NETWORK

- An input/encoder-RNN processes the input sequence of length  $n_x$  and computes a fixed-length context vector  $C$ , usually the final hidden state or simple function of the hidden states.
- One time step after the other information from the input sequence is processed, added to the hidden state and passed forward in time through the recurrent connections between hidden states in the encoder.
- The context vector summarizes important information from the input sequence, e.g. the intent of a question in a question answering task or the meaning of a text in the case of machine translation.
- The decoder RNN uses this information to predict the output, a sequence of length  $n_y$ , which could vary from  $n_x$ .

# ENCODER-DECODER NETWORK

- In machine translation, the decoder is a language model with recurrent connections between the output at one time step and the hidden state at the next time step as well as recurrent connections between the hidden states:

$$p(y^{[1]}, \dots, y^{[n_y]} | x^{[1]}, \dots, x^{[n_x]}) = \prod_{t=1}^{n_y} p(y^{[t]} | C; y^{[1]}, \dots, y^{[t-1]})$$

with  $C$  being the context-vector.

- This architecture is now jointly trained to minimize the translation error given a source sentence.
- Each conditional probability is then

$$p(y^{[t]} | y^{[1]}, \dots, y^{[t-1]}; C) = f(y^{[t-1]}, g^{[t]}, C)$$

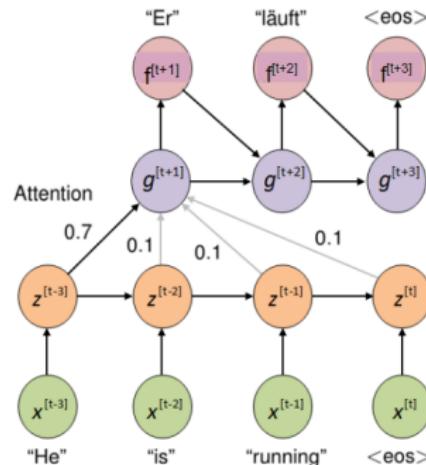
where  $f$  is a non-linear function, e.g. the tanh and  $g^{[t]}$  is the hidden state of the decoder network.

# ATTENTION

- In a classical decoder-encoder RNN all information about the input sequence must be incorporated into the final hidden state, which is then passed as an input to the decoder network.
- With a long input sequence this fixed-sized context vector is unlikely to capture all relevant information about the past.
- Each hidden state contains mostly information from recent inputs. In the case of a bidirectional RNN to encode the input sequence, a hidden state contains information from recent preceding and following inputs.

# ATTENTION

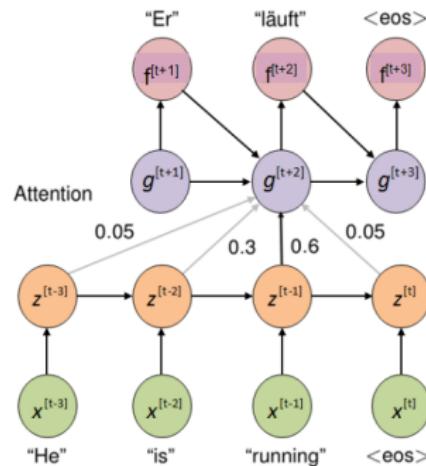
- An **attention mechanism** allows the decoder network to focus on different parts of the input sequence by adding connections from all hidden states of the encoder to each hidden state of the decoder.



**Figure:** Attention at  $t = t + 1$

# ATTENTION

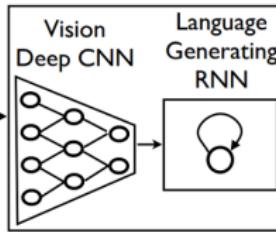
- At each time step  $i$ , a set of weights  $\alpha_{i,j}$  is computed which determine how to combine the hidden states of the encoder into a context vector  $\mathbf{c}_i = \sum_{j=1}^{n_x} \alpha_{i,j} \mathbf{z}^{[j]}$ , which holds the necessary information to predict the correct output.



**Figure:** Attention at  $t = t + 2$

# **More application examples**

# SOME MORE SOPHISTICATED APPLICATIONS



A group of people shopping at an outdoor market.

There are many vegetables at the fruit stand.

**Figure:** Show and Tell: A Neural Image Caption Generator (Oriol Vinyals et al. 2014). A language generating RNN tries to describe in brief the content of different images.

# SOME MORE SOPHISTICATED APPLICATIONS

A person riding a motorcycle on a dirt road.



Two dogs play in the grass.



A skateboarder does a trick on a ramp.



A dog is jumping to catch a frisbee.



A group of young people playing a game of frisbee.



Two hockey players are fighting over the puck.



A little girl in a pink hat is blowing bubbles.



