# Optimal design of experiment:

## supercritical fluid extraction case

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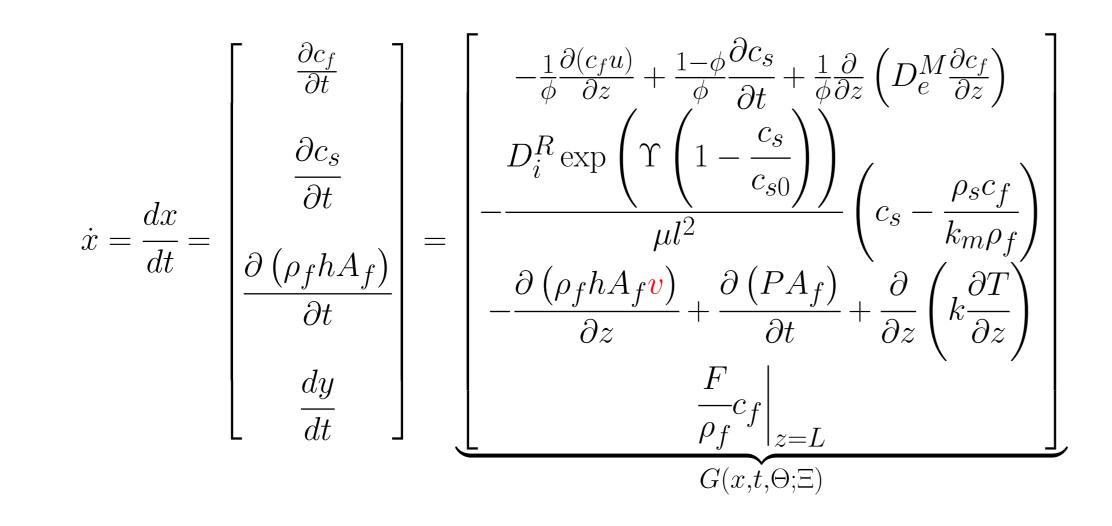


#### Introduction

This study investigates the extraction of valuable components from biomass using supercritical carbon dioxide as a solvent. The interest is in essential oils extracted from chamomile flowers in cylindrical extractors operated in a semi-batch mode. The extraction process is described by a distributed-parameter model, and set of empirical correlations. This work aims to validate the empirical correlations by designing a new experiment with dynamically changing operating conditions.

#### Process Model

- One-dimensional
- Plug flow
- No pressure drop
- Uniform particle distribution
- Based on the two-film theory for a single component
- Peng-Robinson equation of state
- Decaying extraction kinetic
- Empirical correlations



