Module Interface Specification for STEM Moiré GPA

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1 Revision History

Table 1: Revision History

Date	Version	Notes
$\begin{array}{c} \hline 29/11/2017 \\ 15/12/2017 \end{array}$	1.0 1.1	MIS First Draft Correction of matrices expression in section 14

2 Symbols, Abbreviations and Acronyms

The same Symbols, Abbreviations and Acronyms as in the SRS, the TestPlan and the MG (available in STEM Moiré GPA repository) are used in the Module Interface Specifications document.

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3 Introduction

The following document details the Module Interface Specifications for STEM Moiré GPA. The full documentation and implementation can be found in STEM Moiré GPA repository.

4 Notation

The structure of the MIS for modules comes from [1], with the addition that template modules have been adapted from [2]. The following table summarizes the primitive data types used by STEM Moiré GPA.

Data Type	Notation	Description
character	char	a single symbol or digit
integer	\mathbb{Z}	an integer number
$_{ m natural}$	\mathbb{N}	a natural number
real	\mathbb{R}	a real number
complex	\mathbb{C}	a complex number
image space	I	subset of \mathbb{N}^2 such that $\mathbb{I} = \{(x, y) \in \mathbb{N} \times \mathbb{N} : 0 \le x \le N - 1 \land 0 \le y \le N - 1\}$ with $N \in \mathbb{N}$ representing the number of pixels of the image in one direction

[I like the introduction of the image space type. This will help with the specification.—SS]

The specification of STEM Moiré GPA uses some derived data types: sequences, strings, and tuples. Sequences are lists filled with elements of the same data type. Strings are sequences of characters. Tuples contain a list of values, potentially of different types. In addition, STEM Moiré GPA uses functions, which are defined by the data types of their inputs and outputs. Local functions are described by giving their type signature followed by their specification.

5 Module Decomposition

The following table is taken directly from the Module Guide document for this project.

Level 1	Level 2
Hardware-Hiding Module	
Behaviour-Hiding Module	STEM Moiré GPA Control (M 2, section 6) STEM Moiré GPA GUI (M 3, section 7) Input (M 4, section 8) SMH simulation (M 5, section 9) GPA (M 6, section 10) Mask (M 7, section 11) Unstrained region (M 8, section 12) Conversion (M 9, section 13) 2D strain tensor (M 10, section 14)
Software Decision Module	Fourier Transform (M 11, section 15) Gradient (M 12, section 16) Least square fitting method (M 13, section 17) Phase Operation (M 14, section 18) Data structure (M 15, section 19) Generic GUI/Plot (M 16, section 20)

Table 2: Module Hierarchy

6 MIS of STEM Moiré GPA Control Module (M 2)

6.1 Module

main

6.2 Uses

- STEM Moiré GPA GUI (M 3, section 7)
- Processing modules
 - Unstrained region (M 8, section 12)
 - Conversion (M 9, section 13)
 - SMH Simulation (M 5, section 9)
 - GPA(M 6, section 10)
 - 2D Strain Tensors (M 10, section 14)
- Input (M 4, section 8)
- Data Structure (M 15, section 19)

6.3 Syntax

6.3.1 Exported Access Programs

Name	In	Out	Exceptions
main	_	-	-

6.4 Semantics

STEM Moiré GPA is designed to have the process flow driven by user directly through GUI_SMG. The STEM Moiré GPA Control Module uses the events in STEM Moié GPA GUI to use the processing modules in the order defined by the user.

6.4.1 State Variables

None

6.4.2 Access Routine Semantics

main():

• transition:

GUIFlow() # Software permanently running until user abort it by closing the GUI. GUI_Conv() # Open the entry field GUI for the conversion process.

If one of the event below is triggered by the user, an action is performed by STEM Moiré GPA. The possible events are:

```
- event_Input()
→ Get the path pathISMH and pathIC from the user → load_files(pathISMH,pathIC)) → GUI_SMHexp()
- event_SimSMH() → SMHsim() → GUI_SMHsim()
- For each circle GUI object C<sub>j</sub> with j = {1,2} drawn by the user in the of GUI_SMHsim() window :
1. event_GPA() → verifyM(collect_circ(C<sub>j</sub>)) → gpa(collect_circ(C<sub>j</sub>), id(C<sub>j</sub>)) → GUI_Phase()
2. event_URef() → verifyU(collect_rect(Rec)) → ZeroStrain(collect_rect(Rec), id(C<sub>j</sub>)) → update GUI_Phase()
3. event_Conversion() → Read the n and m entry fields in GUI_Conv → verifyNM(n, m) → conversion(n, m, id(C<sub>j</sub>)
- event_StrainCalc() → verifyMdiff(collect_circ(C<sub>1</sub>), collect_circ(C<sub>2</sub>)) →
```

[At current state, the MIS of the control module is not elegant. It is again due to a poor design (or poor understanding) of the control module and its interface with the other modules. The case with the GUI id is not optimum. Ideally, I would like to have the possibility to draw multiple masks and see their intermediate results to only choose the two best ones for the final calculation (StrainCalc(id1,id2)). For that, I would need a new module that could reference the different maks and enable the user to navigate through them. I didn't thought about that enough in advance and got stuck with that version. I will improve that in the future. —Author] [An environment variable for the GUI would help your specification. The environment variable could have fields for SelectInput, SelectSimSMH, Close, etc. You could then write your specification in terms of the values of the GUI environment variable. —SS]

