

# First to Penalty



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## 1 Template

```

1 #include "bits/stdc++.h"
2 //assert(x>0) si falla da RTE
3 using namespace std;
4 #define endl '\n'
5 #define DBG(x) cerr<<#x<< "=" << (x) << endl;
6 #define RAYA cerr<<"====="<<endl;
7 #define RAYAS cerr<<"....."<<endl;
8 // #define DBG(x) ;
9 // #define RAYA ;
10 // #define RAYAS ;
11
12 //-----SOLBEGIN-----
13 int main() {
14     ios_base::sync_with_stdio(false); cout.tie(NULL); cin.tie(NULL);
15     int tC;
16
17     cin >> tC;
18     while (tC-- > 0) {
19
20     }
21 }
22
23 //-----EOSOLUTION-----

```

## 2 Data structures

### 2.1 struct

```

1 #include "bits/stdc++.h"
2 using namespace std;
3 #define endl "\n"
4
5 struct unidad{
6     int costo;
7     int origen;
8     int destino;
9 };
10
11 bool comp(const unidad a, const unidad b){
12     if(a.costo == b.costo){
13         if(a.origen == b.origen){

```

```

14         return a.destino < b.destino;
15     }
16     return a.origen < b.origen;
17 }
18 return a.costo < b.costo;
19 }
20
21 int main()
22 {
23     ios_base::sync_with_stdio(false);cout.tie(NULL);cin.tie(NULL);
24
25     vector<unidad> arr;
26     unidad aux;
27
28     int n;
29     cin>>n;
30
31     while(n--){
32         cin>>aux.origen>>aux.destino>>aux.costo;
33         arr.push_back(aux);
34     }
35
36     sort(arr.begin(), arr.end(), comp);
37
38     for(unidad p : arr){
39         cout<<p.origen<<" " <<p.destino<<" " <<p.costo<<endl;
40     }
41
42     return 0;
43 }

```

### 2.2 segTree

```

1 #include <bits/stdc++.h>
2 using namespace std;
3 vector<long long int> elem;
4 class segmentTree{
5 public:
6     vector<long long int> sT;
7     segmentTree(long long int size);
8     long long int create(long long int left, long long int right, long
        long int indice);
9     long long int query(long long int left, long long int right, long long

```

```

10     int q_left,long long int q_right,long long int ind);
11     long long int update(long long int left,long long int right,long
12         long int val,long long int up_index,long long int indice);
13 };
14 long long int segmentTree::query(long long int left,long long int right,
15     long long int q_left,long long int q_right,long long int indice){
16     long long int neutro = 1000000001;
17     if ((q_left>right) || (q_right<left)){
18         return neutro;
19     }
20     if (left>=q_left && right<=q_right){
21         return sT[indice];
22     }
23
24     long long int mid=(right+left)/2;
25     long long int leftSon=query(left, mid, q_left, q_right, (2*indice+1));
26     long long int rightSon=query(mid+1, right, q_left, q_right, (2*indice
27         +2));
28
29     return min(leftSon, rightSon);
30     // return(leftSon+rightSon);
31 }
32 long long int segmentTree::update(long long int left,long long int right
33     ,long long int val,long long int up_index, long long int indice){
34     long long int mid=(right+left)/2;
35     if(left==right){
36         sT[indice]=val;
37         return sT[indice];
38     }
39     if((left<=up_index) && (up_index<=mid)){
40         sT[indice]=min(sT[(2*indice+2)] , update(left, mid, val, up_index,
41             (2*indice+1)));
42     }
43     else{
44         sT[indice]=min(sT[(2*indice+1)] , update(mid+1, right, val, up_index
45             , (2*indice+2)));
46     }
47     //aqui era val, pero si lo dejabas asi siempre ibas a subir val, lo

```

```

46     cual puede que te cause bugs
47     return sT[indice];
48 }
49 long long int segmentTree::create(long long int left, long long int
50     right, long long int indice ){
51     long long int mid=(right+left)/2;
52     if(left==right){
53         sT[indice]=elem[left];
54         return sT[indice];
55     }
56     long long int leftSon=create(left, mid, (2*indice+1));
57     long long int rightSon=create(mid+1, right, (2*indice+2));
58
59     sT[indice]=min(leftSon, rightSon);
60     // sT[indice]=leftSon + rightSon;
61     // return (leftSon + rightSon);
62     return min(leftSon, rightSon);
63 }
64
65 segmentTree::segmentTree(long long int size) {
66     long long int neutro = 1000000001;
67
68     long long int pot=2;
69     while(pot<size){
70         pot = pot * 2;
71     }
72     while(elem.size()<pot){
73         elem.push_back(neutro);
74     }
75
76     for(int i = 0; i<2*pot-1; i++) sT.push_back(neutro);
77
78     create(0, pot-1, 0);
79
80     // for(int x:sT){
81     //     cout<<x<<endl;
82     // }
83
84     // int res = query(0,7,0,4,0);
85     // cout<<"res: "<<res<<endl;
86 }

```

```

87
88
89 int main() {
90     long long int n,aux,q;
91
92     cin>>n>>q;
93     long long int auxn=n;
94
95     while(n){
96         cin>>aux;
97         elem.push_back(aux);
98         n--;
99     }
100
101     segmentTree st(auxn);
102
103
104     long long int l,r,v;
105     while(q--){
106         cin>>v>>l>>r;
107
108         if(v==1){
109             // r--;
110             st.update(0,elem.size()-1,r,l-1,0);
111         }else{
112             // r--;
113             cout<<st.query(0,elem.size()-1,l-1,r-1,0)<<endl;
114         }
115     }
116
117     return 0;
118 }
119

```

### 3 Graphs

#### 3.1 bfs

```

1 #include<vector>
2 #include<bitset>
3 #include<queue>
4 #include<stack>
5

```

```

6 using namespace std;
7 #define GS 400040
8
9 vector<int> graph[GS];
10 bitset <GS> vis;
11 //anchura O(V+E)
12 void dfs(int curr) {
13     queue<int> fringe;
14     fringe.push(curr);
15     while (fringe.size()) {
16         curr = fringe.front(); fringe.pop();
17         if (!vis[curr]) {
18             vis[curr] = 1;
19             for (int h : graph[curr]) fringe.push(h);
20         }
21     }
22 }

```

#### 3.2 dfs

```

1 #include<vector>
2 #include<bitset>
3 #include<queue>
4 #include<stack>
5
6 using namespace std;
7 #define GS 400040
8
9 vector<int> graph[GS];
10 bitset <GS> vis;
11 //anchura O(V+E)
12 void dfs(int curr) {
13     stack<int> fringe;
14     fringe.push(curr);
15     while (fringe.size()){
16         curr = fringe.top(); fringe.pop();
17         if (!vis[curr]) {
18             vis[curr] = 1;
19             for (int h : graph[curr]) fringe.push(h);
20         }
21     }
22 }

```

## 4 Math

### 4.1 Coeficientes binomiales. (Combinaciones n en k)

Una combinación es una forma de elegir  $k$  elementos de un grupo de tamaño  $n$ , sin importar el orden en que los eliges.

