



will be similar,

1) interpret the box,

$\beta_1 \rightarrow$  slope is significant  
log odds is increasing over the term

2) Normal distribution  $\rightarrow$  recall in logistic regression, we don't independently estimate the mean and variance

• in classic OLS, we could use the  $t$ -distribution

3) don't do Cook's and leverage

overpredicting on the left and right and underpredicting in the middle.

4) Indicator Var.

$\beta_1 \rightarrow$  not sig.

$\beta_2 \rightarrow$  sig.

Attendance on zoom before sep 10 was significantly lower than afterwards. All other inputs are not sig.

5) likelihood ratio test (chi-sq. dist.) Dof = change in # param.  $(4 - 2 = 2)$   
 $L \rightarrow -2 \log(LR) \xrightarrow{d} \chi^2(\dots)$  (Wilks theorem)

6) model 2 better fits the data than model 1.

7)

II

$$1) \hat{\beta} = (X^T X)^{-1} X^T Y$$

2) Recall Gauss Markov.

$$E[\varepsilon_i] = 0$$

$$\text{Var}(\varepsilon_i) = \sigma^2$$

$$\text{Cov}(\varepsilon_i, \varepsilon_j) = 0$$

$$3) Y - \hat{Y} = Y - X\hat{\beta} = (I - X(X^T X)^{-1} X^T) Y$$

$$E[\varepsilon] = E[(I - P)Y] = (I - P) \cdot E[Y]$$

$$= (I - P) X \beta$$

$$= X\beta - X\beta = 0, \quad P X \beta = X\beta \text{ from (assignment)}$$

$$\text{Var}[\varepsilon] = \text{Var}[(I - P)Y] = (I - P) \text{Var} Y (I - P)^T$$

$$= (I - P) \sigma^2 I (I - P)$$

$$= \sigma^2 \cdot (I - P)^2 = \sigma^2 (I - P)$$

$$4) \text{Cov}(\varepsilon, \hat{\beta}) = (\text{our definitions})$$

$$= \text{Cov}((I - P)Y, (X^T X)^{-1} X^T Y)$$

$$= (I - P) \text{Cov}(Y, Y) [X^T X]^{-1} X^T]^T$$

$$= (I - P) \sigma^2 I X (X^T X)^{-1}$$

$$= \sigma^2 [X - X] (X^T X)^{-1} = 0$$

5) Note that the 1<sup>st</sup> col. in  $X$  is all 1's and  $\sum y_i = \sum_{i=1}^n y_i$

$$= 1 \cdot \{(I - P)Y\}$$

$$= \{I - P\}1 = 1 - 1 = 0$$

$$= 0$$

VI HW Qs.

IX Confidence ellipsoid interpretation