[This document is easier to read if every module starts on a new page. —SS]

7 MIS of STEM Moiré GPA GUI Module (M 3)

Specific GUI module to respect the requirements from the SRS

 $CalcStrain(id(C_1), id(C_2)) \rightarrow GUI Strain()$

[I'm confused by there being both a control module and a GUI module. It seems that the GUI module has an environment variable like I was suggesting above, which makes me think I missed the point of the previous module, or you don't need the previous module?
—SS

7.1 Module

GUI_SMG

7.2 Uses

- Generic GUI/Plot (M 16, section 20)
- Data Structure (M 15, section 19)

7.3 Syntax

7.3.1 Exported Access Programs

For the moment, the GUI exceptions are not mentioned to cover the other aspects of STEM Moiré GPA.

Name	In	Out	Exceptions
GUIFlow	-	-	-
GUI_SMHexp	=	-	-
GUI_SMHSim	-	=	-
GUI_Phase	-	=	-
GUI_Conv	-	-	-
GUI_Strain	=	-	-
$\operatorname{event} \underline{\hspace{0.1cm}} \operatorname{Input}$	=	-	-
${\rm event_SMHSim}$	=	-	-
$\operatorname{event}_{\operatorname{CPA}}$	=	-	-
$\operatorname{event} _\operatorname{URef}$	=	-	-
$event_StrainCalc$	=	-	-
$\operatorname{collect} _\operatorname{circ}$	GUI object	$(x_c, y_c) \in \mathbb{I}, R \in$	-
		\mathbb{R}^{+*}	
$\operatorname{collect} _\operatorname{rect}$	GUI object	$U \subset \mathbb{I}$	-
id	GUI object	id of GUI object	-

7.4 Semantics

STEM Moiré GPA process flow is driven by user through GUI_SMG. User triggers the events that start the selected processing step.

7.4.1 State Variables

None

7.4.2 Environment Variables

Win_Flow: GUI object
Win_SMHexp: GUI object
Win_SMHSim: GUI object
Win_Phase: GUI object
Win_FTSMH: GUI object
Win_Conv: GUI object
Win_Deltag: GUI object
Win_Strain: GUI object
button_Input: GUI object
button_SMHSim: GUI object
button_GPA: GUI object
button_URef: GUI object
button_URef: GUI object

7.4.3 Access Routine Semantics

GUI embedding the process flow into buttons triggering events. It is the user role to execute the process flow.

GUIFlow():

- transition:
 - 1. Win Flow=fig('Win Flow')
 - 2. button(Win_Flow,5,'Input','SMHSim','GPA','URef','StrainCalc')
 - 3. plot()

Events triggered by each button pressed by the user.

event_Input():

• transition: Trigger event_Input when button_Input pressed.

event SMHSim():

• transition: Trigger event_SMHSim when button_SMHSim pressed.

```
event\_GPA():
```

• transition: Trigger event GPA when button GPA pressed.

event URef():

• transition: Trigger event_URef when button_URef pressed.

event_StrainCalc():

• transition: Trigger event StrainCalc when button StrainCalc press.

GUI to display the display the input files $I_{SMH_{exp}}$, $I_{C_{ref}}$. $GUI_SMHexp()$:

- transition:
 - 1. Win_SMHexp=fig('Win_SMHexp',load($I_{SMH_{exp}}$), load($I_{C_{ref}}$))
 - 2. plot()

GUI to display the simulated STEM Moiré hologram using the reference image and to let the user input M on the experimental STEM Moiré hologram (from R 4, R 5).

GUI SMHSim():

- transition:
 - 1. Win_SMHSim=fig('Win_SMHSim',load(FTISMHexp), load(FTISMHsim),circle(M))
 - 2. plot()

GUI to display the phase resulting from the GPA algorithm and to let the user input U (from R 8).

 $GUI_Phase(id)$:

- transition:
 - 1. Win_Phase=fig('Win_Phase',load_g(id)(PhasegM),rectangle(U))
 - 2. Win_Deltag=fig('Win_Deltag',load_g(id)(deltagM))
 - 3. plot()

GUI to display the window to let the user input n and m (from R 11). GUI_Conv():

- transition:
 - 1. Win Conv = fig('Win Conv', entry field(n), entry field(m))
 - 2. plot()

GUI to display the window showing the final strain maps (from R 14). GUI_Strain():

- transition:
 - 1. $Win_Strain=fig('Win_Strain',load(Exx),load(Eyy),load(Exy),load(Rxx))$
 - 2. plot()

Reader of the GUI objects drawn by the user (circle M or rectangle U). $\operatorname{collect_circ}(A)$

- output: C such that
 - 1. Execute read user GUI(A)
 - 2. Verify the type of the object read user GUI(A) to match a circle
 - 3. Output $C=(x_c, y_c, R)$ with (x_c, y_c) the coordinate (pixel number) of the center of the circle A and R the radius of the circle A.