$$\binom{n}{k} = \frac{n!}{k!(n-k)!}$$

$$(a+b)^n = \sum_{k=0}^n \binom{n}{k} a^{n-k} b^k$$

$$\binom{n}{k} = \binom{n}{n-k}$$

$$\binom{n}{k} = \binom{n-1}{k} + \binom{n-1}{k-1}$$

$$k \binom{n}{k} = n \binom{n-1}{k-1}$$

$$\sum_{k=0}^n \binom{n}{k} = 2^n$$

$$\sum_{k=0}^n (-1)^k \binom{n}{k} = 0$$

$$\binom{n+m}{t} = \sum_{k=0}^t \binom{n}{k} \binom{m}{t-k}$$

$$\sum_{j=k}^n \binom{j}{k} = \binom{n+1}{k+1}$$

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### 4.2 Numeros catalanes

Los números de Catalan son una secuencia de números enteros que aparecen en varios problemas combinatorios y estructurales en matemáticas. Se utilizan para contar estructuras específicas que siguen reglas particulares, como el número de maneras de emparejar paréntesis correctamente, las maneras de dividir un polígono convexo en triángulos, o las maneras de construir árboles binarios completos.

Los números de Catalan también se aplican en la cuenta de caminos específicos, aunque no para cualquier tipo de camino. En particular, se usan para contar caminos restringidos en una cuadrícula.

Un ejemplo clásico es el conteo de caminos que van desde el punto  $(0,0)$  hasta el punto  $(n,n)$  en una cuadrícula, avanzando solo hacia la derecha o hacia abajo, pero con la condición de que el camino nunca debe cruzar la diagonal principal (es decir, que en todo momento debe estar por encima o sobre la línea  $y = x$ ). En este contexto, el número de caminos que cumplen esta restricción para una cuadrícula de tamaño  $n$  es el  $n$ -ésimo número de Catalan.

$$C_{n+1} = \sum_{i=0}^n C_i C_{n-i}$$

$$C_n = \frac{1}{n+1} \binom{2n}{n} = \binom{2n}{n} - \binom{2n}{n+1}$$

$$C_n = \frac{2(2n-1)}{n+1} C_{n-1}$$

$$C_n \approx \frac{4^n}{n^{3/2} \sqrt{\pi}}$$

### 4.3 Separadores o barras y estrellas

En combinatoria, el método de separadores (o barras y estrellas) es una técnica para contar formas de dividir  $n$  objetos idénticos en  $k$  grupos.

Imagina que tienes  $n$  caramelos idénticos y quieres repartirlos entre  $k$  niños. Para resolver esto, colocas  $k-1$  separadores entre los caramelos, dividiendo el total en  $k$  partes. Cada parte representa la cantidad de caramelos que cada niño recibe, y puede ser cero.

El número de formas de hacer esto es  $\binom{n+k-1}{k-1}$  ya que estamos eligiendo posiciones para los separadores entre los  $n+k-1$  espacios disponibles.

$$\left( \binom{n}{k} \right) = \binom{n-1}{k-1} = \binom{n+k-1}{k-1}$$

### 4.4 Permutaciones

Una permutación es una forma de elegir y organizar  $k$  elementos de un grupo de tamaño  $n$ , donde el orden sí importa. (i.e. 1,2,3 es diferente a 3,1,2)

$$P(n, k) = \frac{n!}{(n - k)!}$$

#### Permutaciones objetos repetidos

Si existen elementos iguales entre los que hay que elegir (i.e. CARTA tiene dos 'A'), definamos la cantidad que ocurre el  $i$ -esimo elemento como  $am_i$  (as in amount)-

$$P(n, k) = \frac{P(n, k)}{e_1!e_2!\dots} = \frac{n!}{(n - k)!e_1!e_2!\dots}$$

### 4.5 Derangement

Un Derangement es una permutación que no deja ningún elemento en su lugar original.

$$Derangement(n) = \begin{cases} 0 & \text{si } n = 1. \\ 1 & \text{si } n = 2. \\ (n - 1)(Derangement(n - 1) + Derangement(n - 2)) & \text{otherwise.} \end{cases}$$

$$Derangement(n) = n! \sum_{k=0}^n \frac{(-1)^k}{k!}$$

### 4.6 Numeros de Fibonacci

$$F_n = F_{n-1} + F_{n-2}$$

$$F_{2n+1} = F_n^2 + F_{n+1}^2$$

$$F_{2n} = F_{n+1}^2 - F_{n-1}^2$$

$$\sum_{i=1}^n F_i = F_{n+2} - 1$$

$$F_{n+i}F_{n+j} - F_nF_{n+i+j} = (-1)^n F_i F_j$$

### 4.7 Cantidad de divisores

Para encontrar la cantidad de divisores de un número, se usa su *factorización prima*. Supongamos que un número  $N$  se factoriza como:

$$N = p_1^{e_1} \times p_2^{e_2} \times \dots \times p_k^{e_k}$$

donde  $(p_1, p_2, \dots, p_k)$  son los factores primos distintos de  $N$ , y  $(e_1, e_2, \dots, e_k)$  son sus respectivos exponentes.

Para obtener la cantidad total de divisores de  $N$ , se toma cada exponente, se le suma uno, y luego se multiplican todos estos valores:

$$\text{Cantidad de divisores} = (e_1 + 1) \times (e_2 + 1) \times \dots \times (e_k + 1)$$

Para fines de programacion competitiva, considera que  $N$  tiene aproximadamente  $\sqrt[3]{N}$  divisores.

### 4.8 Respuesta modulo m

En programacion competitiva, es comun encontrar problemas cuya respuesta pueda exceder el limite de long long int de C++ ( $10^{18}$ ), por lo que para mantener la respuesta en un rango aceptable se pide calcularla modulo  $m$ .

Para calcular una respuesta modulo  $m$ , es necesario construir el codigo tomando en cuenta las siguientes propiedades.

$$(a + b) \% m = (a \% m + b \% m) \% m$$

$$(a - b) \% m = (a \% m - b \% m + m) \% m$$

$$(a * b) \% m = (a \% m * b \% m) \% m$$

En el caso de divisiones es necesario calcular el inverso modular del divisor, expresado por  $b^{-1}$ , esto esta codificado en modinverse.

