Local Sensitivity Analysis of a Supercritical Extraction Model

Oliwer Sliczniuk^{a,*}, Pekka Oinas^a

^aAalto University, School of Chemical Engineering, Espoo, 02150, Finland

ARTICLE INFO

Keywords: Supercritical extraction Sensitivity analysis Mathematical modelling

ABSTRACT

This study investigates the process of chamomile oil extraction from chamomile flowers. A parameter-distributed model, consisting of a set of partial differential equations, was used to describe the governing mass transfer phenomena between solid and fluid phases under supercritical conditions using carbon dioxide as the solvent. The concept of quasi-one-dimensional flow was applied to reduce the number of spatial dimensions. The flow of carbon dioxide is assumed to be uniform across any cross-section, although the area available for the fluid phase can vary along the extractor. The physical properties of the solvent were estimated using the Peng-Robinson equation of state. Laboratory experiments were conducted under various, but constant operating conditions of $30-40\,^{\circ}C$, $100-200\,^{\circ}$ bar and $3.33-6.67\cdot10^{-5}$ kg/s. The local sensitivity analysis method was applied to evaluate the robustness of the model parameters by investigating the impact of infinitesimally small changes in the model parameters and controls on the model outputs. This study focuses on analysing the effect of pressure on the model state space and extraction yield.

1. Introduction

17

19

20

21

24

27

32

Supercritical CO_2 is defined as carbon dioxide that is pressurized and heated above its critical point (31.1 °C, 74 bar). Depending on the operating conditions, the fluid properties such as viscosity and density can vary, which leads to multiple industrial applications of CO_2 .

One of the most popular applications of supercritical CO_2 is the extraction of essential oils, as described by many researchers, for example, by Sodeifian and Sajadian [1], Reverchon et al. [2] or Sovova [3]. Traditional methods, such as distillation and organic solvent extraction, are commonly employed but have drawbacks. Distillation involves high temperatures that can lead to the thermal degradation of heat-sensitive compounds. This limitation has increased the popularity of alternative techniques, such as supercritical fluid extraction. Supercritical CO_2 is appealing due to its distinctive properties: it is inflammable, non-toxic and non-corrosive. Supercritical fluids can exhibit both gasand liquid-like properties, allowing for adjustable dissolving power through changes in operating conditions.

The applications of supercritical carbon dioxide are not limited only to an extraction process but can also be used for impregnation, as described by Weidner [4], Machado et al. [5] or Fathi et al. [6]. Impregnation is defined as modifying the properties of bulk substances by physically or chemically binding/adsorbing impregnates to a bulk material or surface, such as the hydrophobization of surfaces. The main advantage of using supercritical CO₂ is that, after depressurization, it desorbs from the surface and evaporates, leaving a solvent-free product. On the other hand, the main disadvantage of using carbon dioxide for impregnation is the low solubility of many drugs of interest.

*Corresponding author

oliwer.sliczniuk@aalto.fi (O. Sliczniuk)
ORCID(s): 0000-0003-2593-5956 (O. Sliczniuk); 0000-0002-0183-5558
(P. Oinas)

Another application of supercritical CO_2 is nanoparticle formation, as investigated by Padrela et al. [7], Franco and De Marco [8], S. Ardestani et al. [9] or Sodeifian et al. [10]. Supercritical carbon-dioxide-assisted technologies enable the production of different morphologies of different sizes, including nanoparticles and nanocrystals, by modulating the operating conditions. Supercritical fluid-based processes have advantages over techniques conventionally employed to produce nanosized particles or crystals, such as reduced use of toxic solvents. Moreover, the CO_2 is completely removed from the final product by simple depressurization.

This study investigates the extraction of essential oil from chamomile flowers (Matricaria chamomilla L.) via supercritical fluid extraction techniques and the modelling of this process. Chamomile is a medicinal herb widely cultivated in southern and eastern Europe — in countries such as Germany, Hungary, France and Russia. It can also be found outside Europe, for instance in Brazil, as discussed by Singh et al. [11]. This plant is distinguished by its hollow, bright gold cones, housing disc or tubular florets and surrounded by about fifteen white ray or ligulate florets. Chamomile has been used for its medicinal benefits, serving as an anti-inflammatory, antioxidant, mild astringent, and healing remedy. Extracts of chamomile are widely used to calm nerves and mitigate anxiety, hysteria, nightmares, insomnia and other sleep-related conditions, according to Srivastava [12]. Orav et al. [13] reported that oil yields from dried chamomile samples ranged from 0.7 to 6.7 mL/kg. The highest yields of essential oil, between 6.1 and 6.7 mL/kg, were derived from chamomile sourced from Latvia and Ukraine. In comparison, chamomile from Armenia exhibited a lower oil content of 0.7 mL/kg.

The literature offers various mathematical models to describe the extraction of valuable compounds from biomass. Selecting a process model is case-dependent and requires analysis of each model's specific assumptions about mass transfer and thermodynamic equilibrium.

33

34

36

37

38

40

42

44

45

46

48

50

51

52

55

56

57

59

61

63

64

65

67

69

Goto et al. [14] presented the shrinking core (SC) model, which describes a process of irreversible desorption that is followed by diffusion through the pores of a porous solid. When the mass transfer rate of the solute in the non-extracted inner region is significantly slower than in the outer region, where most of the solute has already been extracted or when the solute concentration exceeds its solubility in the solvent, a distinct boundary may form between the inner and outer regions. As extraction progresses, the core of the inner region shrinks. The model envisions supercritical CO₂ extraction as a sharp, inward-moving front, with a completely non-extracted core ahead of the front and a fully extracted shell behind it.

aa

Sovova [3] proposed the broken-and-intact cell (BIC) model, which assumes that a portion of the solute, initially stored within plant structures and protected by cell walls, is released during the mechanical breakdown of the material. The solute located in the region of broken cells near the particle surface is directly exposed to the solvent, while the core of the particle contains intact cells with undamaged walls. This model describes three extraction phases: a fast extraction phase for accessible oil, a transient phase, and a slow phase controlled by diffusion. The model has been successfully applied to the extraction of grape oil (Sovová et al. [15]) and caraway oil (Sovova et al. [16]).

The supercritical fluid extraction (SFE) process can be treated similarly to heat transfer, considering solid particles as hot balls cooling down in a uniform environment. Bartle et al. [17] introduced the hot ball diffusion (HBD) model, where spherical particles with a uniformly distributed solute diffuse similarly to heat diffusion. Unlike the BIC model, where the solute is readily available on the particle surface, the HBD model is suited for systems with small quantities of extractable materials and is not limited by solubility. The model is particularly relevant when internal diffusion controls mass transfer, allowing results from single particles to be extended to the entire bed under uniform conditions. Reverchon et al. [2] have further elaborated on the HBD model and used it to simulate extraction processes for natural materials.