 $\operatorname{collect} \operatorname{rect}(A)$

- output: S such that
 - 1. Execute read user GUI(A)
 - 2. Verify the type of the object read user GUI(A) to match a rectangle
 - 3. Get the coordinate of the upper left corner (x_0, y_0) and the coordinate of the bottom right corner (x_1, y_1) .
 - 4. output $S = ([x_0, x_1], [y_0, y_1])$

Function to read the unique id of a GUI object. id(A)

• output: B such that B is the id part of the read_user_GUI(A) output from the Generic GUI/Plot Module.

8 MIS of Input Module (M 4)

[I made lots of changes with the Input Module between the MG and the MIS. The original design was not optimal and I tried to fit every verification step of the inputs in this input module. It seems to work but I keep in mind the possibility to verify (M,U,n and m) separately in another module —Author]

8.1 Module

Input

8.2 Uses

• Data Structure (M 15, section 19)

8.3 Syntax

8.3.1 Exported Access Programs

Name	In	Out	Exceptions
load_files	string	-	badFilePath, badPixelP, badPixelPref,
			badIC, badISMH, badFileFormat
verifyI	$I:\mathbb{I} o \mathbb{R}$	-	Not2Darray, NotReal
verifyp	$p \in \mathbb{R}^{+*}$	_	$\operatorname{BadPixelP}$
$\operatorname{verifyM}$	$M \in \mathbb{I} \times \mathbb{R}$	-	NoMask, BadMask
verifyU	$U \subset \mathbb{I}$	_	BadSizeU, NoU
verifyMdiff	$(M \in \mathbb{I} \times \mathbb{R})^2$	_	$\operatorname{SameMask}$
${\rm verifyNM}$	$(n,m) \in \mathbb{N}^2$	-	BadNM

8.4 Semantics

8.4.1 State Variables

data: object

8.4.2 Access Routine Semantics

Function to load, verify and store $I_{SMH_{exp}}$, $I_{C_{ref}}$, p and p_{ref} (see R 1 and R 2 from the SRS).

load_files(pathISMH,pathIC):

- transition: pathISMH and pathIC are the file paths for the input files. The following procedure is performed:
 - 1. Verify the format of the files to be .dm3

- 2. From the .dm3 metafile, $I_{SMH_{exp}}$, $I_{C_{ref}}$, p and p_{ref} are extracted.
- 3. verify $I(I_{SMH_{exp}})$, verify $I(I_{C_{ref}})$
- 4. $\operatorname{verifyp}(p)$, $\operatorname{verifyp}(p_{\text{ref}})$
- 5. The variables $I_{SMH_{\mathrm{exp}}},\,I_{C_{\mathrm{ref}}},\,p$ and p_{ref} are stored in the data structure:
 - store(ISMHexp, $I_{SMH_{exp}}$)
 - store(pISMexp, p)
 - store(ICref, $I_{C_{ref}}$)
 - store(pICref, p_{ref})
- exception:

```
\begin{array}{ll} \neg(p>0) & \Rightarrow \text{badPixelP} \\ \neg(p_{\text{ref}}>0) & \Rightarrow \text{badPixelP} \\ (\exists \vec{r} \in \mathbb{I} : I_{SMH_{\text{exp}}}(\vec{r}) \notin \mathbb{R}) & \Rightarrow \text{NotReal} \\ (\exists \vec{r} \in \mathbb{I} : I_{C_{\text{ref}}}(\vec{r}) \notin \mathbb{R}) & \Rightarrow \text{NotReal} \\ \text{If the file targeted by pathISMH or pathIC doesn't exist} & \Rightarrow \text{badFilePath} \\ \text{If the file format is not appropriate} & \Rightarrow \text{badFileFormat} \end{array}
```

[Your document has proven easy to navigate. I was wondering what the type is for $I_{SMH_{exp}}$, and following your documentation, I easily found the answer in Section 19. Since ISMHexp is a function from I to R, how will it be possible for the resulting type to be anything other than R? Thinking about this further, it is probably because for certain inputs the function evaluation will not be real, like the square root of a negative number. This does seem like a situation that would come up, and your programming language is going to generate an exception in those cases, so you will be able to implement your proposed interface. Looks good. —SS] verifyp(p):

- output: None
 - exception: $\neg (p > 0) \Rightarrow \text{badPixelP}$

$\operatorname{verifyI}(I)$:

• output: None

• exception:

```
(\exists \vec{r} \in \mathbb{I} : I(\vec{r}) \notin \mathbb{R}) \Rightarrow \text{NotReal}
\neg (I : \mathbb{I} \to \mathbb{R}) \Rightarrow \text{Not2Darray}
```

Functions to verify the size of the unstrained reference input U (see R 9), the size of the mask input M_j and if both masks are different (see R 6).

verify U(U):

- output: None
- exception: $(U = \emptyset) \Rightarrow \text{NoU}$ $\neg (U \subset \mathbb{I}) \Rightarrow \text{BadSizeU}$

verifyM (M_j) :

- output: None
- exception: $(M_j = \emptyset) \Rightarrow \text{NoMask}$ $\neg((x_j, y_j) \in \mathbb{I}) \Rightarrow \text{BadMask}$

verifyMdiff(M_1, M_2):

- output: None
- exception: $(M_1 = M_2) \Rightarrow \text{SameMask}$

verifyMN (M_1, M_2) :

- output: None
- exception: $\neg (n \in \mathbb{N} \land m \in \mathbb{N}) \Rightarrow \text{BadNM}$

9 MIS of SMH Simulation (M 5)

Module simulating the STEM Moiré hologram using a reference image (see R 3 in the SRS).

