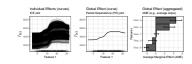
# Interpretable Machine Learning



# Feature Effects Individual Conditional Expectation (ICE) Plot



#### Learning goals

- ICE curves as local effect method
- How to sample grid points for ICE curves

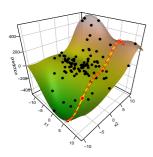
#### **MOTIVATION**

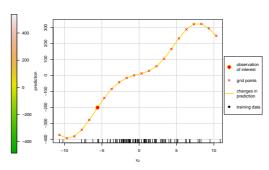
**Question:** How does varying a single feature of an observation affect its predicted outcome?

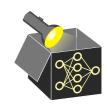
**Idea:** For a given observation, change the value of the feature of interest, and visualize how prediction changes

**Example:** On model prediction surface (left), select observation and visualize changes in prediction for different values of  $x_2$ , while keeping  $x_1$  fixed

 $\Rightarrow$  local interpretation







# INDIVIDUAL CONDITIONAL EXPECTATION (ICE)

▶ "Goldstein et. al" 2013

Partition each observation  $\mathbf{x}$  into  $\mathbf{x}_{S}$  (feature(s) of interest) and  $\mathbf{x}_{-S}$  (remaining features)

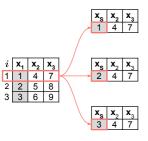


<b>~</b> →	In practice, $\mathbf{x}_S$ consists of one or two features
	(i.e., $ S  \leq 2$ and $-S = S^{\complement}$ ).

Formal definition of ICE curves:

- ullet Define grid points  $\mathbf{x}_S^* = \mathbf{x}_S^{*^{(1)}}, \dots, \mathbf{x}_S^{*^{(g)}}$  to vary  $\mathbf{x}_S$
- Plot point pairs  $\left\{ \left(\mathbf{x}_{S}^{*^{(k)}}, \hat{f}_{S,ICE}^{(i)}(\mathbf{x}_{S}^{*^{(k)}})\right) \right\}_{k=1}^{g}$  where  $\hat{f}_{S,ICE}^{(i)}(\mathbf{x}_{S}^{*}) = \hat{f}(\mathbf{x}_{S}^{*}, \mathbf{x}_{-S}^{(i)})$
- For each k connect point pairs to obtain ICE curve
- $\sim$  ICE curves visualize how prediction of *i*-th observation changes after varying its feature values indexed by S using grid points  $\mathbf{x}_s^*$  while keeping all values in -S fixed

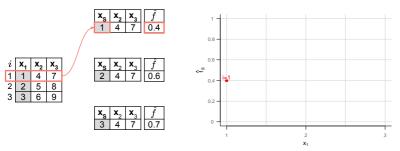


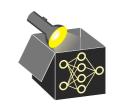




#### 1. Step - Grid points:

- Sample grid values  $\mathbf{x}_{S}^{*^{(1)}}, \dots, \mathbf{x}_{S}^{*^{(g)}}$  along possible values of feature S (|S|=1)
- For  $\mathbf{x}^{(i)} = (\mathbf{x}_S, \mathbf{x}_{-S})$ , replace  $\mathbf{x}_S$  with those grid values
- $\Rightarrow$  Creates new artificial points for *i*-th obs. (here:  $\mathbf{x}_S^* = x_1^* \in \{1, 2, 3\}$  scalar)





#### 2. Step - Predict and visualize:

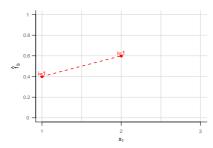
For each artificially created data point of *i*-th observation, plot prediction  $\hat{t}_{S,ICE}^{(i)}(\mathbf{x}_S^*)$  vs. grid values  $\mathbf{x}_S^*$ :

$$\hat{f}_{1,ICE}^{(i)}(x_1^*) = \hat{f}(x_1^*, \mathbf{x}_{2,3}^{(i)}) ext{ vs. } x_1^* \in \{1, 2, 3\}$$

