MOTIVATION

 The graphical way of representing simple functions/models, like logistic regression. Why is that useful? × 0 0 × ×

- Because individual neurons can be used as building blocks of more complicated functions.
- Networks of neurons can represent extremely complex hypothesis spaces.
- Most importantly, it allows us to define the "right" kinds of hypothesis spaces to learn functions that are more common in our universe in a data-efficient way (see Lin, Tegmark et al. 2016).

REPRESENTATION LEARNING

 It is very critical to feed a classifier the "right" features in order for it to perform well.



- Before deep learning took off, features for tasks like machine vision and speech recognition were "hand-designed" by domain experts. This step of the machine learning pipeline is called feature engineering.
- DL automates feature engineering. This is called representation learning.

SINGLE HIDDEN LAYER NETWORKS

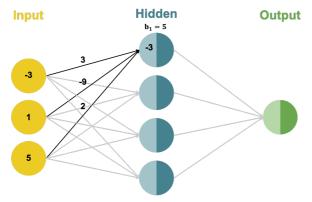
Single neurons perform a 2-step computation:

- **• Affine Transformation:** a weighted sum of inputs plus bias.
- Activation: a non-linear transformation on the weighted sum.

Single hidden layer networks consist of two layers (without input layer):

- Hidden Layer: having a set of neurons.
- Output Layer: having one or more output neurons.
- Multiple inputs are simultaneously fed to the network.
- Each neuron in the hidden layer performs a 2-step computation.
- The final output of the network is then calculated by another 2-step computation performed by the neuron in the output layer.

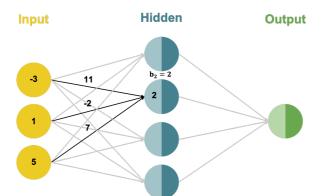




$$z_{\text{in}}^{(1)} = w_{11}x^{(1)} + w_{21}x^{(2)} + w_{31}x^{(3)} + b_1$$

 $z_{\text{in}}^{(1)} = 3*(-3) + (-9)*1 + 2*5 + 5 = -3$

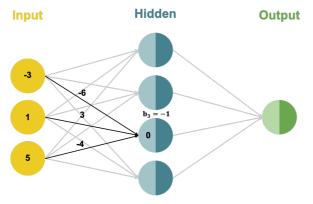




$$z_{\text{in}}^{(2)} = w_{12}x^{(1)} + w_{22}x^{(2)} + w_{32}x^{(3)} + b_2$$

 $z_{\text{in}}^{(2)} = 11 * (-3) + (-2) * 1 + 7 * 5 + 2 = 2$

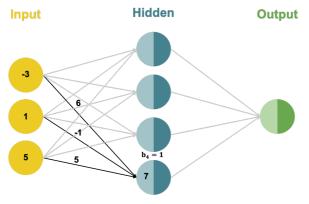




$$z_{\text{in}}^{(3)} = w_{13}x^{(1)} + w_{23}x^{(2)} + w_{33}x^{(3)} + b_3$$

$$z_{\text{in}}^{(3)} = (-6) * (-3) + 3 * 1 + (-4) * 5 - 1 = 0$$

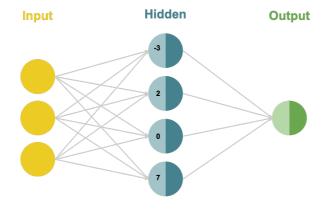




$$z_{\text{in}}^{(4)} = w_{14}x^{(1)} + w_{24}x^{(2)} + w_{34}x^{(3)} + b_4$$

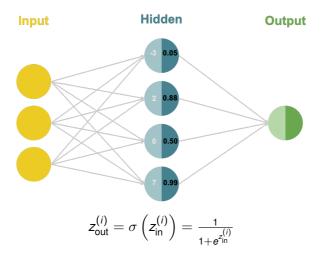
$$z_{\text{in}}^{(4)} = 6 * (-3) + (-1) * 1 + 5 * 5 + 1 = 7$$





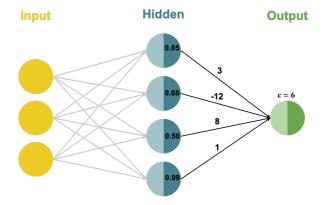


Each hidden neuron performs a non-linear **activation** transformation on the weight sum:





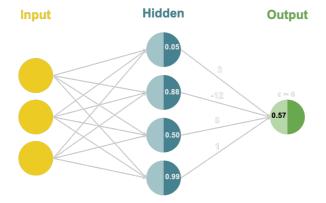
The output neuron performs an **affine transformation** on its inputs:



$$f_{\text{in}} = u_1 z_{\text{out}}^{(1)} + u_2 z_{\text{out}}^{(2)} + u_3 z_{\text{out}}^{(3)} + u_4 z_{\text{out}}^{(4)} + c$$



The output neuron performs an **affine transformation** on its inputs:

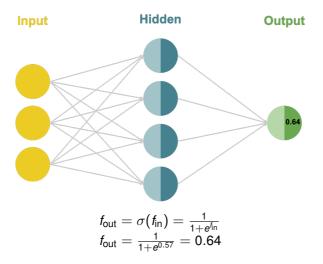


$$f_{\text{in}} = u_1 z_{\text{out}}^{(1)} + u_2 z_{\text{out}}^{(2)} + u_3 z_{\text{out}}^{(3)} + u_4 z_{\text{out}}^{(4)} + c$$

 $f_{\text{in}} = 3 * 0.05 + (-12) * 0.88 + 8 * 0.50 + 1 * 0.99 + 6 = 0.57$



The output neuron performs a non-linear **activation** transformation on the weight sum:





HIDDEN LAYER: ACTIVATION FUNCTION

- If the hidden layer does not have a non-linear activation, the network can only learn linear decision boundaries.
- A lot of different activation functions exist.



HIDDEN LAYER: ACTIVATION FUNCTION

ReLU Activation:

 Currently the most popular choice is the ReLU (rectified linear unit):

$$\sigma(v) = \max(0, v)$$