Reverchon [18] proposed a model for extraction of essential oils, which are mainly located inside the vegetable cells in organules called vacuoles. Only a small fraction of essential oil might be near the particle surface due to the breaking up of cells during grinding or in epidermal hairs located on the leaf surface. The fraction of oil freely available on the particle surface should not be significant in the case of SFE from leaves. Consequently, SFE of essential oil from leaves should be mainly controlled by internal mass-transfer resistance. Therefore, the external mass-transfer coefficient was neglected in the development of the model of Reverchon [18]. The mass balances were developed with the additional hypotheses that axial dispersion can be neglected and that the solvent density and flow rate are constant along the bed.

This work builds upon the linear kinetic model suggested by Reverchon [18], deriving fundamental governing equations to develop a comprehensive model for the

chamomile oil extraction process. This model aims at controloriented simplicity, assuming semi-continuous operation within a cylindrical vessel. The process involves a supercritical solvent being pumped through a fixed bed of finely chopped biomass to extract the solute, followed by separation of the solvent and solute in a flush drum to collect the extract. Parameters such as pressure (P), feed flow rate (F) and inlet temperature (T_{in}) are adjustable and measurable, while the outlet temperature (T_{out}) and the amount of product at the outlet can only be monitored. Figure 1 presents a simplified process flow diagram.

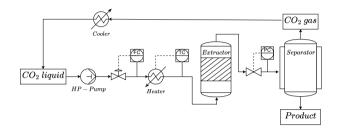


Figure 1: Process flow diagram.

This study aims to analyse the influence of changes in operating conditions on the process model described by Sliczniuk and Oinas [19]. For that, a sensitivity analysis is applied to examine the impact of model parameters or controls on the model output. The results of this sensitivity analysis can be used to identify sources of uncertainty, simplify the model or detect errors by revealing unexpected relationships between inputs and outputs. Various sensitivity analysis methods are available, including:

- One-at-a-time method
- Derivative-based local methods
- · Variance-based methods

Different supercritical extraction models have been analysed using various sensitivity analysis techniques in the literature. For instance, Fiori et al. [20] performed sensitivity calculations by varying parameters within their confidence intervals and observing the changes in model results. Their analysis revealed that the particle diameter and internal mass transfer coefficient significantly influence extraction during the diffusion-control regime.

Santos et al. [21] considered the model of Sovova [3] for semi-continuous isothermal and isobaric extraction processes using carbon dioxide as a solvent. They conducted a parametric sensitivity analysis using a two-level factorial design, disturbing model parameters by 10% and analysing their main effects. They proposed strategies for high-performance operation based on sensitivities related to superficial velocity, particle diameter, initial solute concentration in the solid phase and solute concentration in the fluid phase at the extractor inlet.

Hatami and Ciftci [22] performed a one-factor-at-atime sensitivity analysis to assess the response of net present value (NPV) to variations in technical and economic variables. Their study consisted of two parts. The first part examined how net present value is influenced by changes in individual technical and economic parameters, keeping the extractor volume constant at 300 L. The second part investigated the effects of varying the extractor volume (from 1 to 600 L) on the project's overall profitability. The authors found that the raw material price, discount rate and residence time had the biggest impact on NPV (Hatami and Ciftci [22]).

2. Materials and methods

2.1. Governing equations

The governing equations for a quasi-one-dimensional flow were derived following the work of Jr. [23]. A quasi-one-dimensional flow refers to a fluid flow scenario assuming that the flow properties are uniformly distributed across any cross-section. This simplification is typically applied when the flow channel's cross-sectional area changes, such as through irregular shapes or partial filling of an extractor. According to this assumption, velocity and other flow properties change solely in the flow direction.

As discussed by Jr. [24], all flows are compressible, but some of them can be treated as incompressible since the velocities are low. This assumption leads to the incompressible condition: $\nabla \cdot u = 0$, which is valid for constant density (strict incompressible) or varying density flow. The assumption allows for removing acoustic waves and large perturbations in density and/or temperature. In the 1-D case, the incompressibility condition becomes $\frac{du}{dz} = 0$, so the fluid velocity is constant along the z- direction.

The set of quasi-one-dimensional governing equations in Cartesian coordinates is described by Equations 1 - 3:

$$\frac{\partial \left(\rho_f A_f\right)}{\partial t} + \frac{\partial \left(\rho_f A_f v\right)}{\partial z} = 0,\tag{1}$$

$$\frac{\partial \left(\rho_f v A_f\right)}{\partial t} + \frac{\partial \left(\rho_f A_f v^2\right)}{\partial z} = -A_f \frac{\partial P}{\partial z},\tag{2}$$

$$\frac{\partial \left(\rho_f e A_f\right)}{\partial t} + \frac{\partial \left(\rho_f A_f v e\right)}{\partial z} = -P \frac{\left(A_f v\right)}{\partial z} + \frac{\partial}{\partial z} \left(k \frac{\partial T}{\partial z}\right),\tag{3}$$

where ρ_f is the density of the fluid, A_f is the function which describes a change in the cross-section, v is the velocity, P is the total pressure, e is the internal energy of the fluid, t is time and z is the spatial direction.

2.2. Extraction model

2.2.1. Continuity equation

The previously derived quasi-one-dimensional continuity equation (Equation 1) is redefined by incorporating the function $A_f = A\phi$. This modification distinguishes constant and varying terms, where the varying term accounts for changes in the cross-sectional area available for the fluid. Equation 4 shows the modified continuity equation:

$$\frac{\partial(\rho_f\phi)}{\partial t} + \frac{\partial(\rho_f v A \phi)}{\partial z} = 0, \tag{4}$$

where A is the total cross-section of the extractor and ϕ describes porosity along the extractor.

Assuming that the mass flow rate is constant in time, the temporal derivative becomes the mass flux F, and the spatial derivative can be integrated along z as

$$\int \frac{\partial (\rho_f v A \phi)}{\partial z} dz = F \to F = \rho_f v A \phi \tag{5}$$

To simplify the system dynamics, it is assumed that F is a control variable and affects the whole system instantaneously (due to $\nabla \cdot u = 0$), which allows finding the velocity profile that satisfies mass continuity based on F, ϕ and ρ_f :

$$v = \frac{F}{\rho_f A \phi} \tag{6}$$

Similarly, superficial velocity may be introduced:

$$u = v\phi = \frac{F}{\rho_f A} \tag{7}$$

The fluid density ρ_f can be obtained from the Peng-Robinson equation of state if the temperature and thermodynamic pressure are known along z. Variation in fluid density may occur due to pressure or inlet temperature changes. In a non-isothermal case, in Equations 6 and 7, ρ_f is considered the average fluid density along the extraction column.

