

Module Interface Specification for STEM Moiré GPA

Alexandre Pofelski
macid: pofelska
github: slimpotatoes

November 20, 2017

1 Revision History

| Date | Version | Notes |
|------------|---------|-------------|
| 14/11/2017 | 1.0 | First draft |

2 Symbols, Abbreviations and Acronyms

The same Symbols, Abbreviations and Acronyms as in the SRS, the TestPlan and the MG (available in [STEM Moiré GPA](#) repository) are used in the Module Interface Specifications document.

addition to document

Contents

| | | |
|----------|---|-----------|
| 1 | Revision History | i |
| 2 | Symbols, Abbreviations and Acronyms | ii |
| 3 | Introduction | 1 |
| 4 | Notation | 1 |
| 5 | Module Decomposition | 1 |
| 6 | MIS of STEM Moiré GPA Control Module (M 2) | 3 |
| 6.1 | Module | 3 |
| 6.2 | Uses | 3 |
| 6.3 | Syntax | 3 |
| 6.3.1 | Exported Access Programs | 3 |
| 6.4 | Semantics | 3 |
| 6.4.1 | State Variables | 3 |
| 6.4.2 | Access Routine Semantics | 3 |
| 7 | MIS of STEM Moiré GPA GUI Module (M 3) | 4 |
| 7.1 | Module | 4 |
| 7.2 | Uses | 4 |
| 7.3 | Syntax | 4 |
| 7.3.1 | Exported Access Programs | 4 |
| 7.4 | Semantics | 4 |
| 7.4.1 | State Variables | 4 |
| 7.4.2 | Access Routine Semantics | 5 |
| 8 | MIS of Input Module (M 4) | 6 |
| 8.1 | Module | 6 |
| 8.2 | Uses | 6 |
| 8.3 | Syntax | 7 |
| 8.3.1 | Exported Access Programs | 7 |
| 8.4 | Semantics | 7 |
| 8.4.1 | State Variables | 7 |
| 8.4.2 | Access Routine Semantics | 7 |
| 9 | MIS of SMH Simulation (M 5) | 8 |
| 9.1 | Module | 8 |
| 9.2 | Uses | 8 |
| 9.3 | Syntax | 8 |
| 9.3.1 | Exported Access Programs | 8 |

| | | |
|-----------|--|-----------|
| 9.4 | Semantics | 8 |
| 9.4.1 | State Variables | 8 |
| 9.4.2 | Access Routine Semantics | 9 |
| 10 | MIS of GPA Module (M 6) | 9 |
| 10.1 | Module | 9 |
| 10.2 | Uses | 9 |
| 10.3 | Syntax | 9 |
| 10.3.1 | Exported Access Programs | 9 |
| 10.4 | Semantics | 10 |
| 10.4.1 | State Variables | 10 |
| 10.4.2 | Access Routine Semantics | 10 |
| 11 | MIS of Mask Module (M 7) | 10 |
| 11.1 | Module | 10 |
| 11.2 | Uses | 10 |
| 11.3 | Syntax | 10 |
| 11.3.1 | Exported Access Programs | 10 |
| 11.4 | Semantics | 11 |
| 11.4.1 | State Variables | 11 |
| 11.4.2 | Access Routine Semantics | 11 |
| 12 | MIS of Unstrained region (M 8) | 11 |
| 12.1 | Module | 11 |
| 12.2 | Uses | 11 |
| 12.3 | Syntax | 11 |
| 12.3.1 | Exported Access Programs | 11 |
| 12.4 | Semantics | 12 |
| 12.4.1 | State Variables | 12 |
| 12.4.2 | Access Routine Semantics | 12 |
| 13 | MIS of Conversion Module (M 9) | 12 |
| 13.1 | Module | 12 |
| 13.2 | Uses | 12 |
| 13.3 | Syntax | 12 |
| 13.3.1 | Exported Access Programs | 12 |
| 13.4 | Semantics | 12 |
| 13.4.1 | State Variables | 12 |
| 13.4.2 | Access Routine Semantics | 12 |
| 14 | MIS of 2D Strain Tensor Module (M 10) | 13 |
| 14.1 | Module | 13 |
| 14.2 | Uses | 13 |