$$(a/b) \% m = (a \% m * (b^{-1}) \% m) \% m$$

### 4.9 bits

```
1 #include <iostream>
2 #include <bitset> // For bitset representation
3
4 using namespace std;
5
6 // Function to demonstrate basic bit manipulation operations
```

```

7 void basicBitManipulation() {
8     int num = 29; // Example number: 29 in binary is 11101
9     int k = 3;    // Bit position to manipulate (0-indexed)
10
11     // AND operation
12     int andResult = num & (1 << k);
13     cout << "AND:_ " << (num & (1 << k)) << "_ (Is_k-th_bit_set?)" << (
14         andResult != 0) << ")" << endl;
15
16     // OR operation
17     int orResult = num | (1 << k);
18     cout << "OR:_ " << orResult << "_ (Set_k-th_bit)" << endl;
19
20     // XOR operation
21     int xorResult = num ^ (1 << k);
22     cout << "XOR:_ " << xorResult << "_ (Toggle_k-th_bit)" << endl;
23
24     // NOT operation
25     int notResult = ~num;
26     cout << "NOT:_ " << notResult << "_ (Invert_all_bits)" << endl;
27
28     // Left shift
29     int leftShiftResult = num << 1; // Multiply by 2
30     cout << "Left_Shift:_ " << leftShiftResult << endl;
31
32     // Right shift
33     int rightShiftResult = num >> 1; // Divide by 2
34     cout << "Right_Shift:_ " << rightShiftResult << endl;
35 }
36
37 // Function to demonstrate checking, setting, and clearing bits
38 void checkSetClearBits() {
39     int num = 29; // 11101
40     int k = 2;    // Check and manipulate the k-th bit
41
42     // Check if the k-th bit is set
43     bool isSet = (num & (1 << k)) != 0;
44     cout << "Is_k-th_bit_set?" << (isSet ? "Yes" : "No") << endl;
45
46     // Set the k-th bit
47     num = num | (1 << k);
48     cout << "Set_k-th_bit:_ " << num << endl;

```

```

49     // Clear the k-th bit
50     num = num & ~(1 << k);
51     cout << "Clear_k-th_bit:_ " << num << endl;
52
53     // Toggle the k-th bit
54     num = num ^ (1 << k);
55     cout << "Toggle_k-th_bit:_ " << num << endl;
56 }
57
58 // Function to demonstrate counting bits
59 void countBits() {
60     int num = 29; // 11101
61
62     // Count set bits
63     int count = 0;
64     for (int i = 0; i < 32; i++) {
65         count += (num >> i) & 1; // Check each bit
66     }
67     cout << "Number_of_set_bits:_ " << count << endl;
68
69     // Using bitset for representation
70     bitset<32> b(num);
71     cout << "Binary_representation:_ " << b << endl;
72 }
73
74 int main() {
75     cout << "Basic_Bit_Manipulation_Operations:" << endl;
76     basicBitManipulation();
77
78     cout << "\nChecking,_Setting,_and_Clearing_Bits:" << endl;
79     checkSetClearBits();
80
81     cout << "\nCounting_Bits:" << endl;
82     countBits();
83
84     return 0;
85 }

```

## 4.10 gcd\_lcm

```

1 #include <iostream>
2 #include <algorithm> // For std::swap
3 #include <numeric>   // For std::gcd (C++17)

```

```

4
5 using namespace std;
6
7 // Function to count the number of trailing zeroes in the binary
  representation of n
8 unsigned long long int trailing_zeroes(unsigned long long int n) {
9     unsigned long long int bits = 0;
10    while (n && (n & 1) == 0) {
11        ++bits;
12        n >>= 1;
13    }
14    return bits;
15 }
16
17 // Efficient GCD calculation using the Euclidean algorithm
18 unsigned long long int gcd(unsigned long long int a, unsigned long long
  int b) {
19     if (a == 0 || b == 0) {
20         return a | b; // Return non-zero value
21     }
22
23     unsigned long long int shift = trailing_zeroes(a | b);
24     a >>= trailing_zeroes(a); // Remove factors of 2 from a
25
26     do {
27         b >>= trailing_zeroes(b); // Remove factors of 2 from b
28         if (a > b) {
29             swap(a, b);
30         }
31         b -= a; // Subtract a from b
32     } while (b != 0);
33
34     return a << shift; // Restore factors of 2
35 }
36
37 // LCM calculation using GCD
38 unsigned long long int lcm(unsigned long long int a, unsigned long long
  int b) {
39     if (a == 0 && b == 0) {
40         return 0; // LCM of 0 and 0 is undefined
41     }
42     return (a / gcd(a, b)) * b; // Calculate LCM
43 }

```

```

44
45 // Function to count the number of integers less than a that are coprime
  to a
46 unsigned long long int countCoprimes(unsigned long long int a) {
47     unsigned long long int count = 0;
48     for (unsigned long long int i = 1; i < a; i++) {
49         if (gcd(i, a) == 1) {
50             count++;
51         }
52     }
53     return count;
54 }
55
56 int main() {
57     unsigned long long int a;
58     cin >> a;
59
60     while (a != 0) {
61         unsigned long long int coprimeCount = countCoprimes(a);
62         cout << coprimeCount << endl;
63         cin >> a;
64     }
65
66     return 0;
67 }

```

#### 4.11 min\_sum\_sq

```

1 #include <iostream> // For input and output
2 #include <vector>    // For using the vector container
3 #include <cmath>     // For the sqrt function
4 #include <limits>    // For std::numeric_limits
5
6 using namespace std;
7
8 // Vector to store results of subproblems
9 vector<int> vec(60000, -1);
10
11 // Recursive function to find the minimum number of perfect squares that
  sum up to 'num'
12 int recurF(int num, int cont) {
13     // Variable to store the result; initialized to a large value
14     int res = numeric_limits<int>::max(); // Use a large value to find

```



```

15     the minimum
16
17 // Base case: if num is 1, we need one square (1^2)
18 if (num == 1) return cont + 1;
19
20 // Base case: if num is 0, we don't need any squares
21 if (num == 0) return cont;
22
23 // Calculate the integer square root of num
24 int sq = (int)sqrt(num);
25
26 // If num is a perfect square, we can return the count of squares
27 // used + 1
28 if (num == sq * sq) return cont + 1;
29
30 // Increment count for the current square we're considering
31 cont++;
32
33 // Iterate over all perfect squares less than or equal to num
34 for (int i = sq; i > 0; i--) {
35     // Check if the result for the subproblem (num - i*i) is already
36     // computed
37     if (vec[num - i * i] != -1) {
38         // If it is, use the stored result to update res
39         res = min(res, vec[num - i * i] + cont);
40     } else {
41         // Otherwise, compute the result recursively
42         int ans = recurF(num - i * i, cont);
43         // Update res with the minimum value found
44         res = min(res, ans);
45         // Store the computed result for the subproblem
46         vec[num - i * i] = ans - cont; // Store only the difference
47     }
48 }
49
50 return res; // Return the minimum count of perfect squares
51 }
52
53 int main() {
54     int m; // Variable to hold the input number
55     cout << "Enter a number: ";
56     cin >> m; // Read the input number
57
58 }

```

```

55 // Call the recursive function and output the result
56 cout << "Minimum number of perfect squares for " << m << " is: " <<
57     recurF(m, 0) << endl;
58
59 return 0; // Indicate successful completion of the program
60 }

```

## 4.12 mod

```

1 #include <iostream>
2 #include <vector>
3 #include <numeric> // For std::accumulate
4 #include <cmath>    // For std::pow
5
6 using namespace std;
7
8 const long long MOD = 1000000007;
9
10 // Function to perform modular addition
11 long long sumaMOD(long long a, long long b) {
12     return (a + b) % MOD;
13 }
14
15 // Function to perform modular multiplication
16 long long multMOD(long long a, long long b) {
17     return (a * b) % MOD;
18 }
19
20 // Function to perform modular subtraction
21 long long restaMOD(long long a, long long b) {
22     return ((a - b) % MOD + MOD) % MOD;
23 }
24
25 // Function to perform modular division
26 long long divMOD(long long a, long long b) {
27     // Fermat's Little Theorem for finding modular inverse
28     // Since MOD is prime, use pow for the modular inverse
29     return multMOD(a, static_cast<long long>(pow(b, MOD - 2)));
30 }
31
32 int main() {
33     int n;
34     cin >> n;