 $c_f$  – Soluts concentration in the fluid phase

 $c_s$  – Soluts concentration in the solid phase

h – Enthalpy y – Extraction yield

 $\rho_f$  – Density of fluid

 $A_f$  – Cross-section of the bed - Darcy velocity

 $D_e^M$  – Axial mass diffusivity

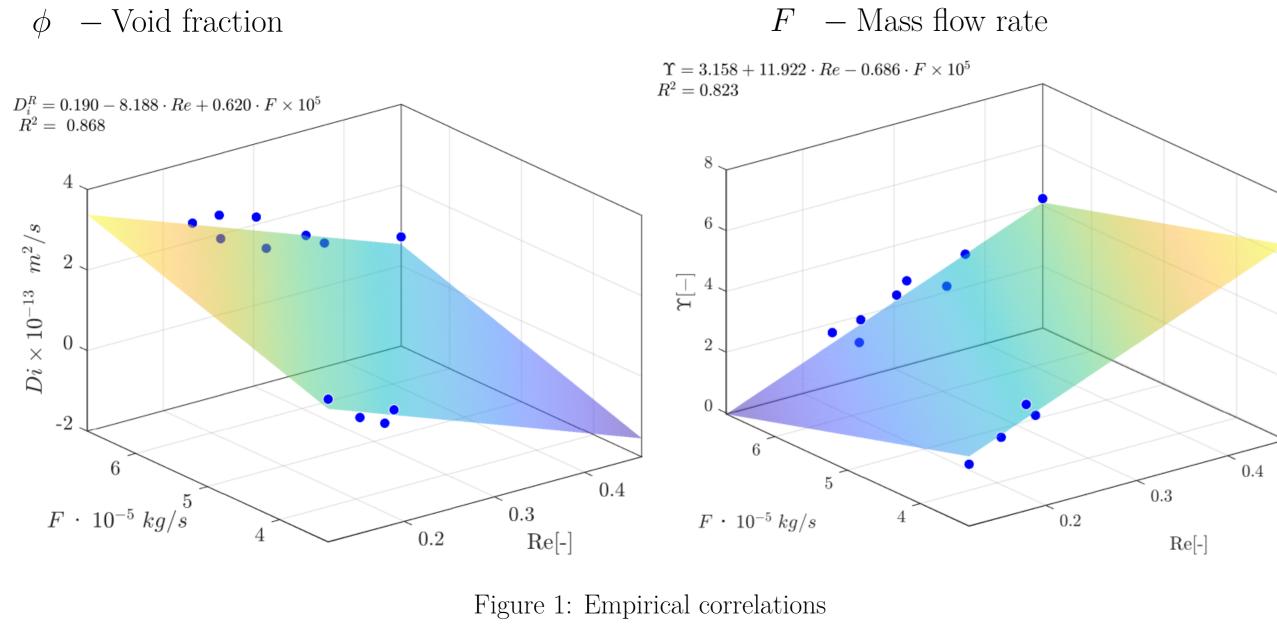
 $D_i^R$  – Internal mass diffusivity

 $\Upsilon$  – Decaying factor

 $\rho_s$  — Bulky density of solid bed  $k_m$  – Partition factor

P - Pressure

T – Temperature



#### Model-based optimal design of experiment

Fisher information  $\mathcal{F}$  measures the amount of information that an observable random variable carries about an unknown parameter of a distribution that models the random variable.  ${\mathcal F}$  is defined as Hessian of the log-likelihood function with respect to the parameters  $\Theta$ , given the covariance matrix  $\Sigma$ .

$$\mathcal{F}(t,\Theta;\Xi) = \frac{\partial y(t,\Theta;\Xi)}{\partial \Theta} \Sigma \frac{\partial y(t,\Theta;\Xi)}{\partial \Theta^{\top}}$$

The optimal design of experiments is a concept that refers to planning an experiment, which allow parameters to be estimated without bias and with minimum variance. The D-optimality criterion is selected as the objective function, which leads to the minimisation of the volume of the ellipsoidal confidence region of parameter estimates given the experimental condition  $\Xi$ .

$$Ξ^*$$

$$= \arg \min_{T^{in}, F \in \Xi} \int_{t_0}^{t_f} -\ln \det \mathcal{F}(t, \Theta; \Xi) dt$$
subject to
$$\dot{x} = G \quad (x, t, \Theta; \Xi)$$