| | | |
|-----------|---|-----------|
| 14.3 | Syntax | 13 |
| 14.3.1 | Exported Access Programs | 13 |
| 14.4 | Semantics | 13 |
| 14.4.1 | State Variables | 13 |
| 14.4.2 | Access Routine Semantics | 13 |
| 15 | MIS of Fourier Transform Module (M 11) | 13 |
| 15.1 | Module | 13 |
| 15.2 | Uses | 13 |
| 15.3 | Syntax | 14 |
| 15.3.1 | Exported Access Programs | 14 |
| 15.4 | Semantics | 14 |
| 15.4.1 | State Variables | 14 |
| 15.4.2 | Access Routine Semantics | 14 |
| 16 | MIS of Gradient Module (M 12) | 14 |
| 16.1 | Module | 14 |
| 16.2 | Uses | 15 |
| 16.3 | Syntax | 15 |
| 16.3.1 | Exported Access Programs | 15 |
| 16.4 | Semantics | 15 |
| 16.4.1 | State Variables | 15 |
| 16.4.2 | Access Routine Semantics | 15 |
| 17 | MIS of Least Square Fit Method Module (M 13) | 15 |
| 17.1 | Module | 15 |
| 17.2 | Uses | 15 |
| 17.3 | Syntax | 15 |
| 17.3.1 | Exported Access Programs | 15 |
| 17.4 | Semantics | 16 |
| 17.4.1 | State Variables | 16 |
| 17.4.2 | Access Routine Semantics | 16 |
| 18 | MIS of Phase Operation Module (M 14) | 16 |
| 18.1 | Module | 16 |
| 18.2 | Uses | 16 |
| 18.3 | Syntax | 16 |
| 18.3.1 | Exported Access Programs | 16 |
| 18.4 | Semantics | 16 |
| 18.4.1 | State Variables | 16 |
| 18.4.2 | Access Routine Semantics | 16 |

| | |
|---|-----------|
| 19 MIS of Data Structure Module (M 15) | 17 |
| 19.1 Module | 17 |
| 19.2 Uses | 17 |
| 19.3 Syntax | 17 |
| 19.3.1 Exported Access Programs | 17 |
| 19.4 Semantics | 18 |
| 19.4.1 State Variables | 18 |
| 19.4.2 Access Routine Semantics | 18 |
| 20 MIS of Generic GUI/Plot Module (M 16) | 18 |
| 20.1 Module | 18 |
| 20.2 Uses | 18 |
| 20.3 Syntax | 19 |
| 20.3.1 Exported Access Programs | 19 |
| 20.4 Semantics | 19 |
| 20.4.1 State Variables | 19 |
| 20.4.2 Access Routine Semantics | 19 |
| 21 Appendix | 20 |

3 Introduction

The following document details the Module Interface Specifications for STEM Moiré GPA. The full documentation and implementation can be found in [STEM Moiré GPA](#) repository.

4 Notation

The structure of the MIS for modules comes from [?], with the addition that template modules have been adapted from [?]. The mathematical notation comes from Chapter 3 of [?]. For instance, the symbol $:=$ is used for a multiple assignment statement and conditional rules follow the form $(c_1 \Rightarrow r_1 | c_2 \Rightarrow r_2 | \dots | c_n \Rightarrow r_n)$.

The following table summarizes the primitive data types used by STEM Moiré GPA.

| Data Type | Notation | Description |
|----------------|--------------|--------------------------|
| character | char | a single symbol or digit |
| integer | \mathbb{Z} | an integer number |
| natural number | \mathbb{N} | a natural number |
| real | \mathbb{R} | a real number |

The specification of STEM Moiré GPA uses some derived data types: sequences, strings, and tuples. Sequences are lists filled with elements of the same data type. Strings are sequences of characters. Tuples contain a list of values, potentially of different types. In addition, STEM Moiré GPA uses functions, which are defined by the data types of their inputs and outputs. Local functions are described by giving their type signature followed by their specification.

