



will be similar,

1) interpret the box,

$\beta_1 \rightarrow$ slope is significant

log odds is increasing over the terms

2) Normal distribution \rightarrow recall in logistic regression, we don't independently estimate the mean and variance

- in classic OLS, we could use the t-distribution

3) don't do Cook's and leverage

overpredicting on the left and right and underpredicting in the middle.

4) Indicator Var.

$\beta_1 \rightarrow$ not sig.

$\beta_2 \rightarrow$ sig.

Attendance on zoom before step 10 was significantly lower than afterwards. All other inputs are not sig.

model 2 ↑ model 1 ↑ ↑

5) likelihood ratio test (chi-sq. dist.) Dof = Change in # param. ($4 - 2 = 2$)
 $\hookrightarrow -2 \log(L_k) \xrightarrow{d} \chi^2(2)$ (Wilkes theorem)

6) model 2 better fits the data than model 1.

7)

II

1) $\hat{\beta} = (X^T X)^{-1} X^T Y$

2) Recall Gauss-Markov.

$$E\{\varepsilon_i\} = 0$$

$$\text{Var}\{\varepsilon_i\} = \sigma^2$$

$$\text{Cov}(\varepsilon_i, \varepsilon_j) = 0$$

3) $Y - \hat{Y} = Y - X\hat{\beta} = (I - X(X^T X)^{-1} X^T)Y$

$$E\{u\} = E\{ (I - P)Y \} = (I - P) \cdot E\{Y\}$$

$$= (I - P)X\beta$$

$$= X\beta - X\beta = 0, P \cdot \beta = X\beta \text{ from (assignment)}$$

$$\text{Var}\{u\} = \text{Var}\{ (I - P)Y \} = (I - P) \text{Var}Y (I - P)^T$$

$$= (I - P) \sigma^2 I (I - P)$$

$$= \sigma^2 \cdot (I - P)^2 = \sigma^2 (I - P)$$

4) $\text{Cov}(u, \hat{\beta}) = (\text{use definitions})$

$$= \text{Cov}((I - P)Y, (X^T X)^{-1} X^T Y)$$

$$= (I - P) \text{Cov}(Y, Y) [(X^T X)^{-1} X^T]^T$$

$$= (I - P) \sigma^2 I X (X^T X)^{-1}$$

$$= \sigma^2 [X - X] (X^T X)^{-1} = 0$$

5) Note that the 1st col. in X is all 1's and $\sum g_{ii} = \sum_{i=1}^n g_{ii} = 1$

$$\begin{aligned} &= 1 \cdot \{ (1-p) Y \} \\ &= \{ 1-p \} 1 = 1-p = 0 \\ &= 0. \end{aligned}$$

VI HW Qs.

IX Confidence ellipsoid interpretation