

$$k(x, x') = ck_1(x, x') \text{ where } c > 0$$

Let Gram matrix with $k_1(x, x')$ be K_1 , which is positive semi-definite,

Gram matrix with $k(x, x')$ be K .

$$k(x, x') = ck_1(x, x') \text{ can be represented as } K = cK_1$$

since K_1 is positive semi-definite, for any nonzero vector u , $u^T K_1 u \geq 0$

$$c > 0 \rightarrow u^T cK_1 u \geq 0 \rightarrow u^T K u \geq 0$$

Thus, $k(x, x') = ck_1(x, x')$ is a valid kernel.