5 Module Decomposition

The following table is taken directly from the Module Guide document for this project.

| Level 1 | Level 2 |
|--------------------------|-----------------------------|
| Hardware-Hiding Module | |
| | Input |
| | STEM Moiré GPA Control |
| | STEM Moiré GPA GUI |
| | User Input |
| Behaviour-Hiding Module | SMH simulation |
| | GPA |
| | Mask |
| | Unstrained region |
| | Conversion |
| | 2D strain tensor |
| | Fourier Transform |
| | Least square fitting method |
| Software Decision Module | Phase calculation |
| | Gradient |
| | Generic GUI/Plot |
| | Data structure |

Table 1: Module Hierarchy

LIST ALL MIS to refer them in other document

6 MIS of STEM Moiré GPA Control Module (M 2)

6.1 Module

main

6.2 Uses

- STEM Moiré GPA GUI
- Processing modules
 - Unstrained region
 - Conversion
 - SMH Simulation
 - GPA
 - 2D Strain Tensors
- Input

6.3 Syntax

6.3.1 Exported Access Programs

| Name | In | Out | Exceptions |
|------|----|-----|------------|
| main | - | - | - |

6.4 Semantics

STEM Moiré GPA is designed to have the different steps of the process flow driven by user directly through GUI_SMG. The STEM Moiré GPA Control Module uses the events in STEM Moiré GPA GUI to use the processing modules in the order defined by the user.

6.4.1 State Variables

6.4.2 Access Routine Semantics

main():

- transition: A réfléchir
GUIFlow(): *# Software permanently running until user abort it by closing the GUI*
(event_Input()
→ Get the path pathISMH and pathIC from the user \wedge
load_files(pathISMH,pathIC))

```

(event_SimSMH() → SMHsim())
(event_GPA() → gpa())
(event_URef() → ZeroStrain())
(event_Conversion() → conversion())
(event_StrainCalc() → CalcStrain())

```

7 MIS of STEM Moiré GPA GUI Module (M 3)

7.1 Module

GUI_SMG

7.2 Uses

- Generic GUI/Plot
- Data Structure

7.3 Syntax

7.3.1 Exported Access Programs

| Name | In | Out | Exceptions |
|--------------------|----|-----|------------|
| GUIFlow | - | - | - |
| GUI_SMH | - | - | - |
| GUI_Phase | - | - | - |
| GUI_Conv | - | - | - |
| event_Input() | - | - | - |
| event_SMHSim() | - | - | - |
| event_GPA() | - | - | - |
| event_URef() | - | - | - |
| event_StrainCalc() | - | - | - |

7.4 Semantics

STEM Moiré GPA process flow is driven by user through GUI_SMG. User triggers the events that start the selected processing step.

7.4.1 State Variables

Win_Flow: GUI object Win_SMHSim: GUI object Win_Phase: GUI object Win_FTSMH:
GUI object Win_Conv: GUI object

7.4.2 Access Routine Semantics

GUI embedding the process flow into buttons triggering events. It is the user role to execute the process flow

GUIFlow():

- transition:
 1. Win_Flow=fig('Win_Flow')
 2. button(Win_Flow,5,'Input','SMHSim','GPA','URef','StrainCalc')
 3. plot()

Events triggered by each button pressed by the user

event_Input():

- transition: Trigger event_Input when button_Input pressed

event_SMHSim():

- transition: Trigger event_SMHSim when button_SMHSim pressed

event_GPA():

- transition: Trigger event_GPA when button_GPA pressed

event_URef():

- transition: Trigger event_URef when button_URef pressed

event_StrainCalc():

- transition: Trigger event_StrainCalc when button_StrainCalc press

GUI to display the simulation of the STEM Moiré hologram using the reference image and to let the user input M (from R 4, R 5)

GUI_SMH():

- transition:
 1. Win_SMHSim=fig('Win_SMHSim',read($I_{SMH_{exp}}$),load($\tilde{I}_{SMH_{exp}}$),load($\tilde{I}_{SMH_{sim}}$),circle(M))
 2. plot()

GUI to display the phase resulting from the GPA algorithm and to let the user input U (from R 8)

GUI_Phase():

- transition:

1. Win_Phase=fig('Win_Phase',red($\Delta \vec{g}^{M_{\text{exp}}}$),rectangle(U))
2. plot()

GUI to display the window to let the user input n and m (from R 11)

GUI_Conv():

- transition:

1. Win_Conv=fig('Win_Conv',entry_field(n),entry_field(m))
2. plot()

8 MIS of Input Module (M 4)

8.1 Module

Input

8.2 Uses

- STEM Moié GPA GUI
- Data Structure

8.3 Syntax

8.3.1 Exported Access Programs

| Name | In | Out | Exceptions |
|-----------------|------------|--|------------|
| load_files | string | - | FilePath |
| load_mask | GUI object | - | NoMask |
| load_U | GUI object | - | NoU |
| load_nm | GUI object | - | NoConv |
| $I_{SMH_{exp}}$ | - | $f : \mathbb{N}^2 \rightarrow \mathbb{R}$ | - |
| p | - | \mathbb{R}^{+*} | - |
| $I_{C_{ref}}$ | - | $f : \mathbb{N}^2 \rightarrow \mathbb{R}$ | - |
| p_{ref} | - | \mathbb{R}^{+*} | - |
| U | - | - | - |
| M | - | $(x_c, y_c) \in \mathbb{R}^2, R \in \mathbb{R}^{+*}$ | - |
| n | - | \mathbb{Z} | - |
| m | - | \mathbb{Z} | - |

8.4 Semantics

8.4.1 State Variables

For R 1 and IM 1 in the SRS document,

$I_{SMH_{exp}} : f : \mathbb{N}^2 \rightarrow \mathbb{R}$

$p : \mathbb{R}^{+*}$

$I_{C_{ref}} : f : \mathbb{N}^2 \rightarrow \mathbb{R}$

$p_{ref} : \mathbb{R}^{+*}$

For R 5 and IM 2 in the SRS document,

$M : (x_c, y_c) \in \mathbb{R}^2, R \in \mathbb{R}^{+*}$

For R 8 and IM 3 in the SRS document,

$U :$

For R 11 and For IM 4 in the SRS document,

$n : \mathbb{Z}$

$m : \mathbb{Z}$

8.4.2 Access Routine Semantics

load_files(pathISMH,pathIC):

- transition: pathISMH and pathIC are the file paths for the input files. The following procedure is performed:
 1. The .dm3 files are read and their respective metafiles are collected.
 2. From the metafile, $I_{SMH_{\text{exp}}}$, $I_{C_{\text{ref}}}$, p and p_{ref} are extracted to modify their respective state variable.
 - 3.
 4. The variables $I_{SMH_{\text{exp}}}$, $I_{C_{\text{ref}}}$, p and p_{ref} are stored in the data structure using the access program store
- output: $I_{SMH_{\text{exp}}}$, $I_{C_{\text{ref}}}$, p , p_{ref}
- exception:

9 MIS of SMH Simulation (M 5)

9.1 Module

SMHSimCalc

9.2 Uses

- Fourier Transform
- Input
- Data Structure

9.3 Syntax

9.3.1 Exported Access Programs

| Name | In | Out | Exceptions |
|--------|---|---|-------------|
| SMHsim | $I_{SMH_{\text{exp}}} : \mathbb{R}^2 \rightarrow \mathbb{R}$ $I_{C_{\text{ref}}} : \mathbb{R}^2 \rightarrow \mathbb{R}$, $p \in \mathbb{R}^{+*}$, $p_{\text{ref}} \in \mathbb{R}^{+*}$ | $\tilde{I}_{SMH_{\text{exp}}} : \mathbb{R}^2 \rightarrow \mathbb{C}$ $\tilde{I}_{SMH_{\text{sim}}} : \mathbb{R}^2 \rightarrow \mathbb{C}$ $N_{\text{lim}} \in \mathbb{N}^*$ | Nlim.zero() |

9.4 Semantics

9.4.1 State Variables

None

9.4.2 Access Routine Semantics

$\text{SMHsim}(I_{SMH_{\text{exp}}}, I_{C_{\text{ref}}}, p, p_{\text{ref}}):$

- output:

– $\tilde{I}_{SMH_{\text{exp}}}$ such that

$$\tilde{I}_{SMH_{\text{exp}}}(\vec{v}) = \mathcal{FT}[I_{SMH_{\text{exp}}}(\vec{r})]$$