A refrigerator filled with lots of food and drinks.



A herd of elephants walking across a dry grass field.



A close up of a cat laying on a couch.



A red motorcycle parked on the side of the road.



A yellow school bus parked in a parking lot.



Describes without errors

Describes with minor errors

Somewhat related to the image

Unrelated to the image

**Figure:** Show and Tell: A Neural Image Caption Generator (Oriol Vinyals et al. 2014). A language generating RNN tries to describe in brief the content of different images.

# SOME MORE SOPHISTICATED APPLICATIONS



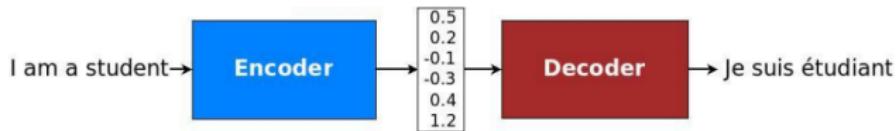
A woman is throwing a frisbee in a park.



A stop sign is on a road with a mountain in the background.

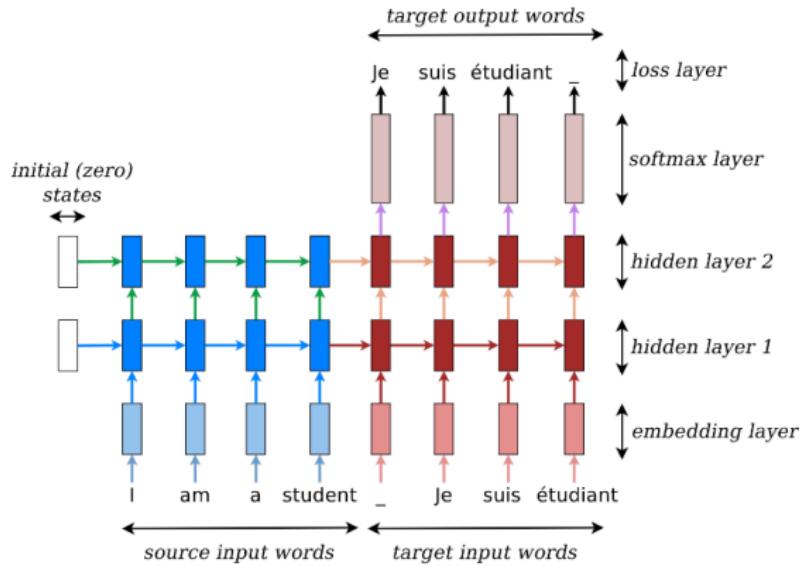
**Figure:** Attention for image captioning: the attention mechanism tells the network roughly which pixels to pay attention to when writing the text (Kelvin Xu al. 2015)

# SOME MORE SOPHISTICATED APPLICATIONS



**Figure:** Neural Machine Translation (seq2seq): Sequence to Sequence Learning with Neural Networks (Ilya Sutskever et al. 2014). As we saw earlier, an encoder converts a source sentence into a “meaning” vector which is passed through a decoder to produce a translation.

# SOME MORE SOPHISTICATED APPLICATIONS



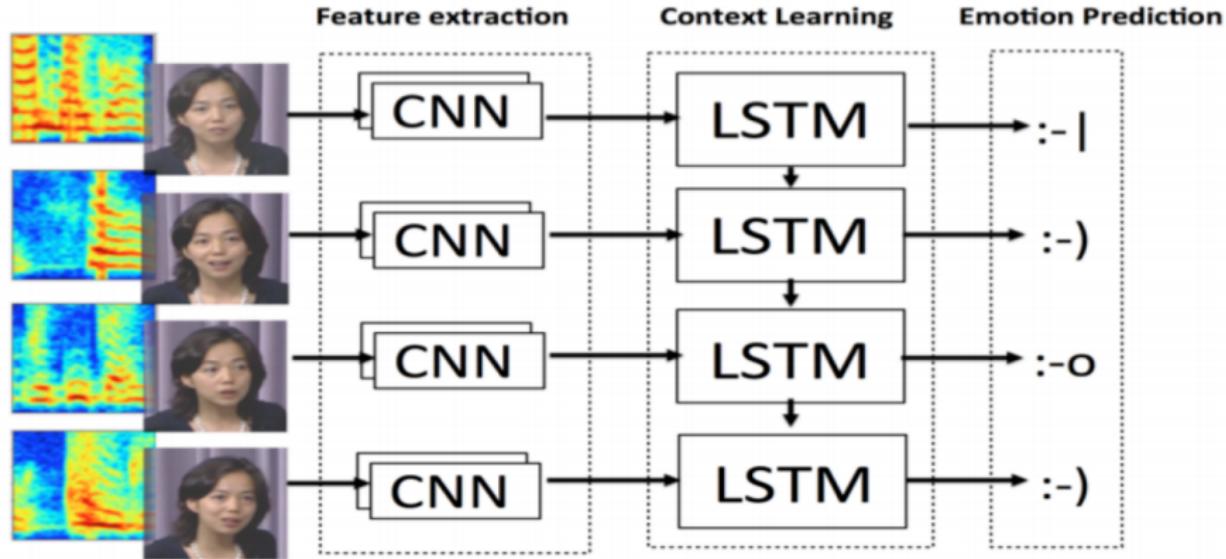
**Figure:** Neural Machine Translation (seq2seq): Sequence to Sequence Learning with Neural Networks (Ilya Sutskever et al. 2014). As we saw earlier, an encoder converts a source sentence into a “meaning” vector which is passed through a decoder to produce a translation.