```

```

35
36     long long answer = 1;
37
38     // Calculate factorial using modular multiplication
39     for (int i = 2; i <= n; i++) {
40         answer = multMOD(answer, i);
41     }
42
43     // Count the number of trailing zeros
44     int cont = 0;
45     while (answer % 10 == 0) {
46         answer /= 10;
47         cont++;
48     }
49
50     cout << cont << endl;
51     return 0;
52 }

```

#### 4.13 perm\_comb

```

1 #include <iostream>
2
3 // Function to calculate factorial
4 long long factorial(int n) {
5     long long result = 1;
6     for (int i = 1; i <= n; i++) {
7         result *= i;
8     }
9     return result;
10 }
11
12 // Function to calculate permutations P(n, r)
13 long long permutation(int n, int r) {
14     return factorial(n) / factorial(n - r);
15 }
16
17 // Function to calculate combinations C(n, r)
18 long long combination(int n, int r) {
19     return factorial(n) / (factorial(r) * factorial(n - r));
20 }
21
22 int main() {

```

```

23     int n = 5;
24     int r = 3;
25     std::cout << "P(" << n << ", " << r << ") = " << permutation(n, r)
26         << std::endl;
27     std::cout << "C(" << n << ", " << r << ") = " << combination(n, r)
28         << std::endl;
29     return 0;
30 }

```

## 5 Geometry

## 6 Strings

### 6.1 Common

```

1 #include <iostream>
2 #include <string>
3 #include <algorithm> // For sort, reverse, etc. // For next_permutation
4 #include <sstream>    // For stringstream (to convert between string and
5                       // int)
6 #include <vector>     // For splitting a string
7 #include <cctype>     // For isdigit()
8
9 using namespace std;
10
11 // Convert string to integer
12 int stringToInt(const string& str) {
13     return stoi(str); // stoi - string to integer
14 }
15
16 // Convert integer to string
17 string intToString(int num) {
18     return to_string(num); // to_string - integer to string
19 }
20
21 // Convert char to integer (ASCII value)
22 int charToInt(char ch) {
23     return ch - '0'; // Convert character to digit
24 }
25
26 // Convert integer to char
27 char intToChar(int num) {
28     return num + '0'; // Convert digit to character
29 }

```

```
28 }
29
30 // Sort a string
31 string sortString(string str) {
32     sort(str.begin(), str.end());
33     return str;
34 }
35
36 // Reverse a string
37 string reverseString(string str) {
38     reverse(str.begin(), str.end());
39     return str;
40 }
41
42 // Search a substring in a string
43 bool searchString(const string& str, const string& sub) {
44     return str.find(sub) != string::npos; // npos means not found
45 }
46
47 // Split a string by a delimiter
48 vector<string> splitString(const string& str, char delimiter) {
49     vector<string> tokens;
50     string token;
51     stringstream ss(str); // Use stringstream to tokenize
52
53     while (getline(ss, token, delimiter)) {
54         tokens.push_back(token);
55     }
56     return tokens;
57 }
58
59 // Check if a string contains only digits
60 bool isNumeric(const string& str) {
61     return all_of(str.begin(), str.end(), ::isdigit);
62 }
63
64 bool hasPrefix(const string& str, const string& prefix) {
65     if (str.size() < prefix.size()) {
66         return false;
67     }
68     return str.compare(0, prefix.size(), prefix) == 0;
69 }
70
```

```
71 bool hasSuffix(const string& str, const string& suffix) {
72     if (str.size() < suffix.size()) {
73         return false;
74     }
75     return str.compare(str.size() - suffix.size(), suffix.size(), suffix
76 ) == 0;
77 }
78 // O(m x n), KMT is O(m + n)
79 vector<int> findAllOccurrences(const string& str, const string& sub) {
80     vector<int> positions;
81     size_t pos = str.find(sub);
82     while (pos != string::npos) {
83         positions.push_back(pos);
84         pos = str.find(sub, pos + 1); // Search from the next position
85     }
86     return positions;
87 }
88
89 vector<int> countCharFrequency(const string& str) {
90     vector<int> freq(256, 0); // For all ASCII characters
91     for (char ch : str) {
92         freq[ch]++;
93     }
94     return freq;
95 }
96
97 void generateSubsets(const string& str) {
98     int n = str.size();
99     for (int i = 0; i < (1 << n); ++i) { // 2^n possible subsets
100         string subset = "";
101         for (int j = 0; j < n; ++j) {
102             if (i & (1 << j)) {
103                 subset += str[j];
104             }
105         }
106         cout << subset << endl;
107     }
108 }
109
110 bool isPalindrome(const string& str) {
111     int n = str.size();
112     for (int i = 0; i < n / 2; ++i) {
```

```

113     if (str[i] != str[n - i - 1]) {
114         return false;
115     }
116 }
117 return true;
118 }
119
120 //
121 =====
122 string longestCommonPrefix(vector<string>& strs) {
123     if (strs.empty()) return "";
124
125     string prefix = strs[0];
126     for (int i = 1; i < strs.size(); ++i) {
127         while (strs[i].find(prefix) != 0) {
128             prefix = prefix.substr(0, prefix.size() - 1); // Reduce the
129                 prefix
130             if (prefix.empty()) return "";
131         }
132     }
133     return prefix;
134 }
135
136 int main() {
137     string str = "hello_world";
138     str.erase(0, 6); // Removes the first 6 characters, str becomes "
139         world"
140
141     string str = "hello_world";
142     str.replace(0, 5, "hi"); // Replaces "hello" with "hi", resulting
143         in "hi world"
144
145     string str = "abc";
146     sort(str.begin(), str.end()); // Sort to start with the
147         lexicographically smallest permutation
148     do {
149         cout << str << endl;
150     } while (next_permutation(str.begin(), str.end()));
151 // =====
152 // String to integer and vice versa

