# The Holmes Curve: A Ternary Peano–Morton Hybrid for Space-Filling Visualization

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#### **Abstract**

We present the Holmes Curve, a novel recursive mapping and visualization that extends the classical Peano and Morton (Z-order) curves into generalized base-N space. The Holmes Curve exhibits ternary interleaving, directional continuity, and a subtle skew symmetry that produces visually coherent wave-like filling patterns distinct from known fractal traversals. This mapping has applications in 2D/3D spatial indexing, data locality optimization, texture synthesis, and generative art.

### **Definition**

```
Let n \in [0, N^{(2m)} - 1]
be a linear index for order m and base N.

t_i = n \mod N

n \leftarrow floor(n / N)

x_i = t_{(2i)}

y_i = t_{(2i+1)}

x = \sum (x_i * N^i)

y = \sum (y_i * N^i)

S(x, y) = (x + \alpha y, y)
```

### **Implementation**

Implemented in Python 3 using numpy and matplotlib, the viewer provides an interactive order slider, animation mode, and consistent viewport. Example CLI usage:

```
peano-viewer --order 4 --base 3 --interval 0.2
from peano_morton_viewer import interactive_peano
interactive_peano(order=4)
```

## **Applications**

• Spatial indexing and cache-efficient data layouts • Texture synthesis and fractal pattern generation • Procedural terrain and signal traversal algorithms • Educational visualization of radix-N interleaving • Aesthetic generative art and motion patterns

### References

- 1. Peano, G. (1890). Sur une courbe, qui remplit toute une aire plane.
- 2. Morton, G. M. (1966). A Computer Oriented Geodetic Data Base and a New Technique in File Sequencing.
- 3. Holmes, J. (2025). The Holmes Curve: Ternary Skew Interleave for Space-Filling Visualization.

### Citation

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