9.1 Module

 ${\rm SMHSimCalc}$

9.2 Uses

- Fourier Transform (M 11, section 15)
- Data Structure (M 15, section 19)

9.3 Syntax

9.3.1 Exported Access Programs

Name	In	Out	Exceptions
SMHsim	-	-	${ m WarnNlimzero}$

9.4 Semantics

9.4.1 State Variables

data: object

9.4.2 Access Routine Semantics

SMHsim():

- transition: [The idea of your data object providing a load method (or read method) is fine. However, if you want to simplify your documentation, you could use the dot notation directly to access fields of your ADT. You could just write data. $I_{SMH_{exp}}$. Since you have the correct uses clause and state variable (data), you could think about skipping the data part and just go with the name of the field directly. Given the number of symbols you have though, your approach might be better because it makes the connection explicit. —SS
 - 1. Load the inputs from the data object
 - $-I_{SMH_{exp}} = load(ISMHexp)$
 - $-I_{C_{\text{ref}}} = \text{load}(\text{ICref})$
 - p = load(pISMHexp)
 - $p_{\text{ref}} = \text{load}(\text{pICref})$
 - 2. store(FTISMHexp, $\widetilde{I}_{SMH_{\text{exp}}}$) such that

$$\widetilde{I}_{SMH_{ ext{exp}}}(ec{
u}) = \mathcal{FT}[I_{SMH_{ ext{exp}}}(ec{r})]$$

3. store(FTISMHsim, $\widetilde{I}_{SMH_{\text{sim}}}$) such that

$$\begin{split} \widetilde{I}_{SMH_{\text{sim}}}(\vec{\nu}) &= \frac{1}{p^2} \sum_{\vec{q} \in Q_{lim}} \mathcal{FT}[I_{C_{\text{ref}}}(\vec{\nu} - \frac{\vec{q}}{p})] \\ \text{with } Q_{\text{lim}} &= \{ \forall (n,m) \in \mathbb{Z}^2 \cap [-N_{\text{lim}}, N_{\text{lim}}]^2, \ \vec{q} = n\vec{u_x} + m\vec{u_y} \} \\ \text{and } N_{\text{lim}} &= \Xi(\frac{p}{p_{\text{ref}}}) \text{ with } \Xi \text{ the floor function} \end{split}$$

• exception:

 $(N_{lim}=0) \Rightarrow \text{WarnNlimzero} \# \textit{Exception warns the user that the sampling parameter chosen is oversampling the crystal periodicity. Classic HRSTEM GPA case!! It's not a STEM Moiré interferometry experiment but the software still works for the classic case.$

10 MIS of GPA Module (M 6)

Module performing the GPA algorithm to isolate one spatial frequency and output the phase component (see R 7 in the SRS).

10.1 Module

GPACalc

10.2 Uses

- Mask (M 7, section 11)
- Fourier Transform (M 11, section 15)
- Phase (M 14, section 18)
- Gradient (M 12, section 16)
- Data Structure (M 15, section 19)

10.3 Syntax

10.3.1 Exported Access Programs

Name	In	Out	Exceptions
gpa	$C \in \mathbb{I} \times \mathbb{R}$, id :	-	-
	id of GUI object		

10.4 Semantics

10.4.1 State Variables

data: object

10.4.2 Access Routine Semantics

gpa(C,id):

• transition:

1.
$$M, \overrightarrow{g}^{M_{\text{exp}}} = \text{MCirc}(C)$$

2. store_g(id, Mask, C), store_g(id, gMuns,
$$\overrightarrow{g}^{M_{\text{exp}}}$$
)

3.
$$\widetilde{I}_{SMH_{\text{exp}}} = \text{load}(\text{FTISMHexp})$$

4. Calculate $P_{\vec{g}}$ such that

$$\forall \vec{r} \in \mathbb{R}^2, \ P_{\vec{g}}(\vec{r}) = \arg(i\mathcal{F}\mathcal{T}[M \times \widetilde{I}_{SMH_{\exp}}])$$

5. store_g(id,deltagM, $\overrightarrow{\Delta g}$) such that

$$\forall \vec{r} \in \mathbb{I}, \ \Delta \overrightarrow{g}(\vec{r}) = \frac{1}{2\pi} \operatorname{grad}(\operatorname{unwrap}(P_{\vec{g}}(\vec{r}))) - \overrightarrow{g}^{M_{\operatorname{exp}}}(\vec{r})$$

6. store_g(id,PhasegM, $P_{\Delta \vec{g}}$) such that

$$\forall \vec{r} \in \mathbb{I}, \ P_{\Delta \vec{q}}(\vec{r}) = \text{wrap}(\text{unwrap}[P_{\vec{q}}(\vec{r})] - 2\pi \overrightarrow{g}^{M_{\text{exp}}}(\vec{0}) \cdot \vec{r})$$

• exception: none

11 MIS of Mask Module (M 7)

Module transforming the circle drawn to a mask function usable by the GPA module.