```

```

150 string strNum = "12345";
151 int num = stringToInt(strNum);
152 cout << "String_to_integer:_ " << num << endl;
153
154 string strFromInt = intToString(num);
155 cout << "Integer_to_string:_ " << strFromInt << endl;
156
157 // Char to integer and vice versa
158 char ch = '7';
159 int chToInt = charToInt(ch);
160 cout << "Char_to_integer:_ " << chToInt << endl;
161
162 char intToCh = intToChar(9);
163 cout << "Integer_to_char:_ " << intToCh << endl;
164
165 // Sorting a string
166 string unsorted = "dcba";
167 string sorted = sortString(unsorted);
168 cout << "Sorted_string:_ " << sorted << endl;
169
170 // Reversing a string
171 string original = "hello";
172 string reversed = reverseString(original);
173 cout << "Reversed_string:_ " << reversed << endl;
174
175 // Searching a substring
176 string mainString = "C++_string_manipulation";
177 string subString = "string";
178 bool found = searchString(mainString, subString);
179 cout << "Substring_found:_ " << (found ? "Yes" : "No") << endl;
180
181 // Splitting a string
182 string sentence = "C++_is_awesome!";
183 vector<string> words = splitString(sentence, '_');
184 cout << "Splitting_sentence:_ ";
185 for (size_t i = 0; i < words.size(); ++i) {
186     cout << words[i] << " ";
187 }
188 cout << endl;
189
190 // Checking if a string is numeric
191 string numericStr = "123456";
192 cout << "Is_the_string_numeric?_" << (isNumeric(numericStr) ? "Yes"

```

```

193         : "No") << endl;
194     return 0;
195 }

```

## 6.2 KMP

```

1  #include <iostream>
2  #include <string>
3  #include <algorithm> // For sort, reverse, etc. // For next_permutation
4  #include <sstream>    // For stringstream (to convert between string and
5                          int)
6  #include <vector>     // For splitting a string
7  #include <cctype>     // For isdigit()
8
9  using namespace std;
10
11 void computeLPSArray(const string& pattern, vector<int>& lps) {
12     int M = pattern.size();
13     int length = 0; // length of the previous longest prefix suffix
14     lps[0] = 0;    // LPS[0] is always 0
15     int i = 1;     // i starts from 1 since lps[0] is already known
16
17     while (i < M) {
18         if (pattern[i] == pattern[length]) {
19             length++;
20             lps[i] = length;
21             i++;
22         } else { // (pattern[i] != pattern[length])
23             if (length != 0) {
24                 length = lps[length - 1];
25                 // do not increment i here
26             } else {
27                 lps[i] = 0;
28                 i++;
29             }
30         }
31     }
32
33 void KMPSearch(const string& text, const string& pattern) {
34     int N = text.size();
35     int M = pattern.size();

```

```

36
37 // Create the LPS table
38 vector<int> lps(M);
39 computeLPSArray(pattern, lps);
40
41 int i = 0; // index for text[]
42 int j = 0; // index for pattern[]
43
44 while (i < N) {
45     if (text[i] == pattern[j]) {
46         i++;
47         j++;
48     }
49
50     // A match is found
51     if (j == M) {
52         cout << "Pattern found at index " << i - j << endl;
53         j = lps[j - 1]; // Prepare for the next match, using LPS
54     }
55
56     // Mismatch after j matches
57     else if (i < N && text[i] != pattern[j]) {
58         // Don't match lps[0..lps[j-1]] characters, they will match
59         // anyway
60         if (j != 0) {
61             j = lps[j - 1]; // Fall back using LPS
62         } else {
63             i++; // Move to the next character in the text
64         }
65     }
66 }

```

## 7 Flow

## 8 Miscellaneous

### 8.1 Backtracking

```

1  #include <iostream>
2  #include <vector>
3  using namespace std;
4

```

```

5 bool isSafe(vector<vector<int>>& board, int row, int col, int N) {
6     for (int i = 0; i < row; i++) {
7         if (board[i][col] == 1) {
8             return false;
9         }
10    }
11
12    for (int i = row, j = col; i >= 0 && j >= 0; i--, j--) {
13        if (board[i][j] == 1) {
14            return false;
15        }
16    }
17
18    for (int i = row, j = col; i >= 0 && j < N; i--, j++) {
19        if (board[i][j] == 1) {
20            return false;
21        }
22    }
23
24    return true;
25 }
26
27 bool solveNQueensUtil(vector<vector<int>>& board, int row, int N) {
28     if (row == N) {
29         return true;
30     }
31
32     for (int col = 0; col < N; col++) {
33         if (isSafe(board, row, col, N)) {
34             board[row][col] = 1;
35
36             if (solveNQueensUtil(board, row + 1, N)) {
37                 return true;
38             }
39
40             board[row][col] = 0;
41         }
42     }
43
44     return false;
45 }
46
47 void printBoard(vector<vector<int>>& board, int N) {

```

```

48     for (int i = 0; i < N; i++) {
49         for (int j = 0; j < N; j++) {
50             if (board[i][j] == 1) {
51                 cout << "Q_";
52             } else {
53                 cout << "_.";
54             }
55         }
56         cout << endl;
57     }
58 }
59
60 void solveNQueens(int N) {
61     vector<vector<int>> board(N, vector<int>(N, 0));
62
63     if (solveNQueensUtil(board, 0, N)) {
64         printBoard(board, N);
65     } else {
66         cout << "No_solution_exists_for_" << N << "_queens." << endl;
67     }
68 }
69
70 int main() {
71     int N;
72     cout << "Enter_the_value_of_N_(for_NxN_board):_";
73     cin >> N;
74
75     solveNQueens(N);
76
77     return 0;
78 }

```

## 8.2 Binary Search

```

1 #include <iostream>
2 #include <vector>
3
4 using namespace std;
5
6 int binarySearch(const vector<int>& arr, int target) {
7     int left = 0;
8     int right = arr.size() - 1;
9

```

```

10 while (left <= right) {
11     int mid = left + (right - left) / 2;
12
13     if (arr[mid] == target) {
14         return mid;
15     }
16     if (arr[mid] < target) {
17         left = mid + 1;
18     }
19     else {
20         right = mid - 1;
21     }
22 }
23 return -1;
24 }
25
26 int firstOccurrence(const vector<int>& arr, int target) {
27     int left = 0, right = arr.size() - 1, result = -1;
28
29     while (left <= right) {
30         int mid = left + (right - left) / 2;
31
32         if (arr[mid] == target) {
33             result = mid;
34             right = mid - 1;
35         } else if (arr[mid] < target) {
36             left = mid + 1;
37         } else {
38             right = mid - 1;
39         }
40     }
41     return result;
42 }
43
44 int lastOccurrence(const vector<int>& arr, int target) {
45     int left = 0, right = arr.size() - 1, result = -1;
46
47     while (left <= right) {
48         int mid = left + (right - left) / 2;
49
50         if (arr[mid] == target) {
51             result = mid;    // Save result
52             left = mid + 1;  // Search in the right half for last

```

```

53         occurrence
54     } else if (arr[mid] < target) {
55         left = mid + 1;
56     } else {
57         right = mid - 1;
58     }
59     return result;
60 }

```

### 8.3 Dijkstra

```

1  #include <iostream>
2  #include <vector>
3  #include <queue>
4  #include <utility> // for std::pair
5  #include <limits>  // for std::numeric_limits
6
7  using namespace std;
8
9  const int INF = numeric_limits<int>::max(); // Represents infinity
10
11 // Dijkstra's algorithm function
12 void dijkstra(int start, const vector<vector<pair<int, int>>>& graph) {
13     int n = graph.size(); // Number of nodes in the graph
14
15     // Distance vector to store the shortest distance from the start
16     // node
17     vector<int> distance(n, INF);
18     distance[start] = 0;
19
20     // Priority queue to process nodes (min-heap), stores pairs {
21     // distance, node}
22     priority_queue<pair<int, int>, vector<pair<int, int>>, greater<>> pq;
23
24     pq.push({0, start}); // Distance to start node is 0
25
26     while (!pq.empty()) {
27         int dist = pq.top().first; // Current distance
28         int node = pq.top().second; // Current node
29         pq.pop();
30
31         // If this distance is already greater than the stored distance,