2.2.2. Mass balance for the fluid phase

Equation 8 describes the movement of the solute in the system, which is constrained to the axial direction due to the quasi-one-dimensional assumption. Given that the solute concentration in the solvent is negligible, the fluid phase is described as pseudo-homogeneous, with properties identical to those of the solvent itself. It is also assumed that the thermodynamic pressure remains constant throughout the device. The analysis further simplifies the flow dynamics by disregarding the boundary layer near the extractor's inner wall. This leads to a uniform velocity profile across any cross-section perpendicular to the axial direction. Thus, the mass balance equation includes convection, diffusion and kinetic terms representing the fluid phase behaviour:

$$\frac{\partial c_f}{\partial t} + \frac{1}{\phi} \frac{\partial \left(c_f u\right)}{\partial z} = \frac{1 - \phi}{\phi} r_e + \frac{1}{\phi} \frac{\partial}{\partial z} \left(D_e^M \frac{\partial c_f}{\partial z}\right),\tag{8}$$

where c_f represents the solute concentration in the fluid phase, r_e is the mass transfer kinetic term and D_e^M is the axial diffusion coefficient.

2.2.3. Mass balance for the solid phase

As given by Equation 9, the solid phase is considered stationary, without convection and diffusion terms in the mass balance equation. Therefore, the only significant term in this equation is the kinetic term of Equation 10, which connects the solid and fluid phases. For simplicity, the extract is represented by a single pseudo-component:

$$\frac{\partial c_s}{\partial t} = \underbrace{r_e}_{\text{Kinetics}} \tag{9}$$

2.2.4. Kinetic term

As the solvent flows through the fixed bed, CO₂ molecules diffuse into the pores, adsorb on the inner surface and form a film due to solvent-solid matrix interactions. The dissolved solute diffuses into the bulk from the particle's core through the solid-fluid interface, the pore and the film. Figure 2 shows the mass transfer mechanism, where the mean solute concentration in the solid phase is denoted by c_s , and the equilibrium concentrations at the solid-fluid interface are denoted by c_s^* and c_p^* for the solid and fluid phases, respectively. The concentration of the solutes in the fluid phase in the centre of the pore is denoted by c_n . As the solute diffuses through the pore, its concentration changes, reaching c_{nf} at the opening. Then, the solute diffuses through the film around the particle and reaches bulk concentration c_f . The two-film theory describes the solid-fluid interface inside the pore. The overall mass transfer coefficient can be determined from the relationship between the solute concentration in one phase and its equilibrium concentration.

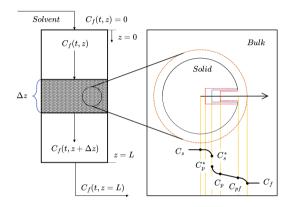


Figure 2: Mass transfer mechanism.

Bulley et al. [25] suggest a process where the driving force for extraction is given by the difference between the concentration of the solute in the bulk, c_f , and in the centre of the pore, c_p^* . The concentration c_p^* is in equilibrium with c_s according to the equilibrium relationship. The rate of extraction is thus $r_e\left(c_f-c_p^*(c_s)\right)$. In contrast, Reverchon [18] proposes a driving force given by the difference between c_s and c_p^* . As given in Equation 10, the concentration c_p^* is determined by the equilibrium relationship with c_f :

$$r_e = \frac{D_i}{\mu l^2} \left(c_s - c_p^* \right),\tag{10}$$

where μ is sphericity, l a characteristic dimension of particles that can be defined as l = r/3, r is the mean particle radius, ρ_s is the solid density, D_i corresponds to the overall diffusion coefficient and c_p^* is the concentration at the solid-fluid interface (which, according to the internal resistance model, is supposed to be at equilibrium with the fluid phase).

According to Bulley et al. [25], a linear equilibrium relationship (Equation 11) can be used to find the equilibrium concentration of the solute in the fluid phase c_f^* based on the concentration of the solute in the solid phase c_s :

$$c_f^* = k_p c_s \tag{11}$$

The volumetric partition coefficient k_p acts as an equilibrium constant between the solute concentration in one phase and the corresponding equilibrium concentration at the solid-fluid interphase. Spiro and Kandiah [26] propose defining the mass partition coefficient k_m as

$$k_m = \frac{k_p \rho_s}{\rho_f} \tag{12}$$

According to Reverchon [18], the kinetic term becomes

$$r_e = -\frac{D_i}{\mu l^2} \left(c_s - \frac{\rho_s c_f}{k_m \rho_f} \right) \tag{13}$$

2.2.5. Uneven distribution of solute in the solid phase

Following the idea of the broken-and-intact cell (BIC) model (Sovova [27]), the internal diffusion coefficient D_i is considered to be a product of the reference value of D_i^R and the exponential decay function γ , as given by Equation 14:

$$D_i = D_i^R \gamma(c_s) = D_i^R \exp\left(\Upsilon\left(1 - \frac{c_s}{c_{s0}}\right)\right),\tag{14}$$

where Υ describes the curvature of the decay function. Equation 15 describes the final form of the kinetic term:

$$r_e = -\frac{D_i^R \gamma}{\mu l^2} \left(c_s - \frac{\rho_s c_f}{k_m \rho_f} \right) \tag{15}$$

The γ function limits the solute's availability in the solid phase. Similarly to the BIC model, the solute is assumed to be contained in the cells, some of which are open because the cell walls were broken by grinding, with the rest remaining intact. The diffusion of the solute from a particle's core takes more time than the diffusion of the solute close to the outer surface. The same idea can be represented by the decaying internal diffusion coefficient, where the decreasing term is a function of the solute concentration in the solid.

An alternative interpretation of the decay function γ involves considering the porous structure of the solid particles, where the pores are initially saturated with the solute. During extraction, the solute within these pores gradually dissolves into the surrounding fluid. Initially, the solute molecules near the pore openings dissolve and diffuse rapidly due to the short diffusion paths. As the extraction progresses, the dissolution front moves deeper into the pore structure, and solute from the inner regions of the pores begins to dissolve. The diffusion of solute molecules from the interior of the pores to the external fluid becomes progressively slower because the effective diffusion path length increases. This lengthening of the diffusion path enhances the mass transfer resistance, reducing the overall diffusion rate.

In an extreme case, this model could be compared with the shrinking core model presented by Goto et al. [14], where the particle radius decreases as the solute content in the solid phase diminishes. In the SC model, the reduction in particle size leads to significant changes in both the diffusion path length and the surface area available for mass transfer. The diminishing particle size increases the diffusion path within the remaining solid core and decreases the external surface

area, both of which contribute to a slower extraction rate. When comparing this to the varying diffusion coefficient in our model, some conceptual similarities can be noticed.