11.1 Module

Mask

11.2 Uses

None

11.3 Syntax

11.3.1 Exported Access Programs

Name	In	Out	Exceptions
MCirc	$(x_c, y_c) \in \mathbb{I} , R \in \mathbb{R}^{+*}$	$M: \mathbb{I} \to \mathbb{R} , \overrightarrow{g_0}: \mathbb{I} \to \mathbb{R}^2$	BadRadius,
			BadCenter

11.4 Semantics

11.4.1 State Variables

None

11.4.2 Access Routine Semantics

 $MCirc(x_c, y_c, R)$:

- output: $M, \overrightarrow{g_0}$
 - -M such that

$$\forall \vec{r} \in \mathbb{I}, \ M(x,y) = \begin{cases} 1, \ (x - x_c)^2 + (y - y_c)^2 \le R^2 \\ 0, \ (x - x_c)^2 + (y - y_c)^2 > R^2 \end{cases}$$

 $-\overrightarrow{g_0}$ such that

$$\forall \vec{r} \in \mathbb{I}, \ \overrightarrow{g_0}(\vec{r}) = \begin{bmatrix} x_c \\ y_c \end{bmatrix}$$

• exception:

$$\neg (R > 0) \Rightarrow \text{BadRadius}$$

 $\neg ((x_c, y_c) \in \mathbb{I}) \Rightarrow \text{BadCenter}$

12 MIS of Unstrained region Module (M 8)

Module correcting the g vector of reference using the user input U (see R 10 in the SRS).

12.1 Module

URefCalc

12.2 Uses

- Least Square Fit (M 13, section 17)
- Data Structure (M 15, section 19)

12.3 Syntax

12.3.1 Exported Access Programs

Name	In	Out	Exceptions
ZeroStrain	$U \subset \mathbb{I}$, id : id of GUI object	-	_

12.4 Semantics

12.4.1 State Variables

data: object

12.4.2 Access Routine Semantics

ZeroStrain(U, id):

- transition:
 - 1. $\overrightarrow{\Delta g}^{M_{\rm exp}} = \text{load_g}(id, \text{ deltag}), \overrightarrow{g}^{M_{\rm exp}} = \text{load_g}(id, \text{ gMuns})$
 - 2. store(U, U)
 - 3. store(id, deltagM, $\overrightarrow{\Delta g}_{\text{cor}}^{M_{\text{exp}}}$) such that

$$\overrightarrow{\Delta g}_{\mathrm{cor}}^{M_{\mathrm{exp}}} = \overrightarrow{\Delta g}^{M_{\mathrm{exp}}} - \mathrm{lsfm}(\overrightarrow{\Delta g}^{M_{\mathrm{exp}}}, U)$$

4. store(id, gMuns, $\overrightarrow{g}_{uns}^{M_{exp}}$) such that

$$\overrightarrow{g}_{\mathrm{uns}}^{M_{\mathrm{exp}}} = \overrightarrow{g}^{M_{\mathrm{exp}}} + \mathrm{lsfm}(\overrightarrow{\Delta g}^{M}, U)$$

• exception: $(\neg U \subset \mathbb{I} \Rightarrow \text{BadSizeU})$

13 MIS of Conversion Module (M 9)

Module converting the Moire g vector into the crystalline g vector (see R 12 in the SRS).

13.1 Module

MtoCConv

13.2 Uses

• Data Structure (M 15, section 19)

13.3 Syntax

13.3.1 Exported Access Programs

Name	In	Out	Exceptions
conversion	$(n,m) \in \mathbb{N}^2$, id :	-	-
	id GUI object		

13.4 Semantics

13.4.1 State Variables

data: object

13.4.2 Access Routine Semantics

conversion(n, m, id):

- transition:
 - 1. store_g(id, shift, (n, m))
 - 2. $\overrightarrow{g_{j}}_{\text{uns}}^{M_{\text{exp}}} = \text{load_g}(id,\text{gMuns}), p = \text{load}(\text{pISMHref})$
 - 3. store_g(id,gCuns, $\overrightarrow{g_j}_{uns}^{C_{exp}}$) such that

$$\forall \vec{r} \in \mathbb{I}, \ \overrightarrow{g_{j\,\mathrm{uns}}^{\prime}}^{C_{\mathrm{exp}}}(\vec{r}) = \overrightarrow{g_{j\,\mathrm{uns}}^{\prime}}^{M_{\mathrm{exp}}}(\vec{r}) + \frac{1}{p} \times \begin{bmatrix} n \\ m \end{bmatrix}$$

• exception:

14 MIS of 2D Strain Tensor Module (M 10)

Module calculating the strain and rotation tensors using two non collinear crystalline wave vectors (see R 13 in the SRS).