```

```

        skip
        if (dist > distance[node]) continue;

        // Explore neighbors
        for (const auto& neighbor : graph[node]) {
            int nextNode = neighbor.first;
            int weight = neighbor.second;

            // If a shorter path to nextNode is found
            if (distance[node] + weight < distance[nextNode]) {
                distance[nextNode] = distance[node] + weight;
                pq.push({distance[nextNode], nextNode});
            }
        }
    }

    // Print the shortest distances from the start node
    cout << "Shortest distances from node " << start << ":\n";
    for (int i = 0; i < n; ++i) {
        if (distance[i] == INF)
            cout << "Node " << i << ": INF (unreachable)\n";
        else
            cout << "Node " << i << ": " << distance[i] << "\n";
    }
}

int main() {
    // Number of nodes (0-indexed graph)
    int n = 5;

    // Graph represented as an adjacency list
    // graph[node] = vector of {neighbor, weight}
    vector<vector<pair<int, int>>> graph(n);

    // Adding edges to the graph
    // Example graph (directed, weighted edges):
    graph[0].push_back({1, 10}); // Edge from 0 to 1 with weight 10
    graph[0].push_back({4, 5});  // Edge from 0 to 4 with weight 5
    graph[1].push_back({2, 1});   // Edge from 1 to 2 with weight 1
    graph[1].push_back({4, 2});   // Edge from 1 to 4 with weight 2
    graph[2].push_back({3, 4});   // Edge from 2 to 3 with weight 4
    graph[3].push_back({0, 7});   // Edge from 3 to 0 with weight 7
    graph[3].push_back({2, 6});   // Edge from 3 to 2 with weight 6

```

```

graph[4].push_back({1, 3}); // Edge from 4 to 1 with weight 3
graph[4].push_back({2, 9}); // Edge from 4 to 2 with weight 9
graph[4].push_back({3, 2}); // Edge from 4 to 3 with weight 2

int startNode = 0; // Starting node for Dijkstra's algorithm

// Run Dijkstra's algorithm from the start node
dijkstra(startNode, graph);

return 0;
}

```

## 8.4 knapsack

```

1 #include <iostream>
2 #include <vector>
3 using namespace std;
4
5 int knapsackDP(int W, vector<int>& weights, vector<int>& values, int n)
6 {
7     vector<vector<int>>> dp(n + 1, vector<int>(W + 1, 0));
8
9     for (int i = 1; i <= n; ++i) {
10         for (int w = 0; w <= W; ++w) {
11             if (weights[i - 1] <= w) {
12                 dp[i][w] = max(dp[i - 1][w], values[i - 1] + dp[i - 1][w]
13                     - weights[i - 1]);
14             } else {
15                 dp[i][w] = dp[i - 1][w];
16             }
17         }
18     }
19
20     return dp[n][W];
21 }
22
23 int main() {
24     vector<int> values = {60, 100, 120};
25     vector<int> weights = {10, 20, 30};
26     int W = 50;
27     int n = values.size();
28
29     cout << "Maximum value in knapsack = " << knapsackDP(W, weights,

```



```

        values, n) << endl;
28
    return 0;
29
30 }

```

## 8.5 laberinto

```

1 #include <bits/stdc++.h>
2 using namespace std;
3 #define max 1002
4
5 char mapa[max][max];
6 bool visited[max][max];
7 queue<pair<pair<int, int>, int>> adj;
8 char fatherMove[max][max];
9 int nivel = 0;
10 string mov="";
11
12 int addEdge(int r, int c, int maxR, int maxC, int nivel){
13     if (mapa[r][c]=='B'){
14         return 1;
15     }
16     if(visited[r][c]) return 0;
17     if(0<=r+1 && r+1<maxR && !visited[r+1][c]){
18         adj.push({{r+1, c}, nivel + 1});
19         fatherMove[r+1][c]='D';
20     }
21     if(0<=r-1 && r-1<maxR && !visited[r-1][c]){
22         adj.push({{r-1, c}, nivel + 1});
23         fatherMove[r-1][c]='U';
24     }
25     if(0<=c+1 && c+1<maxC && !visited[r][c+1]){
26         adj.push({{r, c+1}, nivel + 1});
27         fatherMove[r][c+1]='R';
28     }
29     if(0<=c-1 && c-1<maxC && !visited[r][c-1]){
30         adj.push({{r, c-1}, nivel + 1});
31         fatherMove[r][c-1]='L';
32     }
33     return 0;
34 }
35
36 void moves(int r, int c){

```

```

37     if (mapa[r][c] == 'A'){
38         return;
39     }
40     mov += fatherMove[r][c];
41
42     if(fatherMove[r][c] == 'U'){
43         moves(r+1, c);
44     }
45     else if(fatherMove[r][c] == 'D'){
46         moves(r-1, c);
47     }
48     else if(fatherMove[r][c] == 'R'){
49         moves(r, c-1);
50     }
51     else if(fatherMove[r][c] == 'L'){
52         moves(r, c+1);
53     }
54 }
55
56 int main(){
57     int row;
58     int col;
59     cin>>row>>col;
60
61     for(int i=0 ; i<row ; i++){
62         for(int j=0 ; j<col ; j++){
63             cin>>mapa[i][j];
64             if(mapa[i][j]=='#') visited[i][j]=true;
65             else visited[i][j]=false;
66             fatherMove[i][j]='X';
67         }
68     }
69
70     for(int i=0 ; i<row ; i++){
71         for(int j=0 ; j<col ; j++){
72             if (mapa[i][j]=='A'){
73                 adj.push({{i,j}, 0});
74                 while(adj.size() != 0){
75                     int topR=adj.front().first.first;
76                     int topC=adj.front().first.second;
77                     int level=adj.front().second;
78                     adj.pop();
79                     if (addEdge(topR, topC, row, col, level)==1){

```

```

80         moves(topR, topC);
81         cout<<"YES"<<endl;
82         cout<<level<<endl;
83         reverse(mov.begin(),mov.end());
84         cout<<mov;
85         return 0;
86     }
87     visited[topR][topC]=true;
88 }
89 cout<<"NO";
90 return 0;
91 }
92 }
93 }
94 }
95 }
    
```