$$T^0 = T^{in}(t = 0)$$

$$30°C \le T^{in}(t) \le 40°C$$

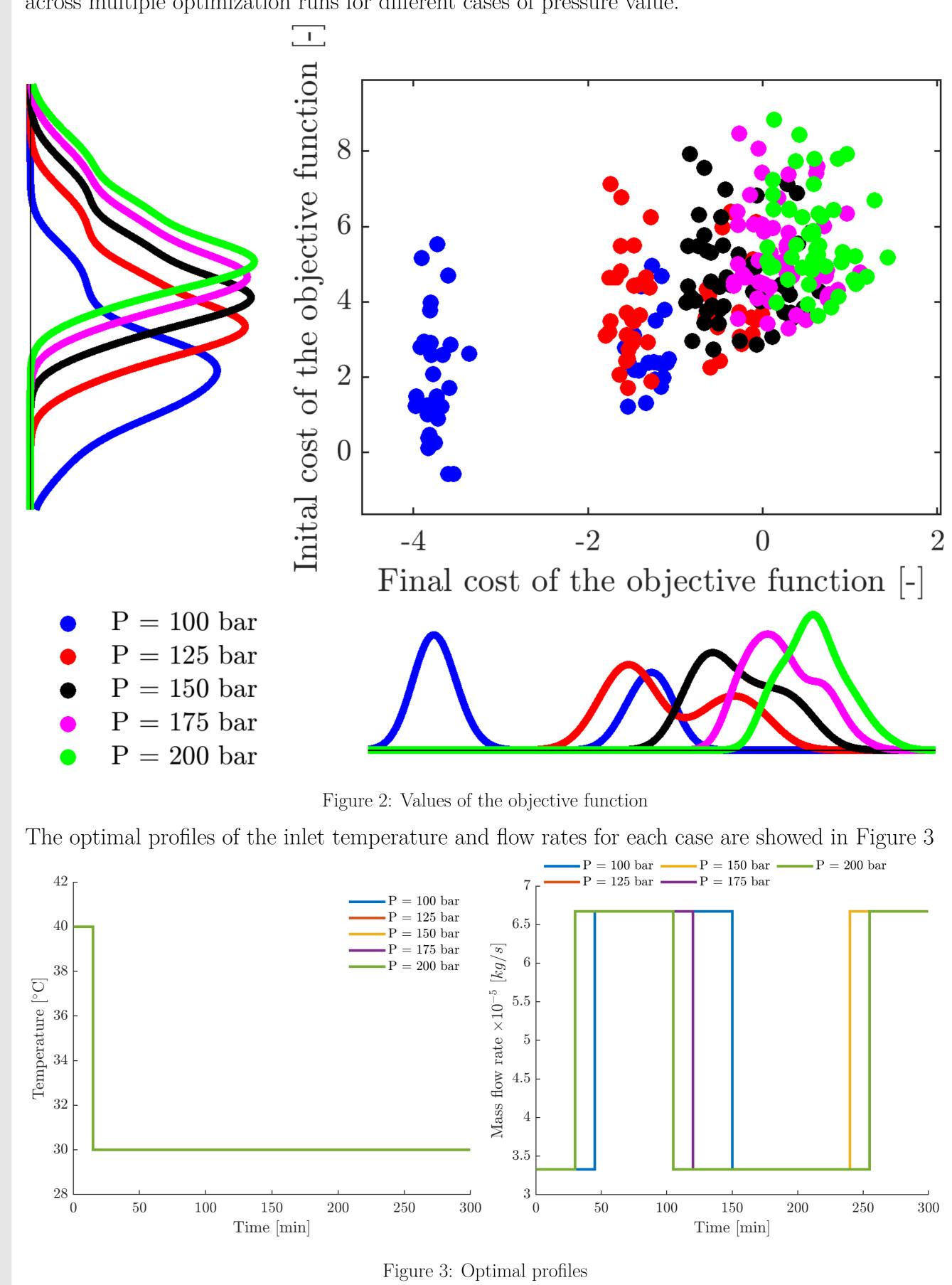
$$3.33 \cdot 10^{-5} \text{ kg/s} \le F \quad (t) \le 6.67 \cdot 10^{-5} \text{ kg/s}$$

$$100 \text{ bar} \le P \quad (t) \le 200 \text{ bar}$$

This work aims to design a dynamic experiment to improve precision of correlation for  $D_i^R$ . The system is assumed to run for 300 min, with sampling time of 10 min. The set of decision variables consists of  $T^{in}$  and F, and each of them is manipulated every 15 min. Each of five analysed cases assumes that P is kept constant at 100, 125, 150, 175 and 200 bar, respectively.

#### Results

To identify the global solution, the optimization problem is solved multiple times, each starting from a random initial solution. Figure 2 compares the initial and final values of the cost function across multiple optimization runs for different cases of pressure value.



#### Conclusions

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#### Forthcoming Research

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### References

[1] A. B. Jones and J. M. Smith. Article Title. Journal title, 13(52):123–456, March 2013.

[2] J. M. Smith and A. B. Jones. Book Title. Publisher, 7th edition, 2012.

#### Acknowledgements

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