

$$A = I - 2uu^T$$

$$A^T A = (I - 2uu^T)^T (I - 2uu^T)$$

$$I^T = I$$

$$A^T A$$

$$= (I - 2uu^T)(I - 2uu^T)$$

$$= I - 4uu^T + 4uu^T uu^T$$

$$= I - 4uu^T + 4u(u^T u)u^T$$

$$= I - 4uu^T + 4uu^T$$

$$= I$$

Thus, $A = I - 2uu^T$ is orthogonal.