

## Homework 2

### 1. Group / field theory

Take the set of bits  $B = \{0, 1\}$  and the operation  $\oplus$  with the following rules:

```
`0 ⊕ 0 = 0`  
`0 ⊕ 1 = 1`  
`1 ⊕ 0 = 1`  
`1 ⊕ 1 = 0`
```

Does the set  $B$  and the operation  $\oplus$  satisfy the group properties ?

### 2. Modular arithmetic - you just need to find examples, you don't need to prove anything.

1. Is it true that all odd squares are  $\equiv 1 \pmod{8}$  ?
2. what about even squares  $\pmod{8}$  ?

### 3. Try out the vanity bitcoin address example at [asecurity](#) or the Ethereum [version](#)

### 4. What do you understand by

1.  $O(n)$
2.  $O(1)$
3.  $O(\log n)$

### 5. Which of those is best when describing a proof size