

# 1 Bogoliubov Tranformation for the Kondo Lattice

We start from the Hamiltonian for the Kondo lattice

$$H = - \sum_{i,\sigma} t_{ij} c_{i\sigma}^\dagger c_{j\sigma} + J \sum_r \mathbf{S}_r \cdot \mathbf{s}_r + \sum_{\langle r,s \rangle} I_{rs} \mathbf{S}_r \cdot \mathbf{S}_s$$

where  $\mathbf{S}_i, \mathbf{s}_i$  are the spin operators for the localized  $f$ -electrons and the itinerant  $d$ -electrons. Next, we use that

$$\mathbf{S}_r = \mathbf{S}_r^f + \mathbf{S}_r^b$$

representing the fermionic and bosonic components of the spin. For the fermionic component, we use

$$\begin{aligned} \mathbf{S}_r^f &= \frac{1}{2} \sum_{\alpha,\beta} f_{r,\alpha}^\dagger \sigma_{\alpha\beta} f_{r,\beta} \\ \mathbf{s}_r &= \frac{1}{2} \sum_{\alpha,\beta} c_{r,\alpha}^\dagger \sigma_{\alpha\beta} c_{r,\beta} \end{aligned}$$

We will assume that the bosonic part of the spins orders antiferromagnetically, and hence use the Holstein-Primakoff transformation on the  $A$  sublattice

$$\begin{aligned} S_r^z &= S - a_r^\dagger a_r \\ S_r^+ &= \sqrt{2S} \sqrt{1 - \frac{a_r^\dagger a_r}{2S}} a_r \\ S_r^- &= \sqrt{2S} a_r^\dagger \sqrt{1 - \frac{a_r^\dagger a_r}{2S}} \end{aligned}$$

and on the  $B$  sublattice

$$\begin{aligned} S_r^z &= -S + a_r^\dagger a_r \\ S_r^- &= \sqrt{2S} a_r^\dagger \sqrt{1 - \frac{a_r^\dagger a_r}{2S}} \\ S_r^+ &= \sqrt{2S} \sqrt{1 - \frac{a_r^\dagger a_r}{2S}} a_r \end{aligned}$$

We obtain

$$H_{MF} = \sum_k \begin{pmatrix} c_{k,\sigma}^\dagger & f_{k,\sigma}^\dagger & c_{k+Q,\sigma}^\dagger & f_{k+Q,\sigma}^\dagger \end{pmatrix} \begin{pmatrix} \varepsilon_k & -V & U_c & 0 \\ -V & \chi_k & 0 & U_f \\ U_c & 0 & \varepsilon_{k+Q} & -V \\ 0 & U_f & -V & \chi_{k+Q} \end{pmatrix} \begin{pmatrix} c_{k,\sigma} \\ f_{k,\sigma} \\ c_{k+Q,\sigma} \\ f_{k+Q,\sigma} \end{pmatrix}$$

$$\hat{H}_k = \begin{pmatrix} \varepsilon_k & -V & U_c & 0 \\ -V & \chi_k & 0 & U_f \\ U_c & 0 & \varepsilon_{k+Q} & -V \\ 0 & U_f & -V & \chi_{k+Q} \end{pmatrix}$$

Where

$$\begin{aligned} \varepsilon_k &= -2 \cdot t(\cos(k_x) + \cos(k_y)) - \mu \\ \chi_k &= -2 \cdot \chi_0(\cos(k_x) + \cos(k_y)) - \varepsilon_f \\ V &= \frac{JN}{4} \sum_{q,\alpha} \langle f_{q\alpha}^\dagger c_{q\alpha} \rangle \\ U_c &= \frac{JS}{2} \text{sgn}(\sigma) \\ U_f &= \frac{IS}{2} \text{sgn}(\sigma) \end{aligned}$$

Then the Green's function matrix is defined as

$$\hat{G}_R(k, \omega + i\delta) = [(\omega + i\delta)\hat{I} - \hat{H}_k]^{-1}$$

From which we calculate the QPI spectrum

$$g(q, \omega) = \int \frac{d^2k}{(2\pi)^2} \text{Im}[[\hat{G}_R(k, \omega)]_{11}[\hat{G}_R(k+q, \omega)]_{11}]$$