– $\tilde{I}_{SMH_{\text{sim}}}$ such that

$$\tilde{I}_{SMH_{\text{sim}}}(\vec{v}) = \frac{1}{p^2} \sum_{\vec{q} \in Q_{\text{lim}}} \mathcal{FT}[I_{C_{\text{ref}}}(\vec{v} - \frac{\vec{q}}{p})]$$

with $Q_{\text{lim}} = \{\forall(n, m) \in \mathbb{Z}^2 \cap [-N_{\text{lim}}, N_{\text{lim}}]^2, \vec{q} = n\vec{u}_x + m\vec{u}_y\}$

and $N_{\text{lim}} = \Xi(\frac{p}{p_{\text{ref}}})$ with Ξ the floor function

- exception:

10 MIS of GPA Module (M 6)

10.1 Module

GPACalc

10.2 Uses

- Mask
- Fourier Transform
- Phase
- Gradient
- Data Structure

10.3 Syntax

10.3.1 Exported Access Programs

| Name | In | Out | Exceptions |
|------|---|--|------------|
| gpa | $\tilde{I}_{SMH_{\text{exp}}} : \mathbb{R}^2 \rightarrow \mathbb{C}$, $M : \mathbb{R}^2 \rightarrow \mathbb{R}$, $\vec{g}_0 : \mathbb{R}^2 \rightarrow \mathbb{R}$ | $P_{\vec{g}} : \mathbb{R}^2 \rightarrow \mathbb{R}$, $\vec{\Delta g} : \mathbb{R}^2 \rightarrow \mathbb{R}$ | - |

10.4 Semantics

10.4.1 State Variables

10.4.2 Access Routine Semantics

$\text{gpa}(\tilde{I}_{SMH_{\text{exp}}}, M, \vec{g}_0)$:

- output:

- $P_{\vec{g}}$ such that

$$\forall \vec{r} \in \mathbb{R}^2, P_{\vec{g}}(\vec{r}) = \arg(i\mathcal{FT}[M \times \tilde{I}_{SMH_{\text{exp}}}])$$

- $\vec{\Delta g}$ such that

$$\forall \vec{r} \in \mathbb{R}^2, \Delta \vec{g}(\vec{r}) = \frac{1}{2\pi} \text{grad}(\text{unwrap}(P_{\vec{g}}(\vec{r}))) - \vec{g}_0(\vec{r})$$

- $P_{\Delta \vec{g}}$ such that

$$\forall \vec{r} \in \mathbb{R}^2, P_{\Delta \vec{g}}(\vec{r}) = \text{wrap}(\text{unwrap}[P_{\vec{g}}(\vec{r})] - 2\pi \vec{g}_0(\vec{0}) \cdot \vec{r})$$

- exception:

11 MIS of Mask Module (M 7)

11.1 Module

Mask

11.2 Uses

- STEM Moiré GPA GUI
- Data structure

11.3 Syntax

11.3.1 Exported Access Programs

| Name | In | Out | Exceptions |
|-------|---|--|------------|
| MCirc | $(x_c, y_c) \in \mathbb{N}^2$, $R \in \mathbb{R}^{+*}$ | $M : \mathbb{R}^2 \rightarrow \mathbb{R}, \vec{g}_0 : \mathbb{R}^2 \rightarrow \mathbb{R}^2$ | - |

11.4 Semantics

11.4.1 State Variables

11.4.2 Access Routine Semantics

MaskGene(x_c, y_c, R):

- output:

- M such that

$$M(x, y) = \begin{cases} 1, & (x - x_c)^2 + (y - y_c)^2 \leq R^2 \\ 0, & (x - x_c)^2 + (y - y_c)^2 > R^2 \end{cases}$$

- \vec{g}_0 such that

$$\forall \vec{r} \in \mathbb{R}^2, \vec{g}_0(\vec{r}) = \begin{bmatrix} x_c \\ y_c \end{bmatrix}$$

- exception:

12 MIS of Unstrained region (M 8)

12.1 Module

URefCalc

12.2 Uses

- Least Square Fit
- Input
- Data Structure

12.3 Syntax

12.3.1 Exported Access Programs

| Name | In | Out | Exceptions |
|------------|---|--|------------|
| ZeroStrain | $\vec{\Delta g}^M : \mathbb{R}^2 \rightarrow \mathbb{R}^2, bla$ | $\vec{\Delta g}^M : \mathbb{R}^2 \rightarrow \mathbb{R}^2$ | - |