2.2.6. Empirical correlations

The empirical correlations for D_i and Υ were derived by Sliczniuk and Oinas [19] and validated for temperatures of $30-40\,^{\circ}C$, pressures of 100-200 bar, and mass flow rates of $3.33-6.67\cdot 10^{-5}$ kg/s. Figures 3 and 4 show the results of multiple linear regression applied to solutions of parameter estimation and selected independent variables. The region marked with the white dashed line represents the confidence region, where the model has been tested. Both correlations should be equal or greater than zero to avoid unphysical behaviour such as reverse mass transfer. The multiple linear regression functions are combined with the rectifier function to ensure non-negativity.

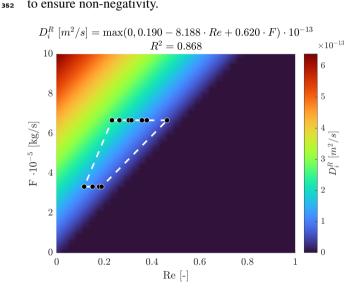


Figure 3: Multiple linear regression $D_i^R = f(Re, F)$.

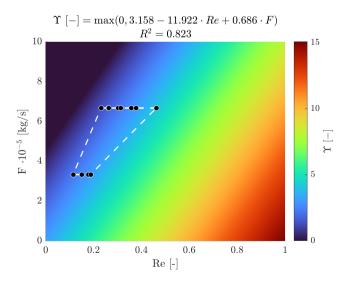


Figure 4: Multiple linear regression $\Upsilon = f(Re, F)$.

2.2.7. Heat balance

The heat balance equation describes the evolution of the enthalpy in the system and is given by Equation 16:

$$\frac{\partial \left(\rho_{f} h A_{f}\right)}{\partial t} = -\frac{\partial \left(\rho_{f} h A_{f} v\right)}{\partial z} + \frac{\partial \left(P A_{f}\right)}{\partial t} + \frac{\partial}{\partial z} \left(k \frac{\partial T}{\partial z}\right) \tag{16}$$

If the value of enthalpy h is known from the time evolution of the energy equation, and pressure P is known from measurement, then temperature T can be reconstructed based on the departure function. The departure function is a mathematical function that characterizes the deviation of a thermodynamic property (enthalpy, entropy or internal energy) of a real substance from that of an ideal gas at the same temperature and pressure. The enthalpy departure function, as presented by Gmehling et al. [28] for the Peng-Robinson equation of state, is defined by Equation 17:

$$h - h^{id} = RT \left[T_r(Z - 1) - 2.078(1 + \kappa) \sqrt{\alpha(T)} \ln \left(\frac{Z + \left(1 + \sqrt{2} \right) B}{Z + \left(1 - \sqrt{2} \right) B} \right) \right], (17)$$

where α is defined as $\left(1 + \kappa \left(1 - \sqrt{T_r}\right)\right)^2$, T_r is the reduced temperature, P_r is the reduced pressure, Z is the compressibility factor, κ is a quadratic function of the acentric factor and B is calculated as $0.07780\frac{P_r}{T}$.

Equation 17 requires a reference state, which is assumed to be $T_{ref} = 298.15$ K and $P_{ref} = 1.01325$ bar.

A root finder can be used to find a temperature value which minimizes the difference between the value of enthalpy coming from the heat balance and the departure functions. The root-finding procedure has to be repeated at every time step to find a temperature profile along spatial direction *z*.

$$\min_{T} \left(\underbrace{h(t,x)}_{\text{Heat balance}} - \underbrace{h(T,P,\rho_f(T,P))}_{\text{Departure function}} \right)^2 \tag{18}$$

2.2.8. Pressure term

As explained in Section 2.1, this low velocity region pressure is nearly constant due to the small pressure wave propagation that occurs at the speed of sound. Under such conditions, the term $\partial P/\partial t$ can be approximated by a difference equation, describing the pressure change in the whole system. The pressure P in the system is considered a state variable, while the pressure in the new time-step P_{in} is considered a control variable.

$$\frac{\partial P}{\partial t} \approx \frac{P_{in} - P}{\Delta t} \tag{19}$$

Such a simplified equation allows for instantaneous pressure change in the system but does not consider a gradual pressure build-up and the effects of pressure losses. In a real system, the dynamics of pressure change would depend on a pump and a back-pressure regulator.

2.2.9. Extraction yield

The process yield is calculated according to Equation 20, as presented by Sovova et al. [16]. The measurement equation evaluates the solute's mass at the extraction unit outlet and sums it up. The integral form of the measurement (Equation 20) can be transformed into the differential form (Equation 21) and augmented with the process model.

$$y = \int_{t_0}^{t_f} \frac{F}{\rho_f} c_f \Big|_{z=L} dt \tag{20}$$

$$\frac{dy}{dt} = \frac{F}{\rho_f} c_f \Big|_{z=L}$$
(21)

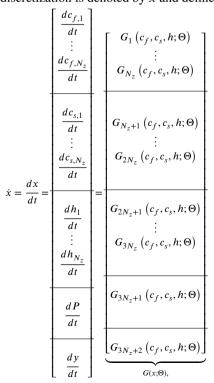
2.2.10. Initial and boundary conditions

It is assumed that the solvent is free of solute at the beginning of the process $c_{f0} = 0$, that all the solid particles have the same initial solute content c_{s0} and that the system is isothermal, hence the initial state is h_0 . The fluid at the inlet is considered not to contain any solute. The initial and boundary conditions are defined as follows:

$$\begin{split} c_f(t=0,z) &= 0 & c_s(t=0,z) = c_{s0} & h(t=0,z) = h_0 \\ c_f(t,z=0) &= 0 & h(t,z=0) = h_{in} & \frac{\partial c_f(t,z=L)}{\partial x} = 0 \\ \frac{\partial h(t,z=L)}{\partial x} &= 0 & c_s(t,z=\{0,L\}) = 0 & y(0) = 0 & P(0) = P_0 \end{split}$$

2.2.11. Discretization methods

The method of lines is used to transform the process model equations into a set of ODEs denoted by $G(x;\Theta)$. The backward finite difference is used to approximate the first-order derivative, while the central difference scheme approximates the second-order derivative z direction. The length of the fixed bed is divided into N_z , i.e. equally distributed points in the z direction. The state-space model after discretization is denoted by x and defined as follows:



where $x \in \mathbb{R}^{N_x=3N_z+2}$ and $\Theta \in \mathbb{R}^{N_\Theta=N_\theta+N_u}$, N_θ is the number of parameters and N_u is the number of control variables.