14.1 Module

 $2 D_Strain$

14.2 Uses

Data Structure (M 15, section 19)

14.3 Syntax

14.3.1 Exported Access Programs

Name	In	Out	Exceptions
CalcStrain	$(id: id of GUI object)^2$	-	MissingGInfo

14.4 Semantics

14.4.1 State Variables

data: object

14.4.2 Access Routine Semantics

CalcStrain(id1, id2):

- transition:
 - 1. Load the variables from the data structure

$$\begin{split} &-g_{1_{\text{uns}}}^{C_{\text{exp}}} = \text{load_g}(id1,\,\text{gCuns}) \\ &-\Delta g_{1_{\text{uns}}}^{C_{\text{exp}}} = \text{load_g}(id1,\,\text{deltagM}) \\ &-g_{2_{\text{uns}}}^{C_{\text{exp}}} = \text{load_g}(id2,\,\text{gCuns}) \\ &-\Delta g_{2_{\text{uns}}}^{C_{\text{exp}}} = \text{load_g}(id2,\,\text{deltagM}) \end{split}$$

2. Form $G_{\mathrm{uns}}^{\mathrm{exp}}$ and ΔG^{exp} matrices such that

$$G_{\text{uns}}^{\text{exp}} = \begin{bmatrix} g_{1_{\text{uns}_x}}^{C_{\text{exp}}} & g_{2_{\text{uns}_x}}^{C_{\text{exp}}} \\ g_{1_{\text{uns}y}}^{C_{\text{exp}}} & g_{2_{\text{uns}y}}^{C_{\text{exp}}} \end{bmatrix}, \ \Delta G^{\text{exp}}(\vec{r}) = \begin{bmatrix} \Delta g_{1_x}^{C_{\text{exp}}} & \Delta g_{2_x}^{C_{\text{exp}}} \\ \Delta g_{1_y}^{C_{\text{exp}}} & \Delta g_{2_y}^{C_{\text{exp}}} \end{bmatrix}$$

3. Calculate $\nabla u^{\rm exp}$ such that

$$\nabla u^{\text{exp}} = ([G_{\text{uns}}^{\text{exp}} + \Delta G^{\text{exp}}]^T)^{-1} G_{\text{uns}}^{\text{exp}} - I_d$$

4. Calculate ε^{exp} and ω^{exp}

$$\varepsilon^{\text{exp}} = \frac{1}{2} (\nabla u^{\text{exp}} + (\nabla u^{\text{exp}})^T) = \begin{bmatrix} \varepsilon_{xx} & \varepsilon_{xy} \\ \varepsilon_{xy} & \varepsilon_{yy} \end{bmatrix}$$
$$\omega^{\text{exp}} = \frac{1}{2} (\nabla u^{\text{exp}} - (\nabla u^{\text{exp}})^T) = \begin{bmatrix} 0 & \omega_{xy} \\ -\omega_{xy} & 0 \end{bmatrix}$$

5. $\operatorname{store}(\operatorname{Exx}, \varepsilon_{xx})$, $\operatorname{store}(\operatorname{Eyy}, \varepsilon_{yy})$, $\operatorname{store}(\operatorname{Exy}, \varepsilon_{xy})$, $\operatorname{store}(\operatorname{Rxy}, \omega_{xy})$

• exception: $(g_{1_{\text{uns}}}^{C_{\text{exp}}} = \emptyset \vee g_{2_{\text{uns}}}^{C_{\text{exp}}} = \emptyset \vee \Delta g_{1_{\text{uns}}}^{C_{\text{exp}}} = \emptyset \vee \Delta g_{2_{\text{uns}}}^{C_{\text{exp}}} = \emptyset) \Rightarrow \text{MissingGinfo}$

15 MIS of Fourier Transform Module (M 11)

2D Fourier transform

15.1 Module

FTCalc

15.2 Uses

None

15.3 Syntax

15.3.1 Exported Access Programs

Name	In	Out	Exceptions
$\mathcal{F}\mathcal{T}$	$f: \mathbb{R}^2 \to \mathbb{R}$	$f: \mathbb{R}^2 o \mathbb{C}$	-
$_{ m i}\mathcal{FT}$	$f: \mathbb{R}^2 \to \mathbb{C}$	$f: \mathbb{R}^2 \to \mathbb{R}$	-

15.4 Semantics

15.4.1 State Variables

None

15.4.2 Access Routine Semantics

Calculate the 2D Fourier transform of a function f $\mathcal{FT}(f(x,y))$:

• output: $\widetilde{f}(\nu,\mu)$ such that

$$\forall (\nu,\mu) \in \mathbb{R}^2 \land \forall (x,y) \in \mathbb{R}^2, \ \widetilde{f}(\nu,\mu) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} f(x,y) e^{-2i\pi(\nu x + \mu y)} dx dy$$

• exception:

Calculate the 2D inverse Fourier transform of a function \widetilde{f} i $\mathcal{FT}(\widetilde{f}(\nu,\mu))$:

• output: f(x,y) such that

$$\forall (x,y) \in \mathbb{R}^2 \land \forall (\nu,\mu) \in \mathbb{R}^2, \ f(x,y) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \widetilde{f}(\nu,\mu) e^{2i\pi(\nu x + \mu y)} dx dy$$

