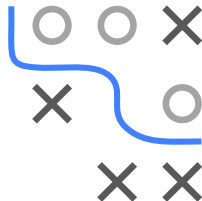
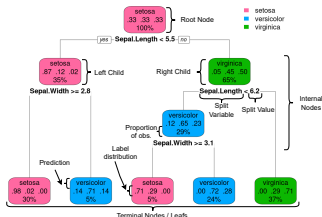


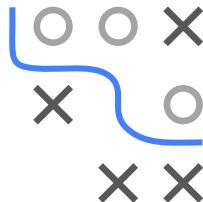
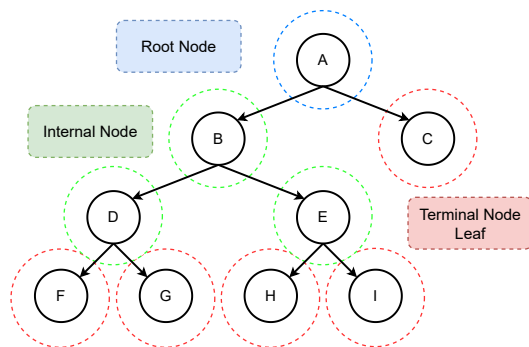
## Predictions with CART



- Understand the basic structure of a tree model
- Understand that the basic idea of a tree model is the same for classification and regression
- Understand how the label of a new observation is predicted via CART
- Know hypothesis space of CART

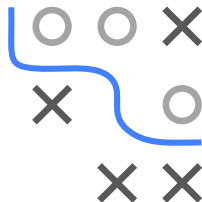
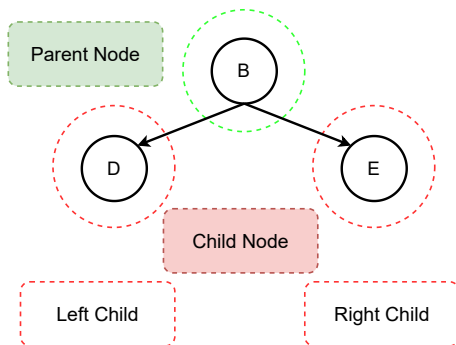


# BINARY TREES



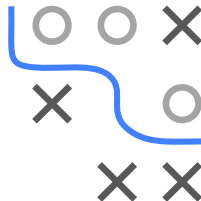
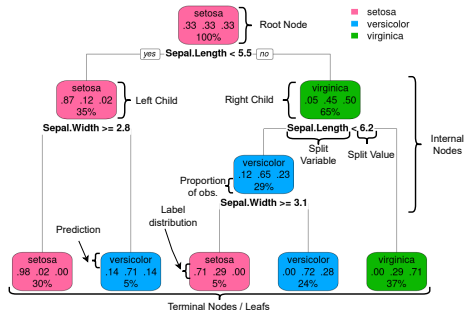
- Binary trees represent a top-down hierarchy with binary splits
- A tree is composed of different node types: a) the root node, b) internal nodes, and c) terminal nodes (also leaves).

# BINARY TREES



- Nodes have relative relationships, they can be:
  - Parent nodes
  - Child nodes
- Root nodes don't have parents – leaves don't have children

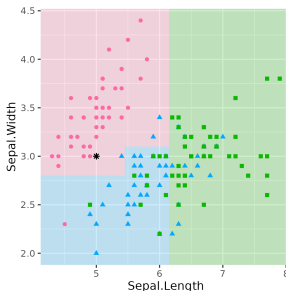
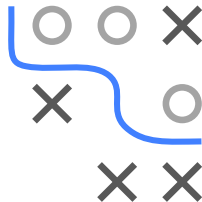
# CLASSIFICATION TREES



- Classification trees use the structure of a binary tree
- Binary splits are constructed top-down in a *data optimal* way
- Each split is a threshold decision for a single feature
- Each node contains the training points which follow its path
- Each leaf contains a constant prediction

# CLASSIFICATION TREE MODEL AND PREDICTION

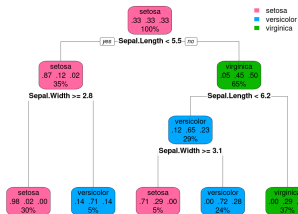
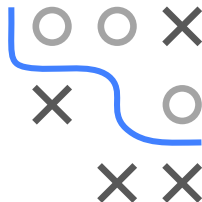
- When predicting new data (here\*: `Sepal.Length = 5`, `Sepal.Width = 3`) we use the learned split points and pass an observation through the tree
- Each observation is assigned to exactly one leaf
- Classification trees can make hard-label predictions (here: `setosa`) or predict probabilities (here: 0.98, 0.02, 0.00)



# CART AS A RULE BASED MODEL

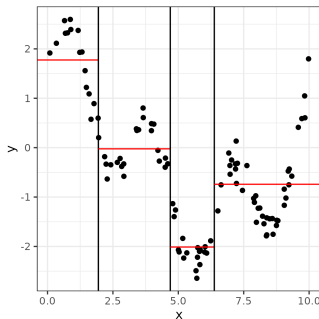
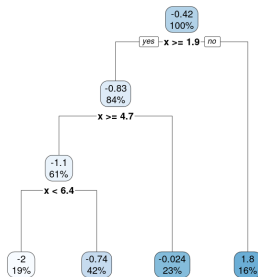
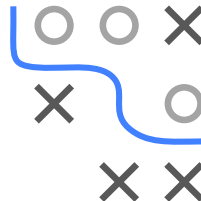
Leaf nodes can be expressed by a set of rules (left to right):

Hard label prediction	Label distribution	Sepal.Width	Sepal.Length
setosa	0.98, 0.02, 0.00	$\geq 2.8$	$< 5.5$
versicolor	0.14, 0.71, 0.14	$< 2.8$	$< 5.5$
setosa	0.71, 0.29, 0.00	$\geq 3.1$	$\geq 5.5 \ \& \ < 6.2$
versicolor	0.00, 0.72, 0.28	$< 3.1$	$\geq 5.5 \ \& \ < 6.2$
virginica	0.00, 0.29, 0.71	—	$\geq 6.2$



# REGRESSION TREE MODEL AND PREDICTION

- Works the same way as for classification
- But predictions in leaf nodes are a numerical scalar

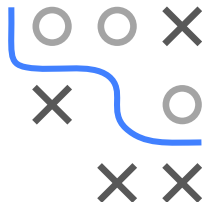
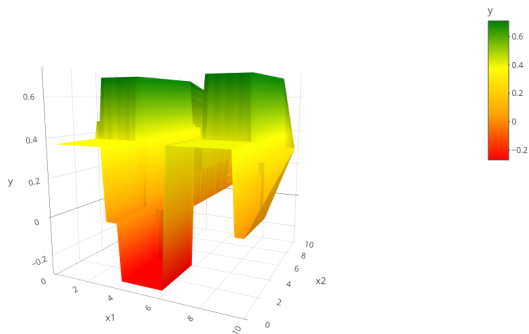






# TREE AS AN ADDITIVE MODEL

A 2D regression example:



(For binary classification with probabilities, 2D surface looks similar.)