For a derivative to be conservative, it must form a telescoping series. In other words, only the boundary terms should remain after adding all terms coming from the discretization over a grid, and the artificial interior points should be cancelled out. Discretization is applied to the conservative form of the model to ensure mass conservation.

2.3. Local sensitivity analysis

Local derivative-based methods involve taking the total derivative of the state vector x with respect to the parameter space Θ . A set of derivatives, known as sensitivity equations, is integrated simultaneously with the process model. Sensitivity analysis shows how responsive the solution is to changes in the parameter Θ . As discussed by Dickinson and Gelinas [29], sensitivity analysis can be used to determine the influence of uncertainty on the solution of the original system. Another application of sensitivity analysis is to distinguish sensitive parameters from insensitive ones, which might be helpful for model reduction. Finally, from a control engineering point of view, sensitivity analysis allows sorting the control variables with respect to the level of effort required to change the model's output.

Following the work of Maly and Petzold [30], sensitivity equations can be defined as follows:

$$S(x;\Theta) = \frac{dx}{d\Theta} \tag{22}$$

The new system of equations can be obtained by taking the total derivative of S with respect to time t:

$$\dot{S}(x;\Theta) = \frac{dS(x;\Theta)}{dt} = \frac{d}{dt} \left(\frac{dx}{d\Theta} \right) = \frac{d}{d\Theta} \left(\frac{dx}{dt} \right) = \frac{dG(x;\Theta)}{d\Theta}$$
 (23)

Sensitivity Equation 24 can be obtained by applying the definition of the total derivative to Equation 23:

$$\frac{dG(x;\Theta)}{d\Theta} = \underbrace{\frac{\partial G(x;\Theta)}{\partial x}}_{\bar{J}_{\chi}(x;\Theta)} \underbrace{\frac{\partial x}{\partial \Theta}}_{\bar{S}(x;\Theta)} + \underbrace{\frac{\partial G(x;\Theta)}{\partial \Theta}}_{\bar{J}_{\Theta}(x;\Theta)}$$
(24)

The Jacobian $\bar{J}_x(x;\Theta)$ represents the matrix of equations of size $N_x \times N_x$, where each equation $\bar{J}_x(n_x,n_x)$ is the derivative of $G_{n_x}(x;\Theta)$ with respect to the state variable $x_{n_{\Theta}}$:

$$\bar{J}_{x}(x;\Theta) = \begin{pmatrix} \frac{\partial G_{1}(x;\Theta)}{\partial x_{1}} & \frac{\partial G_{1}(x;\Theta)}{\partial x_{2}} & \dots & \frac{\partial G_{1}(x;\Theta)}{\partial x_{N_{x}}} \\ \frac{\partial G_{2}(x;\Theta)}{\partial x_{1}} & \frac{\partial G_{2}(x;\Theta)}{\partial x_{2}} & \dots & \frac{\partial G_{2}(x;\Theta)}{\partial x_{N_{x}}} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\partial G_{N_{x}}(x;\Theta)}{\partial x_{1}} & \frac{\partial G_{N_{x}}(x;\Theta)}{\partial x_{2}} & \dots & \frac{\partial G_{N_{x}}(x;\Theta)}{\partial x_{N_{x}}} \end{pmatrix}$$
(25)

The sensitivity matrix $\bar{S}(x;\Theta)$ represents the matrix of equations of size $N_x \times N_\Theta$, where each entry $\bar{S}(n_x,n_\Theta)$ is the derivative of state variable x_{n_x} with respect to parameter Θ_{n_Θ} . Matrix $\bar{J}_x(x;\Theta)$ and $\bar{S}(x;\Theta)$ describe the indirect influence of Θ_{n_Θ} on the state space.

$$\bar{S}(x;\Theta) = \begin{pmatrix}
\frac{\partial x_1}{\partial \Theta_1} & \frac{\partial x_1}{\partial \Theta_2} & \dots & \frac{\partial x_1}{\partial \Theta_{N_{\Theta}}} \\
\frac{\partial x_2}{\partial \Theta_1} & \frac{\partial x_2}{\partial \Theta_2} & \dots & \frac{\partial x_2}{\partial \Theta_{N_{\Theta}}} \\
\vdots & \vdots & \ddots & \vdots \\
\frac{\partial x_{N_x}}{\partial \Theta_1} & \frac{\partial x_{N_x}}{\partial \Theta_2} & \dots & \frac{\partial x_{N_x}}{\partial \Theta_{N_{\Theta}}}
\end{pmatrix}$$
(26)

The Jacobian $\bar{J}_{\Theta}(x;\Theta)$ represents the matrix of equations of size $N_x \times N_{\Theta}$, where each sub-equation $\bar{J}_{\Theta}(n_x,n_{\Theta})$ is the partial derivative of process model equation G_{n_x} with respect to parameter $\Theta_{n_{\Theta}}$. $\bar{J}_{\Theta}(n_x,n_{\Theta})$ defines the direct effect of $\Theta_{n_{\Theta}}$ on the state space:

$$\bar{J}_{\Theta}(x;\Theta) = \begin{pmatrix} \frac{\partial G_{1}(x;\Theta)}{\partial \Theta_{1}} & \frac{\partial G_{1}(x;\Theta)}{\partial \Theta_{2}} & \dots & \frac{\partial G_{1}(x;\Theta)}{\partial \Theta_{N_{\Theta}}} \\ \frac{\partial G_{2}(x;\Theta)}{\partial \Theta_{1}} & \frac{\partial G_{2}(x;\Theta)}{\partial \Theta_{2}} & \dots & \frac{\partial G_{2}(x;\Theta)}{\partial \Theta_{N_{\Theta}}} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\partial G_{N_{x}}(x;\Theta)}{\partial \Theta_{1}} & \frac{\partial G_{N_{x}}(x;\Theta)}{\partial \Theta_{2}} & \dots & \frac{\partial G_{N_{x}}(x;\Theta)}{\partial \Theta_{N_{\Theta}}} \end{pmatrix}$$
(27)

The augmented system containing the original set of equations $G(x; \Theta)$ and sensitivity equations is called $G(x; \Theta)$. The size of $G(x; \Theta)$ is equal to $N_s = N_x(N_{\Theta} + 1)$.

$$\mathbf{G}\left(x;\Theta\right) = \begin{bmatrix} G(x;\Theta) \\ \bar{J}_{x}(x;\Theta)\bar{S}(x;\Theta) + \bar{J}_{\Theta}(x;\Theta) \end{bmatrix} \tag{28}$$