## SOME MORE SOPHISTICATED APPLICATIONS

more of national temperament

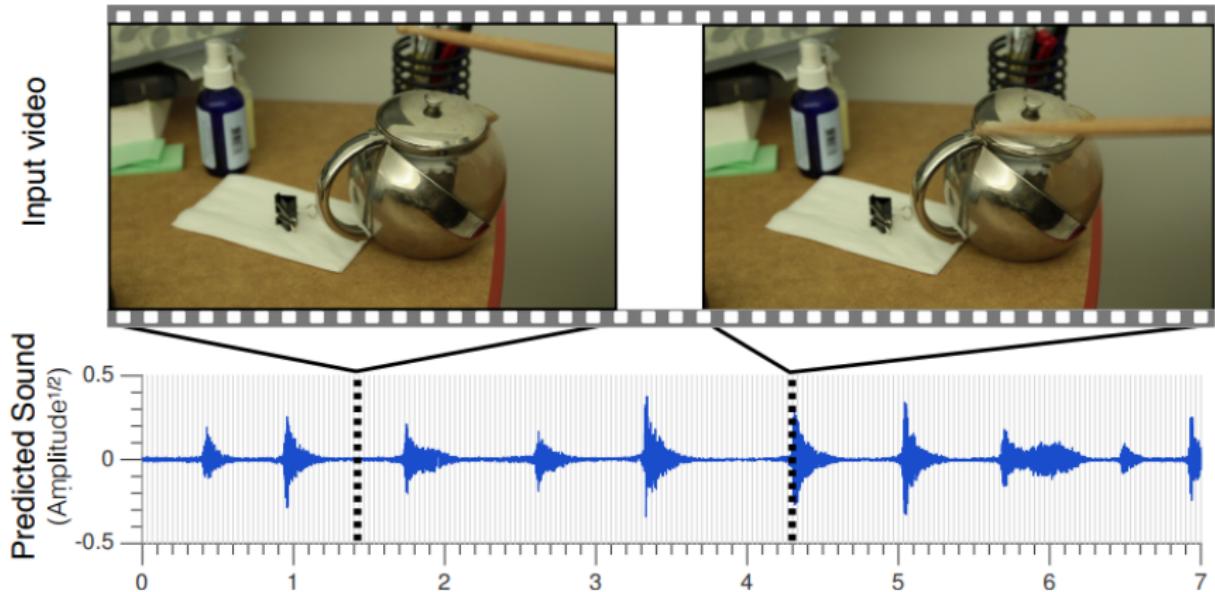
**Figure:** Generating Sequences With Recurrent Neural Networks (Alex Graves, 2013). Top row are real data, the rest are generated by various RNNs.

# SOME MORE SOPHISTICATED APPLICATIONS



**Figure:** Convolutional and recurrent nets for detecting emotion from audio data (Namrata Anand & Prateek Verma, 2016). We already had this example in the CNN chapter!