## 8.6 lcs

```

1  #include <iostream>
2  #include <vector>
3  #include <string>
4  using namespace std;
5
6  string printLCS(string X, string Y) {
7      int m = X.length();
8      int n = Y.length();
9
10     vector<vector<int>> dp(m + 1, vector<int>(n + 1, 0));
11
12     for (int i = 1; i <= m; i++) {
13         for (int j = 1; j <= n; j++) {
14             if (X[i - 1] == Y[j - 1]) {
15                 dp[i][j] = dp[i - 1][j - 1] + 1;
16             } else {
17                 dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
18             }
19         }
20     }
21
22     string lcs = "";
23     int i = m, j = n;
24     while (i > 0 && j > 0) {
    
```

```

25         if (X[i - 1] == Y[j - 1]) {
26             lcs = X[i - 1] + lcs;
27             i--;
28             j--;
29         } else if (dp[i - 1][j] > dp[i][j - 1]) {
30             i--;
31         } else {
32             j--;
33         }
34     }
35
36     return lcs;
37 }
38
39 int main() {
40     string X = "ABCBADAB";
41     string Y = "BDCAB";
42
43     cout << "LCS:␣" << printLCS(X, Y) << endl;
44
45     return 0;
46 }
    
```

## 8.7 most\_data\_structures

```

1  #include <iostream>
2  #include <vector>
3  #include <deque>
4  #include <map>
5  #include <set>
6  #include <unordered_map>
7  #include <stack>
8  #include <queue>
9  #include <algorithm> // for std::binary_search // for std::sort // for
    lower_bound and upper_bound
10
11 using namespace std;
12
13 int main() {
14     // 1. Vector - dynamic array with additional methods
15     vector<int> v = {5, 1, 3, 8, 6};
16
17     sort(v.begin(), v.end()); // Sorting vector in ascending order
    
```

```

18  cout << "Sorted_vector: ";
19  for (int x : v) cout << x << " "; // Output: 1 3 5 6 8
20  cout << endl;
21
22  v.push_back(10); // Adding an element at the end
23  v.pop_back();    // Removing the last element (10)
24  v.erase(v.begin()); // Erasing the first element (1)
25  v.size();
26  v.front(); //return first element
27  v.back();  //return last element
28  cout << "Vector_after_pop_back_and_erase: ";
29  for (int x : v) cout << x << " "; // Output: 3 5 6 8
30  cout << endl;
31
32  const int value_to_find = 4;
33  bool found = binary_search(v.begin(), v.end(), value_to_find);
34  if (found) {
35      cout << value_to_find << " is present in the sorted vector." <<
          endl;
36  } else {
37      cout << value_to_find << " is not present in the sorted vector."
          << endl;
38  }
39
40  int value = 30;
41  // Find the first element >= value
42  vector<int>::iterator lower = lower_bound(v.begin(), v.end(), value)
    ;
43  if (lower != v.end())
44      cout << "Lower bound of " << value << " is at position: " << (
          lower - v.begin()) << endl;
45
46  // Find the first element > value
47  vector<int>::iterator upper = upper_bound(v.begin(), v.end(), value)
    ;
48  if (upper != v.end())
49      cout << "Upper bound of " << value << " is at position: " << (
          upper - v.begin()) << endl;
50
51  //
    =====

```

52

```

53  // 2. Deque - double-ended queue with more operations
54  deque<int> d = {10, 20, 30};
55  d.push_front(5); // Adding element at the front
56  d.push_back(40); // Adding element at the back
57
58  d.pop_front(); // Removing element from the front
59  d.pop_back();  // Removing element from the back
60  d.size();
61
62  cout << "Deque_after_pop_front_and_pop_back: ";
63  for (int x : d) cout << x << " "; // Output: 20 30
64  cout << endl;
65
66  //
    =====
67
68  // 3. Map - ordered key-value pairs
69  map<string, int> mp;
70  mp["apple"] = 3;
71  mp["banana"] = 5;
72  mp["orange"] = 2;
73
74  map<string, int>::iterator it = mp.find("banana"); // Finding a key
          in the map
75  if (it != mp.end()) {
76      cout << "Found banana, value is " << it->second << endl; //
          Output: 5
77      mp.erase(it); // Erase key-value pair for "banana"
78  }
79
80  cout << "Map_after_erasing 'banana':" << endl;
81  for (pair<string, int> p : mp) {
82      cout << p.first << ": " << p.second << endl; // Output: apple:
          3, orange: 2
83  }
84
85  // sort by val
86  // Vector to store pairs of the map
87  vector<pair<string, int>> vec(mp.begin(), mp.end());
88
89  // Sorting the vector based on the values of the map
90  sort(vec.begin(), vec.end(), [](const pair<string, int>& a, const

```

```

91     pair<string, int>& b) {
92         return a.second < b.second; // Compare based on the value (
93             second element of pair)
94     });
95
96     //
97     =====
98
99     // 4. Set - unique sorted elements with additional operations
100     set<int> s = {4, 1, 9, 1, 3}; // Duplicates are ignored
101
102     s.insert(2); // Insert element
103     s.erase(4); // Erase element 4
104     s.size();
105
106     if (s.find(2) != s.end()) { // Finding an element
107         cout << "2 is in the set" << endl; // Output: 2 is in the set
108     }
109
110     cout << "Set elements after insert and erase:";
111     for (int x : s) cout << x << " "; // Output: 1 2 3 9
112     cout << endl;
113
114     multiset<int> ms = {4, 1, 9, 1, 3}; // Duplicates are present
115
116     ms.insert(2); // Insert element
117     ms.erase(4); // Erase element 4
118     ms.count(4); // times in multiset
119     ms.size();
120
121     if (ms.find(2) != ms.end()) { // Finding an element
122         cout << "2 is in the set" << endl; // Output: 2 is in the set
123     }
124
125     int multiset_value = 30;
126     // lower_bound: finds the first element >= value
127     multiset<int>::iterator ms_lower = s.lower_bound(multiset_value);
128     if (ms_lower != s.end())
129         cout << "Lower bound of " << multiset_value << " is: " << *
130             ms_lower << endl;
131
132     // upper_bound: finds the first element > value

```

```

129     multiset<int>::iterator ms_upper = s.upper_bound(multiset_value);
130     if (ms_upper != s.end())
131         cout << "Upper bound of " << multiset_value << " is: " << *
132             ms_upper << endl;
133
134     //
135     =====
136
137     // 5. Unordered_map - hash table based key-value pairs
138     unordered_map<string, int> um;
139     um["cat"] = 1;
140     um["dog"] = 2;
141     um["bird"] = 3;
142
143     um.erase("dog"); // Erasing key-value pair for "dog"
144
145     cout << "Unordered_map after erasing 'dog':" << endl;
146     for (unordered_map<string, int>::iterator p = um.begin(); p != um.
147         end(); ++p) {
148         cout << p->first << ": " << p->second << endl; // Output: cat:
149             1, bird: 3
150     }
151
152     //
153     =====
154
155     // 6. Stack - LIFO structure with additional methods
156     stack<int> st;
157     st.push(10);
158     st.push(20);
159     st.push(30);
160
161     cout << "Stack top: " << st.top() << endl; // Output: 30
162     st.pop(); // Removing the top element
163     cout << "Stack top after pop: " << st.top() << endl; // Output: 20
164
165     //
166     =====
167
168     // 7. Queue - FIFO structure with more operations