• exception:

16 MIS of Gradient Module (M 12)

2D Gradient

16.1 Module

GradCalc

16.2 Uses

None

16.3 Syntax

16.3.1 Exported Access Programs

Name	In	Out	Exceptions
grad	$f: \mathbb{R}^2 \to \mathbb{R}$	$f: \mathbb{R}^2 \to \mathbb{R}^2$	-

16.4 Semantics

16.4.1 State Variables

None

16.4.2 Access Routine Semantics

Calculate the gradient of a 2D function f. grad(f):

• output: $\nabla f(x,y)$ such that

$$\forall (x,y) \in \mathbb{R}^2, \ \nabla f(x,y) = \begin{bmatrix} \frac{\partial f}{\partial x}(x,y) \\ \frac{\partial f}{\partial y}(x,y) \end{bmatrix}$$

• exception:

17 MIS of Least Square Fit Method Module (M 13)

2D linear least square method to fit a function f.

17.1 Module

LSFMCalc

17.2 Uses

None

17.3 Syntax

17.3.1 Exported Access Programs

Name	In	Out	Exceptions
lsfm	$f: \mathbb{R}^2 \to \mathbb{R}^2, \ U \in \mathbb{R}^2$	$f: \mathbb{R}^2 \to \mathbb{R}^2$	-

17.4 Semantics

17.4.1 State Variables

None

17.4.2 Access Routine Semantics

Calculate the 2D fit of a function f using the linear least square method on a domain $U = ([x_0, x_1]; [y_0, y_1]) \in \mathbb{R}^2$.

lsfm(f,U):

• output: fit(x,y) = ax + by such that

$$\begin{split} \forall (x,y) \in U, \ E(a,b) &= \int_{x_0}^{x_1} \int_{y_0}^{y_1} [f(x,y) - fit(x,y)]^2 dx dy \ \text{ is minimized} \\ \Rightarrow \frac{\partial E}{\partial a} &= 0 \wedge \frac{\partial E}{\partial b} = 0 \Rightarrow a = \frac{\int_{x_0}^{x_1} \int_{y_0}^{y_1} x f(x,y) dx dy}{\int_{x_0}^{x_1} \int_{y_0}^{y_1} x^2 dx dy} \wedge b = \frac{\int_{x_0}^{x_1} \int_{y_0}^{y_1} y f(x,y) dx dy}{\int_{x_0}^{x_1} \int_{y_0}^{y_1} y^2 dx dy} \end{split}$$

• exception:

18 MIS of Phase Operation Module (M 14)

Module embedding a few functions to make possible some mathematical operations on the phase (parameter bound between $]-\pi,\pi]$).

18.1 Module

PhaseCalc

18.2 Uses

None

18.3 Syntax

18.3.1 Exported Access Programs

Name	In	Out	Exceptions
unwrap	$f: \mathbb{R}^2 \to]-\pi,\pi]$	$f: \mathbb{R}^2 \to \mathbb{R}$	NotPhase
wrap	$f: \mathbb{R}^2 \to \mathbb{R}$	$f: \mathbb{R}^2 \to]-\pi,\pi]$	-
arg	$z \in \mathbb{C}$	$\phi \in]-\pi,\pi]$	-

18.4 Semantics

18.4.1 State Variables

None

18.4.2 Access Routine Semantics

wrap(f):

• output: g such that

$$\forall (x,y) \in \mathbb{R}^2, \exists k \in \mathbb{Z} | g(x,y) = f(x,y) + 2k\pi \land g(x,y) \in]-\pi,\pi]$$

• exception:

$$(\exists (x_0, y_0) \in \mathbb{R}^2 : f(x_0, y_0) \notin]-\pi, \pi]) \Rightarrow \text{BadPhase}$$

 $\operatorname{unwrap}(f)$:

• output: g such that

$$\forall (x,y) \in \mathbb{R}^2, \exists k \in \mathbb{Z} | g(x,y) = f(x,y) + 2k\pi \wedge g \text{ is continous}$$

$$\Rightarrow \forall (x,y) \in \mathbb{R}^2, \exists k \in \mathbb{Z} | \lim_{(x,y) \to (x_0,y_0)} g(x,y) = g(x_0,y_0) = f(x_0,y_0) + 2k\pi$$

• exception:

arg(z):

• output: ϕ such that

$$\phi = \arg(z)$$
 with $z = e^{i\phi}$

• exception:

19 MIS of Data Structure Module (M 15)

[The role of your data structure module isn't entirely clear to me. Many of your modules have a data object as a state variable. As far as I can tell, each module only changes a few of the fields of the data object. I don't see a way to access the state variable data from outside the modules. For instance, the 2D_Strain module calculates the strain and modifies the data object, but the external world doesn't have an interface to actually get the values from the data object. Should your data object actually be a parameter that is passed between modules? You have documented data as an abstract object, not an ADT, so this implies to me that there is only one data object for the life of your program. If this is the case, then you probably want to remove data as a state variable. The modules can change the state of the one data object and anyone that needs to can read and write the data fields, as appropriate. —SS