12.4 Semantics

12.4.1 State Variables

12.4.2 Access Routine Semantics

():

- transition:
- output:
- exception:

13 MIS of Conversion Module (M 9)

13.1 Module

MtoCConv

13.2 Uses

- Input
- Data Structure

13.3 Syntax

13.3.1 Exported Access Programs

| Name | In | Out | Exceptions |
|------------|---|---|------------|
| conversion | $p \in \mathbb{R}$, $(n, m) \in \mathbb{N}^2$, $\vec{g}_{\text{uns}}^{M_{\text{exp}}} : \mathbb{R}^2 \rightarrow \mathbb{R}^2$ | $\vec{g}_{j_{\text{uns}}}^{C_{\text{exp}}} : \mathbb{R}^2 \rightarrow \mathbb{R}^2$ | - |

13.4 Semantics

13.4.1 State Variables

13.4.2 Access Routine Semantics

conversion(p , $\vec{g}_{\text{uns}}^{M_{\text{exp}}}$):

- output: $\vec{g}_{\text{uns}}^{M_{\text{exp}}}$ such that

$$\forall \vec{r} \in \mathbb{R}^2, \vec{g}_{j_{\text{uns}}}^{C_{\text{exp}}}(\vec{r}) = \vec{g}_{j_{\text{uns}}}^{M_{\text{exp}}}(\vec{r}) + p \times \begin{bmatrix} n \\ m \end{bmatrix}$$

- exception:

14 MIS of 2D Strain Tensor Module (M 10)

14.1 Module

2D_Strain

14.2 Uses

Data Structure

14.3 Syntax

14.3.1 Exported Access Programs

| Name | In | Out | Exceptions |
|------------|--|---|------------|
| CalcStrain | $g_{1_{\text{uns}}}^{C_{\text{exp}}} : \mathbb{R}^2 \rightarrow \mathbb{R}^2$, $g_{2_{\text{uns}}}^{C_{\text{exp}}} : \mathbb{R}^2 \rightarrow \mathbb{R}^2$, $\Delta g_{1_{\text{uns}}}^{C_{\text{exp}}} : \mathbb{R}^2 \rightarrow \mathbb{R}^2$, $\Delta g_{2_{\text{uns}}}^{C_{\text{exp}}} : \mathbb{R}^2 \rightarrow \mathbb{R}^2$ | $T : \mathbb{R}^2 \rightarrow \mathbb{R}^4$ | - |

14.4 Semantics

14.4.1 State Variables

14.4.2 Access Routine Semantics

CalcStrain($g_{1_{\text{uns}}}^{C_{\text{exp}}}$, $g_{2_{\text{uns}}}^{C_{\text{exp}}}$, $\Delta g_{1_{\text{uns}}}^{C_{\text{exp}}}$, $\Delta g_{2_{\text{uns}}}^{C_{\text{exp}}}$):

- output:
- exception:

15 MIS of Fourier Transform Module (M 11)

2D Fourier transform

15.1 Module

FTCalc

15.2 Uses

Data Structure

15.3 Syntax

15.3.1 Exported Access Programs

| Name | In | Out | Exceptions |
|------------------------|---|---|------------|
| \mathcal{FT} | $f : \mathbb{R}^2 \rightarrow \mathbb{R}$ | $f : \mathbb{R}^2 \rightarrow \mathbb{C}$ | - |
| $\text{i}\mathcal{FT}$ | $f : \mathbb{R}^2 \rightarrow \mathbb{C}$ | $f : \mathbb{R}^2 \rightarrow \mathbb{R}$ | - |

15.4 Semantics

15.4.1 State Variables

None

15.4.2 Access Routine Semantics

Calculate the 2D Fourier transform of a function f

$\mathcal{FT}(f(x, y))$:

- output: $\tilde{f}(\nu, \mu)$ such that

$$\forall(\nu, \mu) \in \mathbb{R}^2 \wedge \forall(x, y) \in \mathbb{R}^2, \tilde{f}(\nu, \mu) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} f(x, y) e^{-2i\pi(\nu x + \mu y)} dx dy$$

- exception:

Calculate the 2D inverse Fourier transform of a function \tilde{f}

$\text{i}\mathcal{FT}(\tilde{f}(\nu, \mu))$:

- output: $f(x, y)$ such that

$$\forall(x, y) \in \mathbb{R}^2 \wedge \forall(\nu, \mu) \in \mathbb{R}^2, f(x, y) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \tilde{f}(\nu, \mu) e^{2i\pi(\nu x + \mu y)} dx dy$$

- exception:

16 MIS of Gradient Module (M 12)

2D Gradient

16.1 Module

GradCalc

16.2 Uses

Data Structure

16.3 Syntax

16.3.1 Exported Access Programs

| Name | In | Out | Exceptions |
|------|---|---|------------|
| grad | $f : \mathbb{R}^2 \rightarrow \mathbb{R}$ | $f : \mathbb{R}^2 \rightarrow \mathbb{R}^2$ | - |

16.4 Semantics

16.4.1 State Variables

16.4.2 Access Routine Semantics

Calculate the gradient of a 2D function f

grad(*f*):

- output: $\nabla f(x, y)$ such that

$$\forall (x, y) \in \mathbb{R}^2, \nabla f(x, y) = \begin{bmatrix} \frac{\partial f}{\partial x}(x, y) \\ \frac{\partial f}{\partial y}(x, y) \end{bmatrix}$$

- exception:

17 MIS of Least Square Fit Method Module (M 13)

2D linear least square method to fit a function f

17.1 Module

LSFMCalc

17.2 Uses

Data Structure

17.3 Syntax

17.3.1 Exported Access Programs

| Name | In | Out | Exceptions |
|------|---|---|------------|
| lsfm | $f : \mathbb{R}^2 \rightarrow \mathbb{R}$ | $f : \mathbb{R}^2 \rightarrow \mathbb{R}$ | - |

17.4 Semantics

17.4.1 State Variables

17.4.2 Access Routine Semantics

Calculate the 2D fit of a function f using the linear least square method on a domain $U = ([x_0, x_1]; [y_0, y_1]) \in \mathbb{R}^2$

lsfm(f,U):

- output: $fit(x, y) = ax + by$ such that

$$\begin{aligned} \forall (x, y) \in U, E(a, b) = \int_{x_0}^{x_1} \int_{y_0}^{y_1} [f(x, y) - fit(x, y)]^2 dx dy \text{ is minimized} \\ \Rightarrow \frac{\partial E}{\partial a} = 0 \wedge \frac{\partial E}{\partial b} = 0 \Rightarrow a = \frac{\int_{x_0}^{x_1} \int_{y_0}^{y_1} x f(x, y) dx dy}{\int_{x_0}^{x_1} \int_{y_0}^{y_1} x^2 dx dy} \wedge b = \frac{\int_{x_0}^{x_1} \int_{y_0}^{y_1} y f(x, y) dx dy}{\int_{x_0}^{x_1} \int_{y_0}^{y_1} y^2 dx dy} \end{aligned}$$

- exception:

18 MIS of Phase Operation Module (M 14)

18.1 Module

PhaseCalc

18.2 Uses

Data Structure

18.3 Syntax

18.3.1 Exported Access Programs

| Name | In | Out | Exceptions |
|--------|--|--|------------|
| unwrap | $f : \mathbb{R}^2 \rightarrow] - \pi, \pi]$ | $f : \mathbb{R}^2 \rightarrow \mathbb{R}$ | - |
| wrap | $f : \mathbb{R}^2 \rightarrow \mathbb{R}$ | $f : \mathbb{R}^2 \rightarrow] - \pi, \pi]$ | - |
| arg | $z \in \mathbb{C}$ | $\phi \in] - \pi, \pi]$ | |

18.4 Semantics

18.4.1 State Variables

18.4.2 Access Routine Semantics

wrap(f):

- output: g such that

$$\forall (x, y) \in \mathbb{R}^2, \exists k \in \mathbb{Z} | g(x, y) = f(x, y) + 2k\pi \wedge g(x, y) \in] - \pi, \pi]$$

- exception:

$\text{unwrap}(f)$:

- output: g such that

$$\begin{aligned} & \forall (x, y) \in \mathbb{R}^2, \exists k \in \mathbb{Z} | g(x, y) = f(x, y) + 2k\pi \wedge g \text{ is continuous} \\ \Rightarrow & \forall (x, y) \in \mathbb{R}^2, \exists k \in \mathbb{Z} | \lim_{(x, y) \rightarrow (x_0, y_0)} g(x, y) = g(x_0, y_0) = f(x_0, y_0) + 2k\pi \end{aligned}$$

- exception:

$\text{arg}(z)$:

- output: ϕ such that

$$\phi = \arg(z) \text{ with } z = e^{i\phi}$$

- exception:

19 MIS of Data Structure Module (M 15)

19.1 Module

DataStruct

19.2 Uses

None

19.3 Syntax

19.3.1 Exported Access Programs

| Name | In | Out | Exceptions |
|-------|------------------------|--------|------------|
| store | string \times object | - | - |
| read | string | object | - |

19.4 Semantics

19.4.1 State Variables

Structure of the object carrying the data information

data() : object

- data(ISMHexp) = $I_{SMH_{\text{exp}}}$
- data(pISMHexp) = p
- data(ICref) = $I_{C_{\text{ref}}}$
- data(pICref) = p_{ref}
- data(FTISMHexp) = $\tilde{I}_{SMH_{\text{exp}}}$
- data(FTSMHsim) = $\tilde{I}_{SMH_{\text{sim}}}$
- for each j data(Tj):object
 - data(Tj)(gjMuns) = $\vec{g}_{j_{\text{uns}}}^{M_{\text{exp}}}$
 - data(Tj)(deltagjM) = $\Delta \vec{g}_j^{M_{\text{exp}}}$
 - data(Tj)(PhasegjM) = $P_{\Delta \vec{g}_j^{M_{\text{exp}}}}$
 - data(Tj)(shiftj) = (n_j, m_j)
 - data(Tj)(gjCuns) = $\vec{g}_{j_{\text{uns}}}^{C_{\text{exp}}}$

19.4.2 Access Routine Semantics

store(a, b):

- transition: data(a) = b

load(a):

- output: data(a) = b

20 MIS of Generic GUI/Plot Module (M 16)

20.1 Module

GUIGene

20.2 Uses

Hardware-Hiding Data Structure

20.3 Syntax

20.3.1 Exported Access Programs

| Name | In | Out | Exceptions |
|-------------|---|------------|------------|
| plot | GUI objects | - | - |
| fig | string \times GUI objects | GUI object | - |
| button | $k \in \mathbb{N}$, string ^{<i>k</i>} | GUI object | - |
| entry_field | string | GUI object | - |
| circle | - | GUI object | - |
| rectangle | - | GUI object | - |

20.4 Semantics

20.4.1 State Variables

20.4.2 Access Routine Semantics

plot():

- transition:
- output: Display on the Hardware all the GUI objects

fig('label', optional GUI objects):

- transition:
- output: Create a window GUI object with the optional GUI objects

button(*number*, 'labels'):

- transition:
- output: Create *number* buttons GUI objects with their respective 'labels'

entry_field(*b*):

- transition:
- output: Create a entry field GUI object to collect the input *b* from the user

circle(*C*):

- transition:
- output: Create a circle *C* GUI object

rectangle(*R*):

- transition:
- output: Create a rectangle *R* GUI object

21 Appendix

All variables

$$\begin{aligned}
&P_{\Delta \vec{g}_j^{M_{\text{exp}}}}(\vec{r}), \vec{g}_j^{M_{\text{exp}}}, \Delta \vec{g}_j^{M_{\text{exp}}}(\vec{r}) \\
&\Delta \vec{g}_j^{M_{\text{exp}}}(\vec{r}), U, \vec{g}_j^{M_{\text{exp}}} \\
&\vec{g}_j^{M_{\text{exp}}}, \Delta \vec{g}_j^{M_{\text{exp}}}(\vec{r}) \\
&\vec{g}_j^{M_{\text{exp}}}, \Delta \vec{g}_j^{M_{\text{exp}}}(\vec{r}), \overrightarrow{q_{n_j, m_j}}, p \\
&\Delta \vec{g}_j^{C_{\text{exp}}}(\vec{r}), \vec{g}_j^{C_{\text{exp}}}
\end{aligned}$$