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1) $f(n) = 32n$

$g(n) = n$

$\lim_{n \rightarrow \infty} \frac{32n}{n} =$

$\lim_{n \rightarrow \infty} 32$

$\lim_{n \rightarrow \infty} 32$

Show that
both grow at same rate

2) $f(n) = \ln(n)$ $g(n) = n$

$\lim_{n \rightarrow \infty} \frac{\ln(n)}{n} \rightarrow \lim_{n \rightarrow \infty} \frac{\ln(n)}{n} = 0$

grows towards 0, therefore

$\ln(n)/n$ is not true

$$3) f(n) = \lg(n) \quad g(n) = \ln(n)$$

$$\lim_{n \rightarrow \infty} \frac{\lg(n)}{\ln(n)} \rightarrow \lim_{n \rightarrow \infty} \frac{\frac{1}{n \cdot \ln(2)}}{\frac{1}{n}} \rightarrow \frac{1}{\ln(2)}$$

Therefore it's true, grow at same rate

$$4) f(n) = \log(n) \quad g(n) = \ln(n)$$

$$\lim_{n \rightarrow \infty} \frac{\log(n)}{\ln(n)} \rightarrow \frac{\frac{1}{n \cdot \ln(2)}}{\frac{1}{n}} \rightarrow \frac{1}{\ln(2)}$$

$\frac{1}{\ln(2)}$ when C71 is a constant,
therefore statement is true.

$$5) f(n) = n^2 \quad g(n) = 2^n$$

$$\lim_{n \rightarrow \infty} \frac{n^2}{2^n} \rightarrow \frac{n^2}{2^n} = 0 \text{ when } n \rightarrow \infty$$

therefore statement is true.

$$6) f(n) = n^3 \quad g(n) = n^2$$

$$\lim_{n \rightarrow \infty} \frac{n^3}{n^2} \geq \lim_{n \rightarrow \infty} n = \infty$$

therefore statement is true

$$7) f(n) = 4^{\log_2 n} \quad g(n) = n$$

$$4^{\log_2 n} = 4^{\log_2 n} \geq 2^{2(\log_2 n)} = 2^{n^2 + \log_2 n}$$

$$= n^2 \quad \lim_{n \rightarrow \infty} \frac{n^2}{n} =$$

$\lim_{n \rightarrow \infty} n = \infty$ not a constant therefore not true.

$$8) f(n) = \ln^2(n), g(n) = n$$

$$\lim_{n \rightarrow \infty} \frac{\ln^2(n)}{n} = 0$$

Since logs grow slower

therefore statement is true

$$9) f(n) = \ln^2(\ln n), g(n) = \sqrt{n}$$

$$\lim_{n \rightarrow \infty} \frac{\ln^2(\ln n)}{\sqrt{n}} = 0$$

Since \sqrt{n} grows faster

when $n = 1000,000$

$$= \frac{339}{1000}$$

therefore statement

is true

W)

$$f(n) = \ln n$$

$$g(n) = n^k$$

$$\lim_{n \rightarrow \infty} \frac{\ln n}{n^k} = 0$$

therefore

statement is true

11) $f(n) = \ln(\ln(n))$ $g(n) = \ln(n)$

$\lim_{n \rightarrow \infty} \frac{\ln(\ln(n))}{\ln(n)} = 0$

Therefore L'Hopital's rule is true

12) $f(n) = 2^n$ $g(n) = 2^{n+1}$

$\lim_{n \rightarrow \infty} \frac{2^n}{2^{n+1}} \rightarrow \frac{2^n}{2^n \cdot 2} \rightarrow \frac{1}{2}$

$\lim_{n \rightarrow \infty} \frac{1}{2}$

Therefore statement is true,
 $\frac{1}{2}$ is a constant.