The initial conditions are described as

$$\mathbf{G}\left(x(t_0);\Theta\right) = \begin{bmatrix} x(t_0), & \frac{\mathrm{d}x(t_0)}{d\Theta_1}, & \cdots, & \frac{dx(t_0)}{d\Theta_{N_{\Theta}}} \end{bmatrix}^{\mathsf{T}} = (29)$$

$$= \begin{bmatrix} x_0, & 0, & \cdots, & 0 \end{bmatrix}^{\mathsf{T}}$$

3. Results

454

455

456

458

459

464

468

470

472

473

475

476

477

479

480

481

483

485

The details of the process model and parameters are provided in Sliczniuk and Oinas [19]. The process model was validated in the following range of operating conditions: temperatures between $30-40^{\circ}C$, pressures between 100-200 bar, and mass flow rates between $3.33-6.67\cdot10^{-5}$ kg/s. The sensitivity analysis is performed at the midpoint of the validated range: $35^{\circ}C$, 150 bar and $5\cdot10^{-5}$ kg/s. This study examines the impact of pressure change on the state space and extraction yield through local sensitivity analysis. The local sensitivity analysis results can be interpreted as the system's response to an infinitesimal deviation in pressure.

As discussed in Section 2.1, at low velocity, the fluid can be treated as incompressible, which results in the instant propagation of pressure throughout the system, enabling a single pressure value to be considered for the entire system. In response to a pressure change, the energy equation experiences a simultaneous deviation across the entire spatial domain. This pressure change impacts the fluid temperature within the computational domain, while boundary values are constrained by conditions specified at the domain's extremes. Dirichlet boundary conditions impose a fixed temperature value at the inlet, creating a thermal gradient that propagates through the system. Alternatively, Neumann boundary conditions specify a heat flux at the

extremes. The zero Neumann boundary conditions are applied to ensure a uniform response to the pressure change of temperatures at the inlet, outlet, and within the extractor.

488

490

492

493

494

495

496

497

498

499

500

501

502

503

504

505

507

509

510

511

512

513

514

516

518

520

521

522

523

Figure 5 illustrates the sensitivity of the solute concentration in the solid phase to pressure changes. As discussed in Section 2.2.1, the velocity of a fluid is inversely proportional to its density, indicating that increased pressure reduces the fluid velocity. This results in an extended residence time, allowing for longer interaction between the solute and solvent. Initially, the extraction process operates in the kineticcontrolled regime, where the concentration gradient is high, and solute solubility is the limiting factor. As noted by Sliczniuk and Oinas [19], the system is considered far from saturation, which explains the low initial system response. This low initial response was also observed in the sensitivity analysis by Fiori et al. [20]. The system's response becomes more pronounced as the concentration gradient decreases and the extraction shifts from the kinetic-controlled to the diffusion-controlled regime. In Figure 5, all $\frac{dc_s}{dP}$ values are negative, which indicates a faster mass transfer from the solid phase, corresponding to enhanced mass transfer. Over time, as the amount of solute decreases, it becomes a limiting factor, reducing the effect of pressure changes on the system. Eventually, the sensitivities approach zero asymptotically as the solute is washed out of the bed.

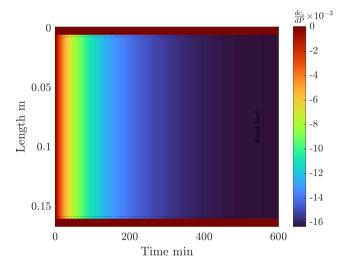


Figure 5: The effect of P_{in} change on C_s .

Figure 6 illustrates the sensitivity of solute concentration in the fluid phase to pressure changes. Compared to Figure 5, the dynamic behaviour of fluid phase sensitivities is more apparent. Due to advection, the sensitivities related to the fluid phase move across the system in the direction of flow. Initially, the system response is low despite the pressure increase improving mass transfer, reflecting the previously discussed idle period. As the process continues, the sensitivities increase, indicating faster mass transfer from the solid phase. The corresponding improvement in the mass transfer from the solid particles to the fluid is represented by the positive values in Figure 6. When the solute in the solid

phase becomes a limiting factor, the extraction rate slows, and sensitivities eventually approach zero asymptotically.

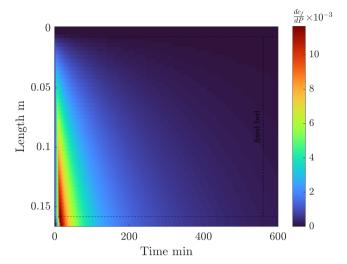


Figure 6: The effect of P_{in} change on C_f .

Figure 7 shows how sensitive the extraction yield is to pressure changes over an extended period for various pressure values. Initially, all sensitivity curves remain nearly flat, indicating a delayed response in the system. Due to the reduced fluid velocity, the solute reaches the extractor's outlet later, causing minor negative sensitivities to appear. Once the solute exits the extractor, the sensitivity curves rise. Positive yield sensitivities indicate improved process efficiency and enhanced mass transfer. The peak in $\frac{dy}{dP_{in}}$ represents the point of greatest deviation from the original system. Eventually, the sensitivities decline and converge towards zero as the concentration gradient becomes a limiting factor, reducing the impact of enhanced mass transfer.

As presented in Figure 7, higher sensitivities are observed for a low-pressure system. At lower pressures, the supercritical fluid has lower density and solvating power, which results in less efficient extraction, as shown by data given by Sliczniuk and Oinas [19]. Small changes in pressure at low pressures can significantly impact the solute's solubility and, consequently, the extraction yield. Moreover, near the critical point, small changes in pressure can lead to significant changes in the physical properties of the supercritical fluid, such as density and viscosity, and therefore to higher sensitivity of the system state-space.

4. Conclusions

Sensitivity analysis is a tool used to understand how the parameters of the model affect its output. The presented formulation involves derivative-based local sensitivity analysis of the model solution with respect to selected parameters and controls. This work implemented automatic differentiation to derive the sensitivity equations. Local sensitivity analysis techniques consider only a small region of parameter space, and the conclusions derived from such an analysis are limited to local conditions. In the case of dynamic systems, the

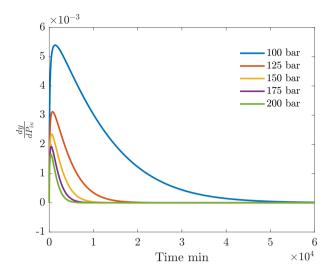


Figure 7: The effect of P_{in} change on y(t).

outcome of local sensitivity analysis quantifies how the state of the system or its output varies over time with respect to small perturbations in parameters.