ĺ	xs	X <sub>2</sub>	<b>X</b> <sub>3</sub>	$\hat{f}$
ĺ	1	4	7	0.4

	xs	<b>X</b> <sub>2</sub>	<b>X</b> <sub>3</sub>	$\hat{f}$
>	2	4	7	0.6

Xs	<b>X</b> <sub>2</sub>	$\mathbf{X}_3$	$\hat{f}$
3	4	7	0.7

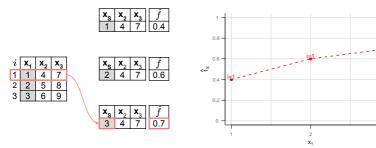




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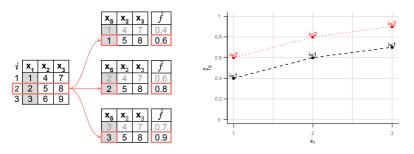




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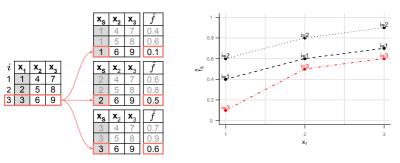
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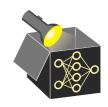




#### 3. Step - Repeat for other observations:

ICE curve for i = 2 connects all predictions at grid values associated to the i-th observation.





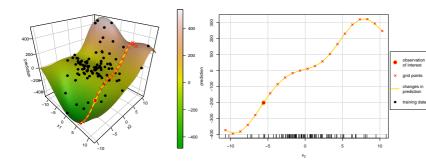
#### 3. Step - Repeat for other observations:

ICE curve for i = 3 connects all predictions at grid values associated to the i-th observation.

# **ICE CURVES - INTERPRETATION**

**Example:** Prediction surface of a model (left), select observation and visualize changes in prediction for different values of  $x_2$  while keeping  $x_1$  fixed

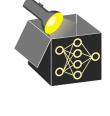
 $\Rightarrow$  local interpretation



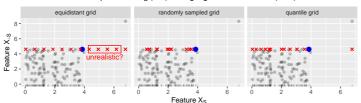


### **COMMENTS ON GRID VALUES**

- ullet Plotting ICE curves involves generating grid values  ${f x}_S^*$ ; shown on x-axis
- Three common strategies for grid definition:
  - Equidistant grid values within feature range
  - Random samples from observed feature values
  - Quantiles of observed feature values
- Marginal realism: Random and quantile grids better reflect the marginal distribution of  $x_S \Rightarrow$  reduce unrealistic values along  $x_S$

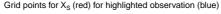


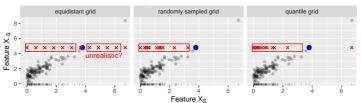
Grid points for X<sub>S</sub> (red) for highlighted observation (blue)

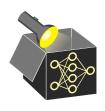


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- Marginal realism: Random and quantile grids better reflect the marginal distribution of  $x_S \Rightarrow$  reduce unrealistic values along  $x_S$
- However: For correlated features, extrapolation remains:







#### PRACTICAL CONSIDERATIONS

**Grid resolution** (instances × grid over feature of interest)

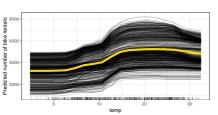
- Too coarse ⇒ may miss sharp nonlinearities or discontinuities
- Too fine ⇒ high runtime (without gaining much)
- ullet Fix: cap at pprox 50 100 grid points; vectorize predictions by feeding the model a single data frame containing all grid-modified instances

ICE curves (number of instances/curves visualized)

- Too few ⇒ hides instance variability, misses subgroup differences
- Too many ⇒ visual overload (many overlapping curves), time intensive
- Fix: Stratified or cluster-based subsample (e.g., 100); facet by subgroup

Default values for popular libraries:

Library	Grid	ICE curves
sklearn (Py)	100	1 000 (random)
PDPbox (Py)	10	num. rows
iml (R)	20	num. rows
pdp (R)	51	num. rows



ICE curves (black lines) and their point-wise average across the grid (yellow line)