19.1 Module

DataStruct

19.2 Uses

None

19.3 Syntax

19.3.1 Exported Access Programs

Name	In	Out	Exceptions
store	$string \times object$	-	-
read	string	object	-
${\rm store}_{\rm g}$	id GUI object × string	-	-
${ m read}_{ m g}$	\times object id GUI object \times string	object	-

[I think in your spec you changed read to load. —SS]

19.4 Semantics

19.4.1 State Variables

Structure of the object carrying the data information.

data: object

- data(ISMHexp)= $I_{SMH_{\text{exp}}}: \mathbb{I} \to \mathbb{R}$
- data(pISMHexp)= $p \in \mathbb{R}^{+*}$

- $data(ICref) = I_{C_{ref}} : \mathbb{I} \to \mathbb{R}$
- data(pICref)= $p_{ref} \in \mathbb{R}^{+*}$
- data(FTISMHexp)= $\widetilde{I}_{SMH_{\text{exp}}}: \mathbb{I} \to \mathbb{C}$
- data(FTISMHsim)= $\widetilde{I}_{SMH_{\text{sim}}}: \mathbb{I} \to \mathbb{C}$
- data(URef)= $U \subset \mathbb{I}$
- for each $j = \{1, 2\} \operatorname{data}(Mj)$: object
 - data(Mj)(mask)= $x_c, y_c, R \in \mathbb{N} \times \mathbb{N} \times \mathbb{R}^{+*}$
 - $-\operatorname{data}(Mj)(gMuns) = \overrightarrow{g_j}_{uns}^{M_{exp}} : \mathbb{I} \to \mathbb{R}^2$
 - data(Mj)(deltagM)= $\Delta \overrightarrow{g_j}^{M_{\text{exp}}} : \mathbb{I} \to \mathbb{R}^2$
 - $\operatorname{data}(Mj)(\operatorname{PhasegM}) = P_{\Delta \overrightarrow{q_i}}M_{\operatorname{exp}} : \mathbb{I} \to \mathbb{R}$
 - data(Mj)(shift)= $(n_j, m_j) \in \mathbb{N}^2$
 - data(Mj)(gCuns)= $\overrightarrow{g_j}_{uns}^{C_{exp}}: \mathbb{I} \to \mathbb{R}^2$
- $data(Exx) = \varepsilon_{xx} : \mathbb{I} \to \mathbb{R}$
- data(Eyy)= $\varepsilon_{vv}: \mathbb{I} \to \mathbb{R}$
- data(Exy)= $\varepsilon_{xy}: \mathbb{I} \to \mathbb{R}$
- data(Rxy)= $\omega_{xy}: \mathbb{I} \to \mathbb{R}$

19.4.2 Access Routine Semantics

store(a,b):

• transition: data(a)=b

load(a):

• output: data(a)

store g(id,a,b):

• transition: data(id)(a)=b

 $load_g(id,a)$:

• output: data(id)(a)

20 MIS of Generic GUI/Plot Module (M 16)

[The description of this module is pretty sparse ... I didn't want to go through all the possible interaction a GUI and a plotter can do. I also think that it is not the major element for the course. On the other hand, a nice GUI makes lots of difference from the user perspective. —Author]

20.1 Module

GUIGene

20.2 Uses

Hardware-Hiding (M 1)

20.3 Syntax

20.3.1 Exported Access Programs

Name	In	Out	Exceptions
plot	GUI objects	-	-
fig	$string \times GUI objects$	GUI object	-
button	$k \in \mathbb{N}$, string ^k	GUI object	-
$\operatorname{entry_field}$	string	GUI object	-
circle	-	GUI object	-
$\operatorname{rectangle}$	-	GUI object	-
read_user_GUI	GUI object	object	

20.4 Semantics

20.4.1 State Variables

None

20.4.2 Access Routine Semantics

plot():

• output: Display on the Hardware all the GUI objects.

fig('label', optional GUI objects):

• output: Create a window GUI object with the optional GUI objects.

button(number, 'labels'):

- output: Create *number* buttons GUI objects with their respective 'labels'. entry_field(b):
- output: Create a entry field GUI object to collect the input b from the user. $circle(C(user_param))$:
- ullet output: Create a circle C GUI object drawn by the user. rectangle($R(user_param)$):
- \bullet output: Create a rectangle R GUI object drawn by the user. ${\tt read_user_GUI}(A) \colon$
 - output: B such that B includes the id of the GUI and the type of the GUI.

[Great work! I do not have the time (or the expertise) to review the details, but everything I looked at had the required detail and the pieces fit together. My only real question is about the data object, as mentioned above (in Section 19). It would be great to do a proper review of the pieces of your design with an actual expert. If there is anyone in your lab that has an interest, you might want to get their feedback. —SS

References

- [1] D. M. Hoffman and P. A. Strooper, Software Design, Automated Testing, and Maintenance: A Practical Approach. New York, NY, USA: International Thomson Computer Press, 1995.
- [2] C. Ghezzi, M. Jazayeri, and D. Mandrioli, Fundamentals of Software Engineering. Upper Saddle River, NJ, USA: Prentice Hall, 2nd ed., 2003.

[Missing bib items —SS]