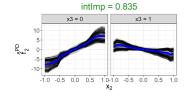
# **Interpretable Machine Learning**

# **Regional Effects**





- Interaction quantification
- REPID interaction importance

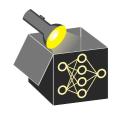


## INTERACTION QUANTIFICATION

It's helpful to know not just how another feature changes the marginal effect of  $x_S$  but how strong that interaction is and want to rank features by it.

#### Approaches:

- H-Statistics: Variance of the deviation between the joint PDP and the sum of marginal PDPs (larger variance ⇒ stronger interaction).
- **Greenwell's Interaction Index:** Difference between the variance of the PDP and the mean variance of centered ICE curves for the same feature pair.
- SHAP interaction index (  $^{\triangleright}$  Herbinger et al. (2022),  $^{\triangleright}$  Lundberg et al. 2018): Proportion of all two-way interactions with  $x_i$  to which the j-th feature contributes.



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#### Pitfalls:

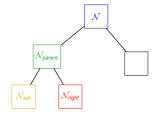
- The values of H-Statistic and the Greenwell's Interaction Index are influenced by the main effects of the two regarded features.
- SHAP interaction index does not suffer from main effect problem. However, correlation between the two features can bias the interaction value. Same applies to the H-Statistic.



On parent node level (for  $\mathcal{N}_{parent}$ ):

$$\textit{intImp}(\mathcal{N}_{\textit{parent}}) = \frac{\mathcal{R}(\mathcal{N}_{\textit{parent}}) - (\mathcal{R}(\frac{\mathcal{N}_{\textit{left}}}{\mathcal{R}(\mathcal{N})}) + \mathcal{R}(\frac{\mathcal{N}_{\textit{right}}}{\mathcal{N}}))}{\mathcal{R}(\mathcal{N})}$$

**Interpretation:** Reduction of ICE curve variance after one split of  $\mathcal{N}_{parent}$  into  $\mathcal{N}_{left}$  and  $\mathcal{N}_{right}$  relative to the ICE curve variance in the root node  $\mathcal{N}$ .

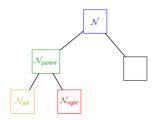


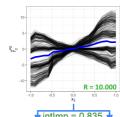


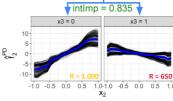
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Split reduces 83.5% of variance.



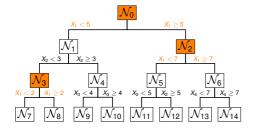
#### On feature level (for $x_i$ ):

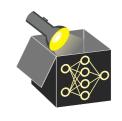
$$intImp_j = \sum_{i \in \mathcal{B}_i} intImp(\mathcal{N}_i)$$

where  $\mathcal{B}_j$  indexes parent nodes split by  $x_j$ .

**Interpretation:** Overall reduction of ICE curve variance due to splits by  $X_j$  (in %).

**Example:** For  $X_1 \Rightarrow \mathcal{B}_1 = \{0, 2, 3\}$ 





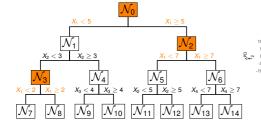
#### On feature level (for $x_i$ ):

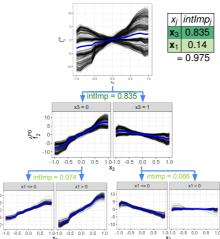
$$intImp_j = \sum_{i \in \mathcal{B}_i} intImp(\mathcal{N}_i)$$

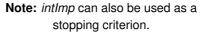
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# **OUTPERFORMING SOTA**