# SOME MORE SOPHISTICATED APPLICATIONS



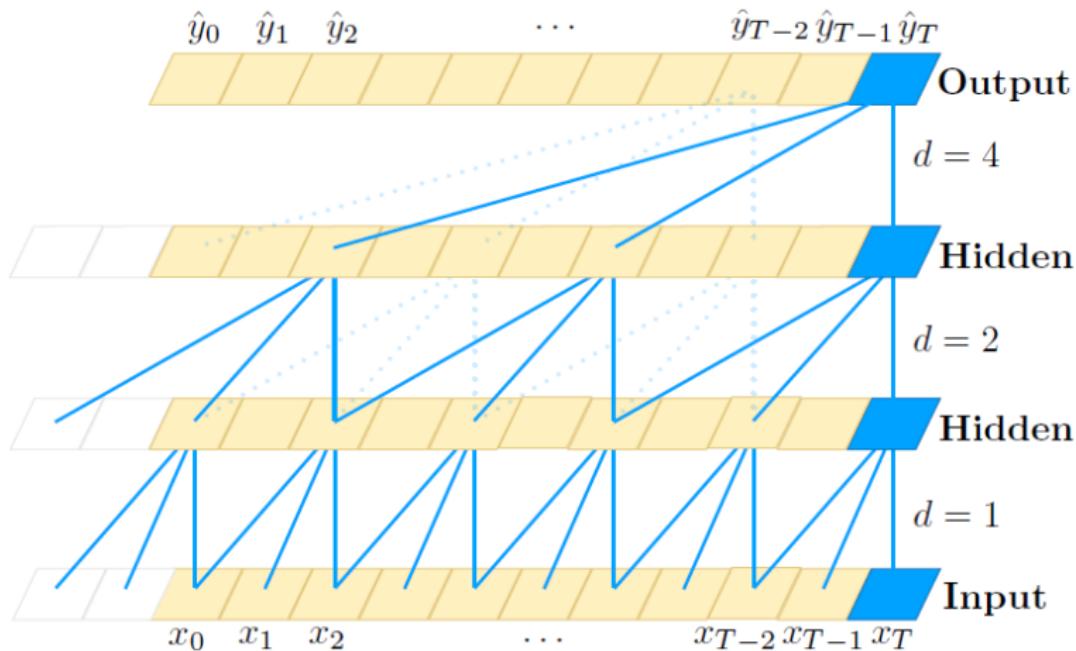
**Figure:** Visually Indicated Sounds (Andrew Owens et al. 2016). A model to synthesize plausible impact sounds from silent videos.

# **CNNs or RNNs?**

# CNNs OR RNNs?

- Historically, RNNs were the default models used in sequence processing tasks.
- However, some families of CNNs (especially those based on Fully Convolutional Networks (FCNs)) *can* be used to process variable-length sequences such as text or time-series data.
- If a CNN doesn't contain any fully-connected layers, the total number of weights in the network is independent of the spatial dimensions of the input because of weight-sharing in the convolutional layers.
- Recent research [Bai et al. , 2018] indicates that such convolutional architectures (which the authors term Temporal Convolutional Networks (TCNs)) can outperform RNNs on a wide range of tasks.
- A major advantage of TCNs is that the entire input sequence can be fed to the network at once (as opposed to sequentially.)

# CNNs OR RNNs?



**Figure:** A TCN (we've already seen this in the previous lecture!) is simply a variant of the one-dimensional FCN which uses a special type of dilated convolutions called **causal dilated** convolutions.

# CNNs OR RNNs?

Sequence Modeling Task	Model Size ( $\approx$ )	Models			
		LSTM	GRU	RNN	TCN
Seq. MNIST (accuracy <sup>h</sup> )	70K	87.2	96.2	21.5	<b>99.0</b>
Permuted MNIST (accuracy)	70K	85.7	87.3	25.3	<b>97.2</b>
Adding problem $T=600$ (loss <sup>ℓ</sup> )	70K	0.164	<b>5.3e-5</b>	0.177	<b>5.8e-5</b>
Copy memory $T=1000$ (loss)	16K	0.0204	0.0197	0.0202	<b>3.5e-5</b>
Music JSB Chorales (loss)	300K	8.45	8.43	8.91	<b>8.10</b>
Music Nottingham (loss)	1M	3.29	3.46	4.05	<b>3.07</b>
Word-level PTB (perplexity <sup>ℓ</sup> )	13M	<b>78.93</b>	92.48	114.50	88.68
Word-level Wiki-103 (perplexity)	-	48.4	-	-	<b>45.19</b>
Word-level LAMBADA (perplexity)	-	4186	-	14725	<b>1279</b>
Char-level PTB (bpc <sup>ℓ</sup> )	3M	1.36	1.37	1.48	<b>1.31</b>
Char-level text8 (bpc)	5M	1.50	1.53	1.69	<b>1.45</b>

**Figure:** Evaluation of TCNs and recurrent architectures on a wide range of sequence modelling tasks. <sup>h</sup> means higher is better and <sup>ℓ</sup> means lower is better. Note : To make the comparisons fair, all models have roughly the same size (for a given task) and the authors used grid search to find good hyperparameters for the recurrent architectures.

# SUMMARY

- RNNs are specifically designed to process sequences of varying length.
- For that recurrent connections are introduced into the network structure.
- The gradient is calculated by backpropagation through time.
- An LSTM replaces the simple hidden neuron by a complex system consisting out of cell state, and forget, input, and output gate.
- An RNN can be used as a language model, which can be improved by word-embeddings.
- Different advanced types of RNNs exist, like bidirectional RNNs or Encoder-Decoder architectures.

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