```

```

163 queue<int> q;
164 q.push(1);
165 q.push(2);
166 q.push(3);
167
168 cout << "Queue_front:_ " << q.front() << endl; // Output: 1
169 q.pop(); // Remove front element
170 cout << "Queue_front_after_pop:_ " << q.front() << endl; // Output: 2
171
172 //
=====
173
174 // 8. Priority Queue - max heap (largest element first) by default
    with more operations
175 priority_queue<int> pq;
176 pq.push(50);
177 pq.push(10);
178 pq.push(30);
179
180 cout << "Priority_queue_top_(max_heap):_ " << pq.top() << endl; //
    Output: 50
181 pq.pop();
182 cout << "Priority_queue_top_after_pop:_ " << pq.top() << endl; //
    Output: 30
183
184 // Min heap priority queue (smallest element first)
185 priority_queue<int, vector<int>, greater<int>> minHeap;
186 minHeap.push(50);
187 minHeap.push(10);
188 minHeap.push(30);
189
190 cout << "Priority_queue_top_(min_heap):_ " << minHeap.top() << endl;
    // Output: 10
191 minHeap.pop();
192 cout << "Priority_queue_top_after_pop:_ " << minHeap.top() << endl;
    // Output: 30
193
194 return 0;
195 }
    
```

## 8.8 num\_prime\_factors

```

1 #include <iostream>
2 #include <vector>
3 #include <bitset>
4 #include <set>
5 #include <cmath>
6
7 using namespace std;
8
9 // Constant to define the maximum limit for prime calculation
10 const int MAX = 3000;
11
12 // Function to generate a list of prime numbers using the Sieve of
    Eratosthenes
13 vector<int> primes() {
14     bitset<MAX> bits;
15     bits[0] = bits[1] = 1; // Mark 0 and 1 as non-prime
16     int sqrt_max = static_cast<int>(sqrt(MAX)) + 1;
17     vector<int> primes_vec;
18
19     // Sieve of Eratosthenes
20     for (int i = 2; i <= sqrt_max; i++) {
21         if (bits[i]) continue; // Skip if i is marked as non-prime
22         for (int j = i * i; j < MAX; j += i) {
23             bits[j] = 1; // Mark multiples of i as non-prime
24         }
25     }
26
27     // Collecting prime numbers
28     for (int i = 2; i < bits.size(); i++) {
29         if (!bits[i]) {
30             primes_vec.push_back(i); // Add prime number to the vector
31         }
32     }
33     return primes_vec;
34 }
35
36 int main() {
37     int n;
38     vector<int> primes_v = primes(); // Generate list of primes
39
40     cin >> n; // Input number
41     int count = 0; // Count of numbers with exactly two distinct prime
        factors
    
```

```

42 // Loop through all numbers from n down to 1
43 while (n > 0) {
44     vector<int> factors; // To store factors of the current number
45     set<int> factorsSet; // To store unique factors
46     int m = n; // Copy of n for factorization
47
48     // Factorization using the list of prime numbers
49     for (int x : primes_v) {
50         while (m % x == 0) {
51             factors.push_back(x); // Store factor
52             m /= x; // Reduce m by the factor
53         }
54     }
55
56     // Insert factors into the set for uniqueness
57     for (int x : factors) {
58         factorsSet.insert(x);
59     }
60
61     // Check if the number has exactly two distinct prime factors
62     if (factorsSet.size() == 2) {
63         count++;
64     }
65     n--; // Decrement n to check the next number
66 }
67
68 cout << count; // Output the count
69 return 0;
70 }
71

```

## 8.9 primes\_in\_range

```

1 #include <iostream>
2 #include <vector>
3 #include <bitset>
4 #include <set>
5 #include <cmath>
6
7 using namespace std;
8
9 // Constant to define the maximum limit for prime calculation
10 const int MAX = 3000;

```

```

11 // Function to generate a list of prime numbers using the Sieve of
12 // Eratosthenes
13 vector<int> primes() {
14     bitset<MAX> bits;
15     bits[0] = bits[1] = 1; // Mark 0 and 1 as non-prime
16     int sqrt_max = static_cast<int>(sqrt(MAX)) + 1;
17     vector<int> primes_vec;
18
19     // Sieve of Eratosthenes
20     for (int i = 2; i <= sqrt_max; i++) {
21         if (bits[i]) continue; // Skip if i is marked as non-prime
22         for (int j = i * i; j < MAX; j += i) {
23             bits[j] = 1; // Mark multiples of i as non-prime
24         }
25     }
26
27     // Collecting prime numbers
28     for (int i = 2; i < bits.size(); i++) {
29         if (!bits[i]) {
30             primes_vec.push_back(i); // Add prime number to the vector
31         }
32     }
33     return primes_vec;
34 }
35
36 int main() {
37     int m, l, u;
38     vector<int> primes_v = primes();
39
40     cin >> m;
41
42     while (m) {
43         cin >> l >> u;
44
45         vector<int>::iterator mi, mx;
46
47         mi = upper_bound(primes_v.begin(), primes_v.end(), l - 1);
48         mx = upper_bound(primes_v.begin(), primes_v.end(), u);
49
50         if (u == 1) {
51             cout << 0 << endl;
52         }

```

```

53     else{
54         cout<<(int)(mx-primes_v.begin())-(int)(mi-primes_v.begin())
           <<endl;
55     }
56     m--;
57 }
58 }

```

## 8.10 weird\_input

```

1  #include <bits/stdc++.h>
2  using namespace std;
3  int r=101;
4  int c=101;
5  int mapa[101][101];
6  int ady[101][101];
7
8  int main(){
9      // For getting input from input.txt file
10     freopen("input.txt", "r", stdin);
11
12     // Printing the Output to output.txt file
13     freopen("output.txt", "w", stdout);
14
15     int rows, cols;
16     cin>>rows>>cols;
17     string inp;
18     for(int i=0 ; i<rows ; i++){
19         cin>>inp;
20         for(int j=0 ; j<cols ; j++){
21             mapa[i][j]=inp[j]-'0';
22         }
23     }
24
25     int pintura;
26
27     for(int i=0 ; i<rows ; i++){
28         for(int j=0 ; j<cols ; j++){
29             if (mapa[i][j] == 0) continue; else pintura += 2;
30
31             if((j-1)<0) {pintura +=mapa[i][j];}
32             else{
33                 if (ady[i][j-1] == 0){

```

```

34                 pintura += abs(mapa[i][j]-mapa[i][j-1]);
35             }
36         }
37         if((j+1)>=cols) {pintura +=mapa[i][j];}
38         else{
39             if (ady[i][j+1] == 0){
40                 pintura += abs(mapa[i][j]-mapa[i][j+1]);
41             }
42         }
43         if((i-1)<0) {pintura +=mapa[i][j];}
44         else{
45             if (ady[i-1][j] == 0){
46                 pintura += abs(mapa[i][j]-mapa[i-1][j]);
47             }
48         }
49         if((i+1)>=rows) {pintura +=mapa[i][j];}
50         else{
51             if (ady[i+1][j] == 0){
52                 pintura += abs(mapa[i][j]-mapa[i+1][j]);
53             }
54         }
55         ady[i][j]=1;
56     }
57 }
58
59 cout<<pintura;
60 return 0;
61 }

```

## 9 Testing