#### Simulation setting

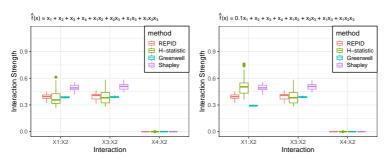
- Draw 1000 i.i.d. samples from  $X_1, \ldots, X_4 \sim \mathcal{U}(-1, 1)$
- ullet True underlying function:  $f(\mathbf{x}) = \sum_{j=1}^4 \mathbf{x}_j + \mathbf{x}_1 \mathbf{x}_2 + \mathbf{x}_2 \mathbf{x}_3 + \mathbf{x}_1 \mathbf{x}_3 + \mathbf{x}_1 \mathbf{x}_2 \mathbf{x}_3 + \epsilon$
- ullet Fit a correctly specified linear model (interactions with  ${f x}_4$  are excluded)
- ullet 30 repetitions, measure interaction strength between  ${f x}_2$  and all other 3 features

# Which methods are sensitive to changes in main effect sizes or feature correlations?



Pitfall	REPID	H-Statistic	Greenwell	SHAP
sensitive to changes of main effect	No	Yes	Yes	No
sensitive to changes of correlation be-	No	Yes	No	Yes
tween $\mathbf{x}_j$ and other features				

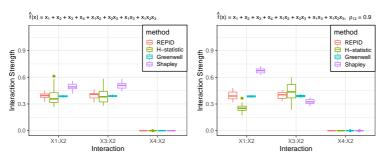
# **OUTPERFORMING SOTA**





- Left (initial setting): Interaction strength of x<sub>1</sub>:x<sub>2</sub> and x<sub>3</sub>:x<sub>2</sub> similar; x<sub>4</sub>:x<sub>2</sub> no interaction
- **Right**: Set main effect  $\beta_1 = 0.1$ 
  - Expectation: Interaction strengths should not change
  - Fail: H-statistic  $(\mathbf{x}_1:\mathbf{x}_2 > \mathbf{x}_3:\mathbf{x}_2)$  and Greenwell  $(\mathbf{x}_1:\mathbf{x}_2 < \mathbf{x}_3:\mathbf{x}_2)$

# **OUTPERFORMING SOTA**

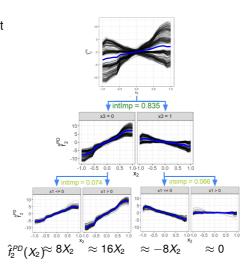




- Left (initial setting): Interaction strength of x<sub>1</sub>:x<sub>2</sub> and x<sub>3</sub>:x<sub>2</sub> similar; x<sub>4</sub>:x<sub>2</sub> no interaction
- **Right**: Increase correlation  $\rho(\mathbf{x}_1, \mathbf{x}_2) = 0.9$ 
  - Expectation: Interaction strengths should not change
  - Fail: H-statistic  $(\mathbf{x}_1:\mathbf{x}_2 < \mathbf{x}_3:\mathbf{x}_2)$  and Shapley  $(\mathbf{x}_1:\mathbf{x}_2 > \mathbf{x}_3:\mathbf{x}_2)$
- $\rightarrow\,$  REPID is the only method which always leads to correct rankings for these settings

# **LIMITATIONS OF REPID**

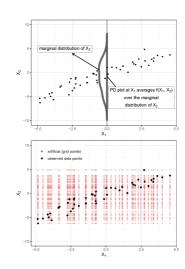
Restricted to one feature of interest
 ⇒ Different regions for different
features





# **LIMITATIONS OF REPID**

- Restricted to one feature of interest
   ⇒ Different regions for different
  features
- 2) Restricted to PD (global) and ICE (local) as feature effect methods ⇒ Inherits extrapolation problem (unlikely combinations of feature values)
- → Follow-up GADGET [under review]





## CONCLUSION

#### **Summary of Contributions (REPID):**

- Regional effects in interpretable regions
- Additive decomposition of feature effect
- Quantify feature interactions
- Outperforms SOTA interaction indices

#### **Summary of Contributions (GADGET):**

- Unique regions for multiple features
- Additive decomposition of prediction function
- Extension to ALE and Shapley Dependence
- Test to identify significant interactions
   Further Directions:

Pruning, GADGET as a predictor, comparing regions across models, efficient implementation, more efficient testing and splitting approach, . . .