Although local sensitivity analysis can be performed with respect to any model parameter, this study focuses specifically on the effect of pressure. Under the selected operating conditions, it was observed for all the cases that a pressure increment enhances mass transfer, leading to a faster mass transfer of solute from the particles. Consequently, negative sensitivities can be observed in the diagram for the solid phase. The corresponding response in the fluid phase is characterized by positive-valued sensitivities, indicating that a greater amount of solute is transported into the fluid phase. As a result, the extraction yield is improved and characterized by positive sensitivities. Given that the results of the local sensitivity analysis depend on the operating point, the analysis was repeated at different pressures. It was observed that the system responses at low pressures were stronger than those at higher pressures. This behaviour can be explained by the rapid changes in solvent properties occurring near the critical point of CO₂.

Local sensitivity analysis results provide valuable information by identifying which parameters are influential and how these influences change over time. One application of sensitivity analysis is to spot discrepancies between model predictions and actual experimental results. Identifying unexpected system responses prompts further investigation and refinement of the process model. The sensitivity analysis results can be used to design future experiments by indicating which parameters should be varied and monitored. Moreover, the parameters which are characterized by low sensitivity can be the subject of model refinement.

Acknowledgements

This work was supported by: NovelBaltic, CEForestry (IBC), BIO4P (BF).

595 References

596

597

600

601

602

603

604

605

606

607

608

609

610

611

612

613

614

617

618

619

620

621

622

623

625

626

627

628

629

630

631

632

633

634

635

636

637

638

639

643

644

646

647

648

651

652

653

654

655

656

657

659

660

661

- [1] G. Sodeifian and S.A. Sajadian. Investigation of essential oil extraction and antioxidant activity of echinophora platyloba dc. using supercritical carbon dioxide. <u>The Journal of Supercritical Fluids</u>, 121: 52–62, March 2017. ISSN 0896-8446. doi: 10.1016/j.supflu.2016.11.
- [2] E. Reverchon, G. Donsi, and L.S. Osseo. Modeling of supercritical fluid extraction from herbaceous matrices. <u>Industrial & Engineering</u> <u>Chemistry Research</u>, 32(11):2721–2726, Nov 1993. doi: 10.1021/ ie00023a039.
- [3] H. Sovova. Rate of the vegetable oil extraction with supercritical CO₂. modelling of extraction curves. <u>Chemical Engineering Science</u>, 49(3): 409–414, 1994. doi: 10.1016/0009-2509(94)87012-8.
- [4] E. Weidner. Impregnation via supercritical CO₂—what we know and what we need to know. <u>The Journal of Supercritical Fluids</u>, 134:220– 227, April 2018. ISSN 0896-8446. doi: 10.1016/j.supflu.2017.12. 024.
- [5] N.D. Machado, J.E. Mosquera, R.E. Martini, María L. Goñi, and N.A. Gañán. Supercritical CO₂-assisted impregnation/deposition of polymeric materials with pharmaceutical, nutraceutical, and biomedical applications: A review (2015–2021). The Journal of Supercritical Fluids, 191:105763, December 2022. ISSN 0896-8446. doi: 10.1016/j.supflu.2022.105763.
- [6] M. Fathi, G. Sodeifian, and S.A Sajadian. Experimental study of ketoconazole impregnation into polyvinyl pyrrolidone and hydroxyl propyl methyl cellulose using supercritical carbon dioxide: Process optimization. <u>The Journal of Supercritical Fluids</u>, 188:105674, Sep 2022. ISSN 0896-8446. doi: 10.1016/j.supflu.2022.105674.
- [7] L. Padrela, M. A. Rodrigues, A. Duarte, Ana M.A. Dias, Mara E.M. Braga, and H. C. de Sousa. Supercritical carbon dioxide-based technologies for the production of drug nanoparticles/nanocrystals a comprehensive review. Advanced Drug Delivery Reviews, 131:22–78, June 2018. ISSN 0169-409X. doi: 10.1016/j.addr.2018.07.010.
- [8] P. Franco and I. De Marco. Nanoparticles and nanocrystals by supercritical CO₂-assisted techniques for pharmaceutical applications: A review. <u>Applied Sciences</u>, 11(4):1476, Feb 2021. ISSN 2076-3417. doi: 10.3390/app11041476.
- [9] N. S. Ardestani, G Sodeifian, and S.A Sajadian. Preparation of phthalocyanine green nano pigment using supercritical CO₂ gas antisolvent (gas): experimental and modeling. <u>Heliyon</u>, 6(9):e04947, Sep 2020. ISSN 2405-8440. doi: 10.1016/j.heliyon.2020.e04947.
- [10] G. Sodeifian, S.A. Sajadian, and R. Derakhsheshpour. CO₂ utilization as a supercritical solvent and supercritical antisolvent in production of sertraline hydrochloride nanoparticles. <u>Journal of CO₂ Utilization</u>, 55:101799, Jan 2022. ISSN 2212-9820. doi: 10.1016/j.jcou.2021. 101799.
- [11] O. Singh, Z. Khanam, N. Misraand, and M.K. Srivastava. Chamomile (matricaria chamomilla l.): An overview. <u>Pharmacognosy Reviews</u>, 5 (9):82, 2011. ISSN 0973-7847. doi: 10.4103/0973-7847.79103.
- [12] J. Srivastava. Extraction, characterization, stability and biological activity of flavonoids isolated from chamomile flowers. <u>Molecular and Cellular Pharmacology</u>, 1(3):138–147, August 2009. ISSN 1938-1247. doi: 10.4255/mcpharmacol.09.18.
- [13] A. Orav, A. Raal, and E. Arak. Content and composition of the essential oil ofchamomilla recutita(l.) rauschert from some european countries. <u>Natural Product Research</u>, 24(1):48–55, Jan 2010. ISSN 1478-6427. doi: 10.1080/14786410802560690.
- [14] M. Goto, B.C. Roy, and T. Hirose. Shrinking-core leaching model for supercritical-fluid extraction. <u>The Journal of Supercritical Fluids</u>, 9 (2):128–133, June 1996. doi: 10.1016/s0896-8446(96)90009-1.
- [15] H. Sovová, J. Kučera, and J. Jež. Rate of the vegetable oil extraction with supercritical CO₂—ii. extraction of grape oil. <u>Chemical Engineering Science</u>, 49(3):415–420, 1994. ISSN 0009-2509. doi: 10.1016/0009-2509(94)87013-6.
- [16] H. Sovova, R. Komers, J. Kucuera, and J. Jezu. Supercritical carbon dioxide extraction of caraway essential oil. <u>Chemical Engineering Science</u>, 49(15):2499–2505, Aug 1994. doi: 10.1016/0009-2509(94) e0058-x.

[17] K. D. Bartle, A. A. Clifford, S. B. Hawthorne, John J. Langenfeld, D. J. Miller, and R. Robinson. A model for dynamic extraction using a supercritical fluid. <u>The Journal of Supercritical Fluids</u>, 3(3):143– 149, September 1990. <u>ISSN 0896-8446</u>. doi: 10.1016/0896-8446(90) 90039-0.

664

665

666

667

668

669

670

671

672

673

674

675

676

677

678

679

680

681

682

683

684

685

686

687

688

690

691

692

693

694

695

696

697

698

699

700

701

702

703

704

705

706

707

708

709

711

712

713

- [18] E. Reverchon. Mathematical modeling of supercritical extraction of sage oil. <u>AIChE Journal</u>, 42(6):1765–1771, June 1996. ISSN 1547-5905. doi: 10.1002/aic.690420627.
- [19] O. Sliczniuk and P. Oinas. Mathematical modelling of essential oil supercritical carbon dioxide extraction from chamomile flowers. <u>The</u> <u>Canadian Journal of Chemical Engineering</u>, 2024. doi: 10.1002/cjce. 25557.
- [20] L. Fiori, D. Calcagno, and P. Costa. Sensitivity analysis and operative conditions of a supercritical fluid extractor. <u>The Journal of Supercritical Fluids</u>, 41(1):31–42, May 2007. doi: 10.1016/j.supflu. 2006.09.005.
- [21] M.M. Santos, E.A. Boss, and R. Maciel Filho. Supercritical extraction of oleaginous: parametric sensitivity analysis. <u>Brazilian Journal of Chemical Engineering</u>, 17(4–7):713–720, December 2000. ISSN 0104-6632, doi: 10.1590/s0104-66322000000400035.
- [22] T. Hatami and O.N. Ciftci. Techno-economic sensitivity assessment for supercritical CO₂ extraction of lycopene from tomato processing waste. <u>The Journal of Supercritical Fluids</u>, 204:106109, Jan 2024. ISSN 0896-8446. doi: 10.1016/j.supflu.2023.106109.
- [23] J. D. Anderson Jr. <u>Computational fluid dynamics: The basics with</u> applications. McGraw-Hill, 1995. ISBN 9780071132107.
- [24] J. D. Anderson Jr. <u>Fundamentals of Aerodynamics</u>. McGraw-Hill Education, 2023. ISBN 9781264151929.
- [25] N. R. Bulley, M. Fattori, A. Meisen, and L. Moyls. Supercritical fluid extraction of vegetable oil seeds. <u>Journal of the American</u> Oil Chemists' Society, 61(8):1362–1365, Aug 1984. doi: 10.1007/ bf02542243.
- [26] M. Spiro and M. Kandiah. Extraction of ginger rhizome: partition constants and other equilibrium properties in organic solvents and in supercritical carbon dioxide. <u>International Journal of Food Science & Technology</u>, 25(5):566–575, <u>June 2007</u>. doi: 10.1111/j.1365-2621. 1990 tb01116 x
- [27] H. Sovova. Broken-and-intact cell model for supercritical fluid extraction: Its origin and limits. The Journal of Supercritical Fluids, 129:3–8, Nov 2017. doi: 10.1016/j.supflu.2017.02.014.
- [28] J. Gmehling, M. Kleiber, B. Kolbe, and J. Rarey. <u>Chemica Thermodynamics for Process Simulation</u>. Wiley, Mar 2019. doi 10.1002/9783527809479.
- [29] R.P. Dickinson and R. J. Gelinas. Sensitivity analysis of ordinary differential equation systems—a direct method. <u>Journal of Computational Physics</u>, 21(2):123–143, June 1976. doi: 10.1016/0021-9991(76)90007-3.
- [30] T. Maly and L.R. Petzold. Numerical methods and software for sensitivity analysis of differential-algebraic systems. <u>Applied Numerical Mathematics</u>, 20(1-2):57–79, Feb 1996. doi: 10.1016/0168-9274(95) 00117-4.

Sensitivity Analysis

714	Nomenclature			Reynolds number	-	750
715			r_e	Mass transfer kinetic term	kg/m ³ /s	751
716	$ar{J}_{\Theta}$	Jacobian matrix with respect to the parameters	S	Sensitivity equations		752
717	$ar{J}_{\scriptscriptstyle X}$	Jacobian matrix with respect to the state variables	T	Temperature	K	753
718	$ar{S}$	Sensitivity matrix	t	Time	S	754
719	\dot{S}	Time derivative of the sensitivity equations	t_0	Initial extraction time	S	755
720	G	Augmented system	t_f	Total extraction time	S	756
721	\boldsymbol{A}	Total cross-section of the bed $$\rm m^2$$	T_{in}	Inlet temperature	K	757
722	A_f	Cross-section of the bed occupied by the fluid $$ $$ m^2	T_{out}	Outlet temperature	K	758
723	c_f	Concentration of solute in the fluid phase kg/m ³	и	Superficial velocity	m/s	759
724	c_f^*	Concentration of solute at the solid-fluid interface	v	Linear velocity	m/s	760
725		kg/m ³	x	State vector		761
726	c_p	Concentration of solute in the core of a pore kg/m ³	y	Extraction yield	g	762
727	c_s	Concentration of solute in the solid phase kg/m ³	Z	Spatial direction	m	763
728	c_s^*	Concentration of solute at the solid-fluid interface	Greek	symbols		764
729		kg ³	ϵ	Unobservable error	g	765
730 731	c_{f0}	Initial concentration of solute in the fluid phase kg/m ³	γ	Decay function	-	766
732	c_{pf}	Concentration of solute at the pore opening kg/m ³	μ	Sphericity coefficient	-	767
733	c_{s0}	Initial concentration of solute in the solid phase	Φ	Bed porosity	-	768
734		kg/m ³	$ ho_f$	Fluid density	kg/m ³	769
735	D_e^M	Axial diffusion coefficient m ² /s	$ ho_s$	Bulk density of the solid	kg/m ³	770
736	D_i	Internal diffusion coefficient m ² /s	σ	Standard deviation	g	771
737	D_i^R	Reference value of internal diffusion coefficient m ² /s	Θ	Parameter space		772
738	0	Internal energy J/kg	θ	Vector of unknown parameters		773
739	e F	Mass flow rate kg/s	Υ	Decay coefficient	-	774
740	G	Vector of discretized differential equations	Abber	rivations		775
741	h	Enthalpy J	BIC	Broke-and-Intact Cell model		776
742		Mass partition coefficient -	HBD	Hot Ball Diffusion		777
743	k _m	Volumetric partition coefficient -	SC	Shrinking Core		778
744	k_p		SFE	Supercritical Fluid Extraction		779
745	L l	Length of the fixed bed m Characteristic dimension of particles m				
746	ı P	Characteristic dimension of particles m Pressure bar				
747						
748	p	Probability distribution model -				
749	r